

Almost distributive lattices edit

Abbreviation: ADLat

Definition 1. An *almost distributive lattice* is a near-distributive lattice $\mathbf{L} = \langle L, \vee, \wedge \rangle$ such that

$$AD_{\wedge}: v \wedge [u \vee (x \wedge [y \vee (x \wedge z)])] \leq u \vee [(x \wedge [y \vee (x \wedge z)]) \wedge (v \vee (x \wedge y) \vee (x \wedge z))]$$

$$AD_{\vee}: v \vee [u \wedge (x \vee [y \wedge (x \vee z)])] \geq u \wedge [(x \vee [y \wedge (x \vee z)]) \vee (v \wedge (x \vee y) \wedge (x \vee z))]$$

Morphisms. Let \mathbf{L} and \mathbf{M} be almost distributive lattices. A morphism from \mathbf{L} to \mathbf{M} is a function $h : L \rightarrow M$ that is a homomorphism:

$$h(x \vee y) = h(x) \vee h(y), \quad h(x \wedge y) = h(x) \wedge h(y)$$

Basic Results.

Examples.

1. $D[d] = \langle D \cup \{d'\}, \vee, \wedge \rangle$, where D is any distributive lattice and d is an element in it that is split into two elements d, d' using Alan Day's doubling construction.

Properties. (description)

Classtype	variety
Equational theory	
Quasiequational theory	
First-order theory	undecidable
Locally finite	no
Residual size	unbounded
Congruence distributive	yes
Congruence modular	yes
Congruence n-permutable	no
Congruence regular	no
Congruence uniform	no
Congruence extension property	
Definable principal congruences	
Equationally def. pr. cong.	
Amalgamation property	no
Strong amalgamation property	no
Epimorphisms are surjective	

Finite Members. $f(n)$ = number of members of size n .

$$f(1) = 1$$

$$f(2) = 1$$

$$f(3) = 1$$

$$f(4) = 2$$

$$f(5) = 4$$

$$f(6) =$$

$$f(7) =$$

Subclasses.

Distributive lattices

Superclasses.

Neardistributive lattices

REFERENCES

[1]