

# SWV axioms

## SWV001-0.ax Program verification axioms

$\text{predecessor}(\text{successor}(x)) = x \quad \text{cnf}(\text{predecessor\_successor}, \text{axiom})$   
 $\text{successor}(\text{predecessor}(x)) = x \quad \text{cnf}(\text{successor\_predecessor}, \text{axiom})$   
 $\text{predecessor}(x) = \text{predecessor}(y) \Rightarrow x = y \quad \text{cnf}(\text{well\_defined\_predecessor}, \text{axiom})$   
 $\text{successor}(x) = \text{successor}(y) \Rightarrow x = y \quad \text{cnf}(\text{well\_defined\_successor}, \text{axiom})$   
 $\text{predecessor}(x) < x \quad \text{cnf}(\text{predecessor\_less\_than}, \text{axiom})$   
 $x < \text{successor}(x) \quad \text{cnf}(\text{less\_than\_successor}, \text{axiom})$   
 $(x < y \text{ and } y < z) \Rightarrow x < z \quad \text{cnf}(\text{transitivity\_of\_less\_than}, \text{axiom})$   
 $x < y \text{ or } y < x \text{ or } x = y \quad \text{cnf}(\text{all\_related}, \text{axiom})$   
 $\neg x < x \quad \text{cnf}(\text{x\_not\_less\_than\_x}, \text{axiom})$   
 $x < y \Rightarrow \neg y < x \quad \text{cnf}(\text{anti\_symmetry\_of\_less\_than}, \text{axiom})$   
 $(x = y \text{ and } x < z) \Rightarrow y < z \quad \text{cnf}(\text{equal\_and\_less\_than\_transitivity}_1, \text{axiom})$   
 $(x = y \text{ and } z < x) \Rightarrow z < y \quad \text{cnf}(\text{equal\_and\_less\_than\_transitivity}_2, \text{axiom})$

## SWV002-0.ax Program verification axioms

These "clauses arose in a natural manner from work done in program verification" [MOW76] p.779.

$q_1(\text{vj}, \text{vt}, \text{vx}) \Rightarrow q_2(\text{vj}, e(\text{vx}, n_1), \text{vx}) \quad \text{cnf}(\text{clause}_1, \text{axiom})$   
 $q_2(\text{vj}, \text{vt}, \text{vx}) \Rightarrow q_3(\text{successor}(n_1), \text{vt}, \text{vWhat}) \quad \text{cnf}(\text{clause}_2, \text{axiom})$   
 $(q_3(\text{vj}, \text{vt}, \text{vx}) \text{ and } \text{vj} \leq n) \Rightarrow q_4(\text{vj}, \text{vt}, \text{vx}) \quad \text{cnf}(\text{clause}_3, \text{axiom})$   
 $q_3(\text{vj}, \text{vt}, \text{vx}) \Rightarrow (\text{vj} \leq n \text{ or } q_7(\text{vj}, \text{vt}, \text{vx})) \quad \text{cnf}(\text{clause}_4, \text{axiom})$   
 $(q_4(\text{vj}, \text{vt}, \text{vx}) \text{ and } d(\text{vj}) \text{ and } e(\text{vx}, \text{vj}) \leq \text{vt}) \Rightarrow q_6(\text{vj}, \text{vt}, \text{vx}) \quad \text{cnf}(\text{clause}_5, \text{axiom})$   
 $(q_4(\text{vj}, \text{vt}, \text{vx}) \text{ and } d(\text{vj})) \Rightarrow (e(\text{vx}, \text{vj}) \leq \text{vt} \text{ or } q_5(\text{vj}, \text{vt}, \text{vx})) \quad \text{cnf}(\text{clause}_6, \text{axiom})$   
 $(q_5(\text{vj}, \text{vt}, \text{vx}) \text{ and } d(\text{vj})) \Rightarrow q_6(\text{vj}, e(\text{vx}, \text{vj}), \text{vx}) \quad \text{cnf}(\text{clause}_7, \text{axiom})$   
 $q_6(\text{vj}, \text{vt}, \text{vx}) \Rightarrow q_3(\text{successor}(\text{vj}), \text{vt}, \text{vx}) \quad \text{cnf}(\text{clause}_8, \text{axiom})$   
 $(n_1 \leq x \text{ and } x \leq n) \Rightarrow d(x) \quad \text{cnf}(\text{definition\_of\_d}_1, \text{axiom})$   
 $d(x) \Rightarrow \neg n_1 \leq x \quad \text{cnf}(\text{definition\_of\_d}_2, \text{axiom})$   
 $d(x) \Rightarrow x \leq n \quad \text{cnf}(\text{definition\_of\_d}_3, \text{axiom})$   
 $d(n_1) \quad \text{cnf}(\text{one\_is\_d}, \text{axiom})$   
 $d(n) \quad \text{cnf}(\text{n\_is\_d}, \text{axiom})$   
 $n_1 \leq n \quad \text{cnf}(\text{clause}_9, \text{axiom})$   
 $(\text{ub}(w_1, x, y, z) \text{ and } w_1 \leq w_2) \Rightarrow \text{ub}(w_2, x, y, z) \quad \text{cnf}(\text{clause}_{10}, \text{axiom})$   
 $(\text{ub}(w, x, y, z_1) \text{ and } \text{successor}(z_1) = z_2 \text{ and } d(z_2) \text{ and } e(x, z_2) \leq w) \Rightarrow \text{ub}(w, x, y, z_2) \quad \text{cnf}(\text{clause}_{11}, \text{axiom})$   
 $\neg \text{successor}(x) \leq x \quad \text{cnf}(\text{successor\_not\_less\_or\_equal}, \text{axiom})$   
 $x \leq \text{successor}(x) \quad \text{cnf}(\text{less\_or\_equal\_than\_successor}, \text{axiom})$   
 $x \leq x \quad \text{cnf}(\text{less\_or\_equal\_reflexivity}, \text{axiom})$   
 $(x \leq y \text{ and } y \leq x) \Rightarrow x = y \quad \text{cnf}(\text{less\_or\_equal\_implies\_equal}, \text{axiom})$   
 $(x \leq y \text{ and } y \leq z) \Rightarrow x \leq z \quad \text{cnf}(\text{transitivity\_of\_less\_or\_equal}, \text{axiom})$   
 $x = y \Rightarrow x \leq y \quad \text{cnf}(\text{equal\_implies\_less\_or\_equal}, \text{axiom})$

## SWV005-4.ax Cryptographic protocol axioms for Yahalom, simplified

$\text{c.in}(\text{c\_Event\_Oevent\_OSays}(\text{v\_A}, \text{v\_B}, \text{v\_X}), \text{c\_List\_Oset}(\text{v\_evs}, \text{tc\_Event\_Oevent}), \text{tc\_Event\_Oevent}) \Rightarrow \text{c.in}(\text{v\_X}, \text{c\_Message\_Oagent}(\text{v\_A}), \text{c\_List\_Oset}(\text{v\_evs}, \text{tc\_Event\_Oevent}))$   
 $(\text{c.in}(\text{v\_Z}, \text{c\_Message\_Oparts}(\text{c.insert}(\text{v\_X}, \text{v\_H}, \text{tc\_Message\_Omsg})), \text{tc\_Message\_Omsg}) \text{ and } \text{c.in}(\text{v\_X}, \text{c\_Message\_Osynth}(\text{c.Message\_Osynth}(\text{v\_Z}, \text{c\_union}(\text{c\_Message\_Osynth}(\text{c\_Message\_Oanalz}(\text{v\_H})), \text{c\_Message\_Oparts}(\text{v\_H}), \text{tc\_Message\_Omsg}), \text{tc\_Message\_Omsg})), \text{tc\_Message\_Omsg})) \Rightarrow \text{c.in}(\text{v\_X}, \text{c\_Message\_Oparts}(\text{v\_H}), \text{tc\_Message\_Omsg})$   
 $\text{c.in}(\text{c\_Message\_Omsg\_OCrypt}(\text{v\_K}, \text{v\_X}), \text{c\_Message\_Oparts}(\text{v\_H}), \text{tc\_Message\_Omsg}) \Rightarrow \text{c.in}(\text{v\_X}, \text{c\_Message\_Oparts}(\text{v\_H}), \text{tc\_Message\_Omsg})$   
 $(\text{c.in}(\text{v\_evs}, \text{c\_Yahalom\_Oyahalom}, \text{tc\_List\_Olist}(\text{tc\_Event\_Oevent})) \text{ and } \text{c.in}(\text{c\_Event\_Oevent\_OGets}(\text{v\_B}, \text{v\_X}), \text{c\_List\_Oset}(\text{v\_evs}, \text{tc\_Event\_Oevent})), \text{tc\_Event\_Oevent})) \Rightarrow \text{c.in}(\text{v\_X}, \text{c\_Message\_Oanalz}(\text{c\_Event\_Oknows}(\text{c\_Message\_Oagent\_OSpy}, \text{v\_evs})), \text{tc\_Message\_Omsg}) \quad \text{cnf}(\text{cls\_Yahalom\_OGet}, \text{axiom})$   
 $(\text{c.in}(\text{v\_evs}, \text{c\_Yahalom\_Oyahalom}, \text{tc\_List\_Olist}(\text{tc\_Event\_Oevent})) \text{ and } \text{c.in}(\text{c\_Message\_Omsg\_OKey}(\text{c\_Public\_OshrK}(\text{v\_A})), \text{c\_Message\_Oparts}(\text{v\_H}), \text{tc\_Message\_Omsg})), \text{tc\_Message\_Omsg})) \Rightarrow \text{c.in}(\text{v\_A}, \text{c\_Event\_Obad}, \text{tc\_Message\_Oagent}) \quad \text{cnf}(\text{cls\_Yahalom\_OSpy\_analz\_shrK}_0, \text{axiom})$   
 $(\text{c.in}(\text{v\_A}, \text{c\_Event\_Obad}, \text{tc\_Message\_Oagent}) \text{ and } \text{c.in}(\text{v\_evs}, \text{c\_Yahalom\_Oyahalom}, \text{tc\_List\_Olist}(\text{tc\_Event\_Oevent}))) \Rightarrow \text{c.in}(\text{c\_Message\_Omsg\_OKey}(\text{c\_Public\_OshrK}(\text{v\_A})), \text{c\_Message\_Oanalz}(\text{c\_Event\_Oknows}(\text{c\_Message\_Oagent\_OSpy}, \text{v\_evs})), \text{tc\_Message\_Omsg}))$   
 $(\text{c.in}(\text{v\_evs}, \text{c\_Yahalom\_Oyahalom}, \text{tc\_List\_Olist}(\text{tc\_Event\_Oevent})) \text{ and } \text{c.in}(\text{c\_Message\_Omsg\_OKey}(\text{c\_Public\_OshrK}(\text{v\_A})), \text{c\_Message\_Oparts}(\text{v\_H}), \text{tc\_Message\_Omsg})), \text{tc\_Message\_Omsg})) \Rightarrow \text{c.in}(\text{v\_A}, \text{c\_Event\_Obad}, \text{tc\_Message\_Oagent}) \quad \text{cnf}(\text{cls\_Yahalom\_OSpy\_see\_shrK}_0, \text{axiom})$   
 $(\text{c.in}(\text{v\_A}, \text{c\_Event\_Obad}, \text{tc\_Message\_Oagent}) \text{ and } \text{c.in}(\text{v\_evs}, \text{c\_Yahalom\_Oyahalom}, \text{tc\_List\_Olist}(\text{tc\_Event\_Oevent}))) \Rightarrow \text{c.in}(\text{c\_Message\_Omsg\_OKey}(\text{c\_Public\_OshrK}(\text{v\_A})), \text{c\_Message\_Oparts}(\text{c\_Event\_Oknows}(\text{c\_Message\_Oagent\_OSpy}, \text{v\_evs})), \text{tc\_Message\_Omsg}))$

## SWV007+0.ax Priority queue checker: quasi-order set with bottom element

$\forall u, v, w: ((u < v \text{ and } v < w) \Rightarrow u < w) \quad \text{fof}(\text{transitivity}, \text{axiom})$   
 $\forall u, v: (u < v \text{ or } v < u) \quad \text{fof}(\text{totality}, \text{axiom})$

$\forall u: u < u \quad \text{fof}(\text{reflexivity, axiom})$   
 $\forall u, v: (\text{strictly\_less\_than}(u, v) \iff (u < v \text{ and } \neg v < u)) \quad \text{fof}(\text{strictly\_smaller\_definition, axiom})$   
 $\forall u: \text{bottom} < u \quad \text{fof}(\text{bottom\_smallest, axiom})$

### SWV007+1.ax Priority queue checker: priority queues

Priority queues are inductively defined.

$\neg \text{isnonempty\_pq}(\text{create\_pq}) \quad \text{fof}(\text{ax}_6, \text{axiom})$   
 $\forall u, v: \text{isnonempty\_pq}(\text{insert\_pq}(u, v)) \quad \text{fof}(\text{ax}_7, \text{axiom})$   
 $\forall u: \neg \text{contains\_pq}(\text{create\_pq}, u) \quad \text{fof}(\text{ax}_8, \text{axiom})$   
 $\forall u, v, w: (\text{contains\_pq}(\text{insert\_pq}(u, v), w) \iff (\text{contains\_pq}(u, w) \text{ or } v = w)) \quad \text{fof}(\text{ax}_9, \text{axiom})$   
 $\forall u, v: (\text{issmallestelement\_pq}(u, v) \iff \forall w: (\text{contains\_pq}(u, w) \Rightarrow v < w)) \quad \text{fof}(\text{ax}_{10}, \text{axiom})$   
 $\forall u, v: \text{remove\_pq}(\text{insert\_pq}(u, v), v) = u \quad \text{fof}(\text{ax}_{11}, \text{axiom})$   
 $\forall u, v, w: ((\text{contains\_pq}(u, w) \text{ and } v \neq w) \Rightarrow \text{remove\_pq}(\text{insert\_pq}(u, v), w) = \text{insert\_pq}(\text{remove\_pq}(u, w), v)) \quad \text{fof}(\text{ax}_{12}, \text{axiom})$   
 $\forall u, v: ((\text{contains\_pq}(u, v) \text{ and } \text{issmallestelement\_pq}(u, v)) \Rightarrow \text{findmin\_pq\_eff}(u, v) = u) \quad \text{fof}(\text{ax}_{13}, \text{axiom})$   
 $\forall u, v: ((\text{contains\_pq}(u, v) \text{ and } \text{issmallestelement\_pq}(u, v)) \Rightarrow \text{findmin\_pq\_res}(u, v) = v) \quad \text{fof}(\text{ax}_{14}, \text{axiom})$   
 $\forall u, v: ((\text{contains\_pq}(u, v) \text{ and } \text{issmallestelement\_pq}(u, v)) \Rightarrow \text{removemin\_pq\_eff}(u, v) = \text{remove\_pq}(u, v)) \quad \text{fof}(\text{ax}_{15}, \text{axiom})$   
 $\forall u, v: ((\text{contains\_pq}(u, v) \text{ and } \text{issmallestelement\_pq}(u, v)) \Rightarrow \text{removemin\_pq\_res}(u, v) = v) \quad \text{fof}(\text{ax}_{16}, \text{axiom})$   
 $\forall u, v, w: \text{insert\_pq}(\text{insert\_pq}(u, v), w) = \text{insert\_pq}(\text{insert\_pq}(u, w), v) \quad \text{fof}(\text{ax}_{17}, \text{axiom})$

### SWV007+2.ax Priority queue checker: system of lower bounds

$\neg \text{isnonempty\_slb}(\text{create\_slb}) \quad \text{fof}(\text{ax}_{18}, \text{axiom})$   
 $\forall u, v, w: \text{isnonempty\_slb}(\text{insert\_slb}(u, \text{pair}(v, w))) \quad \text{fof}(\text{ax}_{19}, \text{axiom})$   
 $\forall u: \neg \text{contains\_slb}(\text{create\_slb}, u) \quad \text{fof}(\text{ax}_{20}, \text{axiom})$   
 $\forall u, v, w, x: (\text{contains\_slb}(\text{insert\_slb}(u, \text{pair}(v, x)), w) \iff (\text{contains\_slb}(u, w) \text{ or } v = w)) \quad \text{fof}(\text{ax}_{21}, \text{axiom})$   
 $\forall u, v: \neg \text{pair\_in\_list}(\text{create\_slb}, u, v) \quad \text{fof}(\text{ax}_{22}, \text{axiom})$   
 $\forall u, v, w, x, y: (\text{pair\_in\_list}(\text{insert\_slb}(u, \text{pair}(v, x)), w, y) \iff (\text{pair\_in\_list}(u, w, y) \text{ or } (v = w \text{ and } x = y))) \quad \text{fof}(\text{ax}_{23}, \text{axiom})$   
 $\forall u, v, w: \text{remove\_slb}(\text{insert\_slb}(u, \text{pair}(v, w)), v) = u \quad \text{fof}(\text{ax}_{24}, \text{axiom})$   
 $\forall u, v, w, x: ((v \neq w \text{ and } \text{contains\_slb}(u, w)) \Rightarrow \text{remove\_slb}(\text{insert\_slb}(u, \text{pair}(v, x)), w) = \text{insert\_slb}(\text{remove\_slb}(u, w), \text{pair}(v, x))) \quad \text{fof}(\text{ax}_{25}, \text{axiom})$   
 $\forall u, v, w: \text{lookup\_slb}(\text{insert\_slb}(u, \text{pair}(v, w)), v) = w \quad \text{fof}(\text{ax}_{26}, \text{axiom})$   
 $\forall u, v, w, x: ((v \neq w \text{ and } \text{contains\_slb}(u, w)) \Rightarrow \text{lookup\_slb}(\text{insert\_slb}(u, \text{pair}(v, x)), w) = \text{lookup\_slb}(u, w)) \quad \text{fof}(\text{ax}_{27}, \text{axiom})$   
 $\forall u: \text{update\_slb}(\text{create\_slb}, u) = \text{create\_slb} \quad \text{fof}(\text{ax}_{28}, \text{axiom})$   
 $\forall u, v, w, x: (\text{strictly\_less\_than}(x, w) \Rightarrow \text{update\_slb}(\text{insert\_slb}(u, \text{pair}(v, x)), w) = \text{insert\_slb}(\text{update\_slb}(u, w), \text{pair}(v, w))) \quad \text{fof}(\text{ax}_{29}, \text{axiom})$   
 $\forall u, v, w, x: (w < x \Rightarrow \text{update\_slb}(\text{insert\_slb}(u, \text{pair}(v, x)), w) = \text{insert\_slb}(\text{update\_slb}(u, w), \text{pair}(v, x))) \quad \text{fof}(\text{ax}_{30}, \text{axiom})$

### SWV007+3.ax Priority queue checker: checked priority queues

This axiom set fully describes checked priority queues. Checked priority queues are defined as triples of a "priority queue pretender", a system of lower bounds and Boolean value that keep track of errors.

$\forall u: \text{succ\_cpq}(u, u) \quad \text{fof}(\text{ax}_{31}, \text{axiom})$   
 $\forall u, v, w: (\text{succ\_cpq}(u, v) \Rightarrow \text{succ\_cpq}(u, \text{insert\_cpq}(v, w))) \quad \text{fof}(\text{ax}_{32}, \text{axiom})$   
 $\forall u, v, w: (\text{succ\_cpq}(u, v) \Rightarrow \text{succ\_cpq}(u, \text{remove\_cpq}(v, w))) \quad \text{fof}(\text{ax}_{33}, \text{axiom})$   
 $\forall u, v: (\text{succ\_cpq}(u, v) \Rightarrow \text{succ\_cpq}(u, \text{findmin\_cpq\_eff}(v))) \quad \text{fof}(\text{ax}_{34}, \text{axiom})$   
 $\forall u, v: (\text{succ\_cpq}(u, v) \Rightarrow \text{succ\_cpq}(u, \text{removemin\_cpq\_eff}(v))) \quad \text{fof}(\text{ax}_{35}, \text{axiom})$   
 $\forall u, v: \text{check\_cpq}(\text{triple}(u, \text{create\_slb}, v)) \quad \text{fof}(\text{ax}_{36}, \text{axiom})$   
 $\forall u, v, w, x, y: (y < x \Rightarrow (\text{check\_cpq}(\text{triple}(u, \text{insert\_slb}(v, \text{pair}(x, y)), w)) \iff \text{check\_cpq}(\text{triple}(u, v, w)))) \quad \text{fof}(\text{ax}_{37}, \text{axiom})$   
 $\forall u, v, w, x, y: (\text{strictly\_less\_than}(x, y) \Rightarrow (\text{check\_cpq}(\text{triple}(u, \text{insert\_slb}(v, \text{pair}(x, y)), w)) \iff \text{\$false})) \quad \text{fof}(\text{ax}_{38}, \text{axiom})$   
 $\forall u, v, w, x: (\text{contains\_cpq}(\text{triple}(u, v, w), x) \iff \text{contains\_slb}(v, x)) \quad \text{fof}(\text{ax}_{39}, \text{axiom})$   
 $\forall u, v: (\text{ok}(\text{triple}(u, v, \text{bad})) \iff \text{\$false}) \quad \text{fof}(\text{ax}_{40}, \text{axiom})$   
 $\forall u, v, w: (\neg \text{ok}(\text{triple}(u, v, w)) \Rightarrow w = \text{bad}) \quad \text{fof}(\text{ax}_{41}, \text{axiom})$   
 $\forall u, v, w, x: \text{insert\_cpq}(\text{triple}(u, v, w), x) = \text{triple}(\text{insert\_pq}(u, x), \text{insert\_slb}(v, \text{pair}(x, \text{bottom})), w) \quad \text{fof}(\text{ax}_{42}, \text{axiom})$   
 $\forall u, v, w, x: (\neg \text{contains\_slb}(v, x) \Rightarrow \text{remove\_cpq}(\text{triple}(u, v, w), x) = \text{triple}(u, v, \text{bad})) \quad \text{fof}(\text{ax}_{43}, \text{axiom})$   
 $\forall u, v, w, x: ((\text{contains\_slb}(v, x) \text{ and } \text{lookup\_slb}(v, x) < x) \Rightarrow \text{remove\_cpq}(\text{triple}(u, v, w), x) = \text{triple}(\text{remove\_pq}(u, x), \text{remove\_slb}(u, w), \text{pair}(v, w))) \quad \text{fof}(\text{ax}_{44}, \text{axiom})$   
 $\forall u, v, w, x: ((\text{contains\_slb}(v, x) \text{ and } \text{strictly\_less\_than}(x, \text{lookup\_slb}(v, x))) \Rightarrow \text{remove\_cpq}(\text{triple}(u, v, w), x) = \text{triple}(\text{remove\_pq}(u, x), \text{remove\_slb}(u, w), \text{pair}(v, w))) \quad \text{fof}(\text{ax}_{45}, \text{axiom})$   
 $\forall u, v: \text{findmin\_cpq\_eff}(\text{triple}(u, \text{create\_slb}, v)) = \text{triple}(u, \text{create\_slb}, \text{bad}) \quad \text{fof}(\text{ax}_{46}, \text{axiom})$   
 $\forall u, v, w, x: ((v \neq \text{create\_slb} \text{ and } \neg \text{contains\_slb}(v, \text{findmin\_cpq\_res}(u))) \Rightarrow \text{findmin\_cpq\_eff}(\text{triple}(u, v, w)) = \text{triple}(u, \text{update\_slb}(u, w), \text{pair}(v, w))) \quad \text{fof}(\text{ax}_{47}, \text{axiom})$   
 $\forall u, v, w, x: ((v \neq \text{create\_slb} \text{ and } \text{contains\_slb}(v, \text{findmin\_cpq\_res}(u)) \text{ and } \text{strictly\_less\_than}(\text{findmin\_cpq\_res}(u), \text{lookup\_slb}(v, \text{findmin\_cpq\_res}(u)))) \Rightarrow \text{findmin\_cpq\_eff}(\text{triple}(u, v, w)) = \text{triple}(u, \text{update\_slb}(v, \text{findmin\_cpq\_res}(u)), \text{bad})) \quad \text{fof}(\text{ax}_{48}, \text{axiom})$   
 $\forall u, v, w, x: ((v \neq \text{create\_slb} \text{ and } \text{contains\_slb}(v, \text{findmin\_cpq\_res}(u)) \text{ and } \text{lookup\_slb}(v, \text{findmin\_cpq\_res}(u)) < \text{findmin\_cpq\_res}(u)) \Rightarrow \text{findmin\_cpq\_eff}(\text{triple}(u, v, w)) = \text{triple}(u, \text{update\_slb}(v, \text{findmin\_cpq\_res}(u)), w)) \quad \text{fof}(\text{ax}_{49}, \text{axiom})$   
 $\forall u, v: \text{findmin\_cpq\_res}(\text{triple}(u, \text{create\_slb}, v)) = \text{bottom} \quad \text{fof}(\text{ax}_{50}, \text{axiom})$   
 $\forall u, v, w, x: (v \neq \text{create\_slb} \Rightarrow \text{findmin\_cpq\_res}(\text{triple}(u, v, w)) = \text{findmin\_cpq\_res}(u)) \quad \text{fof}(\text{ax}_{51}, \text{axiom})$   
 $\forall u: \text{removemin\_cpq\_eff}(u) = \text{remove\_cpq}(\text{findmin\_cpq\_eff}(u), \text{findmin\_cpq\_res}(u)) \quad \text{fof}(\text{ax}_{52}, \text{axiom})$

$\forall u: \text{removemin\_cpq\_res}(u) = \text{findmin\_cpq\_res}(u) \quad \text{fof}(\text{ax}_{53}, \text{axiom})$

**SWV007+4.ax** Priority queue checker: implementation function, Pi, Pi#

$\forall u, v: i(\text{triple}(u, \text{create\_slb}, v)) = \text{create\_pq} \quad \text{fof}(\text{ax}_{54}, \text{axiom})$

$\forall u, v, w, x, y: i(\text{triple}(u, \text{insert\_slb}(v, \text{pair}(x, y)), w)) = \text{insert\_pq}(i(\text{triple}(u, v, w)), x) \quad \text{fof}(\text{ax}_{55}, \text{axiom})$

$\forall u, v: (\text{pi\_sharp\_remove}(u, v) \iff \text{contains\_pq}(u, v)) \quad \text{fof}(\text{ax}_{56}, \text{axiom})$

$\forall u, v: (\text{pi\_remove}(u, v) \iff \text{pi\_sharp\_remove}(i(u), v)) \quad \text{fof}(\text{ax}_{57}, \text{axiom})$

$\forall u, v: (\text{pi\_sharp\_find\_min}(u, v) \iff (\text{contains\_pq}(u, v) \text{ and } \text{issmallestelement\_pq}(u, v))) \quad \text{fof}(\text{ax}_{58}, \text{axiom})$

$\forall u: (\text{pi\_find\_min}(u) \iff \exists v: \text{pi\_sharp\_find\_min}(i(u), v)) \quad \text{fof}(\text{ax}_{59}, \text{axiom})$

