

SWB axioms

SWB003+1.ax RDFS Extensional axioms

$\forall p, c: (\text{iext}(\text{uri_rdfs_domain}, p, c) \iff (\text{ip}(p) \text{ and } \text{ic}(c) \text{ and } \forall x, y: (\text{iext}(p, x, y) \Rightarrow \text{icext}(c, x))))$ fof(owl_rdfsext_domain, axiom)
 $\forall p, c: (\text{iext}(\text{uri_rdfs_range}, p, c) \iff (\text{ip}(p) \text{ and } \text{ip}(c) \text{ and } \forall x, y: (\text{iext}(p, x, y) \Rightarrow \text{icext}(c, y))))$ fof(owl_rdfsext_range, axiom)
 $\forall c_1, c_2: (\text{iext}(\text{uri_rdfs_subClassOf}, c_1, c_2) \iff (\text{ic}(c_1) \text{ and } \text{ic}(c_2) \text{ and } \forall x: (\text{icext}(c_1, x) \Rightarrow \text{icext}(c_2, x))))$ fof(owl_rdfsext_subClassOf, axiom)
 $\forall p_1, p_2: (\text{iext}(\text{uri_rdfs_subPropertyOf}, p_1, p_2) \iff (\text{ip}(p_1) \text{ and } \text{ip}(p_2) \text{ and } \forall x, y: (\text{iext}(p_1, x, y) \Rightarrow \text{iext}(p_2, x, y))))$ fof(owl_rdfsext_subPropertyOf, axiom)

SWB problems

SWB001+1.p Subgraph Entailment

include('Axioms/SWB001+0.ax')
 $\text{iext}(\text{uri_rdf_type}, \text{uri_ex_r}, \text{uri_owl_Restriction}) \text{ and } \text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_r}, \text{uri_ex_p})$ fof(testcase_conclusion_fullish_001_Subgraph_Entailment, conjecture)
 $\text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_ex_c}, \text{uri_ex_r}) \text{ and } \text{iext}(\text{uri_rdf_type}, \text{uri_ex_r}, \text{uri_owl_Restriction}) \text{ and } \text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_r}, \text{uri_ex_p})$ fof(testcase_premise_fullish_001_Subgraph_Entailment, axiom)

SWB001+2.p Subgraph Entailment

$\text{iext}(\text{uri_rdf_type}, \text{uri_ex_r}, \text{uri_owl_Restriction}) \text{ and } \text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_r}, \text{uri_ex_p})$ fof(testcase_conclusion_fullish_002_Subgraph_Entailment, conjecture)
 $\text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_ex_c}, \text{uri_ex_r}) \text{ and } \text{iext}(\text{uri_rdf_type}, \text{uri_ex_r}, \text{uri_owl_Restriction}) \text{ and } \text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_r}, \text{uri_ex_p})$ fof(testcase_premise_fullish_002_Subgraph_Entailment, axiom)

SWB001+3.p Subgraph Entailment

include('Axioms/SWB002+0.ax')
 $\text{iext}(\text{uri_rdf_type}, \text{uri_ex_r}, \text{uri_owl_Restriction}) \text{ and } \text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_r}, \text{uri_ex_p})$ fof(testcase_conclusion_fullish_003_Subgraph_Entailment, conjecture)
 $\text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_ex_c}, \text{uri_ex_r}) \text{ and } \text{iext}(\text{uri_rdf_type}, \text{uri_ex_r}, \text{uri_owl_Restriction}) \text{ and } \text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_r}, \text{uri_ex_p})$ fof(testcase_premise_fullish_003_Subgraph_Entailment, axiom)

SWB001+4.p Subgraph Entailment

include('Axioms/SWB003+0.ax')
 $\text{iext}(\text{uri_rdf_type}, \text{uri_ex_r}, \text{uri_owl_Restriction}) \text{ and } \text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_r}, \text{uri_ex_p})$ fof(testcase_conclusion_fullish_004_Subgraph_Entailment, conjecture)
 $\text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_ex_c}, \text{uri_ex_r}) \text{ and } \text{iext}(\text{uri_rdf_type}, \text{uri_ex_r}, \text{uri_owl_Restriction}) \text{ and } \text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_r}, \text{uri_ex_p})$ fof(testcase_premise_fullish_004_Subgraph_Entailment, axiom)

SWB002+1.p Existential Blank Nodes

include('Axioms/SWB001+0.ax')
 $\exists \text{bNODE}_x, \text{bNODE}_y: (\text{iext}(\text{uri_ex_p}, \text{bNODE}_x, \text{bNODE}_y) \text{ and } \text{iext}(\text{uri_ex_q}, \text{bNODE}_y, \text{bNODE}_x))$ fof(testcase_conclusion_fullish_001_Existential_Blank_Nodes, conjecture)
 $\exists \text{bNODE}_o: (\text{iext}(\text{uri_ex_p}, \text{uri_ex_s}, \text{bNODE}_o) \text{ and } \text{iext}(\text{uri_ex_q}, \text{bNODE}_o, \text{uri_ex_s}))$ fof(testcase_premise_fullish_001_Existential_Blank_Nodes, axiom)

SWB002+2.p Existential Blank Nodes

$\exists \text{bNODE}_x, \text{bNODE}_y: (\text{iext}(\text{uri_ex_p}, \text{bNODE}_x, \text{bNODE}_y) \text{ and } \text{iext}(\text{uri_ex_q}, \text{bNODE}_y, \text{bNODE}_x))$ fof(testcase_conclusion_fullish_002_Existential_Blank_Nodes, conjecture)
 $\exists \text{bNODE}_o: (\text{iext}(\text{uri_ex_p}, \text{uri_ex_s}, \text{bNODE}_o) \text{ and } \text{iext}(\text{uri_ex_q}, \text{bNODE}_o, \text{uri_ex_s}))$ fof(testcase_premise_fullish_002_Existential_Blank_Nodes, axiom)

SWB002+3.p Existential Blank Nodes

include('Axioms/SWB002+0.ax')
 $\exists \text{bNODE}_x, \text{bNODE}_y: (\text{iext}(\text{uri_ex_p}, \text{bNODE}_x, \text{bNODE}_y) \text{ and } \text{iext}(\text{uri_ex_q}, \text{bNODE}_y, \text{bNODE}_x))$ fof(testcase_conclusion_fullish_003_Existential_Blank_Nodes, conjecture)
 $\exists \text{bNODE}_o: (\text{iext}(\text{uri_ex_p}, \text{uri_ex_s}, \text{bNODE}_o) \text{ and } \text{iext}(\text{uri_ex_q}, \text{bNODE}_o, \text{uri_ex_s}))$ fof(testcase_premise_fullish_003_Existential_Blank_Nodes, axiom)

SWB002+4.p Existential Blank Nodes

include('Axioms/SWB003+0.ax')
 $\exists \text{bNODE}_x, \text{bNODE}_y: (\text{iext}(\text{uri_ex_p}, \text{bNODE}_x, \text{bNODE}_y) \text{ and } \text{iext}(\text{uri_ex_q}, \text{bNODE}_y, \text{bNODE}_x))$ fof(testcase_conclusion_fullish_004_Existential_Blank_Nodes, conjecture)
 $\exists \text{bNODE}_o: (\text{iext}(\text{uri_ex_p}, \text{uri_ex_s}, \text{bNODE}_o) \text{ and } \text{iext}(\text{uri_ex_q}, \text{bNODE}_o, \text{uri_ex_s}))$ fof(testcase_premise_fullish_004_Existential_Blank_Nodes, axiom)

SWB003+1.p Blank Nodes for Literals

include('Axioms/SWB001+0.ax')
 $\exists \text{bNODE}_x: \text{iext}(\text{uri_ex_p}, \text{uri_ex_s}, \text{bNODE}_x)$ fof(testcase_conclusion_fullish_003_Blank_Nodes_for_Literals, conjecture)
 $\text{iext}(\text{uri_ex_p}, \text{uri_ex_s}, \text{literal_plain}(\text{dat_str_foo}))$ fof(testcase_premise_fullish_003_Blank_Nodes_for_Literals, axiom)

SWB003+2.p Blank Nodes for Literals

$\exists \text{bNODE}_x: \text{iext}(\text{uri_ex_p}, \text{uri_ex_s}, \text{bNODE}_x)$ fof(testcase_conclusion_fullish_003_Blank_Nodes_for_Literals, conjecture)
 $\text{iext}(\text{uri_ex_p}, \text{uri_ex_s}, \text{literal_plain}(\text{dat_str_foo}))$ fof(testcase_premise_fullish_003_Blank_Nodes_for_Literals, axiom)

SWB003+3.p Blank Nodes for Literals

include('Axioms/SWB002+0.ax')
 $\exists \text{bNODE}_x: \text{iext}(\text{uri_ex_p}, \text{uri_ex_s}, \text{bNODE}_x)$ fof(testcase_conclusion_fullish_003_Blank_Nodes_for_Literals, conjecture)
 $\text{iext}(\text{uri_ex_p}, \text{uri_ex_s}, \text{literal_plain}(\text{dat_str_foo}))$ fof(testcase_premise_fullish_003_Blank_Nodes_for_Literals, axiom)

SWB003+4.p Blank Nodes for Literals

include('Axioms/SWB003+0.ax')
 $\exists \text{bNODE}_x: \text{iext}(\text{uri_ex_p}, \text{uri_ex_s}, \text{bNODE}_x)$ fof(testcase_conclusion_fullish_003_Blank_Nodes_for_Literals, conjecture)
 $\text{iext}(\text{uri_ex_p}, \text{uri_ex_s}, \text{literal_plain}(\text{dat_str_foo}))$ fof(testcase_premise_fullish_003_Blank_Nodes_for_Literals, axiom)

SWB004+1.p Axiomatic Triples

include('Axioms/SWB001+0.ax')

iext(uri_rdf_type, uri_owl_Class, uri_owl_Thing) and iext(uri_rdf_type, uri_owl_Class, uri_owl_Class) and iext(uri_rdfs_subClassOf, uri_owl_Class, uri_owl_Class)

SWB004+2.p Axiomatic Triples

$\forall x: \text{ir}(x) \quad \text{fof}(\text{simple_ir}, \text{axiom})$

$\forall x, c: (\text{iext}(\text{uri_rdf_type}, x, c) \iff \text{icext}(c, x)) \quad \text{fof}(\text{rdfs_cext_def}, \text{axiom})$

$\forall x: (\text{idc}(x) \Rightarrow \text{ic}(x)) \quad \text{fof}(\text{owl_parts_idc_cond_set}, \text{axiom})$

$\text{ic}(\text{uri_owl_Class}) \quad \text{fof}(\text{owl_class_classowl_type}, \text{axiom})$

$\forall x: (\text{icext}(\text{uri_owl_Class}, x) \iff \text{ic}(x)) \quad \text{fof}(\text{owl_class_classowl_ext}, \text{axiom})$

$\text{ic}(\text{uri_rdfs_Class}) \quad \text{fof}(\text{owl_class_classrdfs_type}, \text{axiom})$

$\forall x: (\text{icext}(\text{uri_rdfs_Class}, x) \iff \text{ic}(x)) \quad \text{fof}(\text{owl_class_classrdfs_ext}, \text{axiom})$

$\text{ic}(\text{uri_rdfs_Datatype}) \quad \text{fof}(\text{owl_class_datatype_type}, \text{axiom})$

$\forall x: (\text{icext}(\text{uri_rdfs_Datatype}, x) \iff \text{idc}(x)) \quad \text{fof}(\text{owl_class_datatype_ext}, \text{axiom})$

$\text{ic}(\text{uri_owl_Thing}) \quad \text{fof}(\text{owl_class_thing_type}, \text{axiom})$

$\forall x: (\text{icext}(\text{uri_owl_Thing}, x) \iff \text{ir}(x)) \quad \text{fof}(\text{owl_class_thing_ext}, \text{axiom})$

$\forall c_1, c_2: (\text{iext}(\text{uri_rdfs_subClassOf}, c_1, c_2) \iff (\text{ic}(c_1) \text{ and } \text{ic}(c_2) \text{ and } \forall x: (\text{icext}(c_1, x) \Rightarrow \text{icext}(c_2, x)))) \quad \text{fof}(\text{owl_rdfs_ext_subClassOf}, \text{axiom})$

$\forall c_1, c_2: (\text{iext}(\text{uri_owl_equivalentClass}, c_1, c_2) \iff (\text{ic}(c_1) \text{ and } \text{ic}(c_2) \text{ and } \forall x: (\text{icext}(c_1, x) \iff \text{icext}(c_2, x)))) \quad \text{fof}(\text{owl_eqdis_equivalentClass}, \text{axiom})$

iext(uri_rdf_type, uri_owl_Class, uri_owl_Thing) and iext(uri_rdf_type, uri_owl_Class, uri_owl_Class) and iext(uri_rdfs_subClassOf, uri_owl_Class, uri_owl_Class)

SWB004+3.p Axiomatic Triples

include('Axioms/SWB002+0.ax')

iext(uri_rdf_type, uri_owl_Class, uri_owl_Thing) and iext(uri_rdf_type, uri_owl_Class, uri_owl_Class) and iext(uri_rdfs_subClassOf, uri_owl_Class, uri_owl_Class)

SWB004+4.p Axiomatic Triples

include('Axioms/SWB003+0.ax')

iext(uri_rdf_type, uri_owl_Class, uri_owl_Thing) and iext(uri_rdf_type, uri_owl_Class, uri_owl_Class) and iext(uri_rdfs_subClassOf, uri_owl_Class, uri_owl_Class)

SWB005+1.p Everything is a Resource

include('Axioms/SWB001+0.ax')

iext(uri_rdf_type, uri_ex_s, uri_rdfs_Resource) and iext(uri_rdf_type, uri_ex_s, uri_owl_Thing) and iext(uri_rdf_type, uri_ex_p, uri_ex_s)

iext(uri_ex_p, uri_ex_s, uri_ex_o) fof(testcase_premise_fullish_005_Everything_is_a_Resource, axiom)

SWB005+2.p Everything is a Resource

$\forall x: \text{ir}(x) \quad \text{fof}(\text{simple_ir}, \text{axiom})$

$\forall s, p, o: (\text{iext}(p, s, o) \Rightarrow \text{ip}(p)) \quad \text{fof}(\text{simple_iext_property}, \text{axiom})$

$\forall p: (\text{iext}(\text{uri_rdf_type}, p, \text{uri_rdf_Property}) \iff \text{ip}(p)) \quad \text{fof}(\text{rdf_type_ip}, \text{axiom})$

$\forall x, c: (\text{iext}(\text{uri_rdf_type}, x, c) \iff \text{icext}(c, x)) \quad \text{fof}(\text{rdfs_cext_def}, \text{axiom})$

$\forall x: (\text{ir}(x) \iff \text{icext}(\text{uri_rdfs_Resource}, x)) \quad \text{fof}(\text{rdfs_ir_def}, \text{axiom})$

$\forall x: (\text{icext}(\text{uri_owl_Thing}, x) \iff \text{ir}(x)) \quad \text{fof}(\text{owl_class_thing_ext}, \text{axiom})$

$\forall x: (\text{icext}(\text{uri_owl_ObjectProperty}, x) \iff \text{ip}(x)) \quad \text{fof}(\text{owl_class_objectproperty_ext}, \text{axiom})$

iext(uri_rdf_type, uri_ex_s, uri_rdfs_Resource) and iext(uri_rdf_type, uri_ex_s, uri_owl_Thing) and iext(uri_rdf_type, uri_ex_p, uri_ex_s)

iext(uri_ex_p, uri_ex_s, uri_ex_o) fof(testcase_premise_fullish_005_Everything_is_a_Resource, axiom)

SWB005+3.p Everything is a Resource

include('Axioms/SWB002+0.ax')

iext(uri_rdf_type, uri_ex_s, uri_rdfs_Resource) and iext(uri_rdf_type, uri_ex_s, uri_owl_Thing) and iext(uri_rdf_type, uri_ex_p, uri_ex_s)

iext(uri_ex_p, uri_ex_s, uri_ex_o) fof(testcase_premise_fullish_005_Everything_is_a_Resource, axiom)

SWB005+4.p Everything is a Resource

include('Axioms/SWB003+0.ax')

iext(uri_rdf_type, uri_ex_s, uri_rdfs_Resource) and iext(uri_rdf_type, uri_ex_s, uri_owl_Thing) and iext(uri_rdf_type, uri_ex_p, uri_ex_s)

iext(uri_ex_p, uri_ex_s, uri_ex_o) fof(testcase_premise_fullish_005_Everything_is_a_Resource, axiom)

SWB006+1.p Literal Values represented by URIs and Blank Nodes

include('Axioms/SWB001+0.ax')

iext(uri_owl_sameAs, uri_ex_u, uri_ex_w) fof(testcase_conclusion_fullish_006_Literal_Values_represented_by_URIs_and_Blank_Nodes, axiom)

$\exists \text{bNODE}_x: (\text{iext}(\text{uri_owl_sameAs}, \text{uri_ex_u}, \text{literal_plain}(\text{dat_str_abc})) \text{ and } \text{iext}(\text{uri_owl_sameAs}, \text{bNODE}_x, \text{literal_plain}(\text{dat_str_abc})))$

SWB006+2.p Literal Values represented by URIs and Blank Nodes

$\forall x, y: (\text{iext}(\text{uri_owl_sameAs}, x, y) \iff x = y) \quad \text{fof}(\text{owl_eqdis_sameas}, \text{axiom})$

iext(uri_owl_sameAs, uri_ex_u, uri_ex_w) fof(testcase_conclusion_fullish_006_Literal_Values_represented_by_URIs_and_Blank_Nodes, axiom)

$\exists \text{bNODE}_x: (\text{iext}(\text{uri_owl_sameAs}, \text{uri_ex_u}, \text{literal_plain}(\text{dat_str_abc})) \text{ and } \text{iext}(\text{uri_owl_sameAs}, \text{bNODE}_x, \text{literal_plain}(\text{dat_str_abc})))$

SWB006+3.p Literal Values represented by URIs and Blank Nodes

include('Axioms/SWB002+0.ax')

iext(uri_owl_sameAs, uri_ex_u, uri_ex_w) fof(testcase_conclusion_fullish_006 Literal_Values_represented_by_URIs_and_Blank_Nodes, axiom)
 \exists bNODE_x: (iext(uri_owl_sameAs, uri_ex_u, literal_plain(dat_str_abc)) and iext(uri_owl_sameAs, bNODE_x, literal_plain(dat_str_abc)))

SWB006+4.p Literal Values represented by URIs and Blank Nodes

include('Axioms/SWB003+0.ax')

iext(uri_owl_sameAs, uri_ex_u, uri_ex_w) fof(testcase_conclusion_fullish_006 Literal_Values_represented_by_URIs_and_Blank_Nodes, axiom)
 \exists bNODE_x: (iext(uri_owl_sameAs, uri_ex_u, literal_plain(dat_str_abc)) and iext(uri_owl_sameAs, bNODE_x, literal_plain(dat_str_abc)))

SWB007+1.p Equal Classes

include('Axioms/SWB001+0.ax')

iext(uri_rdf_type, uri_ex_w, uri_ex_c2) and iext(uri_rdfs_subClassOf, uri_ex_c, uri_ex_c2) and iext(uri_rdfs_range, uri_ex_p, uri_ex_c)
iext(uri_owl_sameAs, uri_ex_c1, uri_ex_c2) and iext(uri_rdf_type, uri_ex_w, uri_ex_c1) and iext(uri_rdfs_subClassOf, uri_ex_c, uri_ex_c2)

SWB007+2.p Equal Classes

$\forall x, y: (iext(uri_owl_sameAs, x, y) \iff x = y)$ fof(owl_eqdis_sameas, axiom)

iext(uri_rdf_type, uri_ex_w, uri_ex_c2) and iext(uri_rdfs_subClassOf, uri_ex_c, uri_ex_c2) and iext(uri_rdfs_range, uri_ex_p, uri_ex_c)
iext(uri_owl_sameAs, uri_ex_c1, uri_ex_c2) and iext(uri_rdf_type, uri_ex_w, uri_ex_c1) and iext(uri_rdfs_subClassOf, uri_ex_c, uri_ex_c2)

SWB007+3.p Equal Classes

include('Axioms/SWB002+0.ax')

iext(uri_rdf_type, uri_ex_w, uri_ex_c2) and iext(uri_rdfs_subClassOf, uri_ex_c, uri_ex_c2) and iext(uri_rdfs_range, uri_ex_p, uri_ex_c)
iext(uri_owl_sameAs, uri_ex_c1, uri_ex_c2) and iext(uri_rdf_type, uri_ex_w, uri_ex_c1) and iext(uri_rdfs_subClassOf, uri_ex_c, uri_ex_c2)

