A distributive lattice with non-modular MacNeille completion



The middle example is due to N. Funayama [1944]. Note that the canonical extension L^{δ} of L is still distributive. The blue elements are in $O(L^{\delta})$, the red elements are in $K(L^{\delta})$ and the green elements are neither open nor closed.