$\forall u, v: (\text{pi\_sharp\_removemin}(u, v) \iff (\text{contains\_pq}(u, v) \text{ and } \text{issmallestelement\_pq}(u, v))) \quad \text{fof}(\text{ax}_{60}, \text{axiom})$

$\forall u: (\text{pi\_removemin}(u) \iff \exists v: \text{pi\_sharp\_find\_min}(i(u), v)) \quad \text{fof}(\text{ax}_{61}, \text{axiom})$

$\forall u: (\text{phi}(u) \iff \exists v: (\text{succ\_cpq}(u, v) \text{ and } \text{ok}(v) \text{ and } \text{check\_cpq}(v))) \quad \text{fof}(\text{ax}_{62}, \text{axiom})$

**SWV008^0.ax** ICL logic based upon modal logic based upon simple type theory

$\text{rel}: \$i \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{rel\_type}, \text{type})$

$\text{icl\_atom}: (\$i \rightarrow \$o) \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{icl\_atom\_type}, \text{type})$

$\text{icl\_atom} = (\lambda p: \$i \rightarrow \$o: (\text{mbox@rel@}p)) \quad \text{thf}(\text{icl\_atom}, \text{definition})$

$\text{icl\_princ}: (\$i \rightarrow \$o) \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{icl\_princ\_type}, \text{type})$

$\text{icl\_princ} = (\lambda p: \$i \rightarrow \$o: p) \quad \text{thf}(\text{icl\_princ}, \text{definition})$

$\text{icl\_and}: (\$i \rightarrow \$o) \rightarrow (\$i \rightarrow \$o) \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{icl\_and\_type}, \text{type})$

$\text{icl\_and} = (\lambda a: \$i \rightarrow \$o, b: \$i \rightarrow \$o: (\text{mand@a@}b)) \quad \text{thf}(\text{icl\_and}, \text{definition})$

$\text{icl\_or}: (\$i \rightarrow \$o) \rightarrow (\$i \rightarrow \$o) \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{icl\_or\_type}, \text{type})$

$\text{icl\_or} = (\lambda a: \$i \rightarrow \$o, b: \$i \rightarrow \$o: (\text{mor@a@}b)) \quad \text{thf}(\text{icl\_or}, \text{definition})$

$\text{icl\_impl}: (\$i \rightarrow \$o) \rightarrow (\$i \rightarrow \$o) \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{icl\_impl\_type}, \text{type})$

$\text{icl\_impl} = (\lambda a: \$i \rightarrow \$o, b: \$i \rightarrow \$o: (\text{mbox@rel@}(\text{mimpl@a@}b))) \quad \text{thf}(\text{icl\_impl}, \text{definition})$

$\text{icl\_true}: \$i \rightarrow \$o \quad \text{thf}(\text{icl\_true\_type}, \text{type})$

$\text{icl\_true} = \text{mtrue} \quad \text{thf}(\text{icl\_true}, \text{definition})$

$\text{icl\_false}: \$i \rightarrow \$o \quad \text{thf}(\text{icl\_false\_type}, \text{type})$

$\text{icl\_false} = \text{mfalse} \quad \text{thf}(\text{icl\_false}, \text{definition})$

$\text{icl\_says}: (\$i \rightarrow \$o) \rightarrow (\$i \rightarrow \$o) \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{icl\_says\_type}, \text{type})$

$\text{icl\_says} = (\lambda a: \$i \rightarrow \$o, s: \$i \rightarrow \$o: (\text{mbox@rel@}(\text{mor@a@s}))) \quad \text{thf}(\text{icl\_says}, \text{definition})$

$\text{iclval}: (\$i \rightarrow \$o) \rightarrow \$o \quad \text{thf}(\text{iclval\_decl\_type}, \text{type})$

$\text{iclval} = (\lambda x: \$i \rightarrow \$o: (\text{mvalid@}x)) \quad \text{thf}(\text{icl\_s4\_valid}, \text{definition})$

**SWV008^1.ax** ICL notions of validity wrt S4

$\forall a: \$i \rightarrow \$o: (\text{mvalid@}(\text{mimpl@}(\text{mbox@rel@a@}a))) \quad \text{thf}(\text{refl\_axiom}, \text{axiom})$

$\forall b: \$i \rightarrow \$o: (\text{mvalid@}(\text{mimpl@}(\text{mbox@rel@}b@(\text{mbox@rel@}(\text{mbox@rel@}b)))))) \quad \text{thf}(\text{trans\_axiom}, \text{axiom})$

**SWV008^2.ax** ICL $\wedge\Rightarrow$  logic based upon modal logic

$\text{icl\_impl\_princ}: (\$i \rightarrow \$o) \rightarrow (\$i \rightarrow \$o) \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{icl\_impl\_princ\_type}, \text{type})$

$\text{icl\_impl\_princ} = (\lambda a: \$i \rightarrow \$o, b: \$i \rightarrow \$o: (\text{mbox@rel@}(\text{mimpl@a@}b))) \quad \text{thf}(\text{icl\_impl\_princ}, \text{definition})$

**SWV010^0.ax** Translation from Binder Logic (BL) to CS4

$\text{princ\_inj}: \text{individuals} \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{princ\_inj}, \text{type})$

$\text{bl\_atom}: (\$i \rightarrow \$o) \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{bl\_atom\_decl}, \text{type})$

$\text{bl\_princ}: (\$i \rightarrow \$o) \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{bl\_princ\_decl}, \text{type})$

$\text{bl\_and}: (\$i \rightarrow \$o) \rightarrow (\$i \rightarrow \$o) \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{bl\_and\_decl}, \text{type})$

$\text{bl\_or}: (\$i \rightarrow \$o) \rightarrow (\$i \rightarrow \$o) \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{bl\_or\_decl}, \text{type})$

$\text{bl\_impl}: (\$i \rightarrow \$o) \rightarrow (\$i \rightarrow \$o) \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{bl\_impl\_decl}, \text{type})$

$\text{bl\_all}: (\text{individuals} \rightarrow \$i \rightarrow \$o) \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{bl\_all\_decl}, \text{type})$

$\text{bl\_true}: \$i \rightarrow \$o \quad \text{thf}(\text{bl\_true\_decl}, \text{type})$

$\text{bl\_false}: \$i \rightarrow \$o \quad \text{thf}(\text{bl\_false\_decl}, \text{type})$

$\text{bl\_says}: \text{individuals} \rightarrow (\$i \rightarrow \$o) \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{bl\_says\_decl}, \text{type})$

$\text{bl\_atom} = (\lambda p: \$i \rightarrow \$o: (\text{cs4\_atom@}p)) \quad \text{thf}(\text{bl\_atom}, \text{definition})$

$\text{bl\_princ} = (\lambda p: \$i \rightarrow \$o: (\text{cs4\_atom@}p)) \quad \text{thf}(\text{bl\_princ}, \text{definition})$

$\text{bl\_and} = (\lambda a: \$i \rightarrow \$o, b: \$i \rightarrow \$o: (\text{cs4\_and@a@}b)) \quad \text{thf}(\text{bl\_and}, \text{definition})$

$\text{bl\_or} = (\lambda a: \$i \rightarrow \$o, b: \$i \rightarrow \$o: (\text{cs4\_or@a@}b)) \quad \text{thf}(\text{bl\_or}, \text{definition})$

$\text{bl\_impl} = (\lambda a: \$i \rightarrow \$o, b: \$i \rightarrow \$o: (\text{cs4\_impl@a@}b)) \quad \text{thf}(\text{bl\_impl}, \text{definition})$

$\text{bl\_all} = (\lambda a: \text{individuals} \rightarrow \$i \rightarrow \$o: (\text{cs4\_all@a})) \quad \text{thf}(\text{bl\_all}, \text{definition})$

$\text{bl\_true} = \text{cs4\_true} \quad \text{thf}(\text{bl\_true}, \text{definition})$

$\text{bl\_false} = \text{cs4\_false} \quad \text{thf}(\text{bl\_false}, \text{definition})$

$\text{bl\_says} = (\lambda k: \text{individuals}, a: \$i \rightarrow \$o: (\text{cs4\_box@}(\text{cs4\_impl@}(\text{bl\_princ@}(\text{princ\_inj@}k))@a))) \quad \text{thf}(\text{bl\_says}, \text{definition})$

$\text{bl\_valid}: (\$i \rightarrow \$o) \rightarrow \$o \quad \text{thf}(\text{bl\_valid\_decl}, \text{type})$   
 $\text{bl\_valid} = \text{mvalid} \quad \text{thf}(\text{bl\_valid\_def}, \text{definition})$   
 $\text{loca}: \text{individuals} \quad \text{thf}(\text{loca\_decl}, \text{type})$   
 $\text{cs4\_valid} @ (\text{cs4\_all} @ \lambda k: \text{individuals}: (\text{cs4\_impl} @ (\text{princ\_inj} @ k) @ (\text{princ\_inj} @ \text{loca}))) \quad \text{thf}(\text{loca\_strength}, \text{axiom})$

### SWV013-0.ax Lists in Separation Logic

Axioms for proving entailments between separation logic formulas with list predicates.

$\text{sep}(s, \text{sep}(t, \text{sigma})) = \text{sep}(t, \text{sep}(s, \text{sigma})) \quad \text{cnf}(\text{associative\_commutative}, \text{axiom})$   
 $\text{sep}(\text{lseg}(x, x), \text{sigma}) = \text{sigma} \quad \text{cnf}(\text{normalization}, \text{axiom})$   
 $\neg \text{heap}(\text{sep}(\text{next}(\text{nil}, y), \text{sigma})) \quad \text{cnf}(\text{wellformedness}_1, \text{axiom})$   
 $\text{heap}(\text{sep}(\text{lseg}(\text{nil}, y), \text{sigma})) \Rightarrow y = \text{nil} \quad \text{cnf}(\text{wellformedness}_2, \text{axiom})$   
 $\neg \text{heap}(\text{sep}(\text{next}(x, y), \text{sep}(\text{next}(x, z), \text{sigma}))) \quad \text{cnf}(\text{wellformedness}_3, \text{axiom})$   
 $\text{heap}(\text{sep}(\text{next}(x, y), \text{sep}(\text{lseg}(x, z), \text{sigma}))) \Rightarrow x = z \quad \text{cnf}(\text{wellformedness}_4, \text{axiom})$   
 $\text{heap}(\text{sep}(\text{lseg}(x, y), \text{sep}(\text{lseg}(x, z), \text{sigma}))) \Rightarrow (x = y \text{ or } x = z) \quad \text{cnf}(\text{wellformedness}_5, \text{axiom})$   
 $\text{heap}(\text{sep}(\text{next}(x, y), \text{sep}(\text{lseg}(y, z), \text{sigma}))) \Rightarrow (x = y \text{ or } \text{heap}(\text{sep}(\text{lseg}(x, z), \text{sigma}))) \quad \text{cnf}(\text{unfolding}_2, \text{axiom})$   
 $\text{heap}(\text{sep}(\text{lseg}(x, y), \text{sep}(\text{lseg}(y, \text{nil}), \text{sigma}))) \Rightarrow \text{heap}(\text{sep}(\text{lseg}(x, \text{nil}), \text{sigma})) \quad \text{cnf}(\text{unfolding}_3, \text{axiom})$   
 $\text{heap}(\text{sep}(\text{lseg}(x, y), \text{sep}(\text{lseg}(y, z), \text{sep}(\text{next}(z, w), \text{sigma})))) \Rightarrow \text{heap}(\text{sep}(\text{lseg}(x, z), \text{sep}(\text{next}(z, w), \text{sigma}))) \quad \text{cnf}(\text{unfolding}_4, \text{axiom})$   
 $\text{heap}(\text{sep}(\text{lseg}(x, y), \text{sep}(\text{lseg}(y, z), \text{sep}(\text{lseg}(z, w), \text{sigma})))) \Rightarrow (z = w \text{ or } \text{heap}(\text{sep}(\text{lseg}(x, z), \text{sep}(\text{lseg}(z, w), \text{sigma})))) \quad \text{cnf}(\text{unfolding}_5, \text{axiom})$

## SWV problems

### SWV001-1.p PV1

These "clauses arose in a natural manner from work done in program verification" [MOW76] p.779.

$(x=y \text{ and } \text{less\_or\_equalish}(x, z)) \Rightarrow \text{less\_or\_equalish}(y, z) \quad \text{cnf}(\text{less\_or\_equal\_substitution}_1, \text{axiom})$   
 $(x=y \text{ and } \text{less\_or\_equalish}(z, x)) \Rightarrow \text{less\_or\_equalish}(z, y) \quad \text{cnf}(\text{less\_or\_equal\_substitution}_2, \text{axiom})$   
 $(q_1(x, y, z) \text{ and } \text{less\_or\_equalish}(x, y)) \Rightarrow q_2(x, y, z) \quad \text{cnf}(\text{clause}_1, \text{axiom})$   
 $q_1(x, y, z) \Rightarrow (\text{less\_or\_equalish}(x, y) \text{ or } q_3(x, y, z)) \quad \text{cnf}(\text{clause}_2, \text{axiom})$   
 $q_2(x, y, z) \Rightarrow q_4(x, y, y) \quad \text{cnf}(\text{clause}_3, \text{axiom})$   
 $q_3(x, y, z) \Rightarrow q_4(x, y, x) \quad \text{cnf}(\text{clause}_4, \text{axiom})$   
 $\text{less\_or\_equalish}(x, x) \quad \text{cnf}(\text{less\_or\_equal\_reflexivity}, \text{axiom})$   
 $(\text{less\_or\_equalish}(x, y) \text{ and } \text{less\_or\_equalish}(y, x)) \Rightarrow x=y \quad \text{cnf}(\text{less\_or\_equal\_implies\_equal}, \text{axiom})$   
 $(\text{less\_or\_equalish}(x, y) \text{ and } \text{less\_or\_equalish}(y, z)) \Rightarrow \text{less\_or\_equalish}(x, z) \quad \text{cnf}(\text{transitivity\_of\_less\_or\_equal}, \text{axiom})$   
 $\text{less\_or\_equalish}(x, y) \text{ or } \text{less\_or\_equalish}(y, x) \quad \text{cnf}(\text{all\_less\_or\_equal}, \text{axiom})$   
 $x=y \Rightarrow \text{less\_or\_equalish}(x, y) \quad \text{cnf}(\text{equal\_implies\_less\_or\_equal}, \text{axiom})$   
 $q_1(a, b, c) \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $(q_4(a, b, w) \text{ and } \text{less\_or\_equalish}(a, w) \text{ and } \text{less\_or\_equalish}(b, w)) \Rightarrow \neg \text{less\_or\_equalish}(w, a) \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $(q_4(a, b, w) \text{ and } \text{less\_or\_equalish}(a, w) \text{ and } \text{less\_or\_equalish}(b, w)) \Rightarrow \neg \text{less\_or\_equalish}(w, b) \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$

### SWV002-1.p E1

include('Axioms/SWV001-0.ax')

$\neg n < j \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $k < j \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture})$   
 $\neg k < i \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $i < n \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $a(j) < a(k) \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $(x < j \text{ and } a(x) < a(k)) \Rightarrow x < i \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $(1 < i \text{ and } a(x) < a(\text{predecessor}(i))) \Rightarrow (x < i \text{ or } n < x) \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $(1 < x \text{ and } x < i) \Rightarrow \neg a(x) < a(\text{predecessor}(x)) \quad \text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $\neg q < i \quad \text{cnf}(\text{clause}_9, \text{negated\_conjecture})$   
 $\neg j < q \quad \text{cnf}(\text{clause}_{10}, \text{negated\_conjecture})$   
 $a(q) < a(j) \quad \text{cnf}(\text{clause}_{11}, \text{negated\_conjecture})$

### SWV003-1.p E2

include('Axioms/SWV001-0.ax')

$\neg n < j \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $k < j \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture})$   
 $\neg k < i \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $i < n \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $a(j) < a(k) \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $(x < j \text{ and } a(x) < a(k)) \Rightarrow x < i \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $(1 < i \text{ and } a(x) < a(\text{predecessor}(i))) \Rightarrow (x < i \text{ or } n < x) \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$

$(1 < x \text{ and } x < i) \Rightarrow \neg a(x) < a(\text{predecessor}(x))$      $\text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $j < i$      $\text{cnf}(\text{clause}_9, \text{negated\_conjecture})$

#### SWV004-1.p E3

$\text{include}(\text{'Axioms/SWV001-0.ax'})$   
 $\neg n < j$      $\text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $k < j$      $\text{cnf}(\text{clause}_{23}, \text{negated\_conjecture})$   
 $\neg k < i$      $\text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $i < n$      $\text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $a(j) < a(k)$      $\text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $a(q) < a(k)$      $\text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $(x < j \text{ and } a(x) < a(k)) \Rightarrow x < i$      $\text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $(1 < i \text{ and } a(x) < a(\text{predecessor}(i))) \Rightarrow (x < i \text{ or } n < x)$      $\text{cnf}(\text{clause}_9, \text{negated\_conjecture})$   
 $(1 < x \text{ and } x < i) \Rightarrow \neg a(x) < a(\text{predecessor}(x))$      $\text{cnf}(\text{clause}_{10}, \text{negated\_conjecture})$   
 $\neg q < i$      $\text{cnf}(\text{clause}_{11}, \text{negated\_conjecture})$   
 $\neg j < q$      $\text{cnf}(\text{clause}_{12}, \text{negated\_conjecture})$

#### SWV005-1.p E4

$\text{include}(\text{'Axioms/SWV001-0.ax'})$   
 $\neg n < k$      $\text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $\neg k < l$      $\text{cnf}(\text{clause}_2, \text{negated\_conjecture})$   
 $\neg k < i$      $\text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $l < n$      $\text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $1 < l$      $\text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $a(k) < a(\text{predecessor}(l))$      $\text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $(x < \text{successor}(n) \text{ and } a(x) < a(k)) \Rightarrow x < l$      $\text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $(1 < l \text{ and } a(x) < a(\text{predecessor}(l))) \Rightarrow (x < l \text{ or } n < x)$      $\text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $(1 < x \text{ and } x < l) \Rightarrow \neg a(x) < a(\text{predecessor}(x))$      $\text{cnf}(\text{clause}_9, \text{negated\_conjecture})$

#### SWV006-1.p E5

$\text{include}(\text{'Axioms/SWV001-0.ax'})$   
 $\neg n < m$      $\text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $i < m$      $\text{cnf}(\text{clause}_2, \text{negated\_conjecture})$   
 $i < n$      $\text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $\neg i < 1$      $\text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $a(i) < a(m)$      $\text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $(x < \text{successor}(n) \text{ and } a(x) < a(m)) \Rightarrow x < i$      $\text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $(1 < i \text{ and } a(x) < a(\text{predecessor}(i))) \Rightarrow (x < i \text{ or } n < x)$      $\text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $(1 < x \text{ and } x < i) \Rightarrow \neg a(x) < a(\text{predecessor}(x))$      $\text{cnf}(\text{clause}_8, \text{negated\_conjecture})$

#### SWV007-1.p E6

$\text{include}(\text{'Axioms/SWV001-0.ax'})$   
 $\neg n < k$      $\text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $\neg k < i$      $\text{cnf}(\text{clause}_2, \text{negated\_conjecture})$   
 $i < n$      $\text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $\neg n < m$      $\text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $i < m$      $\text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $\neg i < 1$      $\text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $k \neq m$      $\text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $a(m) < a(k)$      $\text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $(1 < x \text{ and } x < i) \Rightarrow \neg a(x) < a(\text{predecessor}(x))$      $\text{cnf}(\text{clause}_9, \text{negated\_conjecture})$   
 $(1 < x \text{ and } a(x) < a(\text{predecessor}(i))) \Rightarrow (x < i \text{ or } n < x)$      $\text{cnf}(\text{clause}_{10}, \text{negated\_conjecture})$   
 $(x < \text{successor}(n) \text{ and } a(x) < a(k)) \Rightarrow x < i$      $\text{cnf}(\text{clause}_{11}, \text{negated\_conjecture})$

#### SWV008-1.p E7

$\text{include}(\text{'Axioms/SWV001-0.ax'})$   
 $\neg n < l$      $\text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $1 < l$      $\text{cnf}(\text{clause}_2, \text{negated\_conjecture})$   
 $a(l) < a(\text{predecessor}(l))$      $\text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $(1 < n \text{ and } a(x) < a(\text{predecessor}(n))) \Rightarrow (x < n \text{ or } n < x)$      $\text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $(1 < x \text{ and } x < n) \Rightarrow \neg a(x) < a(\text{predecessor}(x))$      $\text{cnf}(\text{clause}_5, \text{negated\_conjecture})$

#### SWV009-1.p A condition from Hoare's FIND program

$x \leq y$  or less( $y, x$ )      cnf( $\text{clause}_1$ , negated\_conjecture)  
 less( $j, i$ )      cnf( $\text{clause}_2$ , negated\_conjecture)  
 $m \leq p$       cnf( $\text{clause}_3$ , negated\_conjecture)  
 $p \leq q$       cnf( $\text{clause}_4$ , negated\_conjecture)  
 $q \leq n$       cnf( $\text{clause}_5$ , negated\_conjecture)  
 $(m \leq x$  and less( $x, i$ ) and less( $j, y$ ) and  $y \leq n$ )  $\Rightarrow a(x) \leq a(y)$       cnf( $\text{clause}_6$ , negated\_conjecture)  
 $(m \leq x$  and  $x \leq y$  and  $y \leq j$ )  $\Rightarrow a(x) \leq a(y)$       cnf( $\text{clause}_7$ , negated\_conjecture)  
 $(i \leq x$  and  $x \leq y$  and  $y \leq n$ )  $\Rightarrow a(x) \leq a(y)$       cnf( $\text{clause}_8$ , negated\_conjecture)  
 $\neg a(p) \leq a(q)$       cnf( $\text{clause}_9$ , negated\_conjecture)

**SWV010+1.p** Fact 1 of the Neumann-Stubblebine analysis

a\_holds(key(at, t))      fof(a\_holds\_key\_at\_for\_t, axiom)  
 party\_of\_protocol(a)      fof(a\_is\_party\_of\_protocol, axiom)  
 message(sent(a, b, pair(a, an\_a\_nonce)))      fof(a\_sent\_message\_i\_to\_b, axiom)  
 a\_stored(pair(b, an\_a\_nonce))      fof(a\_stored\_message\_i, axiom)  
 $\forall u, v, w, x, y, z$ : ((message(sent(t, a, triple(encrypt(quadruple(y, z, w, v), at), x, u))) and a\_stored(pair(y, z)))  $\Rightarrow$  (message(sent(u, b, pair(b, generate\_b\_nonce(v), encrypt(triple(u, w, x, y), bt), encrypt(generate\_b\_nonce(y), v)))) and b\_holds(key(bt, t))      fof(b\_hold\_key\_bt\_for\_t, axiom)  
 party\_of\_protocol(b)      fof(b\_is\_party\_of\_protocol, axiom)  
 fresh\_to\_b(an\_a\_nonce)      fof(nonce\_a\_is\_fresh\_to\_b, axiom)  
 $\forall u, v$ : ((message(sent(u, b, pair(u, v))) and fresh\_to\_b(v))  $\Rightarrow$  (message(sent(b, t, triple(b, generate\_b\_nonce(v), encrypt(triple(u, w, x, y), bt), encrypt(generate\_b\_nonce(y), v)))) and v\_holds(key(v, x))      fof(b\_accepts\_secure\_session\_key, axiom)  
 t\_holds(key(at, a))      fof(t\_holds\_key\_at\_for\_a, axiom)  
 t\_holds(key(bt, b))      fof(t\_holds\_key\_bt\_for\_b, axiom)  
 party\_of\_protocol(t)      fof(t\_is\_party\_of\_protocol, axiom)  
 $\forall u, v, w, x, y, z, x_1$ : ((message(sent(u, t, triple(u, v, encrypt(triple(w, x, y), z)))) and t\_holds(key(z, u)) and t\_holds(key(x<sub>1</sub>, w))) and message(sent(t, w, triple(encrypt(quadruple(u, x, generate\_key(x), y), x<sub>1</sub>), encrypt(triple(w, generate\_key(x), y), z), v))))      fof(t\_holds\_key\_bt\_for\_b, axiom)

**SWV010-1.p** Fact 1 of the Neumann-Stubblebine analysis

message(sent(a, b, pair(a, an\_a\_nonce)))      cnf(a\_sent\_message\_i\_to\_b<sub>3</sub>, axiom)  
 a\_stored(pair(b, an\_a\_nonce))      cnf(a\_stored\_message\_i<sub>4</sub>, axiom)  
 (a\_stored(pair(a, b)) and message(sent(t, a, triple(encrypt(quadruple(a, b, c, d), at), e, f))))  $\Rightarrow$  message(sent(a, a, pair(e, encrypt(generate\_key(an\_a\_nonce), a))))  
 fresh\_to\_b(an\_a\_nonce)      cnf(nonce\_a\_is\_fresh\_to\_b<sub>9</sub>, axiom)  
 (fresh\_to\_b(b) and message(sent(a, b, pair(a, b))))  $\Rightarrow$  message(sent(b, t, triple(b, generate\_b\_nonce(b), encrypt(triple(a, b, generate\_key(an\_a\_nonce), a), bt), encrypt(generate\_b\_nonce(y), v))))  
 t\_holds(key(at, a))      cnf(t\_holds\_key\_at\_for\_a<sub>13</sub>, axiom)  
 t\_holds(key(bt, b))      cnf(t\_holds\_key\_bt\_for\_b<sub>14</sub>, axiom)  
 (message(sent(a, t, triple(a, b, encrypt(triple(c, d, e), f)))) and t\_holds(key(g, c)) and t\_holds(key(f, a)))  $\Rightarrow$  message(sent(t, c, pair(c, generate\_key(an\_a\_nonce), a)))