SWB007+4.p Equal Classes

include('Axioms/SWB003+0.ax')

iext(uri_rdf_type, uri_ex_w, uri_ex_c2) and iext(uri_rdfs_subClassOf, uri_ex_c, uri_ex_c2) and iext(uri_rdfs_range, uri_ex_p, uri_ex_c)
iext(uri_owl_sameAs, uri_ex_c1, uri_ex_c2) and iext(uri_rdf_type, uri_ex_w, uri_ex_c1) and iext(uri_rdfs_subClassOf, uri_ex_c, uri_ex_c2)

SWB008+1.p Inverse Functional Data Properties

include('Axioms/SWB001+0.ax')

iext(uri_owl_sameAs, uri_ex_bob, uri_ex_robort) fof(testcase_conclusion_fullish_008 Inverse_Functional_Data_Properties, axiom)
iext(uri_rdf_type, uri_foaf_mbox_sha1sum, uri_owl_DatatypeProperty) and iext(uri_rdf_type, uri_foaf_mbox_sha1sum, uri_owl_InverseFunctionalProperty)

SWB008+2.p Inverse Functional Data Properties

$\forall x, c: (iext(uri_rdf_type, x, c) \iff icext(c, x))$ fof(rdfs_cext_def, axiom)

$\forall x, y: (iext(uri_owl_sameAs, x, y) \iff x = y)$ fof(owl_eqdis_sameas, axiom)

$\forall p: (icext(uri_owl_InverseFunctionalProperty, p) \iff (ip(p) \text{ and } \forall x_1, x_2, y: ((iext(p, x_1, y) \text{ and } iext(p, x_2, y)) \implies x_1 = x_2)))$ fof(owl_char_inversefunctional, axiom)

iext(uri_owl_sameAs, uri_ex_bob, uri_ex_robort) fof(testcase_conclusion_fullish_008 Inverse_Functional_Data_Properties, axiom)
iext(uri_rdf_type, uri_foaf_mbox_sha1sum, uri_owl_DatatypeProperty) and iext(uri_rdf_type, uri_foaf_mbox_sha1sum, uri_owl_InverseFunctionalProperty)

SWB008+3.p Inverse Functional Data Properties

include('Axioms/SWB002+0.ax')

iext(uri_owl_sameAs, uri_ex_bob, uri_ex_robort) fof(testcase_conclusion_fullish_008 Inverse_Functional_Data_Properties, axiom)
iext(uri_rdf_type, uri_foaf_mbox_sha1sum, uri_owl_DatatypeProperty) and iext(uri_rdf_type, uri_foaf_mbox_sha1sum, uri_owl_InverseFunctionalProperty)

SWB008+4.p Inverse Functional Data Properties

include('Axioms/SWB003+0.ax')

iext(uri_owl_sameAs, uri_ex_bob, uri_ex_robort) fof(testcase_conclusion_fullish_008 Inverse_Functional_Data_Properties, axiom)
iext(uri_rdf_type, uri_foaf_mbox_sha1sum, uri_owl_DatatypeProperty) and iext(uri_rdf_type, uri_foaf_mbox_sha1sum, uri_owl_InverseFunctionalProperty)

SWB009+1.p Existential Restriction Entailments

include('Axioms/SWB001+0.ax')

\exists bNODE_x: (iext(uri_ex_p, uri_ex_s, bNODE_x) and iext(uri_rdf_type, bNODE_x, uri_ex_c)) fof(testcase_conclusion_fullish_009 Existential_Restriction_Entailments, axiom)
 \exists bNODE_z: (iext(uri_rdf_type, uri_ex_p, uri_owl_ObjectProperty) and iext(uri_rdf_type, uri_ex_c, uri_owl_Class) and iext(uri_owl_sameAs, uri_ex_s, uri_ex_c))

SWB009+2.p Existential Restriction Entailments

$\forall x, c: (iext(uri_rdf_type, x, c) \iff icext(c, x))$ fof(rdfs_cext_def, axiom)

$\forall z, p, c: ((iext(uri_owl_someValuesFrom, z, c) \text{ and } iext(uri_owl_onProperty, z, p)) \implies \forall x: (icext(z, x) \iff \exists y: (iext(p, x, y) \text{ and } iext(uri_owl_someValuesFrom, z, c))))$ fof(owl_char_somevaluesfrom, axiom)

\exists bNODE_x: (iext(uri_ex_p, uri_ex_s, bNODE_x) and iext(uri_rdf_type, bNODE_x, uri_ex_c)) fof(testcase_conclusion_fullish_009 Existential_Restriction_Entailments, axiom)
 \exists bNODE_z: (iext(uri_rdf_type, uri_ex_p, uri_owl_ObjectProperty) and iext(uri_rdf_type, uri_ex_c, uri_owl_Class) and iext(uri_owl_sameAs, uri_ex_s, uri_ex_c))

SWB009+3.p Existential Restriction Entailments

include('Axioms/SWB002+0.ax')

\exists bNODE_x: (iext(uri_ex_p, uri_ex_s, bNODE_x) and iext(uri_rdf_type, bNODE_x, uri_ex_c)) fof(testcase_conclusion_fullish_009 Existential_Restriction_Entailments, axiom)
 \exists bNODE_z: (iext(uri_rdf_type, uri_ex_p, uri_owl_ObjectProperty) and iext(uri_rdf_type, uri_ex_c, uri_owl_Class) and iext(uri_owl_sameAs, uri_ex_s, uri_ex_c))

SWB009+4.p Existential Restriction Entailments

include('Axioms/SWB003+0.ax')

$\exists \text{bNODE_x: (iext(uri_ex_p, uri_ex_s, bNODE_x) \text{ and } iext(uri_rdf_type, bNODE_x, uri_ex_c))}$ fof(testcase_conclusion_fullish)

$\exists \text{bNODE_z: (iext(uri_rdf_type, uri_ex_p, uri_owl_ObjectProperty) \text{ and } iext(uri_rdf_type, uri_ex_c, uri_owl_Class) \text{ and } iext(uri_rdf_type, uri_ex_s, uri_owl_Class))}$

SWB010+1.p Negative Property Assertions

include('Axioms/SWB001+0.ax')

$\exists \text{bNODE_z: (iext(uri_rdf_type, bNODE_z, uri_owl_NegativePropertyAssertion) \text{ and } iext(uri_owl_sourceIndividual, bNODE_z, uri_owl_Class))}$

$\exists \text{bNODE_x1, bNODE_x2, bNODE_x3, bNODE_x4: (iext(uri_rdf_type, uri_ex_p, uri_owl_ObjectProperty) \text{ and } iext(uri_rdf_type, uri_ex_s, uri_owl_Class))}$

SWB010+2.p Negative Property Assertions

$\forall x: \text{ir}(x)$ fof(simple_ir, axiom)

$\forall x, c: (iext(uri_rdf_type, x, c) \iff icext(c, x))$ fof(rdfs_cext_def, axiom)

$\forall x, y: (iext(uri_owl_sourceIndividual, x, y) \Rightarrow (icext(uri_owl_NegativePropertyAssertion, x) \text{ and } \text{ir}(y)))$ fof(owl_prop_sourceIndividual, axiom)

$\forall x, y: (iext(uri_owl_onProperty, x, y) \Rightarrow (icext(uri_owl_Restriction, x) \text{ and } ip(y)))$ fof(owl_prop_onproperty_ext, axiom)

$\forall z, c: (iext(uri_owl_complementOf, z, c) \Rightarrow (ic(z) \text{ and } ic(c) \text{ and } \forall x: (icext(z, x) \iff \neg icext(c, x))))$ fof(owl_bool_complementOf, axiom)

$\forall z, s_1, a_1: ((iext(uri_rdf_first, s_1, a_1) \text{ and } iext(uri_rdf_rest, s_1, uri_rdf_nil)) \Rightarrow (iext(uri_owl_oneOf, z, s_1) \iff (ic(z) \text{ and } \forall x: (iext(z, x) \iff x = a_1))))$ fof(owl_enum_class001, axiom)

$\forall z, p, c: ((iext(uri_owl_allValuesFrom, z, c) \text{ and } iext(uri_owl_onProperty, z, p)) \Rightarrow \forall x: (icext(z, x) \iff \forall y: (iext(p, x, y) \Rightarrow icext(c, y))))$ fof(owl_restrict_allvaluesfrom, axiom)

$\forall p, a_1, a_2: ((\text{ir}(a_1) \text{ and } ip(p) \text{ and } \text{ir}(a_2) \text{ and } \neg iext(p, a_1, a_2)) \Rightarrow \exists z: (iext(uri_owl_sourceIndividual, z, a_1) \text{ and } iext(uri_owl_sourceIndividual, z, a_2)))$

$\exists \text{bNODE_z: (iext(uri_rdf_type, bNODE_z, uri_owl_NegativePropertyAssertion) \text{ and } iext(uri_owl_sourceIndividual, bNODE_z, uri_owl_Class))}$

$\exists \text{bNODE_x1, bNODE_x2, bNODE_x3, bNODE_x4: (iext(uri_rdf_type, uri_ex_p, uri_owl_ObjectProperty) \text{ and } iext(uri_rdf_type, uri_ex_s, uri_owl_Class))}$

SWB010+3.p Negative Property Assertions

include('Axioms/SWB002+0.ax')

$\exists \text{bNODE_z: (iext(uri_rdf_type, bNODE_z, uri_owl_NegativePropertyAssertion) \text{ and } iext(uri_owl_sourceIndividual, bNODE_z, uri_owl_Class))}$

$\exists \text{bNODE_x1, bNODE_x2, bNODE_x3, bNODE_x4: (iext(uri_rdf_type, uri_ex_p, uri_owl_ObjectProperty) \text{ and } iext(uri_rdf_type, uri_ex_s, uri_owl_Class))}$

SWB010+4.p Negative Property Assertions

include('Axioms/SWB003+0.ax')

$\exists \text{bNODE_z: (iext(uri_rdf_type, bNODE_z, uri_owl_NegativePropertyAssertion) \text{ and } iext(uri_owl_sourceIndividual, bNODE_z, uri_owl_Class))}$

$\exists \text{bNODE_x1, bNODE_x2, bNODE_x3, bNODE_x4: (iext(uri_rdf_type, uri_ex_p, uri_owl_ObjectProperty) \text{ and } iext(uri_rdf_type, uri_ex_s, uri_owl_Class))}$

SWB011+1.p Entity Types as Classes

include('Axioms/SWB001+0.ax')

$iext(uri_owl_disjointWith, uri_owl_Class, uri_owl_ObjectProperty)$ and $iext(uri_rdf_type, uri_ex_x, uri_owl_Class)$ and $iext(uri_rdf_type, uri_ex_y, uri_owl_Class)$

SWB011+2.p Entity Types as Classes

$\forall x, c: (iext(uri_rdf_type, x, c) \iff icext(c, x))$ fof(rdfs_cext_def, axiom)

$\forall c_1, c_2: (iext(uri_owl_disjointWith, c_1, c_2) \iff (ic(c_1) \text{ and } ic(c_2) \text{ and } \forall x: \neg icext(c_1, x) \text{ and } icext(c_2, x)))$ fof(owl_eqdis_disjointWith, axiom)

$iext(uri_owl_disjointWith, uri_owl_Class, uri_owl_ObjectProperty)$ and $iext(uri_rdf_type, uri_ex_x, uri_owl_Class)$ and $iext(uri_rdf_type, uri_ex_y, uri_owl_Class)$

SWB011+3.p Entity Types as Classes

include('Axioms/SWB002+0.ax')

$iext(uri_owl_disjointWith, uri_owl_Class, uri_owl_ObjectProperty)$ and $iext(uri_rdf_type, uri_ex_x, uri_owl_Class)$ and $iext(uri_rdf_type, uri_ex_y, uri_owl_Class)$

SWB011+4.p Entity Types as Classes

include('Axioms/SWB003+0.ax')

$iext(uri_owl_disjointWith, uri_owl_Class, uri_owl_ObjectProperty)$ and $iext(uri_rdf_type, uri_ex_x, uri_owl_Class)$ and $iext(uri_rdf_type, uri_ex_y, uri_owl_Class)$

SWB012+1.p Template Class

include('Axioms/SWB001+0.ax')

$iext(uri_rdf_type, uri_ex_name, uri_owl_FunctionalProperty)$ and $iext(uri_rdf_type, uri_ex_alice, uri_foaf_Person)$ fof(testcase_conclusion_fullish)

$\exists \text{bNODE_l1, bNODE_l2, bNODE_l3, bNODE_r: (iext(uri_rdf_type, uri_foaf_Person, uri_owl_Class) \text{ and } iext(uri_owl_intersectionOf, bNODE_l1, bNODE_l2, bNODE_l3, bNODE_r))}$

SWB012+2.p Template Class

$\forall x, c: (iext(uri_rdf_type, x, c) \iff icext(c, x))$ fof(rdfs_cext_def, axiom)

$\forall p, c, x, y: ((iext(uri_rdfs_domain, p, c) \text{ and } iext(p, x, y)) \Rightarrow icext(c, x))$ fof(rdfs_domain_main, axiom)

$\forall z, s_1, c_1, s_2, c_2, s_3, c_3: ((iext(uri_rdf_first, s_1, c_1) \text{ and } iext(uri_rdf_rest, s_1, s_2) \text{ and } iext(uri_rdf_first, s_2, c_2) \text{ and } iext(uri_rdf_rest, s_2, s_3) \text{ and } iext(uri_rdf_first, s_3, c_3) \text{ and } iext(uri_owl_intersectionOf, z, s_1) \iff (ic(z) \text{ and } ic(c_1) \text{ and } ic(c_2) \text{ and } ic(c_3) \text{ and } \forall x: (icext(z, x) \iff (icext(c_1, x) \text{ and } icext(c_2, x) \text{ and } icext(c_3, x))))$

$\forall z, p, a: ((iext(uri_owl_hasValue, z, a) \text{ and } iext(uri_owl_onProperty, z, p)) \Rightarrow \forall x: (icext(z, x) \iff iext(p, x, a)))$ fof(owl_restrict_hasvalue, axiom)

$iext(uri_rdf_type, uri_ex_name, uri_owl_FunctionalProperty)$ and $iext(uri_rdf_type, uri_ex_alice, uri_foaf_Person)$ fof(testcase_conclusion_fullish)

$\exists \text{bNODE_l1, bNODE_l2, bNODE_l3, bNODE_r: (iext(uri_rdf_type, uri_foaf_Person, uri_owl_Class) \text{ and } iext(uri_owl_intersectionOf, bNODE_l1, bNODE_l2, bNODE_l3, bNODE_r))}$

SWB012+3.p Template Class

include('Axioms/SWB002+0.ax')

iext(uri_rdf_type, uri_ex_name, uri_owl_FunctionalProperty) and iext(uri_rdf_type, uri_ex_alice, uri_foaf_Person) fof(testcase_conclusion_fullish_013.Cliques, conjecture)

\exists bNODE_{L1}, bNODE_{L2}, bNODE_{L3}, bNODE_{Lr}: (iext(uri_rdf_type, uri_foaf_Person, uri_owl_Class) and iext(uri_owl_intersectionOf, uri_ex_alice, uri_ex_alice, uri_owl_Class)))

SWB012+4.p Template Class

include('Axioms/SWB003+0.ax')

iext(uri_rdf_type, uri_ex_name, uri_owl_FunctionalProperty) and iext(uri_rdf_type, uri_ex_alice, uri_foaf_Person) fof(testcase_conclusion_fullish_013.Cliques, conjecture)

\exists bNODE_{L1}, bNODE_{L2}, bNODE_{L3}, bNODE_{Lr}: (iext(uri_rdf_type, uri_foaf_Person, uri_owl_Class) and iext(uri_owl_intersectionOf, uri_ex_alice, uri_ex_alice, uri_owl_Class)))

SWB013+1.p Cliques

include('Axioms/SWB001+0.ax')

iext(uri_foaf_knows, uri_ex_alice, uri_ex_bob) fof(testcase_conclusion_fullish_013.Cliques, conjecture)

\exists bNODE_{Lr}, bNODE_{Li}, bNODE_{L1}, bNODE_{L2}, bNODE_{L3}: (iext(uri_rdf_type, uri_ex_Clique, uri_owl_Class) and iext(uri_rdfs_subClassOf, uri_ex_alice, uri_ex_bob, uri_owl_Class)))

SWB013+2.p Cliques

$\forall x, c: (iext(uri_rdf_type, x, c) \iff icext(c, x))$ fof(rdfs_cext_def, axiom)

$\forall z, p, c: ((iext(uri_owl_someValuesFrom, z, c) and iext(uri_owl_onProperty, z, p)) \Rightarrow \forall x: (icext(z, x) \iff \exists y: (iext(p, x, y) and iext(y, x, z))))$

$\forall c_1, c_2: (iext(uri_rdfs_subClassOf, c_1, c_2) \iff (ic(c_1) and ic(c_2) and \forall x: (icext(c_1, x) \Rightarrow icext(c_2, x))))$ fof(owl_rdfs_cext_subClassOf, axiom)

$\forall p_1, p_2: (iext(uri_rdfs_subPropertyOf, p_1, p_2) \iff (ip(p_1) and ip(p_2) and \forall x, y: (iext(p_1, x, y) \Rightarrow iext(p_2, x, y))))$ fof(owl_rdfs_subPropertyOf, axiom)

$\forall x, y: (iext(uri_owl_sameAs, x, y) \iff x = y)$ fof(owl_eqdis_sameas, axiom)

$\forall p, s_1, p_1, s_2, p_2, s_3, p_3: ((iext(uri_rdf_first, s_1, p_1) and iext(uri_rdf_rest, s_1, s_2) and iext(uri_rdf_first, s_2, p_2) and iext(uri_rdf_rest, s_2, p_3) and iext(uri_owl_propertyChainAxiom, p, s_1) \iff (ip(p) and ip(p_1) and ip(p_2) and ip(p_3) and \forall y_0, y_1, y_2, y_3: ((iext(p_1, y_0, y_1) and iext(p_2, y_1, y_2) and iext(p_3, y_2, y_3))))))$ fof(owl_chain003, axiom)

$\forall p_1, p_2: (iext(uri_owl_inverseOf, p_1, p_2) \iff (ip(p_1) and ip(p_2) and \forall x, y: (iext(p_1, x, y) \iff iext(p_2, y, x))))$ fof(owl_inv, axiom)

iext(uri_foaf_knows, uri_ex_alice, uri_ex_bob) fof(testcase_conclusion_fullish_013.Cliques, conjecture)

\exists bNODE_{Lr}, bNODE_{Li}, bNODE_{L1}, bNODE_{L2}, bNODE_{L3}: (iext(uri_rdf_type, uri_ex_Clique, uri_owl_Class) and iext(uri_rdfs_subClassOf, uri_ex_alice, uri_ex_bob, uri_owl_Class)))

SWB013+3.p Cliques

include('Axioms/SWB002+0.ax')

iext(uri_foaf_knows, uri_ex_alice, uri_ex_bob) fof(testcase_conclusion_fullish_013.Cliques, conjecture)

\exists bNODE_{Lr}, bNODE_{Li}, bNODE_{L1}, bNODE_{L2}, bNODE_{L3}: (iext(uri_rdf_type, uri_ex_Clique, uri_owl_Class) and iext(uri_rdfs_subClassOf, uri_ex_alice, uri_ex_bob, uri_owl_Class)))

SWB013+4.p Cliques

include('Axioms/SWB003+0.ax')

iext(uri_foaf_knows, uri_ex_alice, uri_ex_bob) fof(testcase_conclusion_fullish_013.Cliques, conjecture)

\exists bNODE_{Lr}, bNODE_{Li}, bNODE_{L1}, bNODE_{L2}, bNODE_{L3}: (iext(uri_rdf_type, uri_ex_Clique, uri_owl_Class) and iext(uri_rdfs_subClassOf, uri_ex_alice, uri_ex_bob, uri_owl_Class)))

SWB014+1.p Harry belongs to some Species

include('Axioms/SWB001+0.ax')

\exists bNODE_{Lx}: (iext(uri_rdf_type, uri_ex_harry, bNODE_{Lx}) and iext(uri_rdf_type, bNODE_{Lx}, uri_ex_Species)) fof(testcase_conclusion_fullish_013.Harry, conjecture)

