

# Complete lattices edit

## Abbreviation: CLat

**Definition 1.** A *complete lattice* is a structure  $\mathbf{L} = \langle L, \bigvee, \bigwedge \rangle$  such that  $\bigvee, \bigwedge$  map subsets of  $L$  to elements of  $L$  and

$\langle L, \bigvee, \bigwedge \rangle$  is a Lattices

$\bigvee S$  is the least upper bound of  $S$

$\bigwedge S$  is the greatest lower bound of  $S$

**Morphisms.** Let  $\mathbf{L}$  and  $\mathbf{M}$  be complete lattices. A morphism from  $\mathbf{L}$  to  $\mathbf{M}$  is a function  $h : L \rightarrow M$  that is a complete homomorphism:

$$h(\bigvee S) = \bigvee h[S] \text{ and } h(\bigwedge S) = \bigwedge h[S]$$

## Basic Results.

### Examples.

1.  $\langle \mathcal{P}(X), \bigcup, \bigcap \rangle$ , the set of all subsets of a set  $X$ , with union and intersection of families of sets.

### Properties. (description)

Classtype	Second-order
Amalgamation property	Yes
Strong amalgamation property	Yes
Epimorphisms are surjective	Yes

### Subclasses.

Algebraic lattices

### Superclasses.

Lattices

## REFERENCES

[1]