**SWV011+1.p** Fact 2 of the Neumann-Stubblebine analysis

a\_holds(key(at, t))      fof(a\_holds\_key\_at\_for\_t, axiom)  
 party\_of\_protocol(a)      fof(a\_is\_party\_of\_protocol, axiom)  
 message(sent(a, b, pair(a, an\_a\_nonce)))      fof(a\_sent\_message\_i\_to\_b, axiom)  
 a\_stored(pair(b, an\_a\_nonce))      fof(a\_stored\_message\_i, axiom)  
 b\_holds(key(bt, t))      fof(b\_hold\_key\_bt\_for\_t, axiom)  
 party\_of\_protocol(b)      fof(b\_is\_party\_of\_protocol, axiom)  
 fresh\_to\_b(an\_a\_nonce)      fof(nonce\_a\_is\_fresh\_to\_b, axiom)  
 t\_holds(key(at, a))      fof(t\_holds\_key\_at\_for\_a, axiom)  
 t\_holds(key(bt, b))      fof(t\_holds\_key\_bt\_for\_b, axiom)  
 party\_of\_protocol(t)      fof(t\_is\_party\_of\_protocol, axiom)  
 b\_holds(key(generate\_key(an\_a\_nonce), a))      fof(ax<sub>1</sub>, axiom)  
 message(sent(a, b, pair(encrypt(triple(a, generate\_key(an\_a\_nonce), generate\_expiration\_time(an\_a\_nonce)), bt), encrypt(generate\_key(an\_a\_nonce), a))))  
 a\_holds(key(generate\_key(an\_a\_nonce), b))      fof(ax<sub>3</sub>, axiom)  
 message(sent(t, a, triple(encrypt(quadruple(b, an\_a\_nonce, generate\_key(an\_a\_nonce), generate\_expiration\_time(an\_a\_nonce)), a, generate\_key(an\_a\_nonce), generate\_expiration\_time(an\_a\_nonce)))) and message(sent(b, t, triple(b, generate\_b\_nonce(an\_a\_nonce), encrypt(triple(a, an\_a\_nonce, generate\_expiration\_time(an\_a\_nonce)), a, generate\_key(an\_a\_nonce), generate\_expiration\_time(an\_a\_nonce)))) and b\_stored(pair(a, an\_a\_nonce))      fof(ax<sub>6</sub>, axiom)  
 $\exists u$ : (a\_holds(key(u, b)) and b\_holds(key(u, a)))      fof(co<sub>1</sub>, conjecture)

**SWV011-1.p** Fact 2 of the Neumann-Stubblebine analysis

b\_holds(key(generate\_key(an\_a\_nonce), a))      cnf(ax<sub>11</sub>, axiom)  
 a\_holds(key(generate\_key(an\_a\_nonce), b))      cnf(ax<sub>13</sub>, axiom)  
 a\_holds(key(a, b))  $\Rightarrow \neg$  b\_holds(key(a, a))      cnf(co<sub>17</sub>, negated\_conjecture)

**SWV012-1.p** Fact 3 of the Neumann-Stubblebine analysis

$\text{party\_of\_protocol}(a) \quad \text{cnf}(\text{a\_is\_party\_of\_protocol}_2, \text{axiom})$   
 $\text{message}(\text{sent}(a, b, \text{pair}(a, \text{an\_a\_nonce}))) \quad \text{cnf}(\text{a\_sent\_message\_i\_to\_b}_3, \text{axiom})$   
 $\text{a\_stored}(\text{pair}(b, \text{an\_a\_nonce})) \quad \text{cnf}(\text{a\_stored\_message\_i}_4, \text{axiom})$   
 $(\text{a\_stored}(\text{pair}(a, b)) \text{ and } \text{message}(\text{sent}(t, a, \text{triple}(\text{encrypt}(\text{quadruple}(a, b, c, d), \text{at}), e, f)))) \Rightarrow \text{message}(\text{sent}(a, a, \text{pair}(e, \text{generate\_b\_nonce}(b))))$   
 $\text{party\_of\_protocol}(b) \quad \text{cnf}(\text{b\_is\_party\_of\_protocol}_8, \text{axiom})$   
 $\text{fresh\_to\_b}(\text{an\_a\_nonce}) \quad \text{cnf}(\text{nonce\_a\_is\_fresh\_to\_b}_9, \text{axiom})$   
 $(\text{fresh\_to\_b}(b) \text{ and } \text{message}(\text{sent}(a, b, \text{pair}(a, b)))) \Rightarrow \text{message}(\text{sent}(b, t, \text{triple}(b, \text{generate\_b\_nonce}(b), \text{encrypt}(\text{triple}(a, b, \text{generate\_b\_nonce}(b)), \text{at}), e, f))))$   
 $\text{t\_holds}(\text{key}(\text{at}, a)) \quad \text{cnf}(\text{t\_holds\_key\_at\_for\_a}_{13}, \text{axiom})$   
 $\text{t\_holds}(\text{key}(\text{bt}, b)) \quad \text{cnf}(\text{t\_holds\_key\_bt\_for\_b}_{14}, \text{axiom})$   
 $\text{party\_of\_protocol}(t) \quad \text{cnf}(\text{t\_is\_party\_of\_protocol}_{15}, \text{axiom})$   
 $(\text{message}(\text{sent}(a, t, \text{triple}(a, b, \text{encrypt}(\text{triple}(c, d, e), f)))) \text{ and } \text{t\_holds}(\text{key}(g, c)) \text{ and } \text{t\_holds}(\text{key}(f, a))) \Rightarrow \text{message}(\text{sent}(t, c, \text{pair}(a, b)))$   
 $\text{message}(\text{sent}(a, b, c)) \Rightarrow \text{intruder\_message}(c) \quad \text{cnf}(\text{intruder\_can\_record}_{17}, \text{axiom})$   
 $\text{intruder\_message}(\text{pair}(a, b)) \Rightarrow \text{intruder\_message}(a) \quad \text{cnf}(\text{intruder\_decomposes\_pairs}_{18}, \text{axiom})$   
 $\text{intruder\_message}(\text{pair}(a, b)) \Rightarrow \text{intruder\_message}(b) \quad \text{cnf}(\text{intruder\_decomposes\_pairs}_{19}, \text{axiom})$   
 $\text{intruder\_message}(\text{triple}(a, b, c)) \Rightarrow \text{intruder\_message}(a) \quad \text{cnf}(\text{intruder\_decomposes\_triples}_{20}, \text{axiom})$   
 $\text{intruder\_message}(\text{triple}(a, b, c)) \Rightarrow \text{intruder\_message}(b) \quad \text{cnf}(\text{intruder\_decomposes\_triples}_{21}, \text{axiom})$   
 $\text{intruder\_message}(\text{triple}(a, b, c)) \Rightarrow \text{intruder\_message}(c) \quad \text{cnf}(\text{intruder\_decomposes\_triples}_{22}, \text{axiom})$   
 $\text{intruder\_message}(\text{quadruple}(a, b, c, d)) \Rightarrow \text{intruder\_message}(a) \quad \text{cnf}(\text{intruder\_decomposes\_quadruples}_{23}, \text{axiom})$   
 $\text{intruder\_message}(\text{quadruple}(a, b, c, d)) \Rightarrow \text{intruder\_message}(b) \quad \text{cnf}(\text{intruder\_decomposes\_quadruples}_{24}, \text{axiom})$   
 $\text{intruder\_message}(\text{quadruple}(a, b, c, d)) \Rightarrow \text{intruder\_message}(c) \quad \text{cnf}(\text{intruder\_decomposes\_quadruples}_{25}, \text{axiom})$   
 $\text{intruder\_message}(\text{quadruple}(a, b, c, d)) \Rightarrow \text{intruder\_message}(d) \quad \text{cnf}(\text{intruder\_decomposes\_quadruples}_{26}, \text{axiom})$   
 $(\text{intruder\_message}(b) \text{ and } \text{intruder\_message}(a)) \Rightarrow \text{intruder\_message}(\text{pair}(a, b)) \quad \text{cnf}(\text{intruder\_composes\_pairs}_{27}, \text{axiom})$   
 $(\text{intruder\_message}(c) \text{ and } \text{intruder\_message}(b) \text{ and } \text{intruder\_message}(a)) \Rightarrow \text{intruder\_message}(\text{triple}(a, b, c)) \quad \text{cnf}(\text{intruder\_composes\_triples}_{28}, \text{axiom})$   
 $(\text{intruder\_message}(d) \text{ and } \text{intruder\_message}(c) \text{ and } \text{intruder\_message}(b) \text{ and } \text{intruder\_message}(a)) \Rightarrow \text{intruder\_message}(\text{quadruple}(a, b, c, d)) \quad \text{cnf}(\text{intruder\_composes\_quadruples}_{29}, \text{axiom})$   
 $(\text{intruder\_holds}(\text{key}(b, c)) \text{ and } \text{intruder\_message}(\text{encrypt}(a, b)) \text{ and } \text{party\_of\_protocol}(c)) \Rightarrow \text{intruder\_message}(b) \quad \text{cnf}(\text{intruder\_holds\_key\_and\_message}_{30}, \text{axiom})$   
 $(\text{intruder\_message}(a) \text{ and } \text{party\_of\_protocol}(c) \text{ and } \text{party\_of\_protocol}(b)) \Rightarrow \text{message}(\text{sent}(b, c, a)) \quad \text{cnf}(\text{intruder\_message\_and\_party}_{31}, \text{axiom})$   
 $(\text{intruder\_message}(a) \text{ and } \text{party\_of\_protocol}(b)) \Rightarrow \text{intruder\_holds}(\text{key}(a, b)) \quad \text{cnf}(\text{intruder\_holds\_key}_{32}, \text{axiom})$   
 $(\text{intruder\_holds}(\text{key}(b, c)) \text{ and } \text{intruder\_message}(a) \text{ and } \text{party\_of\_protocol}(c)) \Rightarrow \text{intruder\_message}(\text{encrypt}(a, b)) \quad \text{cnf}(\text{intruder\_holds\_key\_and\_message}_{33}, \text{axiom})$

**SWV019-1.p** Maximal array element

$x_1 < a \text{ or } b < x_1 \text{ or } \text{in\_array\_bounds}(\text{array}, x_1) \quad \text{cnf}(\text{in\_bounds}, \text{axiom})$   
 $\text{successor}(x) < \text{successor}(y) \Rightarrow x < y \quad \text{cnf}(\text{predecessor\_less}, \text{axiom})$   
 $(x < y \text{ and } y < z) \Rightarrow x < z \quad \text{cnf}(\text{transitivity\_of\_less}, \text{axiom})$   
 $x < \text{successor}(x) \quad \text{cnf}(\text{successor\_greater}, \text{axiom})$   
 $\text{in\_array\_bounds}(\text{array}, \text{index\_of\_maximal}) \Rightarrow \text{maximal\_value} = \text{array\_value\_at}(\text{array}, \text{index\_of\_maximal}) \quad \text{cnf}(\text{this\_is\_maximal}, \text{axiom})$   
 $\text{index\_of\_maximal} < \text{an\_index} \quad \text{cnf}(\text{maximal\_before\_somewhere}, \text{axiom})$   
 $\neg \text{an\_index} < a \quad \text{cnf}(\text{somewhere\_above\_lower\_bound}, \text{axiom})$   
 $\neg b < \text{an\_index} \quad \text{cnf}(\text{somewhere\_below\_upper\_bound}, \text{axiom})$   
 $\neg \text{index\_of\_maximal} < a \quad \text{cnf}(\text{maximal\_above\_lower\_bound}, \text{axiom})$   
 $(\text{in\_array\_bounds}(\text{array}, \text{an\_index}) \text{ and } \text{index\_of\_maximal} < \text{successor}(\text{an\_index}) \text{ and } \text{in\_array\_bounds}(\text{array}, \text{index\_of\_maximal})) \Rightarrow (\text{array\_value\_at}(\text{array}, \text{index\_of\_maximal}) < \text{array\_value\_at}(\text{array}, \text{successor}(\text{an\_index})) \text{ or } \text{array\_value\_at}(\text{array}, \text{index\_of\_maximal}) < \text{array\_value\_at}(\text{array}, \text{an\_index})) \Rightarrow (\text{successor}(\text{an\_index}) < a \text{ or } \text{successor}(b) < \text{successor}(\text{an\_index}) \text{ or } \text{index\_of\_maximal} < \text{an\_index}) \quad \text{cnf}(\text{prove\_this}, \text{negated\_conjecture})$

**SWV020-1.p** Program verification axioms

`include('Axioms/SWV001-0.ax')`

**SWV021-1.p** Show that the add function is commutative.

A proof obligation formulated as a satisfiability problem. Given the definition of "add" on successor-naturals, show that no two terms t1 and t2 can be found such that  $\text{add}(t1, t2) \neq \text{add}(t2, t1)$ . In other words, show that adding the negation of that as a clause is still consistent.

$n_0 \neq s(x) \quad \text{cnf}(\text{zero\_is\_not\_s}, \text{axiom})$   
 $s(x) = s(y) \Rightarrow x = y \quad \text{cnf}(\text{successor\_is\_injective}, \text{axiom})$   
 $n_0 + y = y \quad \text{cnf}(\text{definition\_add}_0, \text{axiom})$   
 $s(x) + y = s(x + y) \quad \text{cnf}(\text{definition\_add}_s, \text{axiom})$   
 $x + y = y + x \quad \text{cnf}(\text{consistency\_of\_add\_commutative}, \text{negated\_conjecture})$

**SWV022+1.p** Unsimplified proof obligation gauss\_init\_0001

Proof obligation emerging from the init-safety verification for the gauss program. init-safety ensures that each variable or individual array element has been assigned a defined value before it is used.

`include('Axioms/SWV003+0.ax')`

```

init = init      fof(gauss_init0001, conjecture)
gt(n5, n4)      fof(gt.54, axiom)
gt(n4, tptp_minus1)  fof(gt.4_tptp_minus1, axiom)
gt(n5, tptp_minus1)  fof(gt.5_tptp_minus1, axiom)
gt(n0, tptp_minus1)  fof(gt.0_tptp_minus1, axiom)
gt(n1, tptp_minus1)  fof(gt.1_tptp_minus1, axiom)
gt(n2, tptp_minus1)  fof(gt.2_tptp_minus1, axiom)
gt(n3, tptp_minus1)  fof(gt.3_tptp_minus1, axiom)
gt(n4, n0)      fof(gt.40, axiom)
gt(n5, n0)      fof(gt.50, axiom)
gt(n1, n0)      fof(gt.10, axiom)
gt(n2, n0)      fof(gt.20, axiom)
gt(n3, n0)      fof(gt.30, axiom)
gt(n4, n1)      fof(gt.41, axiom)
gt(n5, n1)      fof(gt.51, axiom)
gt(n2, n1)      fof(gt.21, axiom)
gt(n3, n1)      fof(gt.31, axiom)
gt(n4, n2)      fof(gt.42, axiom)
gt(n5, n2)      fof(gt.52, axiom)
gt(n3, n2)      fof(gt.32, axiom)
gt(n4, n3)      fof(gt.43, axiom)
gt(n5, n3)      fof(gt.53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

### SWV023+1.p Unsimplified proof obligation gauss\_init\_0005

Proof obligation emerging from the init-safety verification for the gauss program. init-safety ensures that each variable or individual array element has been assigned a defined value before it is used.

```
include('Axioms/SWV003+0.ax')
```

```
(i0_init = init and sigma_init = init and ∀a: ((n0 ≤ a and a ≤ n2) ⇒ ∀b: ((n0 ≤ b and b ≤ n3) ⇒ a_select3(simplex7_init, b,
init)) and ∀c: ((n0 ≤ c and c ≤ n3) ⇒ a_select2(s_values7_init, c) = init)) ⇒ true    fof(gauss_init0005, conjecture)
```

```

gt(n5, n4)      fof(gt.54, axiom)
gt(n4, tptp_minus1)  fof(gt.4_tptp_minus1, axiom)
gt(n5, tptp_minus1)  fof(gt.5_tptp_minus1, axiom)
gt(n0, tptp_minus1)  fof(gt.0_tptp_minus1, axiom)
gt(n1, tptp_minus1)  fof(gt.1_tptp_minus1, axiom)
gt(n2, tptp_minus1)  fof(gt.2_tptp_minus1, axiom)
gt(n3, tptp_minus1)  fof(gt.3_tptp_minus1, axiom)
gt(n4, n0)      fof(gt.40, axiom)
gt(n5, n0)      fof(gt.50, axiom)
gt(n1, n0)      fof(gt.10, axiom)
gt(n2, n0)      fof(gt.20, axiom)
gt(n3, n0)      fof(gt.30, axiom)
gt(n4, n1)      fof(gt.41, axiom)
gt(n5, n1)      fof(gt.51, axiom)
gt(n2, n1)      fof(gt.21, axiom)
gt(n3, n1)      fof(gt.31, axiom)
gt(n4, n2)      fof(gt.42, axiom)
gt(n5, n2)      fof(gt.52, axiom)
gt(n3, n2)      fof(gt.32, axiom)
gt(n4, n3)      fof(gt.43, axiom)

```



```

gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

### SWV040+1.p Unsimplified proof obligation gauss\_init\_0073

Proof obligation emerging from the init-safety verification for the gauss program. init-safety ensures that each variable or individual array element has been assigned a defined value before it is used.

```
include('Axioms/SWV003+0.ax')
```

```
(n0 ≤ pv1374 and pv1374 ≤ n3 and ∀a: ((n0 ≤ a and a ≤ n2) ⇒ ∀b: ((n0 ≤ b and b ≤ -pv1374) ⇒ a_select3(simplex7_init, b, init))) ⇒ (init = init and ∀c: ((n0 ≤ c and c ≤ n2) ⇒ ∀d: ((n0 ≤ d and d ≤ -(n1+pv1374)) ⇒ a_select3(tptp_update3(tptp_init))))    fof(gauss_init_0073, conjecture)
```

```

gt(n5, n4)    fof(gt_54, axiom)
gt(n4, tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt(n5, tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt(n0, tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt(n1, tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt(n2, tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt(n3, tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt(n4, n0)    fof(gt_40, axiom)
gt(n5, n0)    fof(gt_50, axiom)
gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)

```

```

∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

### SWV043+1.p Unsimplified proof obligation cl5\_nebula\_norm\_0001

Proof obligation emerging from the norm-safety verification for the cl5\_nebula program. norm-safety ensures that the contents of certain one-dimensional arrays add up to one.

```
include('Axioms/SWV003+0.ax')
```

```

true ⇒ true    fof(cl5_nebula_norm_0001, conjecture)
gt(n5, n4)    fof(gt_54, axiom)
gt(n4, tptp_minus1)    fof(gt_4_tptp_minus1, axiom)

```

```

gt( $n_5$ , tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt( $n_0$ , tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt( $n_1$ , tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt( $n_2$ , tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt( $n_3$ , tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt( $n_4$ ,  $n_0$ )           fof(gt_40, axiom)
gt( $n_5$ ,  $n_0$ )           fof(gt_50, axiom)
gt( $n_1$ ,  $n_0$ )           fof(gt_10, axiom)
gt( $n_2$ ,  $n_0$ )           fof(gt_20, axiom)
gt( $n_3$ ,  $n_0$ )           fof(gt_30, axiom)
gt( $n_4$ ,  $n_1$ )           fof(gt_41, axiom)
gt( $n_5$ ,  $n_1$ )           fof(gt_51, axiom)
gt( $n_2$ ,  $n_1$ )           fof(gt_21, axiom)
gt( $n_3$ ,  $n_1$ )           fof(gt_31, axiom)
gt( $n_4$ ,  $n_2$ )           fof(gt_42, axiom)
gt( $n_5$ ,  $n_2$ )           fof(gt_52, axiom)
gt( $n_3$ ,  $n_2$ )           fof(gt_32, axiom)
gt( $n_4$ ,  $n_3$ )           fof(gt_43, axiom)
gt( $n_5$ ,  $n_3$ )           fof(gt_53, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$     fof(finite_domain4, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$     fof(finite_domain5, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$     fof(finite_domain0, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$     fof(finite_domain1, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$     fof(finite_domain2, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$     fof(finite_domain3, axiom)
succ(succ(succ(succ( $n_0$ )))) =  $n_4$     fof(successor4, axiom)
succ(succ(succ(succ(succ( $n_0$ )))))) =  $n_5$     fof(successor5, axiom)
succ( $n_0$ ) =  $n_1$     fof(successor1, axiom)
succ(succ( $n_0$ )) =  $n_2$     fof(successor2, axiom)
succ(succ(succ( $n_0$ ))) =  $n_3$     fof(successor3, axiom)

```

### SWV045+1.p Unsimplified proof obligation cl5\_nebula\_norm\_0007

Proof obligation emerging from the norm-safety verification for the cl5\_nebula program. norm-safety ensures that the contents of certain one-dimensional arrays add up to one.

```
include('Axioms/SWV003+0.ax')
```

```

(pv76 =  $n_0 + -n_{135300}$  = a.select3( $q$ , pv77, pv25) and  $n_0 \leq pv_{25}$  and  $pv_{25} \leq -n_5$ )  $\Rightarrow$  true    fof(cl5_nebula_norm0007, conjecture)
gt( $n_5$ ,  $n_4$ )           fof(gt_54, axiom)
gt( $n_{135300}$ ,  $n_4$ )       fof(gt_1353004, axiom)
gt( $n_{135300}$ ,  $n_5$ )       fof(gt_1353005, axiom)
gt( $n_4$ , tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt( $n_5$ , tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt( $n_{135300}$ , tptp_minus1)    fof(gt_135300_tptp_minus1, axiom)
gt( $n_0$ , tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt( $n_1$ , tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt( $n_2$ , tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt( $n_3$ , tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt( $n_4$ ,  $n_0$ )           fof(gt_40, axiom)
gt( $n_5$ ,  $n_0$ )           fof(gt_50, axiom)
gt( $n_{135300}$ ,  $n_0$ )       fof(gt_1353000, axiom)
gt( $n_1$ ,  $n_0$ )           fof(gt_10, axiom)
gt( $n_2$ ,  $n_0$ )           fof(gt_20, axiom)
gt( $n_3$ ,  $n_0$ )           fof(gt_30, axiom)
gt( $n_4$ ,  $n_1$ )           fof(gt_41, axiom)
gt( $n_5$ ,  $n_1$ )           fof(gt_51, axiom)
gt( $n_{135300}$ ,  $n_1$ )       fof(gt_1353001, axiom)
gt( $n_2$ ,  $n_1$ )           fof(gt_21, axiom)
gt( $n_3$ ,  $n_1$ )           fof(gt_31, axiom)
gt( $n_4$ ,  $n_2$ )           fof(gt_42, axiom)
gt( $n_5$ ,  $n_2$ )           fof(gt_52, axiom)
gt( $n_{135300}$ ,  $n_2$ )       fof(gt_1353002, axiom)

```

```

gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
gt(n135300, n3)  fof(gt_1353003, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

### SWV047+1.p Unsimplified proof obligation cl5\_nebula\_norm\_0013

Proof obligation emerging from the norm-safety verification for the cl5\_nebula program. norm-safety ensures that the contents of certain one-dimensional arrays add up to one.

```
include('Axioms/SWV003+0.ax')
```

```
(pv78 = n0 + -n135300 = a_select3(q, pv79, pv35) and pv82 = n0 + -n135300 = times(-a_select2(x, pv83), times(-a_select2(x, pv83),
pv35 and pv35 ≤ -n5) ⇒ true    fof(cl5_nebula_norm0013, conjecture)
```

```

gt(n5, n4)    fof(gt_54, axiom)
gt(n135300, n4)  fof(gt_1353004, axiom)
gt(n135300, n5)  fof(gt_1353005, axiom)
gt(n4, tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt(n5, tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt(n135300, tptp_minus1)    fof(gt_135300_tptp_minus1, axiom)
gt(n0, tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt(n1, tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt(n2, tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt(n3, tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt(n4, n0)    fof(gt_40, axiom)
gt(n5, n0)    fof(gt_50, axiom)
gt(n135300, n0)  fof(gt_1353000, axiom)
gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n135300, n1)  fof(gt_1353001, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n135300, n2)  fof(gt_1353002, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
gt(n135300, n3)  fof(gt_1353003, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)

```

$\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3$      $\text{fof}(\text{successor}_3, \text{axiom})$

**SWV052+1.p** Unsimplified proof obligation cl5\_nebula\_norm\_0028

Proof obligation emerging from the norm-safety verification for the cl5\_nebula program. norm-safety ensures that the contents of certain one-dimensional arrays add up to one.

`include('Axioms/SWV003+0.ax')`

$(\text{pv}_{86} = n_0 + -\text{pv}_{73} = \text{divide}(\text{abs}(-\text{a\_select}_2(\text{mu}, \text{pv}_{87})), \text{abs}(\text{a\_select}_2(\text{mu}, \text{pv}_{87})) + \text{abs}(\text{a\_select}_2(\text{muold}, \text{pv}_{87}))))$  and  $n_0 \leq \text{pv}_{73}$  and  $\text{pv}_{73} \leq -n_5 \Rightarrow \text{pv}_{86} + \text{divide}(\text{abs}(-\text{a\_select}_2(\text{mu}, \text{pv}_{73})), \text{abs}(\text{a\_select}_2(\text{mu}, \text{pv}_{73})) + \text{abs}(\text{a\_select}_2(\text{muold}, \text{pv}_{73}))) = n_0 + -(n_1 + \text{pv}_{73}) = \text{divide}(\text{abs}(-\text{a\_select}_2(\text{mu}, \text{pv}_{87})), \text{abs}(\text{a\_select}_2(\text{mu}, \text{pv}_{87})) + \text{abs}(\text{a\_select}_2(\text{muold}, \text{pv}_{87})))$      $\text{fof}(\text{cl5\_nebula\_}$

$\text{gt}(n_5, n_4)$      $\text{fof}(\text{gt}_5_4, \text{axiom})$   
 $\text{gt}(n_4, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_4\_4\_tptp\_minus_1, \text{axiom})$   
 $\text{gt}(n_5, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_5\_4\_tptp\_minus_1, \text{axiom})$   
 $\text{gt}(n_0, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_0\_4\_tptp\_minus_1, \text{axiom})$   
 $\text{gt}(n_1, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_1\_4\_tptp\_minus_1, \text{axiom})$   
 $\text{gt}(n_2, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_2\_4\_tptp\_minus_1, \text{axiom})$   
 $\text{gt}(n_3, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_3\_4\_tptp\_minus_1, \text{axiom})$   
 $\text{gt}(n_4, n_0)$      $\text{fof}(\text{gt}_4_0, \text{axiom})$   
 $\text{gt}(n_5, n_0)$      $\text{fof}(\text{gt}_5_0, \text{axiom})$   
 $\text{gt}(n_1, n_0)$      $\text{fof}(\text{gt}_1_0, \text{axiom})$   
 $\text{gt}(n_2, n_0)$      $\text{fof}(\text{gt}_2_0, \text{axiom})$   
 $\text{gt}(n_3, n_0)$      $\text{fof}(\text{gt}_3_0, \text{axiom})$   
 $\text{gt}(n_4, n_1)$      $\text{fof}(\text{gt}_4_1, \text{axiom})$   
 $\text{gt}(n_5, n_1)$      $\text{fof}(\text{gt}_5_1, \text{axiom})$   
 $\text{gt}(n_2, n_1)$      $\text{fof}(\text{gt}_2_1, \text{axiom})$   
 $\text{gt}(n_3, n_1)$      $\text{fof}(\text{gt}_3_1, \text{axiom})$   
 $\text{gt}(n_4, n_2)$      $\text{fof}(\text{gt}_4_2, \text{axiom})$   
 $\text{gt}(n_5, n_2)$      $\text{fof}(\text{gt}_5_2, \text{axiom})$   
 $\text{gt}(n_3, n_2)$      $\text{fof}(\text{gt}_3_2, \text{axiom})$   
 $\text{gt}(n_4, n_3)$      $\text{fof}(\text{gt}_4_3, \text{axiom})$   
 $\text{gt}(n_5, n_3)$      $\text{fof}(\text{gt}_5_3, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$      $\text{fof}(\text{finite\_domain}_4, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$      $\text{fof}(\text{finite\_domain}_5, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$      $\text{fof}(\text{finite\_domain}_0, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$      $\text{fof}(\text{finite\_domain}_1, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$      $\text{fof}(\text{finite\_domain}_2, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$      $\text{fof}(\text{finite\_domain}_3, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))) = n_4$      $\text{fof}(\text{successor}_4, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))))) = n_5$      $\text{fof}(\text{successor}_5, \text{axiom})$

$\text{succ}(n_0) = n_1$      $\text{fof}(\text{successor}_1, \text{axiom})$

$\text{succ}(\text{succ}(n_0)) = n_2$      $\text{fof}(\text{successor}_2, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3$      $\text{fof}(\text{successor}_3, \text{axiom})$

**SWV054+1.p** Unsimplified proof obligation cl5\_nebula\_norm\_0034

Proof obligation emerging from the norm-safety verification for the cl5\_nebula program. norm-safety ensures that the contents of certain one-dimensional arrays add up to one.