\exists bNODE_{Lu}, bNODE_{L1}, bNODE_{L2}: (iext(uri_rdf_type, uri_ex_Eagle, uri_ex_Species) and iext(uri_rdf_type, uri_ex_Falcon, uri_ex_Species))

SWB014+2.p Harry belongs to some Species

$\forall x, c: (iext(uri_rdf_type, x, c) \iff icext(c, x))$ fof(rdfs_cext_def, axiom)

$\forall z, s_1, c_1, s_2, c_2: ((iext(uri_rdf_first, s_1, c_1) and iext(uri_rdf_rest, s_1, s_2) and iext(uri_rdf_first, s_2, c_2) and iext(uri_rdf_rest, s_2, ur) and iext(uri_owl_unionOf, z, s_1) \iff (ic(z) and ic(c_1) and ic(c_2) and \forall x: (icext(z, x) \iff (icext(c_1, x) or icext(c_2, x))))))$ fof(owl_unionOf, axiom)

\exists bNODE_{Lx}: (iext(uri_rdf_type, uri_ex_harry, bNODE_{Lx}) and iext(uri_rdf_type, bNODE_{Lx}, uri_ex_Species)) fof(testcase_conclusion_fullish_013.Harry, conjecture)

\exists bNODE_{Lu}, bNODE_{L1}, bNODE_{L2}: (iext(uri_rdf_type, uri_ex_Eagle, uri_ex_Species) and iext(uri_rdf_type, uri_ex_Falcon, uri_ex_Species))

SWB014+3.p Harry belongs to some Species

include('Axioms/SWB002+0.ax')

\exists bNODE_{Lx}: (iext(uri_rdf_type, uri_ex_harry, bNODE_{Lx}) and iext(uri_rdf_type, bNODE_{Lx}, uri_ex_Species)) fof(testcase_conclusion_fullish_013.Harry, conjecture)

\exists bNODE_{Lu}, bNODE_{L1}, bNODE_{L2}: (iext(uri_rdf_type, uri_ex_Eagle, uri_ex_Species) and iext(uri_rdf_type, uri_ex_Falcon, uri_ex_Species))

SWB014+4.p Harry belongs to some Species

include('Axioms/SWB003+0.ax')

\exists bNODE_{Lx}: (iext(uri_rdf_type, uri_ex_harry, bNODE_{Lx}) and iext(uri_rdf_type, bNODE_{Lx}, uri_ex_Species)) fof(testcase_conclusion_fullish_013.Harry, conjecture)

\exists bNODE_{Lu}, bNODE_{L1}, bNODE_{L2}: (iext(uri_rdf_type, uri_ex_Eagle, uri_ex_Species) and iext(uri_rdf_type, uri_ex_Falcon, uri_ex_Species))

SWB015+1.p Reflective Tautologies I

include('Axioms/SWB001+0.ax')

iext(uri_owl_sameAs, uri_owl_sameAs, uri_owl_sameAs) fof(testcase_conclusion_fullish_015.Reflective_Tautologies_I, conjecture)

SWB015+2.p Reflective Tautologies I

$\forall x, y: (iext(uri_owl_sameAs, x, y) \iff x = y)$ fof(owl_eqdis_sameas, axiom)

iext(uri_owl_sameAs, uri_owl_sameAs, uri_owl_sameAs) fof(testcase_conclusion_fullish_015.Reflective_Tautologies_I, conjecture)

SWB015+3.p Reflective Tautologies I

include('Axioms/SWB002+0.ax')

iext(uri_owl_sameAs, uri_owl_sameAs, uri_owl_sameAs) fof(testcase_conclusion_fullish_015_Reflective_Tautologies_I, conjecture)

SWB015+4.p Reflective Tautologies I

include('Axioms/SWB003+0.ax')

iext(uri_owl_sameAs, uri_owl_sameAs, uri_owl_sameAs) fof(testcase_conclusion_fullish_015_Reflective_Tautologies_I, conjecture)

SWB016+1.p Reflective Tautologies II

include('Axioms/SWB001+0.ax')

iext(uri_rdfs_subPropertyOf, uri_owl_equivalentClass, uri_rdfs_subClassOf) fof(testcase_conclusion_fullish_016_Reflective_Tautologies_II, conjecture)

SWB016+2.p Reflective Tautologies II $\forall p: (\text{iext}(\text{uri_rdf_type}, p, \text{uri_rdf_Property}) \iff \text{ip}(p))$ fof(rdf_type_ip, axiom) $\forall x, c: (\text{iext}(\text{uri_rdf_type}, x, c) \iff \text{icext}(c, x))$ fof(rdfs_cext_def, axiom) $\forall p, c, x, y: ((\text{iext}(\text{uri_rdfs_domain}, p, c) \text{ and } \text{iext}(p, x, y)) \Rightarrow \text{icext}(c, x))$ fof(rdfs_domain_main, axiom)

iext(uri_rdfs_domain, uri_rdfs_domain, uri_rdf_Property) fof(rdfs_domain_domain, axiom)

iext(uri_rdfs_domain, uri_rdfs_subClassOf, uri_rdfs_Class) fof(rdfs_subclassof_domain, axiom)

ip(uri_owl_equivalentClass) fof(owl_prop_equivalentclass_type, axiom)

 $\forall x, y: (\text{iext}(\text{uri_owl_equivalentClass}, x, y) \Rightarrow (\text{ic}(x) \text{ and } \text{ic}(y)))$ fof(owl_prop_equivalentclass_ext, axiom) $\forall c_1, c_2: (\text{iext}(\text{uri_rdfs_subClassOf}, c_1, c_2) \iff (\text{ic}(c_1) \text{ and } \text{ic}(c_2) \text{ and } \forall x: (\text{icext}(c_1, x) \Rightarrow \text{icext}(c_2, x))))$ fof(owl_rdfs_ext_subclassof, axiom) $\forall p_1, p_2: (\text{iext}(\text{uri_rdfs_subPropertyOf}, p_1, p_2) \iff (\text{ip}(p_1) \text{ and } \text{ip}(p_2) \text{ and } \forall x, y: (\text{iext}(p_1, x, y) \Rightarrow \text{iext}(p_2, x, y))))$ fof(owl_rdfs_ext_subpropertyof, axiom) $\forall c_1, c_2: (\text{iext}(\text{uri_owl_equivalentClass}, c_1, c_2) \iff (\text{ic}(c_1) \text{ and } \text{ic}(c_2) \text{ and } \forall x: (\text{icext}(c_1, x) \iff \text{icext}(c_2, x))))$ fof(owl_eqdis_ext_equivclass, axiom)

iext(uri_rdfs_subPropertyOf, uri_owl_equivalentClass, uri_rdfs_subClassOf) fof(testcase_conclusion_fullish_016_Reflective_Tautologies_II, conjecture)

SWB016+3.p Reflective Tautologies II

include('Axioms/SWB002+0.ax')

iext(uri_rdfs_subPropertyOf, uri_owl_equivalentClass, uri_rdfs_subClassOf) fof(testcase_conclusion_fullish_016_Reflective_Tautologies_II, conjecture)

SWB016+4.p Reflective Tautologies II

include('Axioms/SWB003+0.ax')

iext(uri_rdfs_subPropertyOf, uri_owl_equivalentClass, uri_rdfs_subClassOf) fof(testcase_conclusion_fullish_016_Reflective_Tautologies_II, conjecture)

SWB017+1.p Built-in Based Definitions

include('Axioms/SWB001+0.ax')

iext(uri_owl_differentFrom, uri_ex_w, uri_ex_u) fof(testcase_conclusion_fullish_017_Built_in_Based_Definitions, conjecture)

iext(uri_owl_propertyDisjointWith, uri_ex_notInstanceOf, uri_rdf_type) and iext(uri_rdf_type, uri_ex_w, uri_ex_c) and iext(uri_ex_w, uri_ex_c, uri_ex_u) fof(testcase_conclusion_fullish_017_Built_in_Based_Definitions, conjecture)

SWB017+2.p Built-in Based Definitions $\forall x, y: (\text{iext}(\text{uri_owl_differentFrom}, x, y) \iff x \neq y)$ fof(owl_eqdis_differentfrom, axiom) $\forall p_1, p_2: (\text{iext}(\text{uri_owl_propertyDisjointWith}, p_1, p_2) \iff (\text{ip}(p_1) \text{ and } \text{ip}(p_2) \text{ and } \forall x, y: \neg \text{iext}(p_1, x, y) \text{ and } \text{iext}(p_2, x, y)))$ fof(owl_propertydisjointwith, axiom)

iext(uri_owl_differentFrom, uri_ex_w, uri_ex_u) fof(testcase_conclusion_fullish_017_Built_in_Based_Definitions, conjecture)

iext(uri_owl_propertyDisjointWith, uri_ex_notInstanceOf, uri_rdf_type) and iext(uri_rdf_type, uri_ex_w, uri_ex_c) and iext(uri_ex_w, uri_ex_c, uri_ex_u) fof(testcase_conclusion_fullish_017_Built_in_Based_Definitions, conjecture)

SWB017+3.p Built-in Based Definitions

include('Axioms/SWB002+0.ax')

iext(uri_owl_differentFrom, uri_ex_w, uri_ex_u) fof(testcase_conclusion_fullish_017_Built_in_Based_Definitions, conjecture)

iext(uri_owl_propertyDisjointWith, uri_ex_notInstanceOf, uri_rdf_type) and iext(uri_rdf_type, uri_ex_w, uri_ex_c) and iext(uri_ex_w, uri_ex_c, uri_ex_u) fof(testcase_conclusion_fullish_017_Built_in_Based_Definitions, conjecture)

SWB017+4.p Built-in Based Definitions

include('Axioms/SWB003+0.ax')

iext(uri_owl_differentFrom, uri_ex_w, uri_ex_u) fof(testcase_conclusion_fullish_017_Built_in_Based_Definitions, conjecture)

iext(uri_owl_propertyDisjointWith, uri_ex_notInstanceOf, uri_rdf_type) and iext(uri_rdf_type, uri_ex_w, uri_ex_c) and iext(uri_ex_w, uri_ex_c, uri_ex_u) fof(testcase_conclusion_fullish_017_Built_in_Based_Definitions, conjecture)

SWB018+1.p Modified Logical Vocabulary Semantics

include('Axioms/SWB001+0.ax')

iext(uri_rdf_type, uri_ex_u, uri_ex_Person) fof(testcase_conclusion_fullish_018_Modified_Logical_Vocabulary_Semantics, conjecture)

iext(uri_rdfs_domain, uri_owl_sameAs, uri_ex_Person) and iext(uri_owl_sameAs, uri_ex_w, uri_ex_u) fof(testcase_premise_fullish_018_Modified_Logical_Vocabulary_Semantics, conjecture)

SWB018+2.p Modified Logical Vocabulary Semantics $\forall x, c: (\text{iext}(\text{uri_rdf_type}, x, c) \iff \text{icext}(c, x))$ fof(rdfs_cext_def, axiom) $\forall p, c, x, y: ((\text{iext}(\text{uri_rdfs_domain}, p, c) \text{ and } \text{iext}(p, x, y)) \Rightarrow \text{icext}(c, x))$ fof(rdfs_domain_main, axiom) $\forall x, y: (\text{iext}(\text{uri_owl_sameAs}, x, y) \iff x = y)$ fof(owl_eqdis_sameas, axiom)

iext(uri_rdf_type, uri_ex_u, uri_ex_Person) fof(testcase_conclusion_fullish_018_Modified_Logical_Vocabulary_Semantics, conjecture)

iext(uri_rdfs_domain, uri_owl_sameAs, uri_ex_Person) and iext(uri_owl_sameAs, uri_ex_w, uri_ex_u) fof(testcase_premise_fullish_018_Modified_Logical_Vocabulary_Semantics, conjecture)

SWB018+3.p Modified Logical Vocabulary Semantics

include('Axioms/SWB002+0.ax')

iext(uri_rdf_type, uri_ex_u, uri_ex_Person) fof(testcase_conclusion_fullish_018_Modified_Logical_Vocabulary_Semantics, conj)

iext(uri_rdfs_domain, uri_owl_sameAs, uri_ex_Person) and iext(uri_owl_sameAs, uri_ex_w, uri_ex_u) fof(testcase_premise_fullish_018_Modified_Logical_Vocabulary_Semantics, conj)

SWB018+4.p Modified Logical Vocabulary Semantics

include('Axioms/SWB003+0.ax')

iext(uri_rdf_type, uri_ex_u, uri_ex_Person) fof(testcase_conclusion_fullish_018_Modified_Logical_Vocabulary_Semantics, conj)

iext(uri_rdfs_domain, uri_owl_sameAs, uri_ex_Person) and iext(uri_owl_sameAs, uri_ex_w, uri_ex_u) fof(testcase_premise_fullish_018_Modified_Logical_Vocabulary_Semantics, conj)

SWB019+1.p Disjoint Annotation Properties

include('Axioms/SWB001+0.ax')

iext(uri_rdf_type, uri_skos_prefLabel, uri_owl_AnnotationProperty) and iext(uri_rdfs_subPropertyOf, uri_skos_prefLabel, uri_owl_AnnotationProperty)

SWB019+2.p Disjoint Annotation Properties

$\forall p_1, p_2: (iext(uri_owl_propertyDisjointWith, p_1, p_2) \iff (ip(p_1) \text{ and } ip(p_2) \text{ and } \forall x, y: \neg iext(p_1, x, y) \text{ and } iext(p_2, x, y)))$

iext(uri_rdf_type, uri_skos_prefLabel, uri_owl_AnnotationProperty) and iext(uri_rdfs_subPropertyOf, uri_skos_prefLabel, uri_owl_AnnotationProperty)

SWB019+3.p Disjoint Annotation Properties

include('Axioms/SWB002+0.ax')

iext(uri_rdf_type, uri_skos_prefLabel, uri_owl_AnnotationProperty) and iext(uri_rdfs_subPropertyOf, uri_skos_prefLabel, uri_owl_AnnotationProperty)

SWB019+4.p Disjoint Annotation Properties

include('Axioms/SWB003+0.ax')

iext(uri_rdf_type, uri_skos_prefLabel, uri_owl_AnnotationProperty) and iext(uri_rdfs_subPropertyOf, uri_skos_prefLabel, uri_owl_AnnotationProperty)

SWB020+1.p Logical Complications

include('Axioms/SWB001+0.ax')

iext(uri_rdfs_subClassOf, uri_ex_d, uri_ex_c3) fof(testcase_conclusion_fullish_020_Logical_Complications, conjecture)

$\exists bNODE_xs, bNODE_xc, bNODE_lu_1, bNODE_lu_2, bNODE_lu_3, bNODE_li_1, bNODE_li_2: (iext(uri_owl_unionOf, uri_ex_c, bNODE_xs, bNODE_xc, bNODE_lu_1, bNODE_lu_2, bNODE_lu_3, bNODE_li_1, bNODE_li_2))$

SWB020+2.p Logical Complications

$\forall x, y: (iext(uri_owl_disjointWith, x, y) \Rightarrow (ic(x) \text{ and } ic(y)))$ fof(owl_prop_disjointwith_ext, axiom)

$\forall z, c: (iext(uri_owl_complementOf, z, c) \Rightarrow (ic(z) \text{ and } ic(c) \text{ and } \forall x: (icext(z, x) \iff \neg icext(c, x))))$ fof(owl_bool_complement, axiom)

$\forall z, s_1, c_1, s_2, c_2: ((iext(uri_rdf_first, s_1, c_1) \text{ and } iext(uri_rdf_rest, s_1, s_2) \text{ and } iext(uri_rdf_first, s_2, c_2) \text{ and } iext(uri_rdf_rest, s_2, s_1)) \iff (ic(z) \text{ and } ic(c_1) \text{ and } ic(c_2) \text{ and } \forall x: (icext(z, x) \iff (icext(c_1, x) \text{ and } icext(c_2, x))))))$ fof(owl_rdf_disjoint, axiom)

$\forall z, s_1, c_1, s_2, c_2, s_3, c_3: ((iext(uri_rdf_first, s_1, c_1) \text{ and } iext(uri_rdf_rest, s_1, s_2) \text{ and } iext(uri_rdf_first, s_2, c_2) \text{ and } iext(uri_rdf_rest, s_2, s_3) \text{ and } iext(uri_rdf_first, s_3, c_3) \text{ and } iext(uri_rdf_rest, s_3, s_1)) \iff (ic(z) \text{ and } ic(c_1) \text{ and } ic(c_2) \text{ and } ic(c_3) \text{ and } \forall x: (icext(z, x) \iff (icext(c_1, x) \text{ or } icext(c_2, x) \text{ or } icext(c_3, x))))))$ fof(owl_rdf_disjoint, axiom)

$\forall c_1, c_2: (iext(uri_rdfs_subClassOf, c_1, c_2) \iff (ic(c_1) \text{ and } ic(c_2) \text{ and } \forall x: (icext(c_1, x) \Rightarrow icext(c_2, x))))$ fof(owl_rdfsext_subclass, axiom)

$\forall c_1, c_2: (iext(uri_owl_disjointWith, c_1, c_2) \iff (ic(c_1) \text{ and } ic(c_2) \text{ and } \forall x: \neg icext(c_1, x) \text{ and } icext(c_2, x)))$ fof(owl_eqdisjoint, axiom)

iext(uri_rdfs_subClassOf, uri_ex_d, uri_ex_c3) fof(testcase_conclusion_fullish_020_Logical_Complications, conjecture)

$\exists bNODE_xs, bNODE_xc, bNODE_lu_1, bNODE_lu_2, bNODE_lu_3, bNODE_li_1, bNODE_li_2: (iext(uri_owl_unionOf, uri_ex_c, bNODE_xs, bNODE_xc, bNODE_lu_1, bNODE_lu_2, bNODE_lu_3, bNODE_li_1, bNODE_li_2))$

$\exists bNODE_xs, bNODE_xc, bNODE_lu_1, bNODE_lu_2, bNODE_lu_3, bNODE_li_1, bNODE_li_2: (iext(uri_owl_unionOf, uri_ex_c, bNODE_xs, bNODE_xc, bNODE_lu_1, bNODE_lu_2, bNODE_lu_3, bNODE_li_1, bNODE_li_2))$

SWB020+3.p Logical Complications

include('Axioms/SWB002+0.ax')

iext(uri_rdfs_subClassOf, uri_ex_d, uri_ex_c3) fof(testcase_conclusion_fullish_020_Logical_Complications, conjecture)

$\exists bNODE_xs, bNODE_xc, bNODE_lu_1, bNODE_lu_2, bNODE_lu_3, bNODE_li_1, bNODE_li_2: (iext(uri_owl_unionOf, uri_ex_c, bNODE_xs, bNODE_xc, bNODE_lu_1, bNODE_lu_2, bNODE_lu_3, bNODE_li_1, bNODE_li_2))$

SWB020+4.p Logical Complications

include('Axioms/SWB003+0.ax')

iext(uri_rdfs_subClassOf, uri_ex_d, uri_ex_c3) fof(testcase_conclusion_fullish_020_Logical_Complications, conjecture)

$\exists bNODE_xs, bNODE_xc, bNODE_lu_1, bNODE_lu_2, bNODE_lu_3, bNODE_li_1, bNODE_li_2: (iext(uri_owl_unionOf, uri_ex_c, bNODE_xs, bNODE_xc, bNODE_lu_1, bNODE_lu_2, bNODE_lu_3, bNODE_li_1, bNODE_li_2))$

SWB021+1.p Composite Enumerations

include('Axioms/SWB001+0.ax')

iext(uri_owl_equivalentClass, uri_ex_c3, uri_ex_c4) fof(testcase_conclusion_fullish_021_Composite_Enumerations, conjecture)

$\exists bNODE_l_{11}, bNODE_l_{12}, bNODE_l_{21}, bNODE_l_{22}, bNODE_l_{31}, bNODE_l_{32}, bNODE_l_{33}, bNODE_l_{41}, bNODE_l_{42}: (iext(uri_owl_equivalentClass, uri_ex_c3, uri_ex_c4, bNODE_l_{11}, bNODE_l_{12}, bNODE_l_{21}, bNODE_l_{22}, bNODE_l_{31}, bNODE_l_{32}, bNODE_l_{33}, bNODE_l_{41}, bNODE_l_{42}))$

SWB021+2.p Composite Enumerations

$\forall x, y: (iext(uri_owl_oneOf, x, y) \Rightarrow (ic(x) \text{ and } icext(uri_rdf_List, y)))$ fof(owl_prop_oneof_ext, axiom)

$\forall x, y: (iext(uri_owl_unionOf, x, y) \Rightarrow (ic(x) \text{ and } icext(uri_rdf_List, y)))$ fof(owl_prop_unionof_ext, axiom)

$\forall z, s_1, c_1, s_2, c_2: ((iext(uri_rdf_first, s_1, c_1) \text{ and } iext(uri_rdf_rest, s_1, s_2) \text{ and } iext(uri_rdf_first, s_2, c_2) \text{ and } iext(uri_rdf_rest, s_2, s_1)) \iff (ic(z) \text{ and } ic(c_1) \text{ and } ic(c_2) \text{ and } \forall x: (icext(z, x) \iff (icext(c_1, x) \text{ or } icext(c_2, x))))))$ fof(owl_rdf_disjoint, axiom)

$\forall z, s_1, a_1, s_2, a_2: ((iext(uri_rdf_first, s_1, a_1) \text{ and } iext(uri_rdf_rest, s_1, s_2) \text{ and } iext(uri_rdf_first, s_2, a_2) \text{ and } iext(uri_rdf_rest, s_2, s_1)) \iff (ic(z) \text{ and } \forall x: (icext(z, x) \iff (x = a_1 \text{ or } x = a_2))))$ fof(owl_enum_class002, axiom)

$\forall z, s_1, a_1, s_2, a_2, s_3, a_3: ((iext(uri_rdf_first, s_1, a_1) \text{ and } iext(uri_rdf_rest, s_1, s_2) \text{ and } iext(uri_rdf_first, s_2, a_2) \text{ and } iext(uri_rdf_rest, s_2, s_3) \text{ and } iext(uri_rdf_first, s_3, a_3) \text{ and } iext(uri_rdf_rest, s_3, s_1)) \iff (ic(z) \text{ and } \forall x: (icext(z, x) \iff (x = a_1 \text{ or } x = a_2 \text{ or } x = a_3))))$ fof(owl_enum_class003, axiom)

$\forall z, s_1, a_1, s_2, a_2, s_3, a_3: ((iext(uri_rdf_first, s_1, a_1) \text{ and } iext(uri_rdf_rest, s_1, s_2) \text{ and } iext(uri_rdf_first, s_2, a_2) \text{ and } iext(uri_rdf_rest, s_2, s_3) \text{ and } iext(uri_rdf_first, s_3, a_3) \text{ and } iext(uri_rdf_rest, s_3, s_1)) \iff (ic(z) \text{ and } \forall x: (icext(z, x) \iff (x = a_1 \text{ or } x = a_2 \text{ or } x = a_3))))$ fof(owl_enum_class003, axiom)

$\forall z, s_1, a_1, s_2, a_2, s_3, a_3: ((iext(uri_rdf_first, s_1, a_1) \text{ and } iext(uri_rdf_rest, s_1, s_2) \text{ and } iext(uri_rdf_first, s_2, a_2) \text{ and } iext(uri_rdf_rest, s_2, s_3) \text{ and } iext(uri_rdf_first, s_3, a_3) \text{ and } iext(uri_rdf_rest, s_3, s_1)) \iff (ic(z) \text{ and } \forall x: (icext(z, x) \iff (x = a_1 \text{ or } x = a_2 \text{ or } x = a_3))))$ fof(owl_enum_class003, axiom)

$\forall z, s_1, a_1, s_2, a_2, s_3, a_3: ((iext(uri_rdf_first, s_1, a_1) \text{ and } iext(uri_rdf_rest, s_1, s_2) \text{ and } iext(uri_rdf_first, s_2, a_2) \text{ and } iext(uri_rdf_rest, s_2, s_3) \text{ and } iext(uri_rdf_first, s_3, a_3) \text{ and } iext(uri_rdf_rest, s_3, s_1)) \iff (ic(z) \text{ and } \forall x: (icext(z, x) \iff (x = a_1 \text{ or } x = a_2 \text{ or } x = a_3))))$ fof(owl_enum_class003, axiom)

$\forall c_1, c_2: (\text{iext}(\text{uri_owl_equivalentClass}, c_1, c_2) \iff (\text{ic}(c_1) \text{ and } \text{ic}(c_2) \text{ and } \forall x: (\text{icext}(c_1, x) \iff \text{icext}(c_2, x))))$ fof(owl_equivalentClass, uri_ex_c3, uri_ex_c4) fof(testcase_conclusion_fullish_021_Composite_Enumerations, conjecture)
 $\exists \text{bNODE_l}_{11}, \text{bNODE_l}_{12}, \text{bNODE_l}_{21}, \text{bNODE_l}_{22}, \text{bNODE_l}_{31}, \text{bNODE_l}_{32}, \text{bNODE_l}_{33}, \text{bNODE_l}_{41}, \text{bNODE_l}_{42}: (\text{iext}(\text{uri_owl_equivalentClass}, \text{uri_ex_c}_3, \text{uri_ex_c}_4) \iff (\text{ic}(\text{bNODE_l}_{11}) \text{ and } \text{ic}(\text{bNODE_l}_{12}) \text{ and } \text{ic}(\text{bNODE_l}_{21}) \text{ and } \text{ic}(\text{bNODE_l}_{22}) \text{ and } \text{ic}(\text{bNODE_l}_{31}) \text{ and } \text{ic}(\text{bNODE_l}_{32}) \text{ and } \text{ic}(\text{bNODE_l}_{33}) \text{ and } \text{ic}(\text{bNODE_l}_{41}) \text{ and } \text{ic}(\text{bNODE_l}_{42})))$

SWB021+3.p Composite Enumerations

include('Axioms/SWB002+0.ax')

$\text{iext}(\text{uri_owl_equivalentClass}, \text{uri_ex_c}_3, \text{uri_ex_c}_4)$ fof(testcase_conclusion_fullish_021_Composite_Enumerations, conjecture)
 $\exists \text{bNODE_l}_{11}, \text{bNODE_l}_{12}, \text{bNODE_l}_{21}, \text{bNODE_l}_{22}, \text{bNODE_l}_{31}, \text{bNODE_l}_{32}, \text{bNODE_l}_{33}, \text{bNODE_l}_{41}, \text{bNODE_l}_{42}: (\text{iext}(\text{uri_owl_equivalentClass}, \text{uri_ex_c}_3, \text{uri_ex_c}_4) \iff (\text{ic}(\text{bNODE_l}_{11}) \text{ and } \text{ic}(\text{bNODE_l}_{12}) \text{ and } \text{ic}(\text{bNODE_l}_{21}) \text{ and } \text{ic}(\text{bNODE_l}_{22}) \text{ and } \text{ic}(\text{bNODE_l}_{31}) \text{ and } \text{ic}(\text{bNODE_l}_{32}) \text{ and } \text{ic}(\text{bNODE_l}_{33}) \text{ and } \text{ic}(\text{bNODE_l}_{41}) \text{ and } \text{ic}(\text{bNODE_l}_{42})))$

SWB021+4.p Composite Enumerations

include('Axioms/SWB003+0.ax')

$\text{iext}(\text{uri_owl_equivalentClass}, \text{uri_ex_c}_3, \text{uri_ex_c}_4)$ fof(testcase_conclusion_fullish_021_Composite_Enumerations, conjecture)
 $\exists \text{bNODE_l}_{11}, \text{bNODE_l}_{12}, \text{bNODE_l}_{21}, \text{bNODE_l}_{22}, \text{bNODE_l}_{31}, \text{bNODE_l}_{32}, \text{bNODE_l}_{33}, \text{bNODE_l}_{41}, \text{bNODE_l}_{42}: (\text{iext}(\text{uri_owl_equivalentClass}, \text{uri_ex_c}_3, \text{uri_ex_c}_4) \iff (\text{ic}(\text{bNODE_l}_{11}) \text{ and } \text{ic}(\text{bNODE_l}_{12}) \text{ and } \text{ic}(\text{bNODE_l}_{21}) \text{ and } \text{ic}(\text{bNODE_l}_{22}) \text{ and } \text{ic}(\text{bNODE_l}_{31}) \text{ and } \text{ic}(\text{bNODE_l}_{32}) \text{ and } \text{ic}(\text{bNODE_l}_{33}) \text{ and } \text{ic}(\text{bNODE_l}_{41}) \text{ and } \text{ic}(\text{bNODE_l}_{42})))$

SWB022+1.p List Member Access

include('Axioms/SWB001+0.ax')

$\text{iext}(\text{uri_skos_member}, \text{uri_ex_MyOrderedCollection}, \text{uri_ex_X})$ and $\text{iext}(\text{uri_skos_member}, \text{uri_ex_MyOrderedCollection}, \text{uri_ex_Y})$
 $\exists \text{bNODE_pL}, \text{bNODE_l}_{11}, \text{bNODE_l}_{12}, \text{bNODE_l}_{21}, \text{bNODE_l}_{22}, \text{bNODE_l}_{31}, \text{bNODE_l}_{32}, \text{bNODE_l}_{33}: (\text{iext}(\text{uri_rdfs_subPropertyOf}, \text{uri_ex_X}, \text{uri_ex_Y}) \iff (\text{ic}(\text{bNODE_pL}) \text{ and } \text{ic}(\text{bNODE_l}_{11}) \text{ and } \text{ic}(\text{bNODE_l}_{12}) \text{ and } \text{ic}(\text{bNODE_l}_{21}) \text{ and } \text{ic}(\text{bNODE_l}_{22}) \text{ and } \text{ic}(\text{bNODE_l}_{31}) \text{ and } \text{ic}(\text{bNODE_l}_{32}) \text{ and } \text{ic}(\text{bNODE_l}_{33})))$

SWB022+2.p List Member Access

$\forall p, q: (\text{iext}(\text{uri_rdfs_subPropertyOf}, p, q) \Rightarrow (\text{ip}(p) \text{ and } \text{ip}(q) \text{ and } \forall x, y: (\text{iext}(p, x, y) \Rightarrow \text{iext}(q, x, y))))$ fof(rdfs_subPropertyOf, uri_ex_X, uri_ex_Y)
 $\forall p, s_1, p_1, s_2, p_2: ((\text{iext}(\text{uri_rdf_first}, s_1, p_1) \text{ and } \text{iext}(\text{uri_rdf_rest}, s_1, s_2) \text{ and } \text{iext}(\text{uri_rdf_first}, s_2, p_2) \text{ and } \text{iext}(\text{uri_rdf_rest}, s_2, p_1)) \iff (\text{iext}(\text{uri_owl_propertyChainAxiom}, p, s_1) \iff (\text{ip}(p) \text{ and } \text{ip}(p_1) \text{ and } \text{ip}(p_2) \text{ and } \forall y_0, y_1, y_2: ((\text{iext}(p_1, y_0, y_1) \text{ and } \text{iext}(p_2, y_1, y_2) \text{ and } \text{iext}(p, y_0, y_2))))))$ fof(owl_chain002, axiom)

$\text{iext}(\text{uri_skos_member}, \text{uri_ex_MyOrderedCollection}, \text{uri_ex_X})$ and $\text{iext}(\text{uri_skos_member}, \text{uri_ex_MyOrderedCollection}, \text{uri_ex_Y})$
 $\exists \text{bNODE_pL}, \text{bNODE_l}_{11}, \text{bNODE_l}_{12}, \text{bNODE_l}_{21}, \text{bNODE_l}_{22}, \text{bNODE_l}_{31}, \text{bNODE_l}_{32}, \text{bNODE_l}_{33}: (\text{iext}(\text{uri_rdfs_subPropertyOf}, \text{uri_ex_X}, \text{uri_ex_Y}) \iff (\text{ic}(\text{bNODE_pL}) \text{ and } \text{ic}(\text{bNODE_l}_{11}) \text{ and } \text{ic}(\text{bNODE_l}_{12}) \text{ and } \text{ic}(\text{bNODE_l}_{21}) \text{ and } \text{ic}(\text{bNODE_l}_{22}) \text{ and } \text{ic}(\text{bNODE_l}_{31}) \text{ and } \text{ic}(\text{bNODE_l}_{32}) \text{ and } \text{ic}(\text{bNODE_l}_{33})))$

SWB022+3.p List Member Access

include('Axioms/SWB002+0.ax')

$\text{iext}(\text{uri_skos_member}, \text{uri_ex_MyOrderedCollection}, \text{uri_ex_X})$ and $\text{iext}(\text{uri_skos_member}, \text{uri_ex_MyOrderedCollection}, \text{uri_ex_Y})$
 $\exists \text{bNODE_pL}, \text{bNODE_l}_{11}, \text{bNODE_l}_{12}, \text{bNODE_l}_{21}, \text{bNODE_l}_{22}, \text{bNODE_l}_{31}, \text{bNODE_l}_{32}, \text{bNODE_l}_{33}: (\text{iext}(\text{uri_rdfs_subPropertyOf}, \text{uri_ex_X}, \text{uri_ex_Y}) \iff (\text{ic}(\text{bNODE_pL}) \text{ and } \text{ic}(\text{bNODE_l}_{11}) \text{ and } \text{ic}(\text{bNODE_l}_{12}) \text{ and } \text{ic}(\text{bNODE_l}_{21}) \text{ and } \text{ic}(\text{bNODE_l}_{22}) \text{ and } \text{ic}(\text{bNODE_l}_{31}) \text{ and } \text{ic}(\text{bNODE_l}_{32}) \text{ and } \text{ic}(\text{bNODE_l}_{33})))$

SWB022+4.p List Member Access

include('Axioms/SWB003+0.ax')

$\text{iext}(\text{uri_skos_member}, \text{uri_ex_MyOrderedCollection}, \text{uri_ex_X})$ and $\text{iext}(\text{uri_skos_member}, \text{uri_ex_MyOrderedCollection}, \text{uri_ex_Y})$
 $\exists \text{bNODE_pL}, \text{bNODE_l}_{11}, \text{bNODE_l}_{12}, \text{bNODE_l}_{21}, \text{bNODE_l}_{22}, \text{bNODE_l}_{31}, \text{bNODE_l}_{32}, \text{bNODE_l}_{33}: (\text{iext}(\text{uri_rdfs_subPropertyOf}, \text{uri_ex_X}, \text{uri_ex_Y}) \iff (\text{ic}(\text{bNODE_pL}) \text{ and } \text{ic}(\text{bNODE_l}_{11}) \text{ and } \text{ic}(\text{bNODE_l}_{12}) \text{ and } \text{ic}(\text{bNODE_l}_{21}) \text{ and } \text{ic}(\text{bNODE_l}_{22}) \text{ and } \text{ic}(\text{bNODE_l}_{31}) \text{ and } \text{ic}(\text{bNODE_l}_{32}) \text{ and } \text{ic}(\text{bNODE_l}_{33})))$

SWB023+1.p Unique List Components

include('Axioms/SWB001+0.ax')

$\text{iext}(\text{uri_owl_sameAs}, \text{uri_ex_w}, \text{uri_ex_u})$ and $\text{iext}(\text{uri_owl_sameAs}, \text{uri_ex_w}, \text{uri_ex_v})$ fof(testcase_conclusion_fullish_023_UniqueListComponents, axiom)
 $\exists \text{bNODE_o}, \text{bNODE_l}: (\text{iext}(\text{uri_rdf_type}, \text{uri_rdf_first}, \text{uri_owl_FunctionalProperty}) \text{ and } \text{iext}(\text{uri_rdf_type}, \text{uri_ex_w}, \text{bNODE_o}))$

SWB023+2.p Unique List Components

$\forall x, c: (\text{iext}(\text{uri_rdf_type}, x, c) \iff \text{icext}(c, x))$ fof(rdfs_cext_def, axiom)

$\forall z, s_1, a_1: ((\text{iext}(\text{uri_rdf_first}, s_1, a_1) \text{ and } \text{iext}(\text{uri_rdf_rest}, s_1, \text{uri_rdf_nil})) \Rightarrow (\text{iext}(\text{uri_owl_oneOf}, z, s_1) \iff (\text{ic}(z) \text{ and } \forall x: (\text{iext}(z, x, a_1) \iff \text{icext}(z, x))))))$ fof(owl_enum_class001, axiom)

$\forall p: (\text{icext}(\text{uri_owl_FunctionalProperty}, p) \iff (\text{ip}(p) \text{ and } \forall x, y_1, y_2: ((\text{iext}(p, x, y_1) \text{ and } \text{iext}(p, x, y_2)) \Rightarrow y_1 = y_2)))$ fof(owl_char_functional, axiom)

$\forall x, y: (\text{iext}(\text{uri_owl_sameAs}, x, y) \iff x = y)$ fof(owl_eqdis_sameas, axiom)

$\text{iext}(\text{uri_owl_sameAs}, \text{uri_ex_w}, \text{uri_ex_u})$ and $\text{iext}(\text{uri_owl_sameAs}, \text{uri_ex_w}, \text{uri_ex_v})$ fof(testcase_conclusion_fullish_023_UniqueListComponents, axiom)
 $\exists \text{bNODE_o}, \text{bNODE_l}: (\text{iext}(\text{uri_rdf_type}, \text{uri_rdf_first}, \text{uri_owl_FunctionalProperty}) \text{ and } \text{iext}(\text{uri_rdf_type}, \text{uri_ex_w}, \text{bNODE_o}))$

SWB023+3.p Unique List Components

include('Axioms/SWB002+0.ax')

$\text{iext}(\text{uri_owl_sameAs}, \text{uri_ex_w}, \text{uri_ex_u})$ and $\text{iext}(\text{uri_owl_sameAs}, \text{uri_ex_w}, \text{uri_ex_v})$ fof(testcase_conclusion_fullish_023_UniqueListComponents, axiom)
 $\exists \text{bNODE_o}, \text{bNODE_l}: (\text{iext}(\text{uri_rdf_type}, \text{uri_rdf_first}, \text{uri_owl_FunctionalProperty}) \text{ and } \text{iext}(\text{uri_rdf_type}, \text{uri_ex_w}, \text{bNODE_o}))$

SWB023+4.p Unique List Components

include('Axioms/SWB003+0.ax')

$\text{iext}(\text{uri_owl_sameAs}, \text{uri_ex_w}, \text{uri_ex_u})$ and $\text{iext}(\text{uri_owl_sameAs}, \text{uri_ex_w}, \text{uri_ex_v})$ fof(testcase_conclusion_fullish_023_UniqueListComponents, axiom)
 $\exists \text{bNODE_o}, \text{bNODE_l}: (\text{iext}(\text{uri_rdf_type}, \text{uri_rdf_first}, \text{uri_owl_FunctionalProperty}) \text{ and } \text{iext}(\text{uri_rdf_type}, \text{uri_ex_w}, \text{bNODE_o}))$

SWB024+1.p Cardinality Restrictions on Complex Properties

include('Axioms/SWB001+0.ax')

$\exists \text{bNODE_x}: (\text{iext}(\text{uri_ex_hasAncestor}, \text{uri_ex_bob}, \text{bNODE_x}) \text{ and } \text{iext}(\text{uri_ex_hasAncestor}, \text{uri_ex_alice}, \text{bNODE_x}))$ fof(testcase_conclusion_fullish_024_CardinalityRestrictions, axiom)
 $\exists \text{bNODE_z}: (\text{iext}(\text{uri_rdf_type}, \text{uri_ex_hasAncestor}, \text{uri_owl_TransitiveProperty}) \text{ and } \text{iext}(\text{uri_rdfs_subclassOf}, \text{uri_ex_Person}, \text{uri_ex_hasAncestor}))$

SWB024+2.p Cardinality Restrictions on Complex Properties

$\forall x, c: (\text{iext}(\text{uri_rdf_type}, x, c) \iff \text{icext}(c, x)) \quad \text{fof}(\text{rdfs_cext_def}, \text{axiom})$
 $\forall z, p: ((\text{iext}(\text{uri_owl_minCardinality}, z, \text{literal_typed}(\text{dat_str}_1, \text{uri_xsd_nonNegativeInteger})) \text{ and } \text{iext}(\text{uri_owl_onProperty}, z, p))$
 $\forall x: (\text{icext}(z, x) \iff \exists y: \text{iext}(p, x, y))) \quad \text{fof}(\text{owl_restrict_mincard}_{001}, \text{axiom})$
 $\forall c_1, c_2: (\text{iext}(\text{uri_rdfs_subClassOf}, c_1, c_2) \iff (\text{ic}(c_1) \text{ and } \text{ic}(c_2) \text{ and } \forall x: (\text{icext}(c_1, x) \Rightarrow \text{icext}(c_2, x)))) \quad \text{fof}(\text{owl_rdfs_ext_su}$
 $\forall p: (\text{icext}(\text{uri_owl_TransitiveProperty}, p) \iff (\text{ip}(p) \text{ and } \forall x, y, z: ((\text{iext}(p, x, y) \text{ and } \text{iext}(p, y, z)) \Rightarrow \text{iext}(p, x, z)))) \quad \text{fof}(\text{ov}$
 $\exists \text{bNODE_x}: (\text{iext}(\text{uri_ex_hasAncestor}, \text{uri_ex_bob}, \text{bNODE_x}) \text{ and } \text{iext}(\text{uri_ex_hasAncestor}, \text{uri_ex_alice}, \text{bNODE_x})) \quad \text{fof}(\text{te}$
 $\exists \text{bNODE_z}: (\text{iext}(\text{uri_rdf_type}, \text{uri_ex_hasAncestor}, \text{uri_owl_TransitiveProperty}) \text{ and } \text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_ex_Person}, \text{b}$