`include('Axioms/SWV003+0.ax')`

$(n_0 \leq \text{pv}_{10} \text{ and } \text{pv}_{10} \leq -n_{135300}) \Rightarrow \text{true}$      $\text{fof}(\text{cl5\_nebula\_norm}_{0034}, \text{conjecture})$

$\text{gt}(n_5, n_4)$      $\text{fof}(\text{gt}_5_4, \text{axiom})$   
 $\text{gt}(n_{135300}, n_4)$      $\text{fof}(\text{gt}_{135300}_4, \text{axiom})$   
 $\text{gt}(n_{135300}, n_5)$      $\text{fof}(\text{gt}_{135300}_5, \text{axiom})$   
 $\text{gt}(n_4, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_4\_4\_tptp\_minus_1, \text{axiom})$   
 $\text{gt}(n_5, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_5\_4\_tptp\_minus_1, \text{axiom})$   
 $\text{gt}(n_{135300}, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{135300}_4\_tptp\_minus_1, \text{axiom})$   
 $\text{gt}(n_0, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_0\_4\_tptp\_minus_1, \text{axiom})$   
 $\text{gt}(n_1, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_1\_4\_tptp\_minus_1, \text{axiom})$   
 $\text{gt}(n_2, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_2\_4\_tptp\_minus_1, \text{axiom})$   
 $\text{gt}(n_3, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_3\_4\_tptp\_minus_1, \text{axiom})$   
 $\text{gt}(n_4, n_0)$      $\text{fof}(\text{gt}_4_0, \text{axiom})$   
 $\text{gt}(n_5, n_0)$      $\text{fof}(\text{gt}_5_0, \text{axiom})$   
 $\text{gt}(n_{135300}, n_0)$      $\text{fof}(\text{gt}_{135300}_0, \text{axiom})$

```

gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n135300, n1)  fof(gt_135300_1, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n135300, n2)  fof(gt_135300_2, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
gt(n135300, n3)  fof(gt_135300_3, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

### SWV056+1.p Unsimplified proof obligation cl5\_nebula\_norm\_0040

Proof obligation emerging from the norm-safety verification for the cl5\_nebula program. norm-safety ensures that the contents of certain one-dimensional arrays add up to one.

```
include('Axioms/SWV003+0.ax')
```

```

(n0 ≤ pv25 and pv25 ≤ -n5) ⇒ (n0 = n0 + -n0 = a_select3(q, pv77, pv25) and n0 ≤ pv25 and pv25 ≤ -n5)    fof(cl5_nebula_norm_0040)
gt(n5, n4)    fof(gt_54, axiom)
gt(n4, tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt(n5, tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt(n0, tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt(n1, tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt(n2, tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt(n3, tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt(n4, n0)    fof(gt_40, axiom)
gt(n5, n0)    fof(gt_50, axiom)
gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)

```

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))))) = n_5$      $\text{fof}(\text{successor}_5, \text{axiom})$   
 $\text{succ}(n_0) = n_1$      $\text{fof}(\text{successor}_1, \text{axiom})$   
 $\text{succ}(\text{succ}(n_0)) = n_2$      $\text{fof}(\text{successor}_2, \text{axiom})$   
 $\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3$      $\text{fof}(\text{successor}_3, \text{axiom})$

**SWV057+1.p** Unsimplified proof obligation cl5\_nebula\_norm\_0043

Proof obligation emerging from the norm-safety verification for the cl5\_nebula program. norm-safety ensures that the contents of certain one-dimensional arrays add up to one.

include('Axioms/SWV003+0.ax')

$(n_0 \leq \text{pv}_{62} \text{ and } \text{pv}_{62} \leq -n_5) \Rightarrow \text{true}$      $\text{fof}(\text{cl5\_nebula\_norm}_{0043}, \text{conjecture})$

$\text{gt}(n_5, n_4)$      $\text{fof}(\text{gt}_{.5_4}, \text{axiom})$

$\text{gt}(n_4, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.4\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_5, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.5\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_0, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.0\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_1, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.1\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_2, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.2\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_3, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.3\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_4, n_0)$      $\text{fof}(\text{gt}_{.4_0}, \text{axiom})$

$\text{gt}(n_5, n_0)$      $\text{fof}(\text{gt}_{.5_0}, \text{axiom})$

$\text{gt}(n_1, n_0)$      $\text{fof}(\text{gt}_{.1_0}, \text{axiom})$

$\text{gt}(n_2, n_0)$      $\text{fof}(\text{gt}_{.2_0}, \text{axiom})$

$\text{gt}(n_3, n_0)$      $\text{fof}(\text{gt}_{.3_0}, \text{axiom})$

$\text{gt}(n_4, n_1)$      $\text{fof}(\text{gt}_{.4_1}, \text{axiom})$

$\text{gt}(n_5, n_1)$      $\text{fof}(\text{gt}_{.5_1}, \text{axiom})$

$\text{gt}(n_2, n_1)$      $\text{fof}(\text{gt}_{.2_1}, \text{axiom})$

$\text{gt}(n_3, n_1)$      $\text{fof}(\text{gt}_{.3_1}, \text{axiom})$

$\text{gt}(n_4, n_2)$      $\text{fof}(\text{gt}_{.4_2}, \text{axiom})$

$\text{gt}(n_5, n_2)$      $\text{fof}(\text{gt}_{.5_2}, \text{axiom})$

$\text{gt}(n_3, n_2)$      $\text{fof}(\text{gt}_{.3_2}, \text{axiom})$

$\text{gt}(n_4, n_3)$      $\text{fof}(\text{gt}_{.4_3}, \text{axiom})$

$\text{gt}(n_5, n_3)$      $\text{fof}(\text{gt}_{.5_3}, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$      $\text{fof}(\text{finite\_domain}_4, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$      $\text{fof}(\text{finite\_domain}_5, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$      $\text{fof}(\text{finite\_domain}_0, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$      $\text{fof}(\text{finite\_domain}_1, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$      $\text{fof}(\text{finite\_domain}_2, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$      $\text{fof}(\text{finite\_domain}_3, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))) = n_4$      $\text{fof}(\text{successor}_4, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))))) = n_5$      $\text{fof}(\text{successor}_5, \text{axiom})$

$\text{succ}(n_0) = n_1$      $\text{fof}(\text{successor}_1, \text{axiom})$

$\text{succ}(\text{succ}(n_0)) = n_2$      $\text{fof}(\text{successor}_2, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3$      $\text{fof}(\text{successor}_3, \text{axiom})$

**SWV058+1.p** Unsimplified proof obligation cl5\_nebula\_norm\_0046

Proof obligation emerging from the norm-safety verification for the cl5\_nebula program. norm-safety ensures that the contents of certain one-dimensional arrays add up to one.

include('Axioms/SWV003+0.ax')

$\neg \text{geq}(\text{pv}_{72}, \text{tptp\_float}_{.0_{001}}) \Rightarrow \text{true}$      $\text{fof}(\text{cl5\_nebula\_norm}_{0046}, \text{conjecture})$

$\text{gt}(n_5, n_4)$      $\text{fof}(\text{gt}_{.5_4}, \text{axiom})$

$\text{gt}(n_4, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.4\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_5, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.5\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_0, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.0\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_1, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.1\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_2, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.2\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_3, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.3\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_4, n_0)$      $\text{fof}(\text{gt}_{.4_0}, \text{axiom})$

$\text{gt}(n_5, n_0)$      $\text{fof}(\text{gt}_{.5_0}, \text{axiom})$

$\text{gt}(n_1, n_0)$      $\text{fof}(\text{gt}_{.1_0}, \text{axiom})$

$\text{gt}(n_2, n_0)$      $\text{fof}(\text{gt}_{.2_0}, \text{axiom})$

$\text{gt}(n_3, n_0)$      $\text{fof}(\text{gt}_{.3_0}, \text{axiom})$

```

gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

**SWV059+1.p** Unsimplified proof obligation cl5\_nebula\_norm\_0049

Proof obligation emerging from the norm-safety verification for the cl5\_nebula program. norm-safety ensures that the contents of certain one-dimensional arrays add up to one.

```
include('Axioms/SWV003+0.ax')
```

```

geq(pv72, tptp_float_0001) ⇒ ((¬gt(n1+loopcounter, n1) ⇒ true) and (gt(n1+loopcounter, n1) ⇒ true))    fof(cl5_nebula.
gt(n5, n4)    fof(gt_54, axiom)
gt(n4, tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt(n5, tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt(n0, tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt(n1, tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt(n2, tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt(n3, tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt(n4, n0)    fof(gt_40, axiom)
gt(n5, n0)    fof(gt_50, axiom)
gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

**SWV060+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0001

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

true  $\Rightarrow$  true    fof(cl5\_nebula\_array0001, conjecture)

gt( $n_5, n_4$ )    fof(gt\_5\_4, axiom)

gt( $n_4, \text{tptp\_minus}_1$ )    fof(gt\_4\_tptp\_minus\_1, axiom)

gt( $n_5, \text{tptp\_minus}_1$ )    fof(gt\_5\_tptp\_minus\_1, axiom)

gt( $n_0, \text{tptp\_minus}_1$ )    fof(gt\_0\_tptp\_minus\_1, axiom)

gt( $n_1, \text{tptp\_minus}_1$ )    fof(gt\_1\_tptp\_minus\_1, axiom)

gt( $n_2, \text{tptp\_minus}_1$ )    fof(gt\_2\_tptp\_minus\_1, axiom)

gt( $n_3, \text{tptp\_minus}_1$ )    fof(gt\_3\_tptp\_minus\_1, axiom)

gt( $n_4, n_0$ )    fof(gt\_4\_0, axiom)

gt( $n_5, n_0$ )    fof(gt\_5\_0, axiom)

gt( $n_1, n_0$ )    fof(gt\_1\_0, axiom)

gt( $n_2, n_0$ )    fof(gt\_2\_0, axiom)

gt( $n_3, n_0$ )    fof(gt\_3\_0, axiom)

gt( $n_4, n_1$ )    fof(gt\_4\_1, axiom)

gt( $n_5, n_1$ )    fof(gt\_5\_1, axiom)

gt( $n_2, n_1$ )    fof(gt\_2\_1, axiom)

gt( $n_3, n_1$ )    fof(gt\_3\_1, axiom)

gt( $n_4, n_2$ )    fof(gt\_4\_2, axiom)

gt( $n_5, n_2$ )    fof(gt\_5\_2, axiom)

gt( $n_3, n_2$ )    fof(gt\_3\_2, axiom)

gt( $n_4, n_3$ )    fof(gt\_4\_3, axiom)

gt( $n_5, n_3$ )    fof(gt\_5\_3, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$     fof(finite\_domain4, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$     fof(finite\_domain5, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$     fof(finite\_domain0, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$     fof(finite\_domain1, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$     fof(finite\_domain2, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$     fof(finite\_domain3, axiom)

succ(succ(succ(succ( $n_0$ )))) =  $n_4$     fof(successor4, axiom)

succ(succ(succ(succ(succ( $n_0$ )))))) =  $n_5$     fof(successor5, axiom)

succ( $n_0$ ) =  $n_1$     fof(successor1, axiom)

succ(succ( $n_0$ )) =  $n_2$     fof(successor2, axiom)

succ(succ(succ( $n_0$ ))) =  $n_3$     fof(successor3, axiom)

**SWV061+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0002

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

true  $\Rightarrow ((\neg \text{gt}(\text{loopcounter}, n_1) \Rightarrow \text{true}) \text{ and } (\text{gt}(\text{loopcounter}, n_1) \Rightarrow \text{true}))$     fof(cl5\_nebula\_array0002, conjecture)

gt( $n_5, n_4$ )    fof(gt\_5\_4, axiom)

gt( $n_4, \text{tptp\_minus}_1$ )    fof(gt\_4\_tptp\_minus\_1, axiom)

gt( $n_5, \text{tptp\_minus}_1$ )    fof(gt\_5\_tptp\_minus\_1, axiom)

gt( $n_0, \text{tptp\_minus}_1$ )    fof(gt\_0\_tptp\_minus\_1, axiom)

gt( $n_1, \text{tptp\_minus}_1$ )    fof(gt\_1\_tptp\_minus\_1, axiom)

gt( $n_2, \text{tptp\_minus}_1$ )    fof(gt\_2\_tptp\_minus\_1, axiom)

gt( $n_3, \text{tptp\_minus}_1$ )    fof(gt\_3\_tptp\_minus\_1, axiom)

gt( $n_4, n_0$ )    fof(gt\_4\_0, axiom)

gt( $n_5, n_0$ )    fof(gt\_5\_0, axiom)

gt( $n_1, n_0$ )    fof(gt\_1\_0, axiom)

gt( $n_2, n_0$ )    fof(gt\_2\_0, axiom)

gt( $n_3, n_0$ )    fof(gt\_3\_0, axiom)

gt( $n_4, n_1$ )    fof(gt\_4\_1, axiom)

gt( $n_5, n_1$ )    fof(gt\_5\_1, axiom)

gt( $n_2, n_1$ )    fof(gt\_2\_1, axiom)

gt( $n_3, n_1$ )    fof(gt\_3\_1, axiom)

gt( $n_4, n_2$ )    fof(gt\_4\_2, axiom)

gt( $n_5, n_2$ )    fof(gt\_5\_2, axiom)



$gt(n_3, n_2) \quad \text{fof(gt\_3}_2, \text{axiom)}$   
 $gt(n_4, n_3) \quad \text{fof(gt\_4}_3, \text{axiom)}$   
 $gt(n_5, n_3) \quad \text{fof(gt\_5}_3, \text{axiom)}$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4)) \quad \text{fof(finite\_domain}_4, \text{axiom)}$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5)) \quad \text{fof(finite\_domain}_5, \text{axiom)}$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0) \quad \text{fof(finite\_domain}_0, \text{axiom)}$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1)) \quad \text{fof(finite\_domain}_1, \text{axiom)}$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2)) \quad \text{fof(finite\_domain}_2, \text{axiom)}$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3)) \quad \text{fof(finite\_domain}_3, \text{axiom)}$   
 $\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))) = n_4 \quad \text{fof(successor}_4, \text{axiom)}$   
 $\text{succ}(\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))))) = n_5 \quad \text{fof(successor}_5, \text{axiom)}$   
 $\text{succ}(n_0) = n_1 \quad \text{fof(successor}_1, \text{axiom)}$   
 $\text{succ}(\text{succ}(n_0)) = n_2 \quad \text{fof(successor}_2, \text{axiom)}$   
 $\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3 \quad \text{fof(successor}_3, \text{axiom)}$

### SWV063+1.p Unsimplified proof obligation cl5\_nebula\_array\_0004

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq pv_{10} \text{ and } n_0 \leq pv_{43} \text{ and } pv_{10} \leq -n_{135300} \text{ and } pv_{43} \leq -n_5) \Rightarrow (n_0 \leq pv_{10} \text{ and } n_0 \leq pv_{43} \text{ and } pv_{10} \leq -n_{135300} \text{ and } pv_{43} \leq -n_5) \quad \text{fof(cl5\_nebula\_array}_{0004}, \text{conjecture})$

$gt(n_5, n_4) \quad \text{fof(gt\_5}_4, \text{axiom)}$   
 $gt(n_{135300}, n_4) \quad \text{fof(gt\_135300}_4, \text{axiom)}$   
 $gt(n_{135300}, n_5) \quad \text{fof(gt\_135300}_5, \text{axiom)}$   
 $gt(n_4, tptp\_minus_1) \quad \text{fof(gt\_4\_tptp\_minus}_1, \text{axiom)}$   
 $gt(n_5, tptp\_minus_1) \quad \text{fof(gt\_5\_tptp\_minus}_1, \text{axiom)}$   
 $gt(n_{135300}, tptp\_minus_1) \quad \text{fof(gt\_135300\_tptp\_minus}_1, \text{axiom)}$   
 $gt(n_0, tptp\_minus_1) \quad \text{fof(gt\_0\_tptp\_minus}_1, \text{axiom)}$   
 $gt(n_1, tptp\_minus_1) \quad \text{fof(gt\_1\_tptp\_minus}_1, \text{axiom)}$   
 $gt(n_2, tptp\_minus_1) \quad \text{fof(gt\_2\_tptp\_minus}_1, \text{axiom)}$   
 $gt(n_3, tptp\_minus_1) \quad \text{fof(gt\_3\_tptp\_minus}_1, \text{axiom)}$   
 $gt(n_4, n_0) \quad \text{fof(gt\_4}_0, \text{axiom)}$   
 $gt(n_5, n_0) \quad \text{fof(gt\_5}_0, \text{axiom)}$   
 $gt(n_{135300}, n_0) \quad \text{fof(gt\_135300}_0, \text{axiom)}$   
 $gt(n_1, n_0) \quad \text{fof(gt\_1}_0, \text{axiom)}$   
 $gt(n_2, n_0) \quad \text{fof(gt\_2}_0, \text{axiom)}$   
 $gt(n_3, n_0) \quad \text{fof(gt\_3}_0, \text{axiom)}$   
 $gt(n_4, n_1) \quad \text{fof(gt\_4}_1, \text{axiom)}$   
 $gt(n_5, n_1) \quad \text{fof(gt\_5}_1, \text{axiom)}$   
 $gt(n_{135300}, n_1) \quad \text{fof(gt\_135300}_1, \text{axiom)}$   
 $gt(n_2, n_1) \quad \text{fof(gt\_2}_1, \text{axiom)}$   
 $gt(n_3, n_1) \quad \text{fof(gt\_3}_1, \text{axiom)}$   
 $gt(n_4, n_2) \quad \text{fof(gt\_4}_2, \text{axiom)}$   
 $gt(n_5, n_2) \quad \text{fof(gt\_5}_2, \text{axiom)}$   
 $gt(n_{135300}, n_2) \quad \text{fof(gt\_135300}_2, \text{axiom)}$   
 $gt(n_3, n_2) \quad \text{fof(gt\_3}_2, \text{axiom)}$   
 $gt(n_4, n_3) \quad \text{fof(gt\_4}_3, \text{axiom)}$   
 $gt(n_5, n_3) \quad \text{fof(gt\_5}_3, \text{axiom)}$   
 $gt(n_{135300}, n_3) \quad \text{fof(gt\_135300}_3, \text{axiom)}$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4)) \quad \text{fof(finite\_domain}_4, \text{axiom)}$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5)) \quad \text{fof(finite\_domain}_5, \text{axiom)}$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0) \quad \text{fof(finite\_domain}_0, \text{axiom)}$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1)) \quad \text{fof(finite\_domain}_1, \text{axiom)}$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2)) \quad \text{fof(finite\_domain}_2, \text{axiom)}$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3)) \quad \text{fof(finite\_domain}_3, \text{axiom)}$   
 $\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))) = n_4 \quad \text{fof(successor}_4, \text{axiom)}$   
 $\text{succ}(\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))))) = n_5 \quad \text{fof(successor}_5, \text{axiom)}$   
 $\text{succ}(n_0) = n_1 \quad \text{fof(successor}_1, \text{axiom)}$   
 $\text{succ}(\text{succ}(n_0)) = n_2 \quad \text{fof(successor}_2, \text{axiom)}$   
 $\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3 \quad \text{fof(successor}_3, \text{axiom)}$

**SWV065+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0006

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq pv_{10} \text{ and } n_0 \leq pv_{53} \text{ and } pv_{10} \leq -n_{135300} \text{ and } pv_{53} \leq -n_5) \Rightarrow (n_0 \leq n_0 \text{ and } n_0 \leq pv_{10} \text{ and } n_0 \leq pv_{53} \text{ and } pv_{10} \leq -n_{135300} \text{ and } pv_{53} \leq -n_5)$  fof(cl5\_nebula\_array\_0006, conjecture)

gt( $n_5, n_4$ ) fof(gt\_5\_4, axiom)

gt( $n_{135300}, n_4$ ) fof(gt\_135300\_4, axiom)

gt( $n_{135300}, n_5$ ) fof(gt\_135300\_5, axiom)

gt( $n_4, tptp\_minus_1$ ) fof(gt\_4\_tptp\_minus\_1, axiom)

gt( $n_5, tptp\_minus_1$ ) fof(gt\_5\_tptp\_minus\_1, axiom)

gt( $n_{135300}, tptp\_minus_1$ ) fof(gt\_135300\_tptp\_minus\_1, axiom)

gt( $n_0, tptp\_minus_1$ ) fof(gt\_0\_tptp\_minus\_1, axiom)

gt( $n_1, tptp\_minus_1$ ) fof(gt\_1\_tptp\_minus\_1, axiom)

gt( $n_2, tptp\_minus_1$ ) fof(gt\_2\_tptp\_minus\_1, axiom)

gt( $n_3, tptp\_minus_1$ ) fof(gt\_3\_tptp\_minus\_1, axiom)

gt( $n_4, n_0$ ) fof(gt\_4\_0, axiom)

gt( $n_5, n_0$ ) fof(gt\_5\_0, axiom)

gt( $n_{135300}, n_0$ ) fof(gt\_135300\_0, axiom)

gt( $n_1, n_0$ ) fof(gt\_1\_0, axiom)

gt( $n_2, n_0$ ) fof(gt\_2\_0, axiom)

gt( $n_3, n_0$ ) fof(gt\_3\_0, axiom)

gt( $n_4, n_1$ ) fof(gt\_4\_1, axiom)

gt( $n_5, n_1$ ) fof(gt\_5\_1, axiom)

gt( $n_{135300}, n_1$ ) fof(gt\_135300\_1, axiom)

gt( $n_2, n_1$ ) fof(gt\_2\_1, axiom)

gt( $n_3, n_1$ ) fof(gt\_3\_1, axiom)

gt( $n_4, n_2$ ) fof(gt\_4\_2, axiom)

gt( $n_5, n_2$ ) fof(gt\_5\_2, axiom)

gt( $n_{135300}, n_2$ ) fof(gt\_135300\_2, axiom)

gt( $n_3, n_2$ ) fof(gt\_3\_2, axiom)

gt( $n_4, n_3$ ) fof(gt\_4\_3, axiom)

gt( $n_5, n_3$ ) fof(gt\_5\_3, axiom)

gt( $n_{135300}, n_3$ ) fof(gt\_135300\_3, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$  fof(finite\_domain\_4, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$  fof(finite\_domain\_5, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$  fof(finite\_domain\_0, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$  fof(finite\_domain\_1, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$  fof(finite\_domain\_2, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$  fof(finite\_domain\_3, axiom)

succ(succ(succ(succ( $n_0$ )))) =  $n_4$  fof(successor\_4, axiom)

succ(succ(succ(succ(succ( $n_0$ )))))) =  $n_5$  fof(successor\_5, axiom)

succ( $n_0$ ) =  $n_1$  fof(successor\_1, axiom)

succ(succ( $n_0$ )) =  $n_2$  fof(successor\_2, axiom)

succ(succ(succ( $n_0$ ))) =  $n_3$  fof(successor\_3, axiom)

**SWV066+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0007

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq pv_{10} \text{ and } n_0 \leq pv_{53} \text{ and } pv_{10} \leq -n_{135300} \text{ and } pv_{53} \leq -n_5) \Rightarrow (n_0 \leq pv_{10} \text{ and } n_0 \leq pv_{53} \text{ and } pv_{10} \leq -n_{135300} \text{ and } pv_{53} \leq -n_5)$  fof(cl5\_nebula\_array\_0007, conjecture)

gt( $n_5, n_4$ ) fof(gt\_5\_4, axiom)

gt( $n_{135300}, n_4$ ) fof(gt\_135300\_4, axiom)

gt( $n_{135300}, n_5$ ) fof(gt\_135300\_5, axiom)

gt( $n_4, tptp\_minus_1$ ) fof(gt\_4\_tptp\_minus\_1, axiom)

gt( $n_5, tptp\_minus_1$ ) fof(gt\_5\_tptp\_minus\_1, axiom)

gt( $n_{135300}, tptp\_minus_1$ ) fof(gt\_135300\_tptp\_minus\_1, axiom)

gt( $n_0, tptp\_minus_1$ ) fof(gt\_0\_tptp\_minus\_1, axiom)

gt( $n_1, tptp\_minus_1$ ) fof(gt\_1\_tptp\_minus\_1, axiom)

```

gt( $n_2$ , tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt( $n_3$ , tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt( $n_4$ ,  $n_0$ )           fof(gt_40, axiom)
gt( $n_5$ ,  $n_0$ )           fof(gt_50, axiom)
gt( $n_{135300}$ ,  $n_0$ )      fof(gt_1353000, axiom)
gt( $n_1$ ,  $n_0$ )           fof(gt_10, axiom)
gt( $n_2$ ,  $n_0$ )           fof(gt_20, axiom)
gt( $n_3$ ,  $n_0$ )           fof(gt_30, axiom)
gt( $n_4$ ,  $n_1$ )           fof(gt_41, axiom)
gt( $n_5$ ,  $n_1$ )           fof(gt_51, axiom)
gt( $n_{135300}$ ,  $n_1$ )      fof(gt_1353001, axiom)
gt( $n_2$ ,  $n_1$ )           fof(gt_21, axiom)
gt( $n_3$ ,  $n_1$ )           fof(gt_31, axiom)
gt( $n_4$ ,  $n_2$ )           fof(gt_42, axiom)
gt( $n_5$ ,  $n_2$ )           fof(gt_52, axiom)
gt( $n_{135300}$ ,  $n_2$ )      fof(gt_1353002, axiom)
gt( $n_3$ ,  $n_2$ )           fof(gt_32, axiom)
gt( $n_4$ ,  $n_3$ )           fof(gt_43, axiom)
gt( $n_5$ ,  $n_3$ )           fof(gt_53, axiom)
gt( $n_{135300}$ ,  $n_3$ )      fof(gt_1353003, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$     fof(finite_domain4, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$     fof(finite_domain5, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$     fof(finite_domain0, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$     fof(finite_domain1, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$     fof(finite_domain2, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$     fof(finite_domain3, axiom)
succ(succ(succ(succ( $n_0$ )))) =  $n_4$     fof(successor4, axiom)
succ(succ(succ(succ(succ( $n_0$ )))))) =  $n_5$     fof(successor5, axiom)
succ( $n_0$ ) =  $n_1$     fof(successor1, axiom)
succ(succ( $n_0$ )) =  $n_2$     fof(successor2, axiom)
succ(succ(succ( $n_0$ ))) =  $n_3$     fof(successor3, axiom)

```

**SWV068+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0009

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