SWB024+3.p Cardinality Restrictions on Complex Properties

$\text{include}(\text{'Axioms/SWB002+0.ax'})$
 $\exists \text{bNODE_x}: (\text{iext}(\text{uri_ex_hasAncestor}, \text{uri_ex_bob}, \text{bNODE_x}) \text{ and } \text{iext}(\text{uri_ex_hasAncestor}, \text{uri_ex_alice}, \text{bNODE_x})) \quad \text{fof}(\text{te}$
 $\exists \text{bNODE_z}: (\text{iext}(\text{uri_rdf_type}, \text{uri_ex_hasAncestor}, \text{uri_owl_TransitiveProperty}) \text{ and } \text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_ex_Person}, \text{b}$

SWB024+4.p Cardinality Restrictions on Complex Properties

$\text{include}(\text{'Axioms/SWB003+0.ax'})$
 $\exists \text{bNODE_x}: (\text{iext}(\text{uri_ex_hasAncestor}, \text{uri_ex_bob}, \text{bNODE_x}) \text{ and } \text{iext}(\text{uri_ex_hasAncestor}, \text{uri_ex_alice}, \text{bNODE_x})) \quad \text{fof}(\text{te}$
 $\exists \text{bNODE_z}: (\text{iext}(\text{uri_rdf_type}, \text{uri_ex_hasAncestor}, \text{uri_owl_TransitiveProperty}) \text{ and } \text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_ex_Person}, \text{b}$

SWB025+1.p Cyclic Dependencies between Complex Properties

$\text{include}(\text{'Axioms/SWB001+0.ax'})$
 $\text{iext}(\text{uri_ex_hasUncle}, \text{uri_ex_alice}, \text{uri_ex_charly}) \text{ and } \text{iext}(\text{uri_ex_hasCousin}, \text{uri_ex_bob}, \text{uri_ex_alice}) \quad \text{fof}(\text{testcase_conclusion}$
 $\exists \text{bNODE_l}_{11}, \text{bNODE_l}_{12}, \text{bNODE_l}_{21}, \text{bNODE_l}_{22}, \text{bNODE_l}_3: (\text{iext}(\text{uri_owl_propertyChainAxiom}, \text{uri_ex_hasUncle}, \text{bNODE_l}$

SWB025+2.p Cyclic Dependencies between Complex Properties

$\forall p, s_1, p_1, s_2, p_2: ((\text{iext}(\text{uri_rdf_first}, s_1, p_1) \text{ and } \text{iext}(\text{uri_rdf_rest}, s_1, s_2) \text{ and } \text{iext}(\text{uri_rdf_first}, s_2, p_2) \text{ and } \text{iext}(\text{uri_rdf_rest}, s_2, \text{ur}$
 $(\text{iext}(\text{uri_owl_propertyChainAxiom}, p, s_1) \iff (\text{ip}(p) \text{ and } \text{ip}(p_1) \text{ and } \text{ip}(p_2) \text{ and } \forall y_0, y_1, y_2: ((\text{iext}(p_1, y_0, y_1) \text{ and } \text{iext}(p_2, y_1, y_2)$
 $\text{iext}(p, y_0, y_2)))) \quad \text{fof}(\text{owl_chain}_{002}, \text{axiom})$
 $\forall p_1, p_2: (\text{iext}(\text{uri_owl_inverseOf}, p_1, p_2) \iff (\text{ip}(p_1) \text{ and } \text{ip}(p_2) \text{ and } \forall x, y: (\text{iext}(p_1, x, y) \iff \text{iext}(p_2, y, x)))) \quad \text{fof}(\text{owl_inv}$
 $\text{iext}(\text{uri_ex_hasUncle}, \text{uri_ex_alice}, \text{uri_ex_charly}) \text{ and } \text{iext}(\text{uri_ex_hasCousin}, \text{uri_ex_bob}, \text{uri_ex_alice}) \quad \text{fof}(\text{testcase_conclusion}$
 $\exists \text{bNODE_l}_{11}, \text{bNODE_l}_{12}, \text{bNODE_l}_{21}, \text{bNODE_l}_{22}, \text{bNODE_l}_3: (\text{iext}(\text{uri_owl_propertyChainAxiom}, \text{uri_ex_hasUncle}, \text{bNODE_l}$

SWB025+3.p Cyclic Dependencies between Complex Properties

$\text{include}(\text{'Axioms/SWB002+0.ax'})$
 $\text{iext}(\text{uri_ex_hasUncle}, \text{uri_ex_alice}, \text{uri_ex_charly}) \text{ and } \text{iext}(\text{uri_ex_hasCousin}, \text{uri_ex_bob}, \text{uri_ex_alice}) \quad \text{fof}(\text{testcase_conclusion}$
 $\exists \text{bNODE_l}_{11}, \text{bNODE_l}_{12}, \text{bNODE_l}_{21}, \text{bNODE_l}_{22}, \text{bNODE_l}_3: (\text{iext}(\text{uri_owl_propertyChainAxiom}, \text{uri_ex_hasUncle}, \text{bNODE_l}$

SWB025+4.p Cyclic Dependencies between Complex Properties

$\text{include}(\text{'Axioms/SWB003+0.ax'})$
 $\text{iext}(\text{uri_ex_hasUncle}, \text{uri_ex_alice}, \text{uri_ex_charly}) \text{ and } \text{iext}(\text{uri_ex_hasCousin}, \text{uri_ex_bob}, \text{uri_ex_alice}) \quad \text{fof}(\text{testcase_conclusion}$
 $\exists \text{bNODE_l}_{11}, \text{bNODE_l}_{12}, \text{bNODE_l}_{21}, \text{bNODE_l}_{22}, \text{bNODE_l}_3: (\text{iext}(\text{uri_owl_propertyChainAxiom}, \text{uri_ex_hasUncle}, \text{bNODE_l}$

SWB026+1.p Inferred Property Characteristics I

$\text{include}(\text{'Axioms/SWB001+0.ax'})$
 $\text{iext}(\text{uri_rdf_type}, \text{uri_ex_p}, \text{uri_owl_InverseFunctionalProperty}) \quad \text{fof}(\text{testcase_conclusion_fullish_026_Inferred_Property_Chara}$
 $\exists \text{bNODE_x}_1, \text{bNODE_x}_2, \text{bNODE_l}_1, \text{bNODE_l}_2: (\text{iext}(\text{uri_rdfs_domain}, \text{uri_ex_p}, \text{bNODE_x}_1) \text{ and } \text{iext}(\text{uri_owl_oneOf}, \text{bNODE}$

SWB026+2.p Inferred Property Characteristics I

$\forall p: (\text{iext}(\text{uri_rdf_type}, p, \text{uri_rdf_Property}) \iff \text{ip}(p)) \quad \text{fof}(\text{rdf_type_ip}, \text{axiom})$
 $\forall x, c: (\text{iext}(\text{uri_rdf_type}, x, c) \iff \text{icext}(c, x)) \quad \text{fof}(\text{rdfs_cext_def}, \text{axiom})$
 $\forall p, c, x, y: ((\text{iext}(\text{uri_rdfs_domain}, p, c) \text{ and } \text{iext}(p, x, y)) \Rightarrow \text{icext}(c, x)) \quad \text{fof}(\text{rdfs_domain_main}, \text{axiom})$
 $\text{iext}(\text{uri_rdfs_domain}, \text{uri_rdfs_domain}, \text{uri_rdf_Property}) \quad \text{fof}(\text{rdfs_domain_domain}, \text{axiom})$
 $\forall z, s_1, a_1: ((\text{iext}(\text{uri_rdf_first}, s_1, a_1) \text{ and } \text{iext}(\text{uri_rdf_rest}, s_1, \text{uri_rdf_nil})) \Rightarrow (\text{iext}(\text{uri_owl_oneOf}, z, s_1) \iff (\text{ic}(z) \text{ and } \forall x: (\text{i}$
 $x = a_1)))) \quad \text{fof}(\text{owl_enum_class}_{001}, \text{axiom})$
 $\forall p: (\text{icext}(\text{uri_owl_InverseFunctionalProperty}, p) \iff (\text{ip}(p) \text{ and } \forall x_1, x_2, y: ((\text{iext}(p, x_1, y) \text{ and } \text{iext}(p, x_2, y)) \Rightarrow$
 $x_1 = x_2))) \quad \text{fof}(\text{owl_char_inversefunctional}, \text{axiom})$
 $\text{iext}(\text{uri_rdf_type}, \text{uri_ex_p}, \text{uri_owl_InverseFunctionalProperty}) \quad \text{fof}(\text{testcase_conclusion_fullish_026_Inferred_Property_Chara}$
 $\exists \text{bNODE_x}_1, \text{bNODE_x}_2, \text{bNODE_l}_1, \text{bNODE_l}_2: (\text{iext}(\text{uri_rdfs_domain}, \text{uri_ex_p}, \text{bNODE_x}_1) \text{ and } \text{iext}(\text{uri_owl_oneOf}, \text{bNODE}$

SWB026+3.p Inferred Property Characteristics I

$\text{include}(\text{'Axioms/SWB002+0.ax'})$
 $\text{iext}(\text{uri_rdf_type}, \text{uri_ex_p}, \text{uri_owl_InverseFunctionalProperty}) \quad \text{fof}(\text{testcase_conclusion_fullish_026_Inferred_Property_Chara}$
 $\exists \text{bNODE_x}_1, \text{bNODE_x}_2, \text{bNODE_l}_1, \text{bNODE_l}_2: (\text{iext}(\text{uri_rdfs_domain}, \text{uri_ex_p}, \text{bNODE_x}_1) \text{ and } \text{iext}(\text{uri_owl_oneOf}, \text{bNODE}$

SWB026+4.p Inferred Property Characteristics I

include('Axioms/SWB003+0.ax')

iext(uri_rdf_type, uri_ex_p, uri_owl_InverseFunctionalProperty) fof(testcase_conclusion_fullish_026_Inferred_Property_Characteristics_II, \exists bNODE_x1, bNODE_x2, bNODE_l1, bNODE_l2: (iext(uri_rdfs_domain, uri_ex_p, bNODE_x1) and iext(uri_owl_oneOf, bNODE_l1, bNODE_l2)))

SWB027+1.p Inferred Property Characteristics II

include('Axioms/SWB001+0.ax')

iext(uri_rdf_type, uri_ex_p, uri_owl_InverseFunctionalProperty) fof(testcase_conclusion_fullish_027_Inferred_Property_Characteristics_II, \exists bNODE_l1, bNODE_l2, bNODE_v: (iext(uri_owl_propertyChainAxiom, uri_owl_sameAs, bNODE_l1) and iext(uri_rdf_first, bNODE_l1, bNODE_l2)))

SWB027+2.p Inferred Property Characteristics II

$\forall x, c: (iext(uri_rdf_type, x, c) \iff icext(c, x))$ fof(rdfs_cext_def, axiom)

$\forall x, y: (iext(uri_owl_sameAs, x, y) \iff x = y)$ fof(owl_eqdis_sameas, axiom)

$\forall p, s_1, p_1, s_2, p_2: ((iext(uri_rdf_first, s_1, p_1) and iext(uri_rdf_rest, s_1, s_2) and iext(uri_rdf_first, s_2, p_2) and iext(uri_rdf_rest, s_2, p_1) and iext(uri_owl_propertyChainAxiom, p, s_1) \iff (ip(p) and ip(p_1) and ip(p_2) and \forall y_0, y_1, y_2: ((iext(p_1, y_0, y_1) and iext(p_2, y_1, y_2) and iext(p, y_0, y_2))))))$ fof(owl_chain002, axiom)

$\forall p: (icext(uri_owl_InverseFunctionalProperty, p) \iff (ip(p) and \forall x_1, x_2, y: ((iext(p, x_1, y) and iext(p, x_2, y)) \implies x_1 = x_2)))$ fof(owl_char_inversefunctional, axiom)

$\forall p_1, p_2: (iext(uri_owl_inverseOf, p_1, p_2) \iff (ip(p_1) and ip(p_2) and \forall x, y: (iext(p_1, x, y) \iff iext(p_2, y, x))))$ fof(owl_inv, axiom)

iext(uri_rdf_type, uri_ex_p, uri_owl_InverseFunctionalProperty) fof(testcase_conclusion_fullish_027_Inferred_Property_Characteristics_II, \exists bNODE_l1, bNODE_l2, bNODE_v: (iext(uri_owl_propertyChainAxiom, uri_owl_sameAs, bNODE_l1) and iext(uri_rdf_first, bNODE_l1, bNODE_l2)))

SWB027+3.p Inferred Property Characteristics II

include('Axioms/SWB002+0.ax')

iext(uri_rdf_type, uri_ex_p, uri_owl_InverseFunctionalProperty) fof(testcase_conclusion_fullish_027_Inferred_Property_Characteristics_II, \exists bNODE_l1, bNODE_l2, bNODE_v: (iext(uri_owl_propertyChainAxiom, uri_owl_sameAs, bNODE_l1) and iext(uri_rdf_first, bNODE_l1, bNODE_l2)))

SWB027+4.p Inferred Property Characteristics II

include('Axioms/SWB003+0.ax')

iext(uri_rdf_type, uri_ex_p, uri_owl_InverseFunctionalProperty) fof(testcase_conclusion_fullish_027_Inferred_Property_Characteristics_II, \exists bNODE_l1, bNODE_l2, bNODE_v: (iext(uri_owl_propertyChainAxiom, uri_owl_sameAs, bNODE_l1) and iext(uri_rdf_first, bNODE_l1, bNODE_l2)))

SWB028+1.p Inferred Property Characteristics III

include('Axioms/SWB001+0.ax')

iext(uri_rdfs_subClassOf, uri_ex_InversesOfFunctionalProperties, uri_owl_InverseFunctionalProperty) fof(testcase_conclusion_fullish_028_Inferred_Property_Characteristics_III, \exists bNODE_z: (iext(uri_owl_equivalentClass, uri_ex_InversesOfFunctionalProperties, bNODE_z) and iext(uri_rdf_type, bNODE_z, uri_ex_InversesOfFunctionalProperties)))

SWB028+2.p Inferred Property Characteristics III

ic(uri_owl_InverseFunctionalProperty) fof(owl_class_inversefunctionalproperty_type, axiom)

$\forall x, y: (iext(uri_owl_inverseOf, x, y) \implies (ip(x) and ip(y)))$ fof(owl_prop_inverseof_ext, axiom)

$\forall x, y: (iext(uri_owl_equivalentClass, x, y) \implies (ic(x) and ic(y)))$ fof(owl_prop_equivalentclass_ext, axiom)

$\forall p: (icext(uri_owl_FunctionalProperty, p) \iff (ip(p) and \forall x, y_1, y_2: ((iext(p, x, y_1) and iext(p, x, y_2)) \implies y_1 = y_2)))$ fof(owl_char_functional, axiom)

$\forall p: (icext(uri_owl_InverseFunctionalProperty, p) \iff (ip(p) and \forall x_1, x_2, y: ((iext(p, x_1, y) and iext(p, x_2, y)) \implies x_1 = x_2)))$ fof(owl_char_inversefunctional, axiom)

$\forall c_1, c_2: (iext(uri_rdfs_subClassOf, c_1, c_2) \iff (ic(c_1) and ic(c_2) and \forall x: (icext(c_1, x) \implies icext(c_2, x))))$ fof(owl_rdfs_ext_subclassof, axiom)

$\forall c_1, c_2: (iext(uri_owl_equivalentClass, c_1, c_2) \iff (ic(c_1) and ic(c_2) and \forall x: (icext(c_1, x) \iff icext(c_2, x))))$ fof(owl_eqdis_ext, axiom)

$\forall z, p, c: ((iext(uri_owl_someValuesFrom, z, c) and iext(uri_owl_onProperty, z, p)) \implies \forall x: (icext(z, x) \iff \exists y: (iext(p, x, y) and iext(y, z, c))))$ fof(owl_svf_ext, axiom)

$\forall p_1, p_2: (iext(uri_owl_inverseOf, p_1, p_2) \iff (ip(p_1) and ip(p_2) and \forall x, y: (iext(p_1, x, y) \iff iext(p_2, y, x))))$ fof(owl_inv, axiom)

iext(uri_rdfs_subClassOf, uri_ex_InversesOfFunctionalProperties, uri_owl_InverseFunctionalProperty) fof(testcase_conclusion_fullish_028_Inferred_Property_Characteristics_III, \exists bNODE_z: (iext(uri_owl_equivalentClass, uri_ex_InversesOfFunctionalProperties, bNODE_z) and iext(uri_rdf_type, bNODE_z, uri_ex_InversesOfFunctionalProperties)))

SWB028+3.p Inferred Property Characteristics III

include('Axioms/SWB002+0.ax')

iext(uri_rdfs_subClassOf, uri_ex_InversesOfFunctionalProperties, uri_owl_InverseFunctionalProperty) fof(testcase_conclusion_fullish_028_Inferred_Property_Characteristics_III, \exists bNODE_z: (iext(uri_owl_equivalentClass, uri_ex_InversesOfFunctionalProperties, bNODE_z) and iext(uri_rdf_type, bNODE_z, uri_ex_InversesOfFunctionalProperties)))

SWB028+4.p Inferred Property Characteristics III

include('Axioms/SWB003+0.ax')

iext(uri_rdfs_subClassOf, uri_ex_InversesOfFunctionalProperties, uri_owl_InverseFunctionalProperty) fof(testcase_conclusion_fullish_028_Inferred_Property_Characteristics_III, \exists bNODE_z: (iext(uri_owl_equivalentClass, uri_ex_InversesOfFunctionalProperties, bNODE_z) and iext(uri_rdf_type, bNODE_z, uri_ex_InversesOfFunctionalProperties)))

SWB029+1.p Ex Falso Quodlibet

include('Axioms/SWB001+0.ax')

iext(uri_rdf_type, uri_ex_w, uri_ex_B) fof(testcase_conclusion_fullish_029_Ex_Falso_Quodlibet, conjecture)

\exists bNODE_x, bNODE_y, bNODE_l1, bNODE_l2: (iext(uri_rdf_type, uri_ex_A, uri_owl_Class) and iext(uri_rdf_type, uri_ex_B, uri_owl_Class))

SWB029+2.p Ex Falso Quodlibet

$\forall x, c: (\text{iext}(\text{uri_rdf_type}, x, c) \iff \text{icext}(c, x)) \quad \text{fof}(\text{rdfs_cext_def}, \text{axiom})$
 $\forall z, c: (\text{iext}(\text{uri_owl_complementOf}, z, c) \Rightarrow (\text{ic}(z) \text{ and } \text{ic}(c) \text{ and } \forall x: (\text{icext}(z, x) \iff \neg \text{icext}(c, x)))) \quad \text{fof}(\text{owl_bool_completer}, \text{axiom})$
 $\forall z, s_1, c_1, s_2, c_2: ((\text{iext}(\text{uri_rdf_first}, s_1, c_1) \text{ and } \text{iext}(\text{uri_rdf_rest}, s_1, s_2) \text{ and } \text{iext}(\text{uri_rdf_first}, s_2, c_2) \text{ and } \text{iext}(\text{uri_rdf_rest}, s_2, \text{uri_rdf_nil}))) \Rightarrow (\text{iext}(\text{uri_owl_intersectionOf}, z, s_1) \iff (\text{ic}(z) \text{ and } \text{ic}(c_1) \text{ and } \text{ic}(c_2) \text{ and } \forall x: (\text{icext}(z, x) \iff (\text{icext}(c_1, x) \text{ and } \text{icext}(c_2, x)))))) \quad \text{fof}(\text{owl_intersection_def}, \text{axiom})$
 $\text{iext}(\text{uri_rdf_type}, \text{uri_ex_w}, \text{uri_ex_B}) \quad \text{fof}(\text{testcase_conclusion_fullish_029_Ex_Falso_Quodlibet}, \text{conjecture})$
 $\exists \text{bNODE_x}, \text{bNODE_y}, \text{bNODE_l}_1, \text{bNODE_l}_2: (\text{iext}(\text{uri_rdf_type}, \text{uri_ex_A}, \text{uri_owl_Class}) \text{ and } \text{iext}(\text{uri_rdf_type}, \text{uri_ex_B}, \text{uri_owl_Class})) \quad \text{fof}(\text{testcase_conclusion_fullish_029_Ex_Falso_Quodlibet}, \text{conjecture})$

SWB029+3.p Ex Falso Quodlibet

$\text{include}(\text{'Axioms/SWB002+0.ax'})$
 $\text{iext}(\text{uri_rdf_type}, \text{uri_ex_w}, \text{uri_ex_B}) \quad \text{fof}(\text{testcase_conclusion_fullish_029_Ex_Falso_Quodlibet}, \text{conjecture})$
 $\exists \text{bNODE_x}, \text{bNODE_y}, \text{bNODE_l}_1, \text{bNODE_l}_2: (\text{iext}(\text{uri_rdf_type}, \text{uri_ex_A}, \text{uri_owl_Class}) \text{ and } \text{iext}(\text{uri_rdf_type}, \text{uri_ex_B}, \text{uri_owl_Class})) \quad \text{fof}(\text{testcase_conclusion_fullish_029_Ex_Falso_Quodlibet}, \text{conjecture})$

SWB029+4.p Ex Falso Quodlibet

$\text{include}(\text{'Axioms/SWB003+0.ax'})$
 $\text{iext}(\text{uri_rdf_type}, \text{uri_ex_w}, \text{uri_ex_B}) \quad \text{fof}(\text{testcase_conclusion_fullish_029_Ex_Falso_Quodlibet}, \text{conjecture})$
 $\exists \text{bNODE_x}, \text{bNODE_y}, \text{bNODE_l}_1, \text{bNODE_l}_2: (\text{iext}(\text{uri_rdf_type}, \text{uri_ex_A}, \text{uri_owl_Class}) \text{ and } \text{iext}(\text{uri_rdf_type}, \text{uri_ex_B}, \text{uri_owl_Class})) \quad \text{fof}(\text{testcase_conclusion_fullish_029_Ex_Falso_Quodlibet}, \text{conjecture})$

SWB030+1.p Bad Class

$\text{include}(\text{'Axioms/SWB001+0.ax'})$
 $\exists \text{bNODE_x}: (\text{iext}(\text{uri_rdf_type}, \text{uri_ex_c}, \text{uri_owl_Class}) \text{ and } \text{iext}(\text{uri_owl_complementOf}, \text{uri_ex_c}, \text{bNODE_x}) \text{ and } \text{iext}(\text{uri_rdf_type}, \text{uri_ex_c}, \text{bNODE_x})) \quad \text{fof}(\text{testcase_conclusion_fullish_029_Ex_Falso_Quodlibet}, \text{conjecture})$

SWB030+2.p Bad Class

$\forall x, c: (\text{iext}(\text{uri_rdf_type}, x, c) \iff \text{icext}(c, x)) \quad \text{fof}(\text{rdfs_cext_def}, \text{axiom})$
 $\forall z, p, v: ((\text{iext}(\text{uri_owl_hasSelf}, z, v) \text{ and } \text{iext}(\text{uri_owl_onProperty}, z, p)) \Rightarrow \forall x: (\text{icext}(z, x) \iff \text{iext}(p, x, x))) \quad \text{fof}(\text{owl_rest_def}, \text{axiom})$
 $\forall z, c: (\text{iext}(\text{uri_owl_complementOf}, z, c) \Rightarrow (\text{ic}(z) \text{ and } \text{ic}(c) \text{ and } \forall x: (\text{icext}(z, x) \iff \neg \text{icext}(c, x)))) \quad \text{fof}(\text{owl_bool_completer}, \text{axiom})$
 $\exists \text{bNODE_x}: (\text{iext}(\text{uri_rdf_type}, \text{uri_ex_c}, \text{uri_owl_Class}) \text{ and } \text{iext}(\text{uri_owl_complementOf}, \text{uri_ex_c}, \text{bNODE_x}) \text{ and } \text{iext}(\text{uri_rdf_type}, \text{uri_ex_c}, \text{bNODE_x})) \quad \text{fof}(\text{testcase_conclusion_fullish_029_Ex_Falso_Quodlibet}, \text{conjecture})$

SWB030+3.p Bad Class

$\text{include}(\text{'Axioms/SWB002+0.ax'})$
 $\exists \text{bNODE_x}: (\text{iext}(\text{uri_rdf_type}, \text{uri_ex_c}, \text{uri_owl_Class}) \text{ and } \text{iext}(\text{uri_owl_complementOf}, \text{uri_ex_c}, \text{bNODE_x}) \text{ and } \text{iext}(\text{uri_rdf_type}, \text{uri_ex_c}, \text{bNODE_x})) \quad \text{fof}(\text{testcase_conclusion_fullish_029_Ex_Falso_Quodlibet}, \text{conjecture})$

SWB030+4.p Bad Class

$\text{include}(\text{'Axioms/SWB003+0.ax'})$
 $\exists \text{bNODE_x}: (\text{iext}(\text{uri_rdf_type}, \text{uri_ex_c}, \text{uri_owl_Class}) \text{ and } \text{iext}(\text{uri_owl_complementOf}, \text{uri_ex_c}, \text{bNODE_x}) \text{ and } \text{iext}(\text{uri_rdf_type}, \text{uri_ex_c}, \text{bNODE_x})) \quad \text{fof}(\text{testcase_conclusion_fullish_029_Ex_Falso_Quodlibet}, \text{conjecture})$

SWB031+1.p Large Universe

$\text{include}(\text{'Axioms/SWB001+0.ax'})$
 $\exists \text{bNODE_x}, \text{bNODE_l}: (\text{iext}(\text{uri_owl_equivalentClass}, \text{uri_owl_Thing}, \text{bNODE_x}) \text{ and } \text{iext}(\text{uri_owl_oneOf}, \text{bNODE_x}, \text{bNODE_l})) \quad \text{fof}(\text{testcase_conclusion_fullish_029_Ex_Falso_Quodlibet}, \text{conjecture})$

SWB031+2.p Large Universe

$\forall x: \text{ir}(x) \quad \text{fof}(\text{simple_ir}, \text{axiom})$
 $\forall x: (\text{icext}(\text{uri_owl_Thing}, x) \iff \text{ir}(x)) \quad \text{fof}(\text{owl_class_thing_ext}, \text{axiom})$
 $\forall x: \neg \text{icext}(\text{uri_owl_Nothing}, x) \quad \text{fof}(\text{owl_class_nothing_ext}, \text{axiom})$
 $\forall z, s_1, a_1: ((\text{iext}(\text{uri_rdf_first}, s_1, a_1) \text{ and } \text{iext}(\text{uri_rdf_rest}, s_1, \text{uri_rdf_nil})) \Rightarrow (\text{iext}(\text{uri_owl_oneOf}, z, s_1) \iff (\text{ic}(z) \text{ and } \forall x: (\text{icext}(z, x) \iff \text{iext}(x, z, x)))))) \quad \text{fof}(\text{owl_enum_class001}, \text{axiom})$
 $\forall c_1, c_2: (\text{iext}(\text{uri_owl_equivalentClass}, c_1, c_2) \iff (\text{ic}(c_1) \text{ and } \text{ic}(c_2) \text{ and } \forall x: (\text{icext}(c_1, x) \iff \text{icext}(c_2, x)))) \quad \text{fof}(\text{owl_eqd_def}, \text{axiom})$
 $\exists \text{bNODE_x}, \text{bNODE_l}: (\text{iext}(\text{uri_owl_equivalentClass}, \text{uri_owl_Thing}, \text{bNODE_x}) \text{ and } \text{iext}(\text{uri_owl_oneOf}, \text{bNODE_x}, \text{bNODE_l})) \quad \text{fof}(\text{testcase_conclusion_fullish_029_Ex_Falso_Quodlibet}, \text{conjecture})$

SWB031+3.p Large Universe

$\text{include}(\text{'Axioms/SWB002+0.ax'})$
 $\exists \text{bNODE_x}, \text{bNODE_l}: (\text{iext}(\text{uri_owl_equivalentClass}, \text{uri_owl_Thing}, \text{bNODE_x}) \text{ and } \text{iext}(\text{uri_owl_oneOf}, \text{bNODE_x}, \text{bNODE_l})) \quad \text{fof}(\text{testcase_conclusion_fullish_029_Ex_Falso_Quodlibet}, \text{conjecture})$

SWB031+4.p Large Universe

$\text{include}(\text{'Axioms/SWB003+0.ax'})$
 $\exists \text{bNODE_x}, \text{bNODE_l}: (\text{iext}(\text{uri_owl_equivalentClass}, \text{uri_owl_Thing}, \text{bNODE_x}) \text{ and } \text{iext}(\text{uri_owl_oneOf}, \text{bNODE_x}, \text{bNODE_l})) \quad \text{fof}(\text{testcase_conclusion_fullish_029_Ex_Falso_Quodlibet}, \text{conjecture})$

SWB032+1.p Datatype Relationships

$\text{include}(\text{'Axioms/SWB001+0.ax'})$
 $\text{iext}(\text{uri_owl_disjointWith}, \text{uri_xsd_decimal}, \text{uri_xsd_string}) \text{ and } \text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_xsd_integer}, \text{uri_xsd_decimal}) \quad \text{fof}(\text{testcase_conclusion_fullish_029_Ex_Falso_Quodlibet}, \text{conjecture})$

SWB032+2.p Datatype Relationships

$\text{idc}(\text{uri_xsd_string}) \quad \text{fof}(\text{owl_dat_dtype_string_type}, \text{axiom})$
 $\text{idc}(\text{uri_xsd_decimal}) \quad \text{fof}(\text{owl_dat_dtype_decimal_type}, \text{axiom})$
 $\text{idc}(\text{uri_xsd_integer}) \quad \text{fof}(\text{owl_dat_dtype_integer_type}, \text{axiom})$
 $\forall x: \neg \text{icext}(\text{uri_rdf_PlainLiteral}, x) \text{ and } \text{icext}(\text{uri_owl_real}, x) \quad \text{fof}(\text{owl_dat_dtype_relation_disjoint_plainliteral_real}, \text{axiom})$
 $\forall x: (\text{icext}(\text{uri_xsd_string}, x) \Rightarrow \text{icext}(\text{uri_rdf_PlainLiteral}, x)) \quad \text{fof}(\text{owl_dat_dtype_relation_subtype_string_plainliteral}, \text{axiom})$

$\forall x: (\text{icext}(\text{uri_owl_rational}, x) \Rightarrow \text{icext}(\text{uri_owl_real}, x)) \quad \text{fof}(\text{owl_dat_dtype_relation_subtype_rational_real}, \text{axiom})$
 $\forall x: (\text{icext}(\text{uri_xsd_decimal}, x) \Rightarrow \text{icext}(\text{uri_owl_rational}, x)) \quad \text{fof}(\text{owl_dat_dtype_relation_subtype_decimal_rational}, \text{axiom})$
 $\forall x: (\text{icext}(\text{uri_xsd_integer}, x) \Rightarrow \text{icext}(\text{uri_xsd_decimal}, x)) \quad \text{fof}(\text{owl_dat_dtype_relation_subtype_integer_decimal}, \text{axiom})$
 $\forall x: (\text{idc}(x) \Rightarrow \text{ic}(x)) \quad \text{fof}(\text{owl_parts_idc_cond_set}, \text{axiom})$
 $\forall c_1, c_2: (\text{iext}(\text{uri_rdfs_subClassOf}, c_1, c_2) \iff (\text{ic}(c_1) \text{ and } \text{ic}(c_2) \text{ and } \forall x: (\text{icext}(c_1, x) \Rightarrow \text{icext}(c_2, x)))) \quad \text{fof}(\text{owl_rdfsext_su}$
 $\forall c_1, c_2: (\text{iext}(\text{uri_owl_disjointWith}, c_1, c_2) \iff (\text{ic}(c_1) \text{ and } \text{ic}(c_2) \text{ and } \forall x: \neg \text{icext}(c_1, x) \text{ and } \text{icext}(c_2, x))) \quad \text{fof}(\text{owl_eqdis_dis}$
 $\text{iext}(\text{uri_owl_disjointWith}, \text{uri_xsd_decimal}, \text{uri_xsd_string}) \text{ and } \text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_xsd_integer}, \text{uri_xsd_decimal}) \quad \text{f}$

SWB032+3.p Datatype Relationships

include('Axioms/SWB002+0.ax')

$\text{iext}(\text{uri_owl_disjointWith}, \text{uri_xsd_decimal}, \text{uri_xsd_string}) \text{ and } \text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_xsd_integer}, \text{uri_xsd_decimal}) \quad \text{f}$

SWB032+4.p Datatype Relationships

include('Axioms/SWB003+0.ax')

$\text{iext}(\text{uri_owl_disjointWith}, \text{uri_xsd_decimal}, \text{uri_xsd_string}) \text{ and } \text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_xsd_integer}, \text{uri_xsd_decimal}) \quad \text{f}$

SWB033+1.p Datatype Relationships

include('Axioms/SWB001+0.ax')

SWB034+1.p Datatype Relationships

include('Axioms/SWB002+0.ax')

SWB035+1.p Datatype Relationships

include('Axioms/SWB003+0.ax')

SWB037+1.p Class Complement Extensional

If a class is an equivalent class to the complement of another class, then the former class defines the complement of the other class. This test checks that class complement is realized as an iff-condition.

include('Axioms/SWB001+0.ax')

$\text{iext}(\text{uri_owl_complementOf}, \text{uri_ex_c}_1, \text{uri_ex_c}_2) \quad \text{fof}(\text{conclusion_rdfbased_sem_bool_complement_ext}, \text{conjecture})$
 $\exists x_0: (\text{iext}(\text{uri_owl_complementOf}, x_0, \text{uri_ex_c}_2) \text{ and } \text{iext}(\text{uri_owl_equivalentClass}, \text{uri_ex_c}_1, x_0)) \quad \text{fof}(\text{premise_rdfbased_sem}$

SWB038+1.p Class De Morgan

The complement of the union of two classes is an equivalent class to the intersection of the complements of the two classes.

include('Axioms/SWB001+0.ax')

$\text{iext}(\text{uri_owl_equivalentClass}, \text{uri_ex_c}_1, \text{uri_ex_c}_2) \quad \text{fof}(\text{conclusion_rdfbased_sem_bool_demorgan}, \text{conjecture})$
 $\exists x_1, x_4, x_0, x_2, x_5, x_3, x_6: (\text{iext}(\text{uri_owl_intersectionOf}, \text{uri_ex_c}_2, x_0) \text{ and } \text{iext}(\text{uri_owl_complementOf}, x_1, \text{uri_ex_x}) \text{ and } \text{iext}(\text{uri}$

SWB039+1.p Class Intersection Extensional

If a class is an equivalent class to the intersection of other classes, then the former class defines the intersection of the other classes. This test checks that class intersection is realized as an iff-condition.

include('Axioms/SWB001+0.ax')

$\exists x_1, x_0: (\text{iext}(\text{uri_rdf_first}, x_0, \text{uri_ex_x}) \text{ and } \text{iext}(\text{uri_rdf_rest}, x_0, x_1) \text{ and } \text{iext}(\text{uri_rdf_first}, x_1, \text{uri_ex_y}) \text{ and } \text{iext}(\text{uri_rdf_rest}, x$
 $\exists x_0, x_1, x_2: (\text{iext}(\text{uri_rdf_first}, x_0, \text{uri_ex_y}) \text{ and } \text{iext}(\text{uri_rdf_rest}, x_0, \text{uri_rdf_nil}) \text{ and } \text{iext}(\text{uri_owl_intersectionOf}, x_1, x_2) \text{ and } \text{iext}$

SWB040+1.p Class Modus Tollens

If a class is subsumed by another class, then the complement of the latter class is subsumed by the complement of the former class.

include('Axioms/SWB001+0.ax')

$\text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_ex_n}_2, \text{uri_ex_n}_1) \quad \text{fof}(\text{conclusion_rdfbased_sem_bool_tollens}, \text{conjecture})$
 $\text{iext}(\text{uri_owl_complementOf}, \text{uri_ex_n}_2, \text{uri_ex_c}_2) \text{ and } \text{iext}(\text{uri_owl_complementOf}, \text{uri_ex_n}_1, \text{uri_ex_c}_1) \text{ and } \text{iext}(\text{uri_rdfs_subCl}$

SWB041+1.p Class Union Extensional

If a class is an equivalent class to the union of two other classes, then the former class defines the union of the other classes. This test checks that class union is realized as an iff-condition.

include('Axioms/SWB001+0.ax')

$\exists x_0, x_1: (\text{iext}(\text{uri_rdf_first}, x_0, \text{uri_ex_x}) \text{ and } \text{iext}(\text{uri_rdf_rest}, x_0, x_1) \text{ and } \text{iext}(\text{uri_rdf_first}, x_1, \text{uri_ex_y}) \text{ and } \text{iext}(\text{uri_rdf_rest}, x$
 $\exists x_2, x_1, x_0: (\text{iext}(\text{uri_owl_unionOf}, x_0, x_1) \text{ and } \text{iext}(\text{uri_rdf_first}, x_1, \text{uri_ex_x}) \text{ and } \text{iext}(\text{uri_rdf_rest}, x_1, x_2) \text{ and } \text{iext}(\text{uri_rdf_first}$

SWB042+1.p Property Chain Extensional

If the chain of extensions of two properties p1 and p2 is a subset of the extension of a property p, then a sub property chain axiom is entailed for p and the chain properties p1 and p2.

include('Axioms/SWB001+0.ax')

$\exists x_0, x_1: (\text{iext}(\text{uri_owl_propertyChainAxiom}, \text{uri_ex_p}, x_0) \text{ and } \text{iext}(\text{uri_rdf_first}, x_1, \text{uri_ex_p}_2) \text{ and } \text{iext}(\text{uri_rdf_rest}, x_1, \text{uri_rdf}$
 $\exists x_2, x_1, x_4, x_5, x_0, x_3: (\text{iext}(\text{uri_rdfs_domain}, \text{uri_ex_p}_1, x_0) \text{ and } \text{iext}(\text{uri_ex_p}_2, \text{uri_ex_z}, \text{uri_ex_y}) \text{ and } \text{iext}(\text{uri_rdf_first}, x_1, \text{uri}$

SWB043+1.p Singleton Property Chain As Subsumption

A sub property chain axiom with a single chain property corresponds to a sub property axiom.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdfs_subPropertyOf, uri_ex_p1, uri_ex_p)    fof(conclusion_rdfbased_sem_chain_subprop, conjecture)
```

```
∃x0: (iext(uri_owl_propertyChainAxiom, uri_ex_p, x0) and iext(uri_rdf_first, x0, uri_ex_p1) and iext(uri_rdf_rest, x0, uri_rdf_nil))
```

SWB044+1.p Asymmetric Property Extensional

If the extension of a property is asymmetric, then the property itself is.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdf_type, uri_ex_p, uri_owl_AsymmetricProperty)    fof(conclusion_rdfbased_sem_char_asymmetric_ext, conjecture)
```

```
∃x2, x3, x0, x1: (iext(uri_owl_oneOf, x0, x1) and iext(uri_rdfs_domain, uri_ex_p, x2) and iext(uri_rdfs_range, uri_ex_p, x0) and iext(uri_rdf_rest, x0, uri_rdf_nil))
```

SWB045+1.p Functional Property Extensional

If the extension of a property is functional, then the property itself is.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdf_type, uri_ex_p, uri_owl_FunctionalProperty)    fof(conclusion_rdfbased_sem_char_functional_ext, conjecture)
```

```
∃x0, x1: (iext(uri_rdfs_range, uri_ex_p, x0) and iext(uri_ex_p, uri_ex_x, uri_ex_y) and iext(uri_rdf_first, x1, uri_ex_y) and iext(uri_rdf_rest, x1, uri_rdf_nil))
```

SWB046+1.p Inverse-Functional Property Extensional

If the extension of a property is inverse functional, then the property itself is.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdf_type, uri_ex_p, uri_owl_InverseFunctionalProperty)    fof(conclusion_rdfbased_sem_char_inversefunc_ext, conjecture)
```

```
∃x1, x0: (iext(uri_rdf_first, x0, uri_ex_x) and iext(uri_rdf_rest, x0, uri_rdf_nil) and iext(uri_owl_oneOf, x1, x0) and iext(uri_ex_p, uri_ex_x, uri_ex_y))
```