```

include('Axioms/SWV003+0.ax')
( $n_0 \leq \text{pv}_{10}$  and  $\text{pv}_{10} \leq -n_{135300}$ )  $\Rightarrow$  true    fof(cl5_nebula_array0009, conjecture)
gt( $n_5$ ,  $n_4$ )           fof(gt_54, axiom)
gt( $n_{135300}$ ,  $n_4$ )      fof(gt_1353004, axiom)
gt( $n_{135300}$ ,  $n_5$ )      fof(gt_1353005, axiom)
gt( $n_4$ , tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt( $n_5$ , tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt( $n_{135300}$ , tptp_minus1)    fof(gt_135300_tptp_minus1, axiom)
gt( $n_0$ , tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt( $n_1$ , tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt( $n_2$ , tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt( $n_3$ , tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt( $n_4$ ,  $n_0$ )           fof(gt_40, axiom)
gt( $n_5$ ,  $n_0$ )           fof(gt_50, axiom)
gt( $n_{135300}$ ,  $n_0$ )      fof(gt_1353000, axiom)
gt( $n_1$ ,  $n_0$ )           fof(gt_10, axiom)
gt( $n_2$ ,  $n_0$ )           fof(gt_20, axiom)
gt( $n_3$ ,  $n_0$ )           fof(gt_30, axiom)
gt( $n_4$ ,  $n_1$ )           fof(gt_41, axiom)
gt( $n_5$ ,  $n_1$ )           fof(gt_51, axiom)
gt( $n_{135300}$ ,  $n_1$ )      fof(gt_1353001, axiom)
gt( $n_2$ ,  $n_1$ )           fof(gt_21, axiom)
gt( $n_3$ ,  $n_1$ )           fof(gt_31, axiom)
gt( $n_4$ ,  $n_2$ )           fof(gt_42, axiom)
gt( $n_5$ ,  $n_2$ )           fof(gt_52, axiom)

```

```

gt( $n_{135300}, n_2$ )    fof(gt_135300_2, axiom)
gt( $n_3, n_2$ )        fof(gt_3_2, axiom)
gt( $n_4, n_3$ )        fof(gt_4_3, axiom)
gt( $n_5, n_3$ )        fof(gt_5_3, axiom)
gt( $n_{135300}, n_3$ )    fof(gt_135300_3, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$     fof(finite_domain_4, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$     fof(finite_domain_5, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$     fof(finite_domain_0, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$     fof(finite_domain_1, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$     fof(finite_domain_2, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$     fof(finite_domain_3, axiom)
succ(succ(succ(succ( $n_0$ )))) =  $n_4$     fof(successor_4, axiom)
succ(succ(succ(succ(succ( $n_0$ )))))) =  $n_5$     fof(successor_5, axiom)
succ( $n_0$ ) =  $n_1$     fof(successor_1, axiom)
succ(succ( $n_0$ )) =  $n_2$     fof(successor_2, axiom)
succ(succ(succ( $n_0$ ))) =  $n_3$     fof(successor_3, axiom)

```

### SWV069+1.p Unsimplified proof obligation cl5\_nebula\_array\_0010

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

```
include('Axioms/SWV003+0.ax')
```

```

( $n_0 \leq \text{pv}_{10}$  and  $\text{pv}_{10} \leq -n_{135300}$ )  $\Rightarrow (n_0 \leq n_0$  and  $n_0 \leq \text{pv}_{10}$  and  $n_0 \leq -n_5$  and  $\text{pv}_{10} \leq -n_{135300})$     fof(cl5_nebula_array_0010)
gt( $n_5, n_4$ )    fof(gt_5_4, axiom)
gt( $n_{135300}, n_4$ )    fof(gt_135300_4, axiom)
gt( $n_{135300}, n_5$ )    fof(gt_135300_5, axiom)
gt( $n_4, \text{tptp\_minus}_1$ )    fof(gt_4_tptp_minus_1, axiom)
gt( $n_5, \text{tptp\_minus}_1$ )    fof(gt_5_tptp_minus_1, axiom)
gt( $n_{135300}, \text{tptp\_minus}_1$ )    fof(gt_135300_tptp_minus_1, axiom)
gt( $n_0, \text{tptp\_minus}_1$ )    fof(gt_0_tptp_minus_1, axiom)
gt( $n_1, \text{tptp\_minus}_1$ )    fof(gt_1_tptp_minus_1, axiom)
gt( $n_2, \text{tptp\_minus}_1$ )    fof(gt_2_tptp_minus_1, axiom)
gt( $n_3, \text{tptp\_minus}_1$ )    fof(gt_3_tptp_minus_1, axiom)
gt( $n_4, n_0$ )    fof(gt_4_0, axiom)
gt( $n_5, n_0$ )    fof(gt_5_0, axiom)
gt( $n_{135300}, n_0$ )    fof(gt_135300_0, axiom)
gt( $n_1, n_0$ )    fof(gt_1_0, axiom)
gt( $n_2, n_0$ )    fof(gt_2_0, axiom)
gt( $n_3, n_0$ )    fof(gt_3_0, axiom)
gt( $n_4, n_1$ )    fof(gt_4_1, axiom)
gt( $n_5, n_1$ )    fof(gt_5_1, axiom)
gt( $n_{135300}, n_1$ )    fof(gt_135300_1, axiom)
gt( $n_2, n_1$ )    fof(gt_2_1, axiom)
gt( $n_3, n_1$ )    fof(gt_3_1, axiom)
gt( $n_4, n_2$ )    fof(gt_4_2, axiom)
gt( $n_5, n_2$ )    fof(gt_5_2, axiom)
gt( $n_{135300}, n_2$ )    fof(gt_135300_2, axiom)
gt( $n_3, n_2$ )    fof(gt_3_2, axiom)
gt( $n_4, n_3$ )    fof(gt_4_3, axiom)
gt( $n_5, n_3$ )    fof(gt_5_3, axiom)
gt( $n_{135300}, n_3$ )    fof(gt_135300_3, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$     fof(finite_domain_4, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$     fof(finite_domain_5, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$     fof(finite_domain_0, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$     fof(finite_domain_1, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$     fof(finite_domain_2, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$     fof(finite_domain_3, axiom)
succ(succ(succ(succ( $n_0$ )))) =  $n_4$     fof(successor_4, axiom)
succ(succ(succ(succ(succ( $n_0$ )))))) =  $n_5$     fof(successor_5, axiom)
succ( $n_0$ ) =  $n_1$     fof(successor_1, axiom)
succ(succ( $n_0$ )) =  $n_2$     fof(successor_2, axiom)

```

$\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3$      $\text{fof}(\text{successor}_3, \text{axiom})$

**SWV070+1.p** Unsimplified proof obligation `cl5_nebula_array_0011`

Proof obligation emerging from the array-safety verification for the `cl5_nebula` program. `array-safety` ensures that each access to an array element is within the specified upper and lower bounds of the array.

`include('Axioms/SWV003+0.ax')`

$(n_0 \leq \text{pv}_{10} \text{ and } \text{pv}_{10} \leq -n_{135300}) \Rightarrow (n_0 \leq \text{pv}_{10} \text{ and } \text{pv}_{10} \leq -n_{135300})$      $\text{fof}(\text{cl5\_nebula\_array}_{0011}, \text{conjecture})$

$\text{gt}(n_5, n_4)$      $\text{fof}(\text{gt}_{.5}_4, \text{axiom})$

$\text{gt}(n_{135300}, n_4)$      $\text{fof}(\text{gt}_{.135300}_4, \text{axiom})$

$\text{gt}(n_{135300}, n_5)$      $\text{fof}(\text{gt}_{.135300}_5, \text{axiom})$

$\text{gt}(n_4, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.4\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_5, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.5\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_{135300}, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.135300\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_0, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.0\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_1, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.1\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_2, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.2\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_3, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.3\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_4, n_0)$      $\text{fof}(\text{gt}_{.4}_0, \text{axiom})$

$\text{gt}(n_5, n_0)$      $\text{fof}(\text{gt}_{.5}_0, \text{axiom})$

$\text{gt}(n_{135300}, n_0)$      $\text{fof}(\text{gt}_{.135300}_0, \text{axiom})$

$\text{gt}(n_1, n_0)$      $\text{fof}(\text{gt}_{.1}_0, \text{axiom})$

$\text{gt}(n_2, n_0)$      $\text{fof}(\text{gt}_{.2}_0, \text{axiom})$

$\text{gt}(n_3, n_0)$      $\text{fof}(\text{gt}_{.3}_0, \text{axiom})$

$\text{gt}(n_4, n_1)$      $\text{fof}(\text{gt}_{.4}_1, \text{axiom})$

$\text{gt}(n_5, n_1)$      $\text{fof}(\text{gt}_{.5}_1, \text{axiom})$

$\text{gt}(n_{135300}, n_1)$      $\text{fof}(\text{gt}_{.135300}_1, \text{axiom})$

$\text{gt}(n_2, n_1)$      $\text{fof}(\text{gt}_{.2}_1, \text{axiom})$

$\text{gt}(n_3, n_1)$      $\text{fof}(\text{gt}_{.3}_1, \text{axiom})$

$\text{gt}(n_4, n_2)$      $\text{fof}(\text{gt}_{.4}_2, \text{axiom})$

$\text{gt}(n_5, n_2)$      $\text{fof}(\text{gt}_{.5}_2, \text{axiom})$

$\text{gt}(n_{135300}, n_2)$      $\text{fof}(\text{gt}_{.135300}_2, \text{axiom})$

$\text{gt}(n_3, n_2)$      $\text{fof}(\text{gt}_{.3}_2, \text{axiom})$

$\text{gt}(n_4, n_3)$      $\text{fof}(\text{gt}_{.4}_3, \text{axiom})$

$\text{gt}(n_5, n_3)$      $\text{fof}(\text{gt}_{.5}_3, \text{axiom})$

$\text{gt}(n_{135300}, n_3)$      $\text{fof}(\text{gt}_{.135300}_3, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$      $\text{fof}(\text{finite\_domain}_4, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$      $\text{fof}(\text{finite\_domain}_5, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$      $\text{fof}(\text{finite\_domain}_0, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$      $\text{fof}(\text{finite\_domain}_1, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$      $\text{fof}(\text{finite\_domain}_2, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$      $\text{fof}(\text{finite\_domain}_3, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))) = n_4$      $\text{fof}(\text{successor}_4, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))))) = n_5$      $\text{fof}(\text{successor}_5, \text{axiom})$

$\text{succ}(n_0) = n_1$      $\text{fof}(\text{successor}_1, \text{axiom})$

$\text{succ}(\text{succ}(n_0)) = n_2$      $\text{fof}(\text{successor}_2, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3$      $\text{fof}(\text{successor}_3, \text{axiom})$

**SWV071+1.p** Unsimplified proof obligation `cl5_nebula_array_0012`

Proof obligation emerging from the array-safety verification for the `cl5_nebula` program. `array-safety` ensures that each access to an array element is within the specified upper and lower bounds of the array.

`include('Axioms/SWV003+0.ax')`

$(n_0 \leq \text{pv}_{21} \text{ and } n_0 \leq \text{pv}_{23} \text{ and } \text{pv}_{21} \leq -n_5 \text{ and } \text{pv}_{23} \leq -n_{135300}) \Rightarrow (n_0 \leq \text{pv}_{21} \text{ and } n_0 \leq \text{pv}_{23} \text{ and } \text{pv}_{21} \leq -n_5 \text{ and } \text{pv}_{23} \leq -n_{135300})$      $\text{fof}(\text{cl5\_nebula\_array}_{0012}, \text{conjecture})$

$\text{gt}(n_5, n_4)$      $\text{fof}(\text{gt}_{.5}_4, \text{axiom})$

$\text{gt}(n_{135300}, n_4)$      $\text{fof}(\text{gt}_{.135300}_4, \text{axiom})$

$\text{gt}(n_{135300}, n_5)$      $\text{fof}(\text{gt}_{.135300}_5, \text{axiom})$

$\text{gt}(n_4, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.4\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_5, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.5\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_{135300}, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.135300\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_0, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.0\_tptp\_minus}_1, \text{axiom})$

```

gt( $n_1$ , tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt( $n_2$ , tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt( $n_3$ , tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt( $n_4$ ,  $n_0$ )           fof(gt_40, axiom)
gt( $n_5$ ,  $n_0$ )           fof(gt_50, axiom)
gt( $n_{135300}$ ,  $n_0$ )      fof(gt_1353000, axiom)
gt( $n_1$ ,  $n_0$ )           fof(gt_10, axiom)
gt( $n_2$ ,  $n_0$ )           fof(gt_20, axiom)
gt( $n_3$ ,  $n_0$ )           fof(gt_30, axiom)
gt( $n_4$ ,  $n_1$ )           fof(gt_41, axiom)
gt( $n_5$ ,  $n_1$ )           fof(gt_51, axiom)
gt( $n_{135300}$ ,  $n_1$ )      fof(gt_1353001, axiom)
gt( $n_2$ ,  $n_1$ )           fof(gt_21, axiom)
gt( $n_3$ ,  $n_1$ )           fof(gt_31, axiom)
gt( $n_4$ ,  $n_2$ )           fof(gt_42, axiom)
gt( $n_5$ ,  $n_2$ )           fof(gt_52, axiom)
gt( $n_{135300}$ ,  $n_2$ )      fof(gt_1353002, axiom)
gt( $n_3$ ,  $n_2$ )           fof(gt_32, axiom)
gt( $n_4$ ,  $n_3$ )           fof(gt_43, axiom)
gt( $n_5$ ,  $n_3$ )           fof(gt_53, axiom)
gt( $n_{135300}$ ,  $n_3$ )      fof(gt_1353003, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$     fof(finite_domain4, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$     fof(finite_domain5, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$     fof(finite_domain0, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$     fof(finite_domain1, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$     fof(finite_domain2, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$     fof(finite_domain3, axiom)
succ(succ(succ(succ( $n_0$ )))) =  $n_4$     fof(successor4, axiom)
succ(succ(succ(succ(succ( $n_0$ )))))) =  $n_5$     fof(successor5, axiom)
succ( $n_0$ ) =  $n_1$     fof(successor1, axiom)
succ(succ( $n_0$ )) =  $n_2$     fof(successor2, axiom)
succ(succ(succ( $n_0$ ))) =  $n_3$     fof(successor3, axiom)

```

**SWV072+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0013

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

```

( $n_0 \leq \text{pv}_{21}$  and  $\text{pv}_{21} \leq -n_5$ )  $\Rightarrow$  ( $n_0 \leq \text{pv}_{21}$  and  $\text{pv}_{21} \leq -n_5$ )    fof(cl5_nebula_array0013, conjecture)
gt( $n_5$ ,  $n_4$ )           fof(gt_54, axiom)
gt( $n_4$ , tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt( $n_5$ , tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt( $n_0$ , tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt( $n_1$ , tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt( $n_2$ , tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt( $n_3$ , tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt( $n_4$ ,  $n_0$ )           fof(gt_40, axiom)
gt( $n_5$ ,  $n_0$ )           fof(gt_50, axiom)
gt( $n_1$ ,  $n_0$ )           fof(gt_10, axiom)
gt( $n_2$ ,  $n_0$ )           fof(gt_20, axiom)
gt( $n_3$ ,  $n_0$ )           fof(gt_30, axiom)
gt( $n_4$ ,  $n_1$ )           fof(gt_41, axiom)
gt( $n_5$ ,  $n_1$ )           fof(gt_51, axiom)
gt( $n_2$ ,  $n_1$ )           fof(gt_21, axiom)
gt( $n_3$ ,  $n_1$ )           fof(gt_31, axiom)
gt( $n_4$ ,  $n_2$ )           fof(gt_42, axiom)
gt( $n_5$ ,  $n_2$ )           fof(gt_52, axiom)
gt( $n_3$ ,  $n_2$ )           fof(gt_32, axiom)
gt( $n_4$ ,  $n_3$ )           fof(gt_43, axiom)
gt( $n_5$ ,  $n_3$ )           fof(gt_53, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$     fof(finite_domain4, axiom)

```

$\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$     fof(finite\_domain<sub>5</sub>, axiom)  
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$     fof(finite\_domain<sub>0</sub>, axiom)  
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$     fof(finite\_domain<sub>1</sub>, axiom)  
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$     fof(finite\_domain<sub>2</sub>, axiom)  
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$     fof(finite\_domain<sub>3</sub>, axiom)  
succ(succ(succ(succ(n<sub>0</sub>)))) = n<sub>4</sub>    fof(successor<sub>4</sub>, axiom)  
succ(succ(succ(succ(succ(n<sub>0</sub>)))))) = n<sub>5</sub>    fof(successor<sub>5</sub>, axiom)  
succ(n<sub>0</sub>) = n<sub>1</sub>    fof(successor<sub>1</sub>, axiom)  
succ(succ(n<sub>0</sub>)) = n<sub>2</sub>    fof(successor<sub>2</sub>, axiom)  
succ(succ(succ(n<sub>0</sub>))) = n<sub>3</sub>    fof(successor<sub>3</sub>, axiom)

**SWV073+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0014

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq pv_{31} \text{ and } n_0 \leq pv_{35} \text{ and } pv_{31} \leq -n_5 \text{ and } pv_{35} \leq -n_{135300}) \Rightarrow (n_0 \leq pv_{31} \text{ and } n_0 \leq pv_{35} \text{ and } pv_{31} \leq -n_5 \text{ and } pv_{35} \leq -n_{135300})$     fof(cl5\_nebula\_array<sub>0014</sub>, conjecture)

gt(n<sub>5</sub>, n<sub>4</sub>)    fof(gt\_5<sub>4</sub>, axiom)

gt(n<sub>135300</sub>, n<sub>4</sub>)    fof(gt\_135300<sub>4</sub>, axiom)

gt(n<sub>135300</sub>, n<sub>5</sub>)    fof(gt\_135300<sub>5</sub>, axiom)

gt(n<sub>4</sub>, tptp\_minus<sub>1</sub>)    fof(gt\_4\_tptp\_minus<sub>1</sub>, axiom)

gt(n<sub>5</sub>, tptp\_minus<sub>1</sub>)    fof(gt\_5\_tptp\_minus<sub>1</sub>, axiom)

gt(n<sub>135300</sub>, tptp\_minus<sub>1</sub>)    fof(gt\_135300\_tptp\_minus<sub>1</sub>, axiom)

gt(n<sub>0</sub>, tptp\_minus<sub>1</sub>)    fof(gt\_0\_tptp\_minus<sub>1</sub>, axiom)

gt(n<sub>1</sub>, tptp\_minus<sub>1</sub>)    fof(gt\_1\_tptp\_minus<sub>1</sub>, axiom)

gt(n<sub>2</sub>, tptp\_minus<sub>1</sub>)    fof(gt\_2\_tptp\_minus<sub>1</sub>, axiom)

gt(n<sub>3</sub>, tptp\_minus<sub>1</sub>)    fof(gt\_3\_tptp\_minus<sub>1</sub>, axiom)

gt(n<sub>4</sub>, n<sub>0</sub>)    fof(gt\_4<sub>0</sub>, axiom)

gt(n<sub>5</sub>, n<sub>0</sub>)    fof(gt\_5<sub>0</sub>, axiom)

gt(n<sub>135300</sub>, n<sub>0</sub>)    fof(gt\_135300<sub>0</sub>, axiom)

gt(n<sub>1</sub>, n<sub>0</sub>)    fof(gt\_1<sub>0</sub>, axiom)

gt(n<sub>2</sub>, n<sub>0</sub>)    fof(gt\_2<sub>0</sub>, axiom)

gt(n<sub>3</sub>, n<sub>0</sub>)    fof(gt\_3<sub>0</sub>, axiom)

gt(n<sub>4</sub>, n<sub>1</sub>)    fof(gt\_4<sub>1</sub>, axiom)

gt(n<sub>5</sub>, n<sub>1</sub>)    fof(gt\_5<sub>1</sub>, axiom)

gt(n<sub>135300</sub>, n<sub>1</sub>)    fof(gt\_135300<sub>1</sub>, axiom)

gt(n<sub>2</sub>, n<sub>1</sub>)    fof(gt\_2<sub>1</sub>, axiom)

gt(n<sub>3</sub>, n<sub>1</sub>)    fof(gt\_3<sub>1</sub>, axiom)

gt(n<sub>4</sub>, n<sub>2</sub>)    fof(gt\_4<sub>2</sub>, axiom)

gt(n<sub>5</sub>, n<sub>2</sub>)    fof(gt\_5<sub>2</sub>, axiom)

gt(n<sub>135300</sub>, n<sub>2</sub>)    fof(gt\_135300<sub>2</sub>, axiom)

gt(n<sub>3</sub>, n<sub>2</sub>)    fof(gt\_3<sub>2</sub>, axiom)

gt(n<sub>4</sub>, n<sub>3</sub>)    fof(gt\_4<sub>3</sub>, axiom)

gt(n<sub>5</sub>, n<sub>3</sub>)    fof(gt\_5<sub>3</sub>, axiom)

gt(n<sub>135300</sub>, n<sub>3</sub>)    fof(gt\_135300<sub>3</sub>, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$     fof(finite\_domain<sub>4</sub>, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$     fof(finite\_domain<sub>5</sub>, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$     fof(finite\_domain<sub>0</sub>, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$     fof(finite\_domain<sub>1</sub>, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$     fof(finite\_domain<sub>2</sub>, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$     fof(finite\_domain<sub>3</sub>, axiom)

succ(succ(succ(succ(n<sub>0</sub>)))) = n<sub>4</sub>    fof(successor<sub>4</sub>, axiom)

succ(succ(succ(succ(succ(n<sub>0</sub>)))))) = n<sub>5</sub>    fof(successor<sub>5</sub>, axiom)

succ(n<sub>0</sub>) = n<sub>1</sub>    fof(successor<sub>1</sub>, axiom)

succ(succ(n<sub>0</sub>)) = n<sub>2</sub>    fof(successor<sub>2</sub>, axiom)

succ(succ(succ(n<sub>0</sub>))) = n<sub>3</sub>    fof(successor<sub>3</sub>, axiom)

**SWV074+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0015

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq pv_{31} \text{ and } n_0 \leq pv_{36} \text{ and } pv_{31} \leq -n_5 \text{ and } pv_{36} \leq -n_{135300}) \Rightarrow (n_0 \leq pv_{31} \text{ and } n_0 \leq pv_{36} \text{ and } pv_{31} \leq -n_5 \text{ and } pv_{36} \leq -n_{135300})$  fof(cl5\_nebula\_array0015, conjecture)

gt( $n_5, n_4$ ) fof(gt\_5\_4, axiom)

gt( $n_{135300}, n_4$ ) fof(gt\_135300\_4, axiom)

gt( $n_{135300}, n_5$ ) fof(gt\_135300\_5, axiom)

gt( $n_4, tptp\_minus_1$ ) fof(gt\_4\_tptp\_minus\_1, axiom)

gt( $n_5, tptp\_minus_1$ ) fof(gt\_5\_tptp\_minus\_1, axiom)

gt( $n_{135300}, tptp\_minus_1$ ) fof(gt\_135300\_tptp\_minus\_1, axiom)

gt( $n_0, tptp\_minus_1$ ) fof(gt\_0\_tptp\_minus\_1, axiom)

gt( $n_1, tptp\_minus_1$ ) fof(gt\_1\_tptp\_minus\_1, axiom)

gt( $n_2, tptp\_minus_1$ ) fof(gt\_2\_tptp\_minus\_1, axiom)

gt( $n_3, tptp\_minus_1$ ) fof(gt\_3\_tptp\_minus\_1, axiom)

gt( $n_4, n_0$ ) fof(gt\_4\_0, axiom)

gt( $n_5, n_0$ ) fof(gt\_5\_0, axiom)

gt( $n_{135300}, n_0$ ) fof(gt\_135300\_0, axiom)

gt( $n_1, n_0$ ) fof(gt\_1\_0, axiom)

gt( $n_2, n_0$ ) fof(gt\_2\_0, axiom)

gt( $n_3, n_0$ ) fof(gt\_3\_0, axiom)

gt( $n_4, n_1$ ) fof(gt\_4\_1, axiom)

gt( $n_5, n_1$ ) fof(gt\_5\_1, axiom)

gt( $n_{135300}, n_1$ ) fof(gt\_135300\_1, axiom)

gt( $n_2, n_1$ ) fof(gt\_2\_1, axiom)

gt( $n_3, n_1$ ) fof(gt\_3\_1, axiom)

gt( $n_4, n_2$ ) fof(gt\_4\_2, axiom)

gt( $n_5, n_2$ ) fof(gt\_5\_2, axiom)

gt( $n_{135300}, n_2$ ) fof(gt\_135300\_2, axiom)

gt( $n_3, n_2$ ) fof(gt\_3\_2, axiom)

gt( $n_4, n_3$ ) fof(gt\_4\_3, axiom)

gt( $n_5, n_3$ ) fof(gt\_5\_3, axiom)

gt( $n_{135300}, n_3$ ) fof(gt\_135300\_3, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$  fof(finite\_domain\_4, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$  fof(finite\_domain\_5, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$  fof(finite\_domain\_0, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$  fof(finite\_domain\_1, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$  fof(finite\_domain\_2, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$  fof(finite\_domain\_3, axiom)

succ(succ(succ(succ( $n_0$ )))) =  $n_4$  fof(successor\_4, axiom)

succ(succ(succ(succ(succ( $n_0$ )))))) =  $n_5$  fof(successor\_5, axiom)

succ( $n_0$ ) =  $n_1$  fof(successor\_1, axiom)

succ(succ( $n_0$ )) =  $n_2$  fof(successor\_2, axiom)

succ(succ(succ( $n_0$ ))) =  $n_3$  fof(successor\_3, axiom)

**SWV075+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0016

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq pv_{31} \text{ and } n_0 \leq pv_{37} \text{ and } pv_{31} \leq -n_5 \text{ and } pv_{37} \leq -n_{135300}) \Rightarrow (n_0 \leq pv_{31} \text{ and } n_0 \leq pv_{37} \text{ and } pv_{31} \leq -n_5 \text{ and } pv_{37} \leq -n_{135300})$  fof(cl5\_nebula\_array0016, conjecture)

gt( $n_5, n_4$ ) fof(gt\_5\_4, axiom)

gt( $n_{135300}, n_4$ ) fof(gt\_135300\_4, axiom)

gt( $n_{135300}, n_5$ ) fof(gt\_135300\_5, axiom)

gt( $n_4, tptp\_minus_1$ ) fof(gt\_4\_tptp\_minus\_1, axiom)

gt( $n_5, tptp\_minus_1$ ) fof(gt\_5\_tptp\_minus\_1, axiom)

gt( $n_{135300}, tptp\_minus_1$ ) fof(gt\_135300\_tptp\_minus\_1, axiom)

gt( $n_0, tptp\_minus_1$ ) fof(gt\_0\_tptp\_minus\_1, axiom)

gt( $n_1, tptp\_minus_1$ ) fof(gt\_1\_tptp\_minus\_1, axiom)

gt( $n_2, tptp\_minus_1$ ) fof(gt\_2\_tptp\_minus\_1, axiom)

gt( $n_3, tptp\_minus_1$ ) fof(gt\_3\_tptp\_minus\_1, axiom)

gt( $n_4, n_0$ ) fof(gt\_4\_0, axiom)