SWB047+1.p Functional Inverse Property As Inverse-Functional

The inverse of a functional property is an inverse functional property.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdf_type, uri_ex_p2, uri_owl_InverseFunctionalProperty)    fof(conclusion_rdfbased_sem_char_inversefunc_term, conjecture)
```

```
iext(uri_owl_inverseOf, uri_ex_p2, uri_ex_p1) and iext(uri_rdf_type, uri_ex_p1, uri_owl_FunctionalProperty)    fof(premise_rdfbased_sem_char_inversefunc_term, axiom)
```

SWB048+1.p Irreflexive Property Extensional

If the extension of a property is irreflexive, then the property itself is.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdf_type, uri_ex_p, uri_owl_IrreflexiveProperty)    fof(conclusion_rdfbased_sem_char_irreflexive_ext, conjecture)
```

```
∃x0, x3, x1, x2: (iext(uri_rdfs_domain, uri_ex_p, x0) and iext(uri_rdfs_range, uri_ex_p, x1) and iext(uri_owl_oneOf, x1, x2) and iext(uri_rdf_rest, x0, uri_rdf_nil))
```

SWB049+1.p Reflexive Property Extensional

If the extension of a property is reflexive, then the property itself is. Note that reflexivity is globally defined on the whole universe, which has infinite cardinality under the RDF-Based Semantics. Therefore, instead of explicitly defining the extension of some custom property, the extension of the built-in property owl:topObjectProperty is referred to.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdf_type, uri_ex_p, uri_owl_ReflexiveProperty)    fof(conclusion_rdfbased_sem_char_reflexive_ext, conjecture)
```

```
iext(uri_owl_equivalentProperty, uri_ex_p, uri_owl_topObjectProperty)    fof(premise_rdfbased_sem_char_reflexive_ext, axiom)
```

SWB050+1.p Symmetric Property Extensional

If the extension of a property is symmetric, then the property itself is.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdf_type, uri_ex_p, uri_owl_SymmetricProperty)    fof(conclusion_rdfbased_sem_char_symmetric_ext, conjecture)
```

```
∃x0, x2, x3, x5, x1, x4: (iext(uri_rdfs_domain, uri_ex_p, x0) and iext(uri_rdfs_range, uri_ex_p, x1) and iext(uri_owl_oneOf, x0, x2) and iext(uri_rdf_rest, x0, uri_rdf_nil))
```

SWB051+1.p Transitive Property Extensional

If the extension of a property is transitive, then the property itself is.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdf_type, uri_ex_p, uri_owl_TransitiveProperty)    fof(conclusion_rdfbased_sem_char_transitive_ext, conjecture)
```

```
∃x5, x0, x3, x1, x2, x4: (iext(uri_owl_oneOf, x0, x1) and iext(uri_rdfs_domain, uri_ex_p, x0) and iext(uri_rdfs_range, uri_ex_p, x2) and iext(uri_rdf_rest, x0, uri_rdf_nil))
```

SWB052+1.p Transitive Irreflexive Property As Asymmetric

A transitive and irreflexive property is an asymmetric property.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdf_type, uri_ex_p, uri_owl_AsymmetricProperty)    fof(conclusion_rdfbased_sem_char_transitive_term, conjecture)
```

```
iext(uri_rdf_type, uri_ex_p, uri_owl_TransitiveProperty) and iext(uri_rdf_type, uri_ex_p, uri_owl_IrreflexiveProperty)    fof(premise_rdfbased_sem_char_transitive_term, axiom)
```

SWB053+1.p Empty Class As Sub-Class

Every OWL class is a super class of the vocabulary class owl:Nothing.

```
include('Axioms/SWB001+0.ax')
iext(uri_rdfs_subClassOf, uri_owl_Nothing, uri_ex_c)    fof(conclusion_rdfbased_sem_class_nothing_term, conjecture)
iext(uri_rdf_type, uri_ex_c, uri_owl_Class)           fof(premise_rdfbased_sem_class_nothing_term, axiom)
```

SWB054+1.p Universal Class As Super-Class

Every OWL class is a sub class of the vocabulary class owl:Thing.

```
include('Axioms/SWB001+0.ax')
iext(uri_rdfs_subClassOf, uri_ex_c, uri_owl_Thing)    fof(conclusion_rdfbased_sem_class_thing_term, conjecture)
iext(uri_rdf_type, uri_ex_c, uri_owl_Class)           fof(premise_rdfbased_sem_class_thing_term, axiom)
```

SWB055+1.p Individual Enumeration Extensional

If a class is an equivalent class to the enumeration of two individuals, then the class defines the enumeration of the two individuals. This test checks that enumeration is realized as an iff-condition.

```
include('Axioms/SWB001+0.ax')
 $\exists x_0, x_1: (iext(uri_rdf_first, x_0, uri_ex_y) \text{ and } iext(uri_rdf_rest, x_0, uri_rdf_nil) \text{ and } iext(uri_owl_oneOf, uri_ex_e, x_1) \text{ and } iext(uri_owl_equivalentClass, uri_ex_e, x_0) \text{ and } iext(uri_rdf_first, x_1, uri_ex_x) \text{ and } iext(uri_rdf_rest, x_1, uri_rdf_nil))$ 
```

SWB056+1.p Individual Enumeration Closed

If a class defines an enumeration class expression from two individuals, and if an individual is an instance of the class but is different from one of the two component individuals, then the individual equals the remaining component individual.

```
include('Axioms/SWB001+0.ax')
iext(uri_owl_sameAs, uri_ex_z, uri_ex_y)    fof(conclusion_rdfbased_sem_enum_inst_closed, conjecture)
 $\exists x_0, x_1: (iext(uri_rdf_type, uri_ex_z, uri_ex_e) \text{ and } iext(uri_owl_differentFrom, uri_ex_z, uri_ex_x) \text{ and } iext(uri_owl_oneOf, uri_ex_e, x_0) \text{ and } iext(uri_owl_oneOf, uri_ex_e, x_1))$ 
```

SWB057+1.p Individual Difference Extensional

If two individuals are distinct, then the owl:differentFrom relation holds between them.

```
include('Axioms/SWB001+0.ax')
iext(uri_owl_differentFrom, uri_ex_w, uri_ex_u)    fof(conclusion_rdfbased_sem_eqdis_different_ext, conjecture)
 $\exists x_0: (iext(uri_rdf_type, uri_ex_u, x_0) \text{ and } iext(uri_owl_complementOf, x_0, uri_ex_c) \text{ and } iext(uri_rdf_type, uri_ex_w, uri_ex_c))$ 
```

SWB058+1.p Class Disjointness Extensional

If the non-empty extensions of two classes are disjoint, then the classes themselves are disjoint.

```
include('Axioms/SWB001+0.ax')
iext(uri_owl_disjointWith, uri_ex_c1, uri_ex_c2)    fof(conclusion_rdfbased_sem_eqdis_disclass_ext, conjecture)
 $\exists x_1, x_0: (iext(uri_owl_oneOf, uri_ex_c2, x_0) \text{ and } iext(uri_rdf_first, x_1, uri_ex_x) \text{ and } iext(uri_rdf_rest, x_1, uri_rdf_nil) \text{ and } iext(uri_owl_disjointWith, uri_ex_c1, uri_ex_c2))$ 
```

SWB059+1.p Disjoint Class Union Composite

If a class expresses the union of two disjoint component classes, then the class expresses a disjoint union class axiom for the component classes.

```
include('Axioms/SWB001+0.ax')
 $\exists x_1, x_0: (iext(uri_owl_disjointUnionOf, uri_ex_c3, x_0) \text{ and } iext(uri_rdf_first, x_0, uri_ex_c1) \text{ and } iext(uri_rdf_rest, x_0, x_1) \text{ and } iext(uri_owl_disjointWith, uri_ex_c1, uri_ex_c2) \text{ and } iext(uri_rdf_first, x_1, uri_ex_x) \text{ and } iext(uri_rdf_rest, x_1, uri_rdf_nil))$ 
```

SWB060+1.p Disjoint Class Union As Disjointness

The component classes on the right hand side of a disjoint-union axiom are pairwise disjoint.

```
include('Axioms/SWB001+0.ax')
iext(uri_owl_disjointWith, uri_ex_c1, uri_ex_c2)    fof(conclusion_rdfbased_sem_eqdis_disjointunion_disjoint, conjecture)
 $\exists x_1, x_0: (iext(uri_owl_disjointUnionOf, uri_ex_c3, x_0) \text{ and } iext(uri_rdf_first, x_1, uri_ex_c2) \text{ and } iext(uri_rdf_rest, x_1, uri_rdf_nil) \text{ and } iext(uri_owl_disjointWith, uri_ex_c1, uri_ex_c2))$ 
```

SWB061+1.p Disjoint Class Union As Union

If a class is defined by a disjoint-union axiom for two component classes, then the class expresses the union of the two classes.

```
include('Axioms/SWB001+0.ax')
 $\exists x_0, x_1: (iext(uri_rdf_first, x_0, uri_ex_c1) \text{ and } iext(uri_rdf_rest, x_0, x_1) \text{ and } iext(uri_rdf_first, x_1, uri_ex_c2) \text{ and } iext(uri_rdf_rest, x_1, uri_rdf_nil) \text{ and } iext(uri_owl_disjointUnionOf, uri_ex_c3, x_0) \text{ and } iext(uri_rdf_first, x_1, uri_ex_c2) \text{ and } iext(uri_rdf_rest, x_1, uri_rdf_nil))$ 
```

SWB062+1.p Property Disjointness Extensional

If the non-empty extensions of two properties are disjoint, then the properties themselves are disjoint.

```
include('Axioms/SWB001+0.ax')
iext(uri_owl_propertyDisjointWith, uri_ex_p1, uri_ex_p2)    fof(conclusion_rdfbased_sem_eqdis_disprop_ext, conjecture)
 $\exists x_1, x_2, x_0, x_3: (iext(uri_rdfs_domain, uri_ex_p1, uri_ex_x1) \text{ and } iext(uri_rdfs_range, uri_ex_p1, uri_ex_y1) \text{ and } iext(uri_ex_p2, uri_ex_x2, uri_ex_y2) \text{ and } iext(uri_rdfs_domain, uri_ex_p2, uri_ex_x3) \text{ and } iext(uri_rdfs_range, uri_ex_p2, uri_ex_y3) \text{ and } iext(uri_rdfs_domain, uri_ex_p1, uri_ex_x3) \text{ and } iext(uri_rdfs_range, uri_ex_p1, uri_ex_y3))$ 
```

SWB063+1.p Class Equivalence Extensional

If the extensions of two classes are equal, then the classes are themselves equivalent.

include('Axioms/SWB001+0.ax')

iext(uri_owl_equivalentClass, uri_ex_c1, uri_ex_c2) fof(conclusion_rdfbased_sem_eqdis_eqclass_ext, conjecture)

$\exists x_0, x_1$: (iext(uri_owl_oneOf, uri_ex_c2, x_0) and iext(uri_owl_oneOf, uri_ex_c1, x_1) and iext(uri_rdf_first, x_0 , uri_ex_x) and iext(uri_rdf_type, uri_ex_x, uri_owl_oneOf))

SWB064+1.p Property Equivalence Extensional

If the extensions of two properties are equal, then the properties themselves are equivalent.

include('Axioms/SWB001+0.ax')

iext(uri_owl_equivalentProperty, uri_ex_p1, uri_ex_p2) fof(conclusion_rdfbased_sem_eqdis_eqprop_ext, conjecture)

$\exists x_1, x_0$: (iext(uri_rdfs_domain, uri_ex_p1, uri_ex_x) and iext(uri_rdfs_range, uri_ex_p1, uri_ex_y) and iext(uri_ex_p1, uri_ex_s, uri_ex_x) and iext(uri_ex_p2, uri_ex_s, uri_ex_y))

SWB065+1.p Individual Equality Extensional

If two individuals are equal, then the owl:sameAs relation holds between them.

include('Axioms/SWB001+0.ax')

iext(uri_owl_sameAs, uri_ex_w, uri_ex_u) fof(conclusion_rdfbased_sem_eqdis_sameas_ext, conjecture)

$\exists x_0, x_1$: (iext(uri_rdf_first, x_0 , uri_ex_u) and iext(uri_rdf_rest, x_0 , uri_rdf_nil) and iext(uri_owl_oneOf, x_1 , x_0) and iext(uri_rdf_type, uri_ex_u, uri_owl_oneOf))

SWB066+1.p Inverse Property Extensional

If the extensions of two properties are inverse, then the properties themselves are.

include('Axioms/SWB001+0.ax')

iext(uri_owl_inverseOf, uri_ex_q, uri_ex_p) fof(conclusion_rdfbased_sem_inv_ext, conjecture)

$\exists x_3, x_7, x_0, x_6, x_4, x_5, x_1, x_2$: (iext(uri_owl_oneOf, x_0 , x_1) and iext(uri_rdfs_domain, uri_ex_p, x_2) and iext(uri_rdfs_range, uri_ex_q, x_3))

SWB067+1.p Double Inverse Property As Equivalence

Transitively related inverse properties are equivalent.

include('Axioms/SWB001+0.ax')

iext(uri_owl_equivalentProperty, uri_ex_p3, uri_ex_p1) fof(conclusion_rdfbased_sem_inv_trans, conjecture)

iext(uri_owl_inverseOf, uri_ex_p3, uri_ex_p2) and iext(uri_owl_inverseOf, uri_ex_p2, uri_ex_p1) fof(premise_rdfbased_sem_inv_trans, axiom)

SWB068+1.p N-Ary Individual Difference Extensional

For a group of mutually different individuals, the corresponding owl:AllDifferent construct exist.

include('Axioms/SWB001+0.ax')

$\exists x_2, x_0, x_1, x_3$: (iext(uri_rdf_first, x_0 , uri_ex_w1) and iext(uri_rdf_rest, x_0 , x_1) and iext(uri_rdf_first, x_1 , uri_ex_w2) and iext(uri_rdf_rest, x_1 , uri_ex_w3))

$\exists x_0, x_2, x_1$: (iext(uri_owl_differentFrom, uri_ex_w1, uri_ex_w2) and iext(uri_owl_differentFrom, uri_ex_w1, uri_ex_w3) and iext(uri_owl_differentFrom, uri_ex_w2, uri_ex_w3))

SWB069+1.p N-Ary Class Disjointness Extensional

For a group of mutually disjoint classes, the corresponding owl:AllDisjointClasses construct exists.

include('Axioms/SWB001+0.ax')

$\exists x_2, x_3, x_0, x_1$: (iext(uri_rdf_first, x_0 , uri_ex_c2) and iext(uri_rdf_rest, x_0 , x_1) and iext(uri_rdf_first, x_1 , uri_ex_c3) and iext(uri_rdf_rest, x_1 , uri_ex_c4))

$\exists x_1, x_2, x_0$: (iext(uri_owl_disjointWith, uri_ex_c2, uri_ex_c3) and iext(uri_rdf_first, x_0 , uri_ex_c2) and iext(uri_rdf_rest, x_0 , x_1))

SWB070+1.p N-Ary Property Disjointness Extensional

For a group of mutually disjoint properties the corresponding owl:AllDisjointProperties construct exists.

include('Axioms/SWB001+0.ax')

$\exists x_1, x_0, x_3, x_2$: (iext(uri_rdf_first, x_0 , uri_ex_p2) and iext(uri_rdf_rest, x_0 , x_1) and iext(uri_rdf_first, x_1 , uri_ex_p3) and iext(uri_rdf_rest, x_1 , uri_ex_p4))

$\exists x_2, x_0, x_1$: (iext(uri_owl_propertyDisjointWith, uri_ex_p1, uri_ex_p2) and iext(uri_owl_propertyDisjointWith, uri_ex_p1, uri_ex_p3))

SWB071+1.p Negative Individual Property Assertion Extensional

If a triple 's p o' does not hold, then the negative property assertion NPA(s p o) is entailed.

include('Axioms/SWB001+0.ax')

$\exists x_0$: (iext(uri_owl_sourceIndividual, x_0 , uri_ex_s) and iext(uri_owl_assertionProperty, x_0 , uri_ex_p) and iext(uri_owl_targetIndividual, x_0 , uri_ex_o))

iext(uri_rdf_type, uri_ex_p, uri_owl_FunctionalProperty) and iext(uri_ex_p, uri_ex_s, uri_ex_o1) and iext(uri_owl_differentFrom, uri_ex_o, uri_ex_o1)

SWB072+1.p Empty Data Property Extensional Low

The extension of the vocabulary property owl:bottomDataProperty is empty. See also rdfbased-sem-prop-bottomdataproperty-ext-hi for a weaker variant of this test case.

include('Axioms/SWB001+0.ax')

iext(uri_rdfs_domain, uri_owl_bottomDataProperty, uri_owl_Nothing) and iext(uri_rdfs_range, uri_owl_bottomDataProperty, uri_owl_Nothing)

tautology or \neg tautology fof(premise_rdfbased_sem_prop_bottomdataproperty_ext_lo, axiom)

SWB073+1.p Empty Data Property As Sub-Property

Every data property is a super property of the vocabulary property owl:bottomDataProperty.

include('Axioms/SWB001+0.ax')

iext(uri_rdfs_subPropertyOf, uri_owl_bottomDataProperty, uri_ex_p) fof(conclusion_rdfbased_sem_prop_bottomdataproperty_ext_hi, conjecture)

iext(uri_rdf_type, uri_ex_p, uri_owl_DatatypeProperty) fof(premise_rdfbased_sem_prop_bottomdataproperty_term, axiom)

SWB074+1.p Universal Data Property Extensional Low

The extension of the vocabulary property owl:topDataProperty equals the class product of OWL individuals and data values, and thus subsumes that class product. See also rdfbased-sem-prop-topdataproperty-ext-hi for a test case checking the exact upper bounds of the domain and range.

include('Axioms/SWB001+0.ax')

iext(uri_owl_topDataProperty, uri_ex_x, uri_ex_y) fof(conclusion_rdfbased_sem_prop_topdataproperty_ext_lo, conjecture)

iext(uri_rdf_type, uri_ex_y, uri_rdfs_Literal) and iext(uri_rdf_type, uri_ex_x, uri_owl_Thing) fof(premise_rdfbased_sem_prop-

SWB075+1.p Universal Data Property As Super-Property

Every data property is a sub property of the vocabulary property owl:topDataProperty.

include('Axioms/SWB001+0.ax')

iext(uri_rdfs_subPropertyOf, uri_ex_p, uri_owl_topDataProperty) fof(conclusion_rdfbased_sem_prop_topdataproperty_term,

iext(uri_rdf_type, uri_ex_p, uri_owl_DatatypeProperty) fof(premise_rdfbased_sem_prop_topdataproperty_term, axiom)

SWB076+1.p Property Range Extensional OWL

If the extension of a given class is a range for the extension of a given property, then the class is a range for the property.

include('Axioms/SWB001+0.ax')

iext(uri_rdfs_range, uri_ex_p, uri_ex_c) fof(conclusion_rdfbased_sem_rdfsext_range_ext, conjecture)

$\exists x_0$: (iext(uri_owl_allValuesFrom, x_0 , uri_ex_c) and iext(uri_owl_onProperty, x_0 , uri_ex_p) and iext(uri_rdfs_subClassOf, uri_owl_Thing,

SWB077+1.p Property Range Sub-Property OWL

Every sub property of a given property with a given range also has this range.

include('Axioms/SWB001+0.ax')

iext(uri_rdfs_range, uri_ex_p₁, uri_ex_c) fof(conclusion_rdfbased_sem_rdfsext_range_subprop, conjecture)

iext(uri_rdfs_range, uri_ex_p₂, uri_ex_c) and iext(uri_rdfs_subPropertyOf, uri_ex_p₁, uri_ex_p₂) fof(premise_rdfbased_sem_rdfsext_range,

SWB078+1.p Property Range Super-Class OWL

Every super class of a range for a given property is itself a range for that property.

include('Axioms/SWB001+0.ax')

iext(uri_rdfs_range, uri_ex_p, uri_ex_c₂) fof(conclusion_rdfbased_sem_rdfsext_range_superclass, conjecture)

iext(uri_rdfs_range, uri_ex_p, uri_ex_c₁) and iext(uri_rdfs_subClassOf, uri_ex_c₁, uri_ex_c₂) fof(premise_rdfbased_sem_rdfsext_range,