```

gt(n5, n0)    fof(gt_50, axiom)
gt(n135300, n0)  fof(gt_135300_0, axiom)
gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n135300, n1)  fof(gt_135300_1, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n135300, n2)  fof(gt_135300_2, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
gt(n135300, n3)  fof(gt_135300_3, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

**SWV076+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0017

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

```

(n0 ≤ pv31 and pv31 ≤ -n5) ⇒ (n0 ≤ pv31 and pv31 ≤ -n5)    fof(cl5_nebula_array0017, conjecture)
gt(n5, n4)    fof(gt_54, axiom)
gt(n4, tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt(n5, tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt(n0, tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt(n1, tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt(n2, tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt(n3, tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt(n4, n0)    fof(gt_40, axiom)
gt(n5, n0)    fof(gt_50, axiom)
gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)

```

$\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$     fof(finite\_domain3, axiom)  
 $\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))) = n_4$     fof(successor4, axiom)  
 $\text{succ}(\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))))) = n_5$     fof(successor5, axiom)  
 $\text{succ}(n_0) = n_1$     fof(successor1, axiom)  
 $\text{succ}(\text{succ}(n_0)) = n_2$     fof(successor2, axiom)  
 $\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3$     fof(successor3, axiom)

**SWV077+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0018

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq \text{pv}_{31} \text{ and } \text{pv}_{31} \leq -n_5) \Rightarrow (n_0 \leq \text{pv}_{31} \text{ and } \text{pv}_{31} \leq -n_5 \text{ and } (n_0 \neq \text{pv}_{40} \Rightarrow (n_0 \leq \text{pv}_{31} \text{ and } \text{pv}_{31} \leq -n_5))) \text{ and } (n_0 = \text{pv}_{40} \Rightarrow \text{true})$     fof(cl5\_nebula\_array0018, conjecture)

$\text{gt}(n_5, n_4)$     fof(gt\_54, axiom)  
 $\text{gt}(n_4, \text{tptp\_minus}_1)$     fof(gt\_4\_tptp\_minus1, axiom)  
 $\text{gt}(n_5, \text{tptp\_minus}_1)$     fof(gt\_5\_tptp\_minus1, axiom)  
 $\text{gt}(n_0, \text{tptp\_minus}_1)$     fof(gt\_0\_tptp\_minus1, axiom)  
 $\text{gt}(n_1, \text{tptp\_minus}_1)$     fof(gt\_1\_tptp\_minus1, axiom)  
 $\text{gt}(n_2, \text{tptp\_minus}_1)$     fof(gt\_2\_tptp\_minus1, axiom)  
 $\text{gt}(n_3, \text{tptp\_minus}_1)$     fof(gt\_3\_tptp\_minus1, axiom)  
 $\text{gt}(n_4, n_0)$     fof(gt\_40, axiom)  
 $\text{gt}(n_5, n_0)$     fof(gt\_50, axiom)  
 $\text{gt}(n_1, n_0)$     fof(gt\_10, axiom)  
 $\text{gt}(n_2, n_0)$     fof(gt\_20, axiom)  
 $\text{gt}(n_3, n_0)$     fof(gt\_30, axiom)  
 $\text{gt}(n_4, n_1)$     fof(gt\_41, axiom)  
 $\text{gt}(n_5, n_1)$     fof(gt\_51, axiom)  
 $\text{gt}(n_2, n_1)$     fof(gt\_21, axiom)  
 $\text{gt}(n_3, n_1)$     fof(gt\_31, axiom)  
 $\text{gt}(n_4, n_2)$     fof(gt\_42, axiom)  
 $\text{gt}(n_5, n_2)$     fof(gt\_52, axiom)  
 $\text{gt}(n_3, n_2)$     fof(gt\_32, axiom)  
 $\text{gt}(n_4, n_3)$     fof(gt\_43, axiom)  
 $\text{gt}(n_5, n_3)$     fof(gt\_53, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$     fof(finite\_domain4, axiom)  
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$     fof(finite\_domain5, axiom)  
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$     fof(finite\_domain0, axiom)  
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$     fof(finite\_domain1, axiom)  
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$     fof(finite\_domain2, axiom)  
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$     fof(finite\_domain3, axiom)  
 $\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))) = n_4$     fof(successor4, axiom)  
 $\text{succ}(\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))))) = n_5$     fof(successor5, axiom)  
 $\text{succ}(n_0) = n_1$     fof(successor1, axiom)  
 $\text{succ}(\text{succ}(n_0)) = n_2$     fof(successor2, axiom)  
 $\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3$     fof(successor3, axiom)

**SWV078+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0019

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq \text{pv}_{31} \text{ and } \text{pv}_{31} \leq -n_5) \Rightarrow ((n_0 \neq \text{pv}_{70} \Rightarrow (n_0 \leq \text{pv}_{31} \text{ and } \text{pv}_{31} \leq -n_5)) \text{ and } (n_0 = \text{pv}_{70} \Rightarrow \text{true}))$     fof(cl5\_nebula\_array0019, conjecture)

$\text{gt}(n_5, n_4)$     fof(gt\_54, axiom)  
 $\text{gt}(n_4, \text{tptp\_minus}_1)$     fof(gt\_4\_tptp\_minus1, axiom)  
 $\text{gt}(n_5, \text{tptp\_minus}_1)$     fof(gt\_5\_tptp\_minus1, axiom)  
 $\text{gt}(n_0, \text{tptp\_minus}_1)$     fof(gt\_0\_tptp\_minus1, axiom)  
 $\text{gt}(n_1, \text{tptp\_minus}_1)$     fof(gt\_1\_tptp\_minus1, axiom)  
 $\text{gt}(n_2, \text{tptp\_minus}_1)$     fof(gt\_2\_tptp\_minus1, axiom)  
 $\text{gt}(n_3, \text{tptp\_minus}_1)$     fof(gt\_3\_tptp\_minus1, axiom)  
 $\text{gt}(n_4, n_0)$     fof(gt\_40, axiom)  
 $\text{gt}(n_5, n_0)$     fof(gt\_50, axiom)

```

gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

### SWV079+1.p Unsimplified proof obligation cl5\_nebula\_array\_0020

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

```
include('Axioms/SWV003+0.ax')
```

```
(n0 ≤ pv51 and pv51 ≤ -n5) ⇒ (n0 ≤ n0 and n0 ≤ pv51 and n0 ≤ uniform_int_rnd(n1, -(-n135300)) and pv51 ≤ -n5 and uniform_int_rnd(n1, -(-n135300)) ≤ -n135300)    fof(cl5_nebula_array_0020, conjecture)
```

```

gt(n5, n4)    fof(gt_54, axiom)
gt(n135300, n4)    fof(gt_1353004, axiom)
gt(n135300, n5)    fof(gt_1353005, axiom)
gt(n4, tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt(n5, tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt(n135300, tptp_minus1)    fof(gt_135300_tptp_minus1, axiom)
gt(n0, tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt(n1, tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt(n2, tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt(n3, tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt(n4, n0)    fof(gt_40, axiom)
gt(n5, n0)    fof(gt_50, axiom)
gt(n135300, n0)    fof(gt_1353000, axiom)
gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n135300, n1)    fof(gt_1353001, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n135300, n2)    fof(gt_1353002, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
gt(n135300, n3)    fof(gt_1353003, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)

```

$\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0) \quad \text{fof}(\text{finite\_domain}_0, \text{axiom})$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1)) \quad \text{fof}(\text{finite\_domain}_1, \text{axiom})$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2)) \quad \text{fof}(\text{finite\_domain}_2, \text{axiom})$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3)) \quad \text{fof}(\text{finite\_domain}_3, \text{axiom})$   
 $\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))) = n_4 \quad \text{fof}(\text{successor}_4, \text{axiom})$   
 $\text{succ}(\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))))) = n_5 \quad \text{fof}(\text{successor}_5, \text{axiom})$   
 $\text{succ}(n_0) = n_1 \quad \text{fof}(\text{successor}_1, \text{axiom})$   
 $\text{succ}(\text{succ}(n_0)) = n_2 \quad \text{fof}(\text{successor}_2, \text{axiom})$   
 $\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3 \quad \text{fof}(\text{successor}_3, \text{axiom})$

**SWV080+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0021

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq \text{pv}_{56} \text{ and } \text{pv}_{56} \leq -n_5) \Rightarrow (n_0 \leq \text{pv}_{56} \text{ and } \text{pv}_{56} \leq -n_5) \quad \text{fof}(\text{cl5\_nebula\_array}_{0021}, \text{conjecture})$

$\text{gt}(n_5, n_4) \quad \text{fof}(\text{gt}_{.5_4}, \text{axiom})$

$\text{gt}(n_4, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.4\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_5, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.5\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_0, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.0\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_1, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.1\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_2, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.2\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_3, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.3\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_4, n_0) \quad \text{fof}(\text{gt}_{.4_0}, \text{axiom})$

$\text{gt}(n_5, n_0) \quad \text{fof}(\text{gt}_{.5_0}, \text{axiom})$

$\text{gt}(n_1, n_0) \quad \text{fof}(\text{gt}_{.1_0}, \text{axiom})$

$\text{gt}(n_2, n_0) \quad \text{fof}(\text{gt}_{.2_0}, \text{axiom})$

$\text{gt}(n_3, n_0) \quad \text{fof}(\text{gt}_{.3_0}, \text{axiom})$

$\text{gt}(n_4, n_1) \quad \text{fof}(\text{gt}_{.4_1}, \text{axiom})$

$\text{gt}(n_5, n_1) \quad \text{fof}(\text{gt}_{.5_1}, \text{axiom})$

$\text{gt}(n_2, n_1) \quad \text{fof}(\text{gt}_{.2_1}, \text{axiom})$

$\text{gt}(n_3, n_1) \quad \text{fof}(\text{gt}_{.3_1}, \text{axiom})$

$\text{gt}(n_4, n_2) \quad \text{fof}(\text{gt}_{.4_2}, \text{axiom})$

$\text{gt}(n_5, n_2) \quad \text{fof}(\text{gt}_{.5_2}, \text{axiom})$

$\text{gt}(n_3, n_2) \quad \text{fof}(\text{gt}_{.3_2}, \text{axiom})$

$\text{gt}(n_4, n_3) \quad \text{fof}(\text{gt}_{.4_3}, \text{axiom})$

$\text{gt}(n_5, n_3) \quad \text{fof}(\text{gt}_{.5_3}, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4)) \quad \text{fof}(\text{finite\_domain}_4, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5)) \quad \text{fof}(\text{finite\_domain}_5, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0) \quad \text{fof}(\text{finite\_domain}_0, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1)) \quad \text{fof}(\text{finite\_domain}_1, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2)) \quad \text{fof}(\text{finite\_domain}_2, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3)) \quad \text{fof}(\text{finite\_domain}_3, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))) = n_4 \quad \text{fof}(\text{successor}_4, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))))) = n_5 \quad \text{fof}(\text{successor}_5, \text{axiom})$

$\text{succ}(n_0) = n_1 \quad \text{fof}(\text{successor}_1, \text{axiom})$

$\text{succ}(\text{succ}(n_0)) = n_2 \quad \text{fof}(\text{successor}_2, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3 \quad \text{fof}(\text{successor}_3, \text{axiom})$

**SWV081+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0022

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq \text{pv}_{57} \text{ and } \text{pv}_{57} \leq -n_5) \Rightarrow (n_0 \leq \text{pv}_{57} \text{ and } \text{pv}_{57} \leq -n_5) \quad \text{fof}(\text{cl5\_nebula\_array}_{0022}, \text{conjecture})$

$\text{gt}(n_5, n_4) \quad \text{fof}(\text{gt}_{.5_4}, \text{axiom})$

$\text{gt}(n_4, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.4\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_5, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.5\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_0, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.0\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_1, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.1\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_2, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.2\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_3, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.3\_tptp\_minus}_1, \text{axiom})$

```

gt(n4, n0)    fof(gt_40, axiom)
gt(n5, n0)    fof(gt_50, axiom)
gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

**SWV082+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0023

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

```
include('Axioms/SWV003+0.ax')
```

```

(n0 ≤ pv58 and pv58 ≤ -n5) ⇒ (n0 ≤ pv58 and pv58 ≤ -n5)    fof(cl5_nebula_array0023, conjecture)
gt(n5, n4)    fof(gt_54, axiom)
gt(n4, tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt(n5, tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt(n0, tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt(n1, tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt(n2, tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt(n3, tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt(n4, n0)    fof(gt_40, axiom)
gt(n5, n0)    fof(gt_50, axiom)
gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)

```

$\text{succ}(n_0) = n_1 \quad \text{fof}(\text{successor}_1, \text{axiom})$   
 $\text{succ}(\text{succ}(n_0)) = n_2 \quad \text{fof}(\text{successor}_2, \text{axiom})$   
 $\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3 \quad \text{fof}(\text{successor}_3, \text{axiom})$

**SWV083+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0024

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq \text{pv}_{66} \text{ and } \text{pv}_{66} \leq -n_5) \Rightarrow (n_0 \leq \text{pv}_{66} \text{ and } \text{pv}_{66} \leq -n_5) \quad \text{fof}(\text{cl5\_nebula\_array}_{0024}, \text{conjecture})$

$\text{gt}(n_5, n_4) \quad \text{fof}(\text{gt}_{.5_4}, \text{axiom})$

$\text{gt}(n_4, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.4\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_5, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.5\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_0, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.0\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_1, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.1\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_2, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.2\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_3, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.3\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_4, n_0) \quad \text{fof}(\text{gt}_{.4_0}, \text{axiom})$

$\text{gt}(n_5, n_0) \quad \text{fof}(\text{gt}_{.5_0}, \text{axiom})$

$\text{gt}(n_1, n_0) \quad \text{fof}(\text{gt}_{.1_0}, \text{axiom})$

$\text{gt}(n_2, n_0) \quad \text{fof}(\text{gt}_{.2_0}, \text{axiom})$

$\text{gt}(n_3, n_0) \quad \text{fof}(\text{gt}_{.3_0}, \text{axiom})$

$\text{gt}(n_4, n_1) \quad \text{fof}(\text{gt}_{.4_1}, \text{axiom})$

$\text{gt}(n_5, n_1) \quad \text{fof}(\text{gt}_{.5_1}, \text{axiom})$

$\text{gt}(n_2, n_1) \quad \text{fof}(\text{gt}_{.2_1}, \text{axiom})$

$\text{gt}(n_3, n_1) \quad \text{fof}(\text{gt}_{.3_1}, \text{axiom})$

$\text{gt}(n_4, n_2) \quad \text{fof}(\text{gt}_{.4_2}, \text{axiom})$

$\text{gt}(n_5, n_2) \quad \text{fof}(\text{gt}_{.5_2}, \text{axiom})$

$\text{gt}(n_3, n_2) \quad \text{fof}(\text{gt}_{.3_2}, \text{axiom})$

$\text{gt}(n_4, n_3) \quad \text{fof}(\text{gt}_{.4_3}, \text{axiom})$

$\text{gt}(n_5, n_3) \quad \text{fof}(\text{gt}_{.5_3}, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4)) \quad \text{fof}(\text{finite\_domain}_4, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5)) \quad \text{fof}(\text{finite\_domain}_5, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0) \quad \text{fof}(\text{finite\_domain}_0, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1)) \quad \text{fof}(\text{finite\_domain}_1, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2)) \quad \text{fof}(\text{finite\_domain}_2, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3)) \quad \text{fof}(\text{finite\_domain}_3, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))) = n_4 \quad \text{fof}(\text{successor}_4, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))))) = n_5 \quad \text{fof}(\text{successor}_5, \text{axiom})$

$\text{succ}(n_0) = n_1 \quad \text{fof}(\text{successor}_1, \text{axiom})$

$\text{succ}(\text{succ}(n_0)) = n_2 \quad \text{fof}(\text{successor}_2, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3 \quad \text{fof}(\text{successor}_3, \text{axiom})$

**SWV084+1.p** Unsimplified proof obligation cl5\_nebula\_array\_0025

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq \text{pv}_{67} \text{ and } \text{pv}_{67} \leq -n_5) \Rightarrow (n_0 \leq \text{pv}_{67} \text{ and } \text{pv}_{67} \leq -n_5) \quad \text{fof}(\text{cl5\_nebula\_array}_{0025}, \text{conjecture})$

$\text{gt}(n_5, n_4) \quad \text{fof}(\text{gt}_{.5_4}, \text{axiom})$

$\text{gt}(n_4, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.4\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_5, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.5\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_0, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.0\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_1, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.1\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_2, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.2\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_3, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.3\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_4, n_0) \quad \text{fof}(\text{gt}_{.4_0}, \text{axiom})$

$\text{gt}(n_5, n_0) \quad \text{fof}(\text{gt}_{.5_0}, \text{axiom})$

$\text{gt}(n_1, n_0) \quad \text{fof}(\text{gt}_{.1_0}, \text{axiom})$

$\text{gt}(n_2, n_0) \quad \text{fof}(\text{gt}_{.2_0}, \text{axiom})$

$\text{gt}(n_3, n_0) \quad \text{fof}(\text{gt}_{.3_0}, \text{axiom})$

$\text{gt}(n_4, n_1) \quad \text{fof}(\text{gt}_{.4_1}, \text{axiom})$

$gt(n_5, n_1)$      $fof(gt\_5_1, axiom)$   
 $gt(n_2, n_1)$      $fof(gt\_2_1, axiom)$   
 $gt(n_3, n_1)$      $fof(gt\_3_1, axiom)$   
 $gt(n_4, n_2)$      $fof(gt\_4_2, axiom)$   
 $gt(n_5, n_2)$      $fof(gt\_5_2, axiom)$   
 $gt(n_3, n_2)$      $fof(gt\_3_2, axiom)$   
 $gt(n_4, n_3)$      $fof(gt\_4_3, axiom)$   
 $gt(n_5, n_3)$      $fof(gt\_5_3, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$      $fof(finite\_domain_4, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$      $fof(finite\_domain_5, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$      $fof(finite\_domain_0, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$      $fof(finite\_domain_1, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$      $fof(finite\_domain_2, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$      $fof(finite\_domain_3, axiom)$   
 $succ(succ(succ(succ(n_0)))) = n_4$      $fof(successor_4, axiom)$   
 $succ(succ(succ(succ(succ(n_0)))))) = n_5$      $fof(successor_5, axiom)$   
 $succ(n_0) = n_1$      $fof(successor_1, axiom)$   
 $succ(succ(n_0)) = n_2$      $fof(successor_2, axiom)$   
 $succ(succ(succ(n_0))) = n_3$      $fof(successor_3, axiom)$

### SWV085+1.p Unsimplified proof obligation cl5\_nebula\_array\_0026

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq pv_{68} \text{ and } pv_{68} \leq -n_5) \Rightarrow (n_0 \leq pv_{68} \text{ and } pv_{68} \leq -n_5)$      $fof(cl5\_nebula\_array_{0026}, conjecture)$   
 $gt(n_5, n_4)$      $fof(gt\_5_4, axiom)$   
 $gt(n_4, tptp\_minus_1)$      $fof(gt\_4\_tptp\_minus_1, axiom)$   
 $gt(n_5, tptp\_minus_1)$      $fof(gt\_5\_tptp\_minus_1, axiom)$   
 $gt(n_0, tptp\_minus_1)$      $fof(gt\_0\_tptp\_minus_1, axiom)$   
 $gt(n_1, tptp\_minus_1)$      $fof(gt\_1\_tptp\_minus_1, axiom)$   
 $gt(n_2, tptp\_minus_1)$      $fof(gt\_2\_tptp\_minus_1, axiom)$   
 $gt(n_3, tptp\_minus_1)$      $fof(gt\_3\_tptp\_minus_1, axiom)$   
 $gt(n_4, n_0)$      $fof(gt\_4_0, axiom)$   
 $gt(n_5, n_0)$      $fof(gt\_5_0, axiom)$   
 $gt(n_1, n_0)$      $fof(gt\_1_0, axiom)$   
 $gt(n_2, n_0)$      $fof(gt\_2_0, axiom)$   
 $gt(n_3, n_0)$      $fof(gt\_3_0, axiom)$   
 $gt(n_4, n_1)$      $fof(gt\_4_1, axiom)$   
 $gt(n_5, n_1)$      $fof(gt\_5_1, axiom)$   
 $gt(n_2, n_1)$      $fof(gt\_2_1, axiom)$   
 $gt(n_3, n_1)$      $fof(gt\_3_1, axiom)$   
 $gt(n_4, n_2)$      $fof(gt\_4_2, axiom)$   
 $gt(n_5, n_2)$      $fof(gt\_5_2, axiom)$   
 $gt(n_3, n_2)$      $fof(gt\_3_2, axiom)$   
 $gt(n_4, n_3)$      $fof(gt\_4_3, axiom)$   
 $gt(n_5, n_3)$      $fof(gt\_5_3, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$      $fof(finite\_domain_4, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$      $fof(finite\_domain_5, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$      $fof(finite\_domain_0, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$      $fof(finite\_domain_1, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$      $fof(finite\_domain_2, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$      $fof(finite\_domain_3, axiom)$   
 $succ(succ(succ(succ(n_0)))) = n_4$      $fof(successor_4, axiom)$   
 $succ(succ(succ(succ(succ(n_0)))))) = n_5$      $fof(successor_5, axiom)$   
 $succ(n_0) = n_1$      $fof(successor_1, axiom)$   
 $succ(succ(n_0)) = n_2$      $fof(successor_2, axiom)$   
 $succ(succ(succ(n_0))) = n_3$      $fof(successor_3, axiom)$

### SWV086+1.p Unsimplified proof obligation cl5\_nebula\_array\_0027

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$\neg \text{geq}(\text{pv}_{65}, \text{tptp\_float\_0}_{001}) \Rightarrow \text{true}$        $\text{fof}(\text{cl5\_nebula\_array}_{0027}, \text{conjecture})$

$\text{gt}(n_5, n_4)$        $\text{fof}(\text{gt}_{.5_4}, \text{axiom})$

$\text{gt}(n_4, \text{tptp\_minus}_1)$        $\text{fof}(\text{gt}_{.4\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_5, \text{tptp\_minus}_1)$        $\text{fof}(\text{gt}_{.5\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_0, \text{tptp\_minus}_1)$        $\text{fof}(\text{gt}_{.0\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_1, \text{tptp\_minus}_1)$        $\text{fof}(\text{gt}_{.1\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_2, \text{tptp\_minus}_1)$        $\text{fof}(\text{gt}_{.2\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_3, \text{tptp\_minus}_1)$        $\text{fof}(\text{gt}_{.3\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_4, n_0)$        $\text{fof}(\text{gt}_{.4_0}, \text{axiom})$

$\text{gt}(n_5, n_0)$        $\text{fof}(\text{gt}_{.5_0}, \text{axiom})$

$\text{gt}(n_1, n_0)$        $\text{fof}(\text{gt}_{.1_0}, \text{axiom})$

$\text{gt}(n_2, n_0)$        $\text{fof}(\text{gt}_{.2_0}, \text{axiom})$

$\text{gt}(n_3, n_0)$        $\text{fof}(\text{gt}_{.3_0}, \text{axiom})$

$\text{gt}(n_4, n_1)$        $\text{fof}(\text{gt}_{.4_1}, \text{axiom})$

$\text{gt}(n_5, n_1)$        $\text{fof}(\text{gt}_{.5_1}, \text{axiom})$

$\text{gt}(n_2, n_1)$        $\text{fof}(\text{gt}_{.2_1}, \text{axiom})$

$\text{gt}(n_3, n_1)$        $\text{fof}(\text{gt}_{.3_1}, \text{axiom})$

$\text{gt}(n_4, n_2)$        $\text{fof}(\text{gt}_{.4_2}, \text{axiom})$

$\text{gt}(n_5, n_2)$        $\text{fof}(\text{gt}_{.5_2}, \text{axiom})$

$\text{gt}(n_3, n_2)$        $\text{fof}(\text{gt}_{.3_2}, \text{axiom})$

$\text{gt}(n_4, n_3)$        $\text{fof}(\text{gt}_{.4_3}, \text{axiom})$

$\text{gt}(n_5, n_3)$        $\text{fof}(\text{gt}_{.5_3}, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$        $\text{fof}(\text{finite\_domain}_4, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$        $\text{fof}(\text{finite\_domain}_5, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$        $\text{fof}(\text{finite\_domain}_0, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$        $\text{fof}(\text{finite\_domain}_1, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$        $\text{fof}(\text{finite\_domain}_2, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$        $\text{fof}(\text{finite\_domain}_3, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))) = n_4$        $\text{fof}(\text{successor}_4, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))))) = n_5$        $\text{fof}(\text{successor}_5, \text{axiom})$

$\text{succ}(n_0) = n_1$        $\text{fof}(\text{successor}_1, \text{axiom})$

$\text{succ}(\text{succ}(n_0)) = n_2$        $\text{fof}(\text{successor}_2, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3$        $\text{fof}(\text{successor}_3, \text{axiom})$

### SWV087+1.p Unsimplified proof obligation cl5\_nebula\_array\_0028

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$\text{geq}(\text{pv}_{65}, \text{tptp\_float\_0}_{001}) \Rightarrow ((\neg \text{gt}(n_1 + \text{loopcounter}, n_1) \Rightarrow \text{true}) \text{ and } (\text{gt}(n_1 + \text{loopcounter}, n_1) \Rightarrow \text{true}))$        $\text{fof}(\text{cl5\_nebula\_array}_{0028}, \text{conjecture})$

$\text{gt}(n_5, n_4)$        $\text{fof}(\text{gt}_{.5_4}, \text{axiom})$

$\text{gt}(n_4, \text{tptp\_minus}_1)$        $\text{fof}(\text{gt}_{.4\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_5, \text{tptp\_minus}_1)$        $\text{fof}(\text{gt}_{.5\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_0, \text{tptp\_minus}_1)$        $\text{fof}(\text{gt}_{.0\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_1, \text{tptp\_minus}_1)$        $\text{fof}(\text{gt}_{.1\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_2, \text{tptp\_minus}_1)$        $\text{fof}(\text{gt}_{.2\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_3, \text{tptp\_minus}_1)$        $\text{fof}(\text{gt}_{.3\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_4, n_0)$        $\text{fof}(\text{gt}_{.4_0}, \text{axiom})$

$\text{gt}(n_5, n_0)$        $\text{fof}(\text{gt}_{.5_0}, \text{axiom})$

$\text{gt}(n_1, n_0)$        $\text{fof}(\text{gt}_{.1_0}, \text{axiom})$

$\text{gt}(n_2, n_0)$        $\text{fof}(\text{gt}_{.2_0}, \text{axiom})$

$\text{gt}(n_3, n_0)$        $\text{fof}(\text{gt}_{.3_0}, \text{axiom})$

$\text{gt}(n_4, n_1)$        $\text{fof}(\text{gt}_{.4_1}, \text{axiom})$

$\text{gt}(n_5, n_1)$        $\text{fof}(\text{gt}_{.5_1}, \text{axiom})$

$\text{gt}(n_2, n_1)$        $\text{fof}(\text{gt}_{.2_1}, \text{axiom})$

$\text{gt}(n_3, n_1)$        $\text{fof}(\text{gt}_{.3_1}, \text{axiom})$

$\text{gt}(n_4, n_2)$        $\text{fof}(\text{gt}_{.4_2}, \text{axiom})$

$\text{gt}(n_5, n_2)$        $\text{fof}(\text{gt}_{.5_2}, \text{axiom})$



```

gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

### SWV088+1.p Unsimplified proof obligation cl5\_nebula\_array\_0029

Proof obligation emerging from the array-safety verification for the cl5\_nebula program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

```
include('Axioms/SWV003+0.ax')
```

```

geq(-n135300, n0) ⇒ true    fof(cl5_nebula_array0029, conjecture)
gt(n5, n4)    fof(gt_54, axiom)
gt(n135300, n4)    fof(gt_1353004, axiom)
gt(n135300, n5)    fof(gt_1353005, axiom)
gt(n4, tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt(n5, tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt(n135300, tptp_minus1)    fof(gt_135300_tptp_minus1, axiom)
gt(n0, tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt(n1, tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt(n2, tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt(n3, tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt(n4, n0)    fof(gt_40, axiom)
gt(n5, n0)    fof(gt_50, axiom)
gt(n135300, n0)    fof(gt_1353000, axiom)
gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n135300, n1)    fof(gt_1353001, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n135300, n2)    fof(gt_1353002, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
gt(n135300, n3)    fof(gt_1353003, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

**SWV126+1.p** Unsimplified proof obligation thruster\_init\_0001

Proof obligation emerging from the init-safety verification for the thruster program. inuse-safety ensures that each sensor reading passed as an input to the Kalman filter algorithm is actually used during the computation of the output estimate.

```
include('Axioms/SWV003+0.ax')
```

```
init = init      fof(thruster_init0001, conjecture)
```

```
gt(n5, n4)      fof(gt.5_4, axiom)
```

```
gt(n4, tptp_minus_1)  fof(gt.4_tptp_minus_1, axiom)
```

```
gt(n5, tptp_minus_1)  fof(gt.5_tptp_minus_1, axiom)
```

```
gt(n0, tptp_minus_1)  fof(gt.0_tptp_minus_1, axiom)
```

```
gt(n1, tptp_minus_1)  fof(gt.1_tptp_minus_1, axiom)
```

```
gt(n2, tptp_minus_1)  fof(gt.2_tptp_minus_1, axiom)
```

```
gt(n3, tptp_minus_1)  fof(gt.3_tptp_minus_1, axiom)
```

```
gt(n4, n0)      fof(gt.4_0, axiom)
```

```
gt(n5, n0)      fof(gt.5_0, axiom)
```

```
gt(n1, n0)      fof(gt.1_0, axiom)
```

```
gt(n2, n0)      fof(gt.2_0, axiom)
```

```
gt(n3, n0)      fof(gt.3_0, axiom)
```

```
gt(n4, n1)      fof(gt.4_1, axiom)
```

```
gt(n5, n1)      fof(gt.5_1, axiom)
```

```
gt(n2, n1)      fof(gt.2_1, axiom)
```

```
gt(n3, n1)      fof(gt.3_1, axiom)
```

```
gt(n4, n2)      fof(gt.4_2, axiom)
```

```
gt(n5, n2)      fof(gt.5_2, axiom)
```

```
gt(n3, n2)      fof(gt.3_2, axiom)
```

```
gt(n4, n3)      fof(gt.4_3, axiom)
```

```
gt(n5, n3)      fof(gt.5_3, axiom)
```

```
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))      fof(finite_domain4, axiom)
```

```
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))      fof(finite_domain5, axiom)
```

```
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)      fof(finite_domain0, axiom)
```

```
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))      fof(finite_domain1, axiom)
```

```
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))      fof(finite_domain2, axiom)
```

```
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))      fof(finite_domain3, axiom)
```

```
succ(succ(succ(succ(n0)))) = n4      fof(successor4, axiom)
```

```
succ(succ(succ(succ(succ(n0)))))) = n5      fof(successor5, axiom)
```

```
succ(n0) = n1      fof(successor1, axiom)
```

```
succ(succ(n0)) = n2      fof(successor2, axiom)
```

```
succ(succ(succ(n0))) = n3      fof(successor3, axiom)
```

**SWV133+1.p** Simplified proof obligation gauss\_array\_0003

Proof obligation emerging from the array-safety verification for the gauss program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

```
include('Axioms/SWV003+0.ax')
```

```
(¬ a_select2(s.values7, pv_1325) ≤ a_select2(s.values7, s.worst7) and n0 ≤ s.best7 and n0 ≤ s.sworst7 and n0 ≤ s.worst7 and n2  
pv_1325 and s.best7 ≤ n3 and s.sworst7 ≤ n3 and s.worst7 ≤ n3 and pv_1325 ≤ n3 and a_select2(s.values7, pv_1325) ≤  
a_select2(s.values7, s.best7)) ⇒ n0 ≤ pv_1325      fof(gauss_array0003, conjecture)
```

```
gt(n5, n4)      fof(gt.5_4, axiom)
```

```
gt(n4, tptp_minus_1)  fof(gt.4_tptp_minus_1, axiom)
```

```
gt(n5, tptp_minus_1)  fof(gt.5_tptp_minus_1, axiom)
```

```
gt(n0, tptp_minus_1)  fof(gt.0_tptp_minus_1, axiom)
```

```
gt(n1, tptp_minus_1)  fof(gt.1_tptp_minus_1, axiom)
```

```
gt(n2, tptp_minus_1)  fof(gt.2_tptp_minus_1, axiom)
```

```
gt(n3, tptp_minus_1)  fof(gt.3_tptp_minus_1, axiom)
```

```
gt(n4, n0)      fof(gt.4_0, axiom)
```

```
gt(n5, n0)      fof(gt.5_0, axiom)
```

```
gt(n1, n0)      fof(gt.1_0, axiom)
```

```
gt(n2, n0)      fof(gt.2_0, axiom)
```

```
gt(n3, n0)      fof(gt.3_0, axiom)
```

```
gt(n4, n1)      fof(gt.4_1, axiom)
```

```
gt(n5, n1)      fof(gt.5_1, axiom)
```

```

gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

### SWV134+1.p Simplified proof obligation gauss\_array\_0004

Proof obligation emerging from the array-safety verification for the gauss program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

```
include('Axioms/SWV003+0.ax')
```

```
(¬ a_select2(s_values7, pv_1325) ≤ a_select2(s_values7, s_worst7) and n0 ≤ s_best7 and n0 ≤ s_sworst7 and n0 ≤ s_worst7 and n2
pv_1325 and s_best7 ≤ n3 and s_sworst7 ≤ n3 and s_worst7 ≤ n3 and pv_1325 ≤ n3 and a_select2(s_values7, pv_1325) ≤
a_select2(s_values7, s_best7) and a_select2(s_values7, pv_1325) ≤ a_select2(s_values7, s_sworst7)) ⇒ n0 ≤ pv_1325    fof(gauss_ar
```

```

gt(n5, n4)    fof(gt_54, axiom)
gt(n4, tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt(n5, tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt(n0, tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt(n1, tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt(n2, tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt(n3, tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt(n4, n0)    fof(gt_40, axiom)
gt(n5, n0)    fof(gt_50, axiom)
gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

### SWV135+1.p Simplified proof obligation gauss\_array\_0005

Proof obligation emerging from the array-safety verification for the gauss program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq s\_best_7 \text{ and } n_0 \leq s\_sworst_7 \text{ and } n_0 \leq s\_worst_7 \text{ and } n_2 \leq pv_{1325} \text{ and } s\_best_7 \leq n_3 \text{ and } s\_sworst_7 \leq n_3 \text{ and } s\_worst_7 \leq n_3 \text{ and } pv_{1325} \leq n_3) \Rightarrow n_0 \leq pv_{1325}$     fof(gauss\_array0005, conjecture)

gt( $n_5, n_4$ )    fof(gt\_5\_4, axiom)

gt( $n_4, tptp\_minus_1$ )    fof(gt\_4\_tptp\_minus\_1, axiom)

gt( $n_5, tptp\_minus_1$ )    fof(gt\_5\_tptp\_minus\_1, axiom)

gt( $n_0, tptp\_minus_1$ )    fof(gt\_0\_tptp\_minus\_1, axiom)

gt( $n_1, tptp\_minus_1$ )    fof(gt\_1\_tptp\_minus\_1, axiom)

gt( $n_2, tptp\_minus_1$ )    fof(gt\_2\_tptp\_minus\_1, axiom)

gt( $n_3, tptp\_minus_1$ )    fof(gt\_3\_tptp\_minus\_1, axiom)

gt( $n_4, n_0$ )    fof(gt\_4\_0, axiom)

gt( $n_5, n_0$ )    fof(gt\_5\_0, axiom)

gt( $n_1, n_0$ )    fof(gt\_1\_0, axiom)

gt( $n_2, n_0$ )    fof(gt\_2\_0, axiom)

gt( $n_3, n_0$ )    fof(gt\_3\_0, axiom)

gt( $n_4, n_1$ )    fof(gt\_4\_1, axiom)

gt( $n_5, n_1$ )    fof(gt\_5\_1, axiom)

gt( $n_2, n_1$ )    fof(gt\_2\_1, axiom)

gt( $n_3, n_1$ )    fof(gt\_3\_1, axiom)

gt( $n_4, n_2$ )    fof(gt\_4\_2, axiom)

gt( $n_5, n_2$ )    fof(gt\_5\_2, axiom)

gt( $n_3, n_2$ )    fof(gt\_3\_2, axiom)

gt( $n_4, n_3$ )    fof(gt\_4\_3, axiom)

gt( $n_5, n_3$ )    fof(gt\_5\_3, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$     fof(finite\_domain4, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$     fof(finite\_domain5, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$     fof(finite\_domain0, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$     fof(finite\_domain1, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$     fof(finite\_domain2, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$     fof(finite\_domain3, axiom)

succ(succ(succ(succ( $n_0$ )))) =  $n_4$     fof(successor4, axiom)

succ(succ(succ(succ(succ( $n_0$ )))))) =  $n_5$     fof(successor5, axiom)

succ( $n_0$ ) =  $n_1$     fof(successor1, axiom)

succ(succ( $n_0$ )) =  $n_2$     fof(successor2, axiom)

succ(succ(succ( $n_0$ ))) =  $n_3$     fof(successor3, axiom)

**SWV136+1.p** Simplified proof obligation gauss\_array\_0006

Proof obligation emerging from the array-safety verification for the gauss program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq s\_best_7 \text{ and } n_0 \leq s\_sworst_7 \text{ and } n_0 \leq s\_worst_7 \text{ and } n_2 \leq pv_{1325} \text{ and } s\_best_7 \leq n_3 \text{ and } s\_sworst_7 \leq n_3 \text{ and } s\_worst_7 \leq n_3 \text{ and } pv_{1325} \leq n_3 \text{ and } a\_select_2(s\_values_7, pv_{1325}) \leq a\_select_2(s\_values_7, s\_best_7)) \Rightarrow n_0 \leq pv_{1325}$     fof(gauss\_array0006, conjecture)

gt( $n_5, n_4$ )    fof(gt\_5\_4, axiom)

gt( $n_4, tptp\_minus_1$ )    fof(gt\_4\_tptp\_minus\_1, axiom)

gt( $n_5, tptp\_minus_1$ )    fof(gt\_5\_tptp\_minus\_1, axiom)

gt( $n_0, tptp\_minus_1$ )    fof(gt\_0\_tptp\_minus\_1, axiom)

gt( $n_1, tptp\_minus_1$ )    fof(gt\_1\_tptp\_minus\_1, axiom)

gt( $n_2, tptp\_minus_1$ )    fof(gt\_2\_tptp\_minus\_1, axiom)

gt( $n_3, tptp\_minus_1$ )    fof(gt\_3\_tptp\_minus\_1, axiom)

gt( $n_4, n_0$ )    fof(gt\_4\_0, axiom)

gt( $n_5, n_0$ )    fof(gt\_5\_0, axiom)

gt( $n_1, n_0$ )    fof(gt\_1\_0, axiom)

gt( $n_2, n_0$ )    fof(gt\_2\_0, axiom)

gt( $n_3, n_0$ )    fof(gt\_3\_0, axiom)

gt( $n_4, n_1$ )    fof(gt\_4\_1, axiom)

gt( $n_5, n_1$ )    fof(gt\_5\_1, axiom)

gt( $n_2, n_1$ )    fof(gt\_2\_1, axiom)

gt( $n_3, n_1$ )    fof(gt\_3\_1, axiom)

```

gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

### SWV137+1.p Simplified proof obligation gauss\_array\_0007

Proof obligation emerging from the array-safety verification for the gauss program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

```
include('Axioms/SWV003+0.ax')
```

```

(n0 ≤ s.best7 and n0 ≤ s.sworst7 and n0 ≤ s.worst7 and n2 ≤ pv_1325 and s.best7 ≤ n3 and s.sworst7 ≤ n3 and s.worst7 ≤ n3 and pv_1325 ≤ n3 and a.select2(s.values7, pv_1325) ≤ a.select2(s.values7, s.best7) and a.select2(s.values7, pv_1325) ≤ a.select2(s.values7, s.worst7)) ⇒ n0 ≤ pv_1325    fof(gauss_array0007, conjecture)

```

```

gt(n5, n4)    fof(gt_54, axiom)
gt(n4, tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt(n5, tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt(n0, tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt(n1, tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt(n2, tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt(n3, tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt(n4, n0)    fof(gt_40, axiom)
gt(n5, n0)    fof(gt_50, axiom)
gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

### SWV138+1.p Simplified proof obligation gauss\_array\_0008

Proof obligation emerging from the array-safety verification for the gauss program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$(n_0 \leq s\_best_7 \text{ and } n_0 \leq s\_sworst_7 \text{ and } n_0 \leq s\_worst_7 \text{ and } n_2 \leq pv_{1325} \text{ and } s\_best_7 \leq n_3 \text{ and } s\_sworst_7 \leq n_3 \text{ and } s\_worst_7 \leq n_3 \text{ and } pv_{1325} \leq n_3 \text{ and } gt(a\_select_2(s\_values_7, pv_{1325}), a\_select_2(s\_values_7, s\_best_7))) \Rightarrow n_0 \leq pv_{1325}$       fof(gauss\_array0008,

gt( $n_5, n_4$ )      fof(gt.5<sub>4</sub>, axiom)

gt( $n_4, tptp\_minus_1$ )      fof(gt.4\_tptp\_minus\_1, axiom)

gt( $n_5, tptp\_minus_1$ )      fof(gt.5\_tptp\_minus\_1, axiom)

gt( $n_0, tptp\_minus_1$ )      fof(gt.0\_tptp\_minus\_1, axiom)

gt( $n_1, tptp\_minus_1$ )      fof(gt.1\_tptp\_minus\_1, axiom)

gt( $n_2, tptp\_minus_1$ )      fof(gt.2\_tptp\_minus\_1, axiom)

gt( $n_3, tptp\_minus_1$ )      fof(gt.3\_tptp\_minus\_1, axiom)

gt( $n_4, n_0$ )      fof(gt.4<sub>0</sub>, axiom)

gt( $n_5, n_0$ )      fof(gt.5<sub>0</sub>, axiom)

gt( $n_1, n_0$ )      fof(gt.1<sub>0</sub>, axiom)

gt( $n_2, n_0$ )      fof(gt.2<sub>0</sub>, axiom)

gt( $n_3, n_0$ )      fof(gt.3<sub>0</sub>, axiom)

gt( $n_4, n_1$ )      fof(gt.4<sub>1</sub>, axiom)

gt( $n_5, n_1$ )      fof(gt.5<sub>1</sub>, axiom)

gt( $n_2, n_1$ )      fof(gt.2<sub>1</sub>, axiom)

gt( $n_3, n_1$ )      fof(gt.3<sub>1</sub>, axiom)

gt( $n_4, n_2$ )      fof(gt.4<sub>2</sub>, axiom)

gt( $n_5, n_2$ )      fof(gt.5<sub>2</sub>, axiom)

gt( $n_3, n_2$ )      fof(gt.3<sub>2</sub>, axiom)

gt( $n_4, n_3$ )      fof(gt.4<sub>3</sub>, axiom)

gt( $n_5, n_3$ )      fof(gt.5<sub>3</sub>, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$       fof(finite\_domain<sub>4</sub>, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$       fof(finite\_domain<sub>5</sub>, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$       fof(finite\_domain<sub>0</sub>, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$       fof(finite\_domain<sub>1</sub>, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$       fof(finite\_domain<sub>2</sub>, axiom)

$\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$       fof(finite\_domain<sub>3</sub>, axiom)

succ(succ(succ(succ( $n_0$ )))) =  $n_4$       fof(successor<sub>4</sub>, axiom)

succ(succ(succ(succ(succ( $n_0$ )))))) =  $n_5$       fof(successor<sub>5</sub>, axiom)

succ( $n_0$ ) =  $n_1$       fof(successor<sub>1</sub>, axiom)

succ(succ( $n_0$ )) =  $n_2$       fof(successor<sub>2</sub>, axiom)

succ(succ(succ( $n_0$ ))) =  $n_3$       fof(successor<sub>3</sub>, axiom)

**SWV145+1.p** Simplified proof obligation gauss\_array\_0015

Proof obligation emerging from the array-safety verification for the gauss program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$\neg tptp\_float\_0_{001} \leq tptp\_float\_0_{001} \Rightarrow n_0 \leq s\_best_7$       fof(gauss\_array0015, conjecture)

gt( $n_5, n_4$ )      fof(gt.5<sub>4</sub>, axiom)

gt( $n_4, tptp\_minus_1$ )      fof(gt.4\_tptp\_minus\_1, axiom)

gt( $n_5, tptp\_minus_1$ )      fof(gt.5\_tptp\_minus\_1, axiom)

gt( $n_0, tptp\_minus_1$ )      fof(gt.0\_tptp\_minus\_1, axiom)

gt( $n_1, tptp\_minus_1$ )      fof(gt.1\_tptp\_minus\_1, axiom)

gt( $n_2, tptp\_minus_1$ )      fof(gt.2\_tptp\_minus\_1, axiom)

gt( $n_3, tptp\_minus_1$ )      fof(gt.3\_tptp\_minus\_1, axiom)

gt( $n_4, n_0$ )      fof(gt.4<sub>0</sub>, axiom)

gt( $n_5, n_0$ )      fof(gt.5<sub>0</sub>, axiom)

gt( $n_1, n_0$ )      fof(gt.1<sub>0</sub>, axiom)

gt( $n_2, n_0$ )      fof(gt.2<sub>0</sub>, axiom)

gt( $n_3, n_0$ )      fof(gt.3<sub>0</sub>, axiom)

gt( $n_4, n_1$ )      fof(gt.4<sub>1</sub>, axiom)

gt( $n_5, n_1$ )      fof(gt.5<sub>1</sub>, axiom)

gt( $n_2, n_1$ )      fof(gt.2<sub>1</sub>, axiom)

gt( $n_3, n_1$ )      fof(gt.3<sub>1</sub>, axiom)

gt( $n_4, n_2$ )      fof(gt.4<sub>2</sub>, axiom)

gt( $n_5, n_2$ )      fof(gt.5<sub>2</sub>, axiom)

gt( $n_3, n_2$ )      fof(gt.3<sub>2</sub>, axiom)

```

gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

### SWV146+1.p Simplified proof obligation gauss\_array\_0016

Proof obligation emerging from the array-safety verification for the gauss program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

```
include('Axioms/SWV003+0.ax')
```

```
¬ tptp_float_0001 ≤ tptp_float_0001 ⇒ n0 ≤ s_worst7    fof(gauss_array0016, conjecture)
```

```

gt(n5, n4)    fof(gt_54, axiom)
gt(n4, tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt(n5, tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt(n0, tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt(n1, tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt(n2, tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt(n3, tptp_minus1)    fof(gt_3_tptp_minus1, axiom)

```

```

gt(n4, n0)    fof(gt_40, axiom)
gt(n5, n0)    fof(gt_50, axiom)
gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)

```

```

∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

### SWV147+1.p Simplified proof obligation gauss\_array\_0017

Proof obligation emerging from the array-safety verification for the gauss program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

```
include('Axioms/SWV003+0.ax')
```

```
¬ tptp_float_0001 ≤ tptp_float_0001 ⇒ n0 ≤ s_worst7    fof(gauss_array0017, conjecture)
```

```

gt(n5, n4)    fof(gt_54, axiom)
gt(n4, tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt(n5, tptp_minus1)    fof(gt_5_tptp_minus1, axiom)

```

```

gt( $n_0$ , tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt( $n_1$ , tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt( $n_2$ , tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt( $n_3$ , tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt( $n_4$ ,  $n_0$ )           fof(gt_40, axiom)
gt( $n_5$ ,  $n_0$ )           fof(gt_50, axiom)
gt( $n_1$ ,  $n_0$ )           fof(gt_10, axiom)
gt( $n_2$ ,  $n_0$ )           fof(gt_20, axiom)
gt( $n_3$ ,  $n_0$ )           fof(gt_30, axiom)
gt( $n_4$ ,  $n_1$ )           fof(gt_41, axiom)
gt( $n_5$ ,  $n_1$ )           fof(gt_51, axiom)
gt( $n_2$ ,  $n_1$ )           fof(gt_21, axiom)
gt( $n_3$ ,  $n_1$ )           fof(gt_31, axiom)
gt( $n_4$ ,  $n_2$ )           fof(gt_42, axiom)
gt( $n_5$ ,  $n_2$ )           fof(gt_52, axiom)
gt( $n_3$ ,  $n_2$ )           fof(gt_32, axiom)
gt( $n_4$ ,  $n_3$ )           fof(gt_43, axiom)
gt( $n_5$ ,  $n_3$ )           fof(gt_53, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$     fof(finite_domain4, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$     fof(finite_domain5, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$     fof(finite_domain0, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$     fof(finite_domain1, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$     fof(finite_domain2, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$     fof(finite_domain3, axiom)
succ(succ(succ(succ( $n_0$ )))) =  $n_4$     fof(successor4, axiom)
succ(succ(succ(succ(succ( $n_0$ )))))) =  $n_5$     fof(successor5, axiom)
succ( $n_0$ ) =  $n_1$     fof(successor1, axiom)
succ(succ( $n_0$ )) =  $n_2$     fof(successor2, axiom)
succ(succ(succ( $n_0$ ))) =  $n_3$     fof(successor3, axiom)

```

### SWV148+1.p Simplified proof obligation gauss\_array\_0018

Proof obligation emerging from the array-safety verification for the gauss program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

```

include('Axioms/SWV003+0.ax')
 $\neg \text{tptp\_float}_{0001} \leq \text{tptp\_float}_{0001} \Rightarrow s\_best_7 \leq n_3$     fof(gauss_array0018, conjecture)
gt( $n_5$ ,  $n_4$ )           fof(gt_54, axiom)
gt( $n_4$ , tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt( $n_5$ , tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt( $n_0$ , tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt( $n_1$ , tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt( $n_2$ , tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt( $n_3$ , tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt( $n_4$ ,  $n_0$ )           fof(gt_40, axiom)
gt( $n_5$ ,  $n_0$ )           fof(gt_50, axiom)
gt( $n_1$ ,  $n_0$ )           fof(gt_10, axiom)
gt( $n_2$ ,  $n_0$ )           fof(gt_20, axiom)
gt( $n_3$ ,  $n_0$ )           fof(gt_30, axiom)
gt( $n_4$ ,  $n_1$ )           fof(gt_41, axiom)
gt( $n_5$ ,  $n_1$ )           fof(gt_51, axiom)
gt( $n_2$ ,  $n_1$ )           fof(gt_21, axiom)
gt( $n_3$ ,  $n_1$ )           fof(gt_31, axiom)
gt( $n_4$ ,  $n_2$ )           fof(gt_42, axiom)
gt( $n_5$ ,  $n_2$ )           fof(gt_52, axiom)
gt( $n_3$ ,  $n_2$ )           fof(gt_32, axiom)
gt( $n_4$ ,  $n_3$ )           fof(gt_43, axiom)
gt( $n_5$ ,  $n_3$ )           fof(gt_53, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$     fof(finite_domain4, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$     fof(finite_domain5, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$     fof(finite_domain0, axiom)
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$     fof(finite_domain1, axiom)

```



$\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2)) \quad \text{fof}(\text{finite\_domain}_2, \text{axiom})$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3)) \quad \text{fof}(\text{finite\_domain}_3, \text{axiom})$   
 $\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))) = n_4 \quad \text{fof}(\text{successor}_4, \text{axiom})$   
 $\text{succ}(\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))))) = n_5 \quad \text{fof}(\text{successor}_5, \text{axiom})$   
 $\text{succ}(n_0) = n_1 \quad \text{fof}(\text{successor}_1, \text{axiom})$   
 $\text{succ}(\text{succ}(n_0)) = n_2 \quad \text{fof}(\text{successor}_2, \text{axiom})$   
 $\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3 \quad \text{fof}(\text{successor}_3, \text{axiom})$

### SWV149+1.p Simplified proof obligation gauss\_array\_0019

Proof obligation emerging from the array-safety verification for the gauss program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$\neg \text{tptp\_float\_0}_{001} \leq \text{tptp\_float\_0}_{001} \Rightarrow \text{s\_sworst}_7 \leq n_3 \quad \text{fof}(\text{gauss\_array}_{0019}, \text{conjecture})$