SWB079+1.p Class Subsumption Extensional OWL

If the extension of a given class is subsumed by the extension of a second class, then the first class is a subclass of the second class.

include('Axioms/SWB001+0.ax')

iext(uri_rdfs_subClassOf, uri_ex_c₁, uri_ex_c₂) fof(conclusion_rdfbased_sem_rdfsext_subclass_ext, conjecture)

$\exists x_0, x_1, x_2$: (iext(uri_owl_oneOf, uri_ex_c₂, x_0) and iext(uri_rdf_first, x_0 , uri_ex_w) and iext(uri_rdf_rest, x_0, x_1) and iext(uri_owl_Thing,

SWB080+1.p Property Subsumption Extensional OWL

If the extension of a given property is subsumed by the extension of a second property, then the first property is a subproperty of the second property.

include('Axioms/SWB001+0.ax')

iext(uri_rdfs_subPropertyOf, uri_ex_p₁, uri_ex_p₂) fof(conclusion_rdfbased_sem_rdfsext_subprop_ext, conjecture)

$\exists x_8, x_4, x_2, x_5, x_1, x_6, x_3, x_7, x_0$: (iext(uri_rdfs_domain, uri_ex_p₁, x_0) and iext(uri_rdfs_range, uri_ex_p₁, x_1) and iext(uri_rdf_first,

SWB081+1.p Universal Restriction Comparison By Class

A universal restriction on some property and some class is a sub class of another universal restriction on the same property but on a super class.

include('Axioms/SWB001+0.ax')

iext(uri_rdfs_subClassOf, uri_ex_x₁, uri_ex_x₂) fof(conclusion_rdfbased_sem_restrict_allvalues_cmp_class, conjecture)

iext(uri_owl_allValuesFrom, uri_ex_x₂, uri_ex_c₂) and iext(uri_owl_onProperty, uri_ex_x₂, uri_ex_p) and iext(uri_owl_allValuesFrom,

SWB082+1.p Universal Restriction Comparison By Property

A universal restriction on some property and some class is a sub class of another universal restriction on the same class but on a sub property.

include('Axioms/SWB001+0.ax')

iext(uri_rdfs_subClassOf, uri_ex_x₂, uri_ex_x₁) fof(conclusion_rdfbased_sem_restrict_allvalues_cmp_prop, conjecture)

iext(uri_owl_allValuesFrom, uri_ex_x₂, uri_ex_c) and iext(uri_owl_onProperty, uri_ex_x₂, uri_ex_p₂) and iext(uri_owl_allValuesFrom,

SWB083+1.p Universal Restriction Extensional

If the range of property p is defined to be class c, then every individual is an instance of the universal restriction on p to c.

include('Axioms/SWB001+0.ax')

iext(uri_rdf_type, uri_ex_w, uri_ex_z) fof(conclusion_rdfbased_sem_restrict_allvalues_inst_subj, conjecture)

$\text{iext}(\text{uri_owl_allValuesFrom}, \text{uri_ex_z}, \text{uri_ex_c})$ and $\text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_z}, \text{uri_ex_p})$ and $\text{iext}(\text{uri_rdfs_range}, \text{uri_ex_z}, \text{uri_ex_c})$

SWB084+1.p Exact-2-QCR Intensional

If an individual w is an instance of the exact-2-QCR on property p to class c , then two distinct individuals x_1 and x_2 exist in c with $w p x_1$ and $w p x_2$

`include('Axioms/SWB001+0.ax')`

$\exists x_1, x_0: (\text{iext}(\text{uri_rdf_type}, x_0, \text{uri_ex_c}) \text{ and } \text{iext}(\text{uri_owl_differentFrom}, x_0, x_1) \text{ and } \text{iext}(\text{uri_rdf_type}, x_1, \text{uri_ex_c}) \text{ and } \text{iext}(\text{uri_owl_qualifiedCardinality}, \text{uri_ex_z}, \text{literal_typed}(\text{dat_str}_2, \text{uri_xsd_nonNegativeInteger})) \text{ and } \text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_z}, \text{uri_ex_p}))$

SWB085+1.p Exact-2-QCR Extensional

For an individual w , if there are exactly two triples $w p x_1$ and $w p x_2$ with x_1 and x_2 being instances of class c , then w is an instance of the exact-2-QCR on p to c .

`include('Axioms/SWB001+0.ax')`

$\text{iext}(\text{uri_rdf_type}, \text{uri_ex_w}, \text{uri_ex_z}) \quad \text{fof}(\text{conclusion_rdfs_sem_restrict_exactqcr_inst_subj_two}, \text{conjecture})$

$\exists x_3, x_4, x_0, x_1, x_2: (\text{iext}(\text{uri_rdfs_range}, \text{uri_ex_p}, x_0) \text{ and } \text{iext}(\text{uri_owl_complementOf}, x_1, \text{uri_ex_c}) \text{ and } \text{iext}(\text{uri_owl_qualifiedCardinality}, \text{uri_ex_z}, \text{literal_typed}(\text{dat_str}_2, \text{uri_xsd_nonNegativeInteger})))$

SWB086+1.p Self-Restriction Comparison By Property

A self restriction on some property is a sub class of another self restriction on a super property.

`include('Axioms/SWB001+0.ax')`

$\text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_ex_x}_1, \text{uri_ex_x}_2) \quad \text{fof}(\text{conclusion_rdfs_sem_restrict_hasself_cmp_prop}, \text{conjecture})$

$\text{iext}(\text{uri_owl_hasSelf}, \text{uri_ex_x}_2, \text{literal_typed}(\text{dat_str_true}, \text{uri_xsd_boolean})) \text{ and } \text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_x}_2, \text{uri_ex_p}_2)$

SWB087+1.p Self-Restriction Extensional

For a triple $w p w$, the individual w is an instance of the self restriction on p .

`include('Axioms/SWB001+0.ax')`

$\text{iext}(\text{uri_rdf_type}, \text{uri_ex_w}, \text{uri_ex_z}) \quad \text{fof}(\text{conclusion_rdfs_sem_restrict_hasself_inst_subj}, \text{conjecture})$

$\text{iext}(\text{uri_owl_hasSelf}, \text{uri_ex_z}, \text{literal_typed}(\text{dat_str_true}, \text{uri_xsd_boolean})) \text{ and } \text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_z}, \text{uri_ex_p})$ and

SWB088+1.p Max-QCR Comparison By Cardinality

A max-QCR for some cardinality on some property and to some class is a subclass of another max-QCR on the same property to the same class and for some larger cardinality.

`include('Axioms/SWB001+0.ax')`

$\text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_ex_x}_1, \text{uri_ex_x}_2) \quad \text{fof}(\text{conclusion_rdfs_sem_restrict_maxqcr_cmp_card}, \text{conjecture})$

$\text{iext}(\text{uri_owl_maxQualifiedCardinality}, \text{uri_ex_x}_2, \text{literal_typed}(\text{dat_str}_2, \text{uri_xsd_nonNegativeInteger})) \text{ and } \text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_x}_2, \text{uri_ex_p}_2)$

SWB089+1.p Max-QCR Comparison By Class

A max-QCR for some cardinality on some property and to some class is a subclass of another max-QCR for the same cardinality on the same property and to some sub class.

`include('Axioms/SWB001+0.ax')`

$\text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_ex_x}_1, \text{uri_ex_x}_2) \quad \text{fof}(\text{conclusion_rdfs_sem_restrict_maxqcr_cmp_class}, \text{conjecture})$

$\text{iext}(\text{uri_owl_maxQualifiedCardinality}, \text{uri_ex_x}_2, \text{literal_typed}(\text{dat_str}_1, \text{uri_xsd_nonNegativeInteger})) \text{ and } \text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_x}_2, \text{uri_ex_p}_2)$

SWB090+1.p Max-QCR Comparison By Property

A max-QCR for some cardinality on some property and to some class is a subclass of another max-QCR for the same cardinality to the same class and on a sub property.

`include('Axioms/SWB001+0.ax')`

$\text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_ex_x}_1, \text{uri_ex_x}_2) \quad \text{fof}(\text{conclusion_rdfs_sem_restrict_maxqcr_cmp_prop}, \text{conjecture})$

$\text{iext}(\text{uri_owl_maxQualifiedCardinality}, \text{uri_ex_x}_2, \text{literal_typed}(\text{dat_str}_1, \text{uri_xsd_nonNegativeInteger})) \text{ and } \text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_x}_2, \text{uri_ex_p}_2)$

SWB091+1.p Max-1-QCR Extensional

For an individual w , if there is at most one triple $w p x$ with x in class c , then w is an instance of the max-1-QCR on p to c .

`include('Axioms/SWB001+0.ax')`

$\text{iext}(\text{uri_rdf_type}, \text{uri_ex_w}, \text{uri_ex_z}) \quad \text{fof}(\text{conclusion_rdfs_sem_restrict_maxqcr_inst_subj_one}, \text{conjecture})$

$\exists x_1, x_3, x_2, x_0: (\text{iext}(\text{uri_rdfs_range}, \text{uri_ex_p}, x_0) \text{ and } \text{iext}(\text{uri_owl_maxQualifiedCardinality}, \text{uri_ex_z}, \text{literal_typed}(\text{dat_str}_1, \text{uri_xsd_nonNegativeInteger})))$

SWB092+1.p Max-0-QCR Extensional

For an individual w , if there is no triple $w p x$, with x being an instance of class c , then w is an instance of the max-0-QCR on p to c .

`include('Axioms/SWB001+0.ax')`

$\text{iext}(\text{uri_rdf_type}, \text{uri_ex_w}, \text{uri_ex_z}) \quad \text{fof}(\text{conclusion_rdfs_sem_restrict_maxqcr_inst_subj_zero}, \text{conjecture})$

$\exists x_2, x_4, x_0, x_3, x_1: (\text{iext}(\text{uri_owl_complementOf}, x_0, \text{uri_ex_c}) \text{ and } \text{iext}(\text{uri_rdfs_range}, \text{uri_ex_p}, x_1) \text{ and } \text{iext}(\text{uri_owl_maxQualifiedCardinality}, \text{uri_ex_z}, \text{literal_typed}(\text{dat_str}_1, \text{uri_xsd_nonNegativeInteger})))$

SWB093+1.p Min-QCR Comparison By Cardinality

A min-QCR for some cardinality on some property and to some class is a subclass of another min-QCR on the same property to the same class and for some smaller cardinality.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdfs_subClassOf, uri_ex_x1, uri_ex_x2) fof(conclusion_rdfbased_sem_restrict_minqcr_cmp_card, conjecture)
```

```
iext(uri_owl_minQualifiedCardinality, uri_ex_x2, literal_typed(dat_str1, uri_xsd_nonNegativeInteger)) and iext(uri_owl_onProperty, uri_ex_x1, uri_ex_x2)
```

SWB094+1.p Min-QCR Comparison By Class

A min-QCR for some cardinality on some property and to some class is a subclass of another min-QCR for the same cardinality on the same property and to some super class.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdfs_subClassOf, uri_ex_x1, uri_ex_x2) fof(conclusion_rdfbased_sem_restrict_minqcr_cmp_class, conjecture)
```

```
iext(uri_owl_minQualifiedCardinality, uri_ex_x2, literal_typed(dat_str1, uri_xsd_nonNegativeInteger)) and iext(uri_owl_onProperty, uri_ex_x1, uri_ex_x2)
```

SWB095+1.p Min-QCR Comparison By Property

A min-QCR for some cardinality on some property and to some class is a subclass of another min-QCR for the same cardinality to the same class and on a super property.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdfs_subClassOf, uri_ex_x1, uri_ex_x2) fof(conclusion_rdfbased_sem_restrict_minqcr_cmp_prop, conjecture)
```

```
iext(uri_owl_minQualifiedCardinality, uri_ex_x2, literal_typed(dat_str1, uri_xsd_nonNegativeInteger)) and iext(uri_owl_onProperty, uri_ex_x1, uri_ex_x2)
```

SWB096+1.p Min-1-QCR Intensional

If an individual w is an instance of the min-1-QCR on property p to class c , then an individual x exists with $w p x$ and x in c .

```
include('Axioms/SWB001+0.ax')
```

```
 $\exists x_0: (iext(uri_rdf_type, x_0, uri_ex_c) \text{ and } iext(uri_ex_p, uri_ex_w, x_0))$  fof(conclusion_rdfbased_sem_restrict_minqcr_inst_obj, conjecture)
```

```
iext(uri_owl_minQualifiedCardinality, uri_ex_z, literal_typed(dat_str1, uri_xsd_nonNegativeInteger)) and iext(uri_owl_onProperty, uri_ex_x1, uri_ex_x2)
```

SWB097+1.p Min-1-QCR Extensional

For a triple $w p x$, with x being an instance of the class c , the individual w is an instance of the min-1-QCR on p to c .

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdf_type, uri_ex_w, uri_ex_z) fof(conclusion_rdfbased_sem_restrict_minqcr_inst_subj_one, conjecture)
```

```
iext(uri_owl_minQualifiedCardinality, uri_ex_z, literal_typed(dat_str1, uri_xsd_nonNegativeInteger)) and iext(uri_owl_onProperty, uri_ex_x1, uri_ex_x2)
```

SWB098+1.p Existential Restriction Comparison By Class

An existential restriction on some property and some class is a sub class of another existential restriction on the same property but on a super class.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdfs_subClassOf, uri_ex_x1, uri_ex_x2) fof(conclusion_rdfbased_sem_restrict_somevalues_cmp_class, conjecture)
```

```
iext(uri_owl_someValuesFrom, uri_ex_x2, uri_ex_c2) and iext(uri_owl_onProperty, uri_ex_x2, uri_ex_p) and iext(uri_owl_someValuesFrom, uri_ex_x1, uri_ex_c1)
```

SWB099+1.p Existential Restriction Comparison By Property

An existential restriction on some property and some class is a sub class of another existential restriction on the same class but on a super property.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_rdfs_subClassOf, uri_ex_x1, uri_ex_x2) fof(conclusion_rdfbased_sem_restrict_somevalues_cmp_prop, conjecture)
```

```
iext(uri_owl_someValuesFrom, uri_ex_x2, uri_ex_c) and iext(uri_owl_onProperty, uri_ex_x2, uri_ex_p2) and iext(uri_owl_someValuesFrom, uri_ex_x1, uri_ex_c)
```

SWB100+1.p Existential Restriction Intensional

If an individual w is an instance of the existential restriction on property p and class c , then an individual x exists with $w p x$ and x in c .

```
include('Axioms/SWB001+0.ax')
```

```
 $\exists x_0: (iext(uri_rdf_type, x_0, uri_ex_c) \text{ and } iext(uri_ex_p, uri_ex_w, x_0))$  fof(conclusion_rdfbased_sem_restrict_somevalues_inst, conjecture)
```

```
iext(uri_owl_someValuesFrom, uri_ex_z, uri_ex_c) and iext(uri_owl_onProperty, uri_ex_z, uri_ex_p) and iext(uri_rdf_type, uri_ex_w, uri_ex_c)
```

SWB101+1.p Cardinality Restriction As QCR

A cardinality restriction can be written as a QCR to class `owl:Thing`.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_owl_equivalentClass, uri_ex_z1, uri_ex_z2) fof(conclusion_rdfbased_sem_restrict_term_cardqcr, conjecture)
```

```
iext(uri_owl_qualifiedCardinality, uri_ex_z2, literal_typed(dat_str1, uri_xsd_nonNegativeInteger)) and iext(uri_owl_onProperty, uri_ex_x1, uri_ex_x2)
```

SWB102+1.p Data-QCR As Object-QCR

An object-QCR on a data property to a datatype is a data-QCR. Also, every data-QCR is an object-QCR.

```
include('Axioms/SWB001+0.ax')
```

```
iext(uri_owl_equivalentClass, uri_ex_z1, uri_ex_z2) fof(conclusion_rdfbased_sem_restrict_term_dataqcr, conjecture)
```

$\text{iext}(\text{uri_rdf_type}, \text{uri_ex_p}, \text{uri_owl_DatatypeProperty})$ and $\text{iext}(\text{uri_owl_qualifiedCardinality}, \text{uri_ex_z}_2, \text{literal_typed}(\text{dat_str}_1, u$

SWB103+1.p Exact-QCR As Min-QCR Max-QCR Intersection

The intersection of a min- and a max-QCR for the same cardinality, property and class is equivalent to an exact-QCR for the same cardinality, property and class.

`include('Axioms/SWB001+0.ax')`

$\text{iext}(\text{uri_owl_equivalentClass}, \text{uri_ex_z}_4, \text{uri_ex_z}_1)$ $\text{fof}(\text{conclusion_rdfbased_sem_restrict_term_minmaxexact}, \text{conjecture})$
 $\exists x_0, x_1: (\text{iext}(\text{uri_owl_minQualifiedCardinality}, \text{uri_ex_z}_2, \text{literal_typed}(\text{dat_str}_1, \text{uri_xsd_nonNegativeInteger}))$ and $\text{iext}(\text{uri_owl}$

SWB104+1.p Universal Class As Min-QCR Max-QCR Union

The union of a min- and a max-QCR for the same cardinality, property and class covers the whole universe.

`include('Axioms/SWB001+0.ax')`

$\text{iext}(\text{uri_owl_equivalentClass}, \text{uri_ex_z}_3, \text{uri_owl_Thing})$ $\text{fof}(\text{conclusion_rdfbased_sem_restrict_term_minmaxthing}, \text{conjecture})$
 $\exists x_0, x_1: (\text{iext}(\text{uri_owl_maxQualifiedCardinality}, \text{uri_ex_z}_2, \text{literal_typed}(\text{dat_str}_1, \text{uri_xsd_nonNegativeInteger}))$ and $\text{iext}(\text{uri_owl}$

SWB105+1.p Universal Existential Restriction Duality

Universal and existential restrictions are dual: The universal restriction on property p to the complement of class c is equivalent to the complement of the existential restriction on p to c.

`include('Axioms/SWB001+0.ax')`

$\text{iext}(\text{uri_owl_equivalentClass}, \text{uri_ex_z}_1, \text{uri_ex_nz}_2)$ $\text{fof}(\text{conclusion_rdfbased_sem_restrict_term_sameall}, \text{conjecture})$
 $\text{iext}(\text{uri_owl_complementOf}, \text{uri_ex_nz}_2, \text{uri_ex_z}_2)$ and $\text{iext}(\text{uri_owl_complementOf}, \text{uri_ex_nc}, \text{uri_ex_c})$ and $\text{iext}(\text{uri_owl_someV}$

SWB106+1.p Self-Restriction As Existential Restriction

Self restrictions are more specific than unconstrained existential restrictions.

`include('Axioms/SWB001+0.ax')`

$\text{iext}(\text{uri_rdfs_subClassOf}, \text{uri_ex_z}_1, \text{uri_ex_z}_2)$ $\text{fof}(\text{conclusion_rdfbased_sem_restrict_term_selfsome}, \text{conjecture})$
 $\text{iext}(\text{uri_owl_someValuesFrom}, \text{uri_ex_z}_2, \text{uri_owl_Thing})$ and $\text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_z}_2, \text{uri_ex_p})$ and $\text{iext}(\text{uri_owl_has}$

SWB107+1.p Has-Restriction As Existential Restriction

A has-value restriction for a value v can be written as an existential restriction to a singleton class containing v.

`include('Axioms/SWB001+0.ax')`

$\text{iext}(\text{uri_owl_equivalentClass}, \text{uri_ex_z}_1, \text{uri_ex_z}_2)$ $\text{fof}(\text{conclusion_rdfbased_sem_restrict_term_somehas}, \text{conjecture})$
 $\exists x_1, x_0: (\text{iext}(\text{uri_owl_hasValue}, \text{uri_ex_z}_2, \text{uri_ex_u})$ and $\text{iext}(\text{uri_owl_onProperty}, \text{uri_ex_z}_2, \text{uri_ex_p})$ and $\text{iext}(\text{uri_owl_oneOf}, a$

SWB108+1.p Existential Restriction As Min-QCR

An existential restriction can be written as a min-1-QCR.

`include('Axioms/SWB001+0.ax')`

$\text{iext}(\text{uri_owl_equivalentClass}, \text{uri_ex_z}_1, \text{uri_ex_z}_2)$ $\text{fof}(\text{conclusion_rdfbased_sem_restrict_term_someqcr}, \text{conjecture})$
 $\text{iext}(\text{uri_owl_minQualifiedCardinality}, \text{uri_ex_z}_2, \text{literal_typed}(\text{dat_str}_1, \text{uri_xsd_nonNegativeInteger}))$ and $\text{iext}(\text{uri_owl_onPrope}$