$\text{gt}(n_5, n_4) \quad \text{fof}(\text{gt}_{.5}_4, \text{axiom})$   
 $\text{gt}(n_4, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.4\_tptp\_minus}_1, \text{axiom})$   
 $\text{gt}(n_5, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.5\_tptp\_minus}_1, \text{axiom})$   
 $\text{gt}(n_0, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.0\_tptp\_minus}_1, \text{axiom})$   
 $\text{gt}(n_1, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.1\_tptp\_minus}_1, \text{axiom})$   
 $\text{gt}(n_2, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.2\_tptp\_minus}_1, \text{axiom})$   
 $\text{gt}(n_3, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.3\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_4, n_0) \quad \text{fof}(\text{gt}_{.4}_0, \text{axiom})$   
 $\text{gt}(n_5, n_0) \quad \text{fof}(\text{gt}_{.5}_0, \text{axiom})$   
 $\text{gt}(n_1, n_0) \quad \text{fof}(\text{gt}_{.1}_0, \text{axiom})$   
 $\text{gt}(n_2, n_0) \quad \text{fof}(\text{gt}_{.2}_0, \text{axiom})$   
 $\text{gt}(n_3, n_0) \quad \text{fof}(\text{gt}_{.3}_0, \text{axiom})$   
 $\text{gt}(n_4, n_1) \quad \text{fof}(\text{gt}_{.4}_1, \text{axiom})$   
 $\text{gt}(n_5, n_1) \quad \text{fof}(\text{gt}_{.5}_1, \text{axiom})$   
 $\text{gt}(n_2, n_1) \quad \text{fof}(\text{gt}_{.2}_1, \text{axiom})$   
 $\text{gt}(n_3, n_1) \quad \text{fof}(\text{gt}_{.3}_1, \text{axiom})$   
 $\text{gt}(n_4, n_2) \quad \text{fof}(\text{gt}_{.4}_2, \text{axiom})$   
 $\text{gt}(n_5, n_2) \quad \text{fof}(\text{gt}_{.5}_2, \text{axiom})$   
 $\text{gt}(n_3, n_2) \quad \text{fof}(\text{gt}_{.3}_2, \text{axiom})$   
 $\text{gt}(n_4, n_3) \quad \text{fof}(\text{gt}_{.4}_3, \text{axiom})$   
 $\text{gt}(n_5, n_3) \quad \text{fof}(\text{gt}_{.5}_3, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4)) \quad \text{fof}(\text{finite\_domain}_4, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5)) \quad \text{fof}(\text{finite\_domain}_5, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0) \quad \text{fof}(\text{finite\_domain}_0, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1)) \quad \text{fof}(\text{finite\_domain}_1, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2)) \quad \text{fof}(\text{finite\_domain}_2, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3)) \quad \text{fof}(\text{finite\_domain}_3, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))) = n_4 \quad \text{fof}(\text{successor}_4, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))))) = n_5 \quad \text{fof}(\text{successor}_5, \text{axiom})$

$\text{succ}(n_0) = n_1 \quad \text{fof}(\text{successor}_1, \text{axiom})$

$\text{succ}(\text{succ}(n_0)) = n_2 \quad \text{fof}(\text{successor}_2, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3 \quad \text{fof}(\text{successor}_3, \text{axiom})$

### SWV150+1.p Simplified proof obligation gauss\_array\_0020

Proof obligation emerging from the array-safety verification for the gauss program. array-safety ensures that each access to an array element is within the specified upper and lower bounds of the array.

include('Axioms/SWV003+0.ax')

$\neg \text{tptp\_float\_0}_{001} \leq \text{tptp\_float\_0}_{001} \Rightarrow \text{s\_worst}_7 \leq n_3 \quad \text{fof}(\text{gauss\_array}_{0020}, \text{conjecture})$

$\text{gt}(n_5, n_4) \quad \text{fof}(\text{gt}_{.5}_4, \text{axiom})$   
 $\text{gt}(n_4, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.4\_tptp\_minus}_1, \text{axiom})$   
 $\text{gt}(n_5, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.5\_tptp\_minus}_1, \text{axiom})$   
 $\text{gt}(n_0, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.0\_tptp\_minus}_1, \text{axiom})$   
 $\text{gt}(n_1, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.1\_tptp\_minus}_1, \text{axiom})$   
 $\text{gt}(n_2, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.2\_tptp\_minus}_1, \text{axiom})$   
 $\text{gt}(n_3, \text{tptp\_minus}_1) \quad \text{fof}(\text{gt}_{.3\_tptp\_minus}_1, \text{axiom})$   
 $\text{gt}(n_4, n_0) \quad \text{fof}(\text{gt}_{.4}_0, \text{axiom})$   
 $\text{gt}(n_5, n_0) \quad \text{fof}(\text{gt}_{.5}_0, \text{axiom})$

```

gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)
succ(succ(succ(n0))) = n3    fof(successor3, axiom)

```

### SWV151+1.p Simplified proof obligation cl5\_nebula\_norm\_0001

Proof obligation emerging from the norm-safety verification for the cl5\_nebula program. norm-safety ensures that the contents of certain one-dimensional arrays add up to one.

```
include('Axioms/SWV003+0.ax')
```

```

∀a: ((n0 ≤ a and a ≤ tptp_minus1) ⇒ n0+n4=a.select3(q, a, tptp_sum_index) = n1)    fof(cl5_nebula_norm0001, conjecture)
gt(n5, n4)    fof(gt_54, axiom)
gt(n4, tptp_minus1)    fof(gt_4_tptp_minus1, axiom)
gt(n5, tptp_minus1)    fof(gt_5_tptp_minus1, axiom)
gt(n0, tptp_minus1)    fof(gt_0_tptp_minus1, axiom)
gt(n1, tptp_minus1)    fof(gt_1_tptp_minus1, axiom)
gt(n2, tptp_minus1)    fof(gt_2_tptp_minus1, axiom)
gt(n3, tptp_minus1)    fof(gt_3_tptp_minus1, axiom)
gt(n4, n0)    fof(gt_40, axiom)
gt(n5, n0)    fof(gt_50, axiom)
gt(n1, n0)    fof(gt_10, axiom)
gt(n2, n0)    fof(gt_20, axiom)
gt(n3, n0)    fof(gt_30, axiom)
gt(n4, n1)    fof(gt_41, axiom)
gt(n5, n1)    fof(gt_51, axiom)
gt(n2, n1)    fof(gt_21, axiom)
gt(n3, n1)    fof(gt_31, axiom)
gt(n4, n2)    fof(gt_42, axiom)
gt(n5, n2)    fof(gt_52, axiom)
gt(n3, n2)    fof(gt_32, axiom)
gt(n4, n3)    fof(gt_43, axiom)
gt(n5, n3)    fof(gt_53, axiom)
∀x: ((n0 ≤ x and x ≤ n4) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4))    fof(finite_domain4, axiom)
∀x: ((n0 ≤ x and x ≤ n5) ⇒ (x = n0 or x = n1 or x = n2 or x = n3 or x = n4 or x = n5))    fof(finite_domain5, axiom)
∀x: ((n0 ≤ x and x ≤ n0) ⇒ x = n0)    fof(finite_domain0, axiom)
∀x: ((n0 ≤ x and x ≤ n1) ⇒ (x = n0 or x = n1))    fof(finite_domain1, axiom)
∀x: ((n0 ≤ x and x ≤ n2) ⇒ (x = n0 or x = n1 or x = n2))    fof(finite_domain2, axiom)
∀x: ((n0 ≤ x and x ≤ n3) ⇒ (x = n0 or x = n1 or x = n2 or x = n3))    fof(finite_domain3, axiom)
succ(succ(succ(succ(n0)))) = n4    fof(successor4, axiom)
succ(succ(succ(succ(succ(n0)))))) = n5    fof(successor5, axiom)
succ(n0) = n1    fof(successor1, axiom)
succ(succ(n0)) = n2    fof(successor2, axiom)

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$\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3$      $\text{fof}(\text{successor}_3, \text{axiom})$

**SWV152+1.p** Simplified proof obligation cl5\_nebula\_norm\_0002

Proof obligation emerging from the norm-safety verification for the cl5\_nebula program. norm-safety ensures that the contents of certain one-dimensional arrays add up to one.

$\text{include}('Axioms/SWV003+0.ax')$

$\forall a: ((n_0 \leq a \text{ and } a \leq \text{tptp\_minus}_1) \Rightarrow n_0 + n_4 = a \cdot \text{select}_3(q, a, \text{tptp\_sum\_index}) = n_1)$      $\text{fof}(\text{cl5\_nebula\_norm}_{0002}, \text{conjecture})$

$\text{gt}(n_5, n_4)$      $\text{fof}(\text{gt}_{.5_4}, \text{axiom})$

$\text{gt}(n_4, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.4\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_5, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.5\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_0, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.0\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_1, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.1\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_2, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.2\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_3, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.3\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_4, n_0)$      $\text{fof}(\text{gt}_{.4_0}, \text{axiom})$

$\text{gt}(n_5, n_0)$      $\text{fof}(\text{gt}_{.5_0}, \text{axiom})$

$\text{gt}(n_1, n_0)$      $\text{fof}(\text{gt}_{.1_0}, \text{axiom})$

$\text{gt}(n_2, n_0)$      $\text{fof}(\text{gt}_{.2_0}, \text{axiom})$

$\text{gt}(n_3, n_0)$      $\text{fof}(\text{gt}_{.3_0}, \text{axiom})$

$\text{gt}(n_4, n_1)$      $\text{fof}(\text{gt}_{.4_1}, \text{axiom})$

$\text{gt}(n_5, n_1)$      $\text{fof}(\text{gt}_{.5_1}, \text{axiom})$

$\text{gt}(n_2, n_1)$      $\text{fof}(\text{gt}_{.2_1}, \text{axiom})$

$\text{gt}(n_3, n_1)$      $\text{fof}(\text{gt}_{.3_1}, \text{axiom})$

$\text{gt}(n_4, n_2)$      $\text{fof}(\text{gt}_{.4_2}, \text{axiom})$

$\text{gt}(n_5, n_2)$      $\text{fof}(\text{gt}_{.5_2}, \text{axiom})$

$\text{gt}(n_3, n_2)$      $\text{fof}(\text{gt}_{.3_2}, \text{axiom})$

$\text{gt}(n_4, n_3)$      $\text{fof}(\text{gt}_{.4_3}, \text{axiom})$

$\text{gt}(n_5, n_3)$      $\text{fof}(\text{gt}_{.5_3}, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$      $\text{fof}(\text{finite\_domain}_4, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$      $\text{fof}(\text{finite\_domain}_5, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$      $\text{fof}(\text{finite\_domain}_0, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$      $\text{fof}(\text{finite\_domain}_1, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$      $\text{fof}(\text{finite\_domain}_2, \text{axiom})$

$\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$      $\text{fof}(\text{finite\_domain}_3, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))) = n_4$      $\text{fof}(\text{successor}_4, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(\text{succ}(\text{succ}(n_0)))))) = n_5$      $\text{fof}(\text{successor}_5, \text{axiom})$

$\text{succ}(n_0) = n_1$      $\text{fof}(\text{successor}_1, \text{axiom})$

$\text{succ}(\text{succ}(n_0)) = n_2$      $\text{fof}(\text{successor}_2, \text{axiom})$

$\text{succ}(\text{succ}(\text{succ}(n_0))) = n_3$      $\text{fof}(\text{successor}_3, \text{axiom})$

**SWV165+1.p** Simplified proof obligation cl5\_nebula\_init\_0001

Proof obligation emerging from the init-safety verification for the cl5\_nebula program. init-safety ensures that each variable or individual array element has been assigned a defined value before it is used.

$\text{include}('Axioms/SWV003+0.ax')$

$\forall a: ((n_0 \leq a \text{ and } a \leq \text{tptp\_minus}_1) \Rightarrow \text{uninit} = \text{init})$      $\text{fof}(\text{cl5\_nebula\_init}_{0001}, \text{conjecture})$

$\text{gt}(n_5, n_4)$      $\text{fof}(\text{gt}_{.5_4}, \text{axiom})$

$\text{gt}(n_4, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.4\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_5, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.5\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_0, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.0\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_1, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.1\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_2, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.2\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_3, \text{tptp\_minus}_1)$      $\text{fof}(\text{gt}_{.3\_tptp\_minus}_1, \text{axiom})$

$\text{gt}(n_4, n_0)$      $\text{fof}(\text{gt}_{.4_0}, \text{axiom})$

$\text{gt}(n_5, n_0)$      $\text{fof}(\text{gt}_{.5_0}, \text{axiom})$

$\text{gt}(n_1, n_0)$      $\text{fof}(\text{gt}_{.1_0}, \text{axiom})$

$\text{gt}(n_2, n_0)$      $\text{fof}(\text{gt}_{.2_0}, \text{axiom})$

$\text{gt}(n_3, n_0)$      $\text{fof}(\text{gt}_{.3_0}, \text{axiom})$

$\text{gt}(n_4, n_1)$      $\text{fof}(\text{gt}_{.4_1}, \text{axiom})$

$\text{gt}(n_5, n_1)$      $\text{fof}(\text{gt}_{.5_1}, \text{axiom})$

$\text{gt}(n_2, n_1)$      $\text{fof}(\text{gt}_{.2_1}, \text{axiom})$

$gt(n_3, n_1)$      $fof(gt\_3_1, axiom)$   
 $gt(n_4, n_2)$      $fof(gt\_4_2, axiom)$   
 $gt(n_5, n_2)$      $fof(gt\_5_2, axiom)$   
 $gt(n_3, n_2)$      $fof(gt\_3_2, axiom)$   
 $gt(n_4, n_3)$      $fof(gt\_4_3, axiom)$   
 $gt(n_5, n_3)$      $fof(gt\_5_3, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$      $fof(finite\_domain_4, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$      $fof(finite\_domain_5, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$      $fof(finite\_domain_0, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$      $fof(finite\_domain_1, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$      $fof(finite\_domain_2, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$      $fof(finite\_domain_3, axiom)$   
 $succ(succ(succ(succ(n_0)))) = n_4$      $fof(successor_4, axiom)$   
 $succ(succ(succ(succ(succ(n_0)))))) = n_5$      $fof(successor_5, axiom)$   
 $succ(n_0) = n_1$      $fof(successor_1, axiom)$   
 $succ(succ(n_0)) = n_2$      $fof(successor_2, axiom)$   
 $succ(succ(succ(n_0))) = n_3$      $fof(successor_3, axiom)$

### SWV189+1.p Simplified proof obligation cl5\_nebula\_init\_0121

Proof obligation emerging from the init-safety verification for the cl5\_nebula program. init-safety ensures that each variable or individual array element has been assigned a defined value before it is used.

`include('Axioms/SWV003+0.ax')`

$\forall a: ((n_0 \leq a \text{ and } a \leq n_4) \Rightarrow a\_select_3(center\_init, a, n_0) = init) \Rightarrow \forall b: ((n_0 \leq b \text{ and } b \leq tptp\_minus_1) \Rightarrow$   
 $\forall c: ((n_0 \leq c \text{ and } c \leq n_4) \Rightarrow a\_select_3(q\_init, b, c) = init))$      $fof(cl5\_nebula\_init_{0121}, conjecture)$

$gt(n_5, n_4)$      $fof(gt\_5_4, axiom)$   
 $gt(n_4, tptp\_minus_1)$      $fof(gt\_4\_tptp\_minus_1, axiom)$   
 $gt(n_5, tptp\_minus_1)$      $fof(gt\_5\_tptp\_minus_1, axiom)$   
 $gt(n_0, tptp\_minus_1)$      $fof(gt\_0\_tptp\_minus_1, axiom)$   
 $gt(n_1, tptp\_minus_1)$      $fof(gt\_1\_tptp\_minus_1, axiom)$   
 $gt(n_2, tptp\_minus_1)$      $fof(gt\_2\_tptp\_minus_1, axiom)$   
 $gt(n_3, tptp\_minus_1)$      $fof(gt\_3\_tptp\_minus_1, axiom)$   
 $gt(n_4, n_0)$      $fof(gt\_4_0, axiom)$   
 $gt(n_5, n_0)$      $fof(gt\_5_0, axiom)$   
 $gt(n_1, n_0)$      $fof(gt\_1_0, axiom)$   
 $gt(n_2, n_0)$      $fof(gt\_2_0, axiom)$   
 $gt(n_3, n_0)$      $fof(gt\_3_0, axiom)$   
 $gt(n_4, n_1)$      $fof(gt\_4_1, axiom)$   
 $gt(n_5, n_1)$      $fof(gt\_5_1, axiom)$   
 $gt(n_2, n_1)$      $fof(gt\_2_1, axiom)$   
 $gt(n_3, n_1)$      $fof(gt\_3_1, axiom)$   
 $gt(n_4, n_2)$      $fof(gt\_4_2, axiom)$   
 $gt(n_5, n_2)$      $fof(gt\_5_2, axiom)$   
 $gt(n_3, n_2)$      $fof(gt\_3_2, axiom)$   
 $gt(n_4, n_3)$      $fof(gt\_4_3, axiom)$   
 $gt(n_5, n_3)$      $fof(gt\_5_3, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_4) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4))$      $fof(finite\_domain_4, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_5) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3 \text{ or } x = n_4 \text{ or } x = n_5))$      $fof(finite\_domain_5, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_0) \Rightarrow x = n_0)$      $fof(finite\_domain_0, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_1) \Rightarrow (x = n_0 \text{ or } x = n_1))$      $fof(finite\_domain_1, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_2) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2))$      $fof(finite\_domain_2, axiom)$   
 $\forall x: ((n_0 \leq x \text{ and } x \leq n_3) \Rightarrow (x = n_0 \text{ or } x = n_1 \text{ or } x = n_2 \text{ or } x = n_3))$      $fof(finite\_domain_3, axiom)$   
 $succ(succ(succ(succ(n_0)))) = n_4$      $fof(successor_4, axiom)$   
 $succ(succ(succ(succ(succ(n_0)))))) = n_5$      $fof(successor_5, axiom)$   
 $succ(n_0) = n_1$      $fof(successor_1, axiom)$   
 $succ(succ(n_0)) = n_2$      $fof(successor_2, axiom)$   
 $succ(succ(succ(n_0))) = n_3$      $fof(successor_3, axiom)$

### SWV233+1.p Protocol attack problem

$\forall e_1, e_2: ((knows(encrypt(e_1, e_2)) \text{ and } knows(e'_2)) \Rightarrow knows(e_1))$      $fof(encrypt\_equation, axiom)$   
 $\forall e_1, e_2: ((knows(symmetric\_encrypt(e_1, e_2)) \text{ and } knows(e_2)) \Rightarrow knows(e_1))$      $fof(symmetric\_encrypt\_equation, axiom)$

$\forall e, k: ((\text{knows}(\text{sign}(e, k')) \text{ and } \text{knows}(k)) \Rightarrow \text{knows}(e)) \quad \text{fof}(\text{sign\_equation, axiom})$   
 $\forall e_1, e_2: ((\text{knows}(e_1) \text{ and } \text{knows}(e_2)) \Rightarrow (\text{knows}(\text{concatenate}(e_1, e_2)) \text{ and } \text{knows}(\text{encrypt}(e_1, e_2)) \text{ and } \text{knows}(\text{symmetric\_encrypt}(e_1, e_2)))) \quad \text{fof}(\text{construct\_message}_1, \text{axiom})$   
 $\forall e_1, e_2: (\text{knows}(\text{concatenate}(e_1, e_2)) \Rightarrow (\text{knows}(e_1) \text{ and } \text{knows}(e_2))) \quad \text{fof}(\text{construct\_message}_2, \text{axiom})$   
 $\forall e: (\text{knows}(e) \Rightarrow (\text{knows}(\text{head}(e)) \text{ and } \text{knows}(\text{tail}(e)) \text{ and } \text{knows}(\text{hash}(e)))) \quad \text{fof}(\text{construct\_message}_3, \text{axiom})$   
 $\forall e, k: \text{decrypt}(\text{encrypt}(e, k), k) = e \quad \text{fof}(\text{decrypt\_axiom, axiom})$   
 $\forall e, k: \text{symmetric\_decrypt}(\text{symmetric\_encrypt}(e, k), k) = e \quad \text{fof}(\text{symmetric\_decrypt\_axiom, axiom})$   
 $\forall e, k: \text{extract}(\text{sign}(e, k'), k) = e \quad \text{fof}(\text{sign\_axiom, axiom})$   
 $\forall x, y: \text{head}(\text{concatenate}(x, y)) = x \quad \text{fof}(\text{head\_axiom, axiom})$   
 $\forall x, y: \text{tail}(\text{concatenate}(x, y)) = y \quad \text{fof}(\text{tail\_axiom, axiom})$   
 $\forall x: \text{first}(x) = \text{head}(x) \quad \text{fof}(\text{first\_axiom, axiom})$   
 $\forall x: \text{second}(x) = \text{head}(\text{tail}(x)) \quad \text{fof}(\text{second\_axiom, axiom})$   
 $\forall x: \text{third}(x) = \text{head}(\text{tail}(\text{tail}(x))) \quad \text{fof}(\text{third\_axiom, axiom})$   
 $\forall x: \text{fourth}(x) = \text{head}(\text{tail}(\text{tail}(\text{tail}(x)))) \quad \text{fof}(\text{fourth\_axiom, axiom})$   
 $\forall x, y: ((\text{knows}(x) \text{ and } \text{knows}(y)) \Rightarrow \text{knows}(\text{mac}(x, y))) \quad \text{fof}(\text{symmac\_axiom, axiom})$   
 $\text{knows}(k\_ca) \text{ and } \text{knows}(k\_a') \text{ and } \text{knows}(k\_a) \quad \text{fof}(\text{previous\_knowledge, axiom})$   
 $\forall \text{init}_1, \text{init}_2, \text{init}_3, \text{resp}_1, \text{resp}_2: (\text{knows}(\text{concatenate}(n, \text{concatenate}(k\_c, \text{sign}(\text{concatenate}(c, \text{concatenate}(k\_c, \text{eol})), k\_c')))) \text{ and } \text{second}(\text{extract}(\text{decrypt}(\text{resp}_1, k\_c'), \text{second}(\text{extract}(\text{resp}_2, k\_ca)))) = n) \Rightarrow \text{knows}(\text{symmetric\_encrypt}(\text{secret}, \text{first}(\text{extract}(\text{init}_2) \Rightarrow \text{knows}(\text{concatenate}(\text{encrypt}(\text{sign}(\text{concatenate}(kgen}(\text{init}_2), \text{concatenate}(\text{init}_1, \text{eol})), k\_s'), \text{init}_2), \text{sign}(\text{concatenate}(s, \text{concatenate}(k\_ca, \text{eol})), k\_c')))) \Rightarrow \text{knows}(\text{secret}) \quad \text{fof}(\text{attack, conjecture})$

### SWV234+2.p 4758 typecast attack

Mike Bond's version of a model for the 4758 typecast attack.

$\forall u, v: ((\text{public}(u) \text{ and } \text{public}(v)) \Rightarrow \text{public}(\text{xor}(u, v))) \quad \text{fof}(\text{ability\_to\_xor, axiom})$   
 $\forall u: \text{public}(u) \Rightarrow \text{public}(\text{kp}(u)) \quad \text{fof}(\text{kp\_set, axiom})$   
 $\forall u, v: ((\text{public}(u) \text{ and } \text{public}(v)) \Rightarrow \text{public}(\text{enc}(u, v))) \quad \text{fof}(\text{ability\_to\_encrypt, axiom})$   
 $\forall u, v: ((\text{public}(u) \text{ and } \text{public}(v)) \Rightarrow \text{public}(\text{enc}(u^{-1}, v))) \quad \text{fof}(\text{ability\_to\_decrypt, axiom})$   
 $\forall u, v: ((\text{public}(u) \text{ and } \text{public}(v)) \Rightarrow \text{public}(\text{enc}(\text{enc}(\text{xor}(\text{data}, \text{km})^{-1}, u), v))) \quad \text{fof}(\text{encrypt\_data\_cmd, axiom})$   
 $\forall u, v, w: ((\text{public}(v) \text{ and } \text{public}(\text{enc}(\text{xor}(u, v), w)) \text{ and } \text{public}(\text{enc}(\text{xor}(\text{km}, \text{imp}), u))) \Rightarrow \text{public}(\text{enc}(\text{xor}(\text{km}, v), w))) \quad \text{fof}(\text{key\_xor\_cancel, axiom})$   
 $\forall u, v, w: ((\text{public}(\text{kp}(v)) \text{ and } \text{public}(w) \text{ and } \text{public}(\text{enc}(\text{xor}(\text{km}, \text{kp}(v)), u))) \Rightarrow \text{public}(\text{enc}(\text{xor}(\text{km}, v), \text{xor}(u, w)))) \quad \text{fof}(\text{key\_xor\_cancel, axiom})$   
 $\forall u, v, w: \text{enc}(u, \text{enc}(u^{-1}, v)) = v \quad \text{fof}(\text{encrypt\_decrypt\_cancel, axiom})$   
 $\forall u, v, w: \text{xor}(u, v) = \text{xor}(v, u) \quad \text{fof}(\text{xor\_commutes, axiom})$   
 $\forall u, v, w: \text{xor}(u, \text{xor}(v, w)) = \text{xor}(\text{xor}(u, v), w) \quad \text{fof}(\text{xor\_associative, axiom})$   
 $\forall u, v, w: \text{xor}(u, u) = z \quad \text{fof}(\text{xor\_self\_cancel, axiom})$   
 $\forall u, v, w: \text{xor}(u, z) = u \quad \text{fof}(\text{xor\_zero, axiom})$   
 $\text{public}(\text{imp}) \quad \text{fof}(\text{initial\_knowledge}_1, \text{axiom})$   
 $\text{public}(\text{data}) \quad \text{fof}(\text{initial\_knowledge}_2, \text{axiom})$   
 $\text{public}(z) \quad \text{fof}(\text{initial\_knowledge}_3, \text{axiom})$   
 $\text{public}(\text{pin}) \quad \text{fof}(\text{initial\_knowledge}_4, \text{axiom})$   
 $\text{public}(\text{enc}(\text{xor}(\text{kek}, \text{pin}), \text{pp})) \quad \text{fof}(\text{initial\_knowledge}_5, \text{axiom})$   
 $\text{public}(k_3) \quad \text{fof}(\text{initial\_knowledge}_6, \text{axiom})$   
 $\text{public}(\text{enc}(\text{xor}(\text{km}, \text{kp}(\text{imp})), \text{xor}(\text{kek}, k_3))) \quad \text{fof}(\text{initial\_knowledge}_7, \text{axiom})$   
 $\text{public}(a) \quad \text{fof}(\text{initial\_knowledge}_8, \text{axiom})$   
 $\text{public}(\text{enc}(\text{xor}(\text{km}, \text{imp}), \text{xor}(\text{kek}, \text{xor}(\text{pin}, \text{data})))) \quad \text{fof}(\text{initial\_knowledge}_9, \text{axiom})$   
 $\text{public}(\text{enc}(\text{pp}, a)) \quad \text{fof}(\text{co}_1, \text{conjecture})$

### SWV237+1.p Visa Security Module (VSM) attack

This models the API of the Visa Security Module (VSM). The conjecture allows the discovery of Bond's attack.

$\forall u, v: \text{enc}(i(u), \text{enc}(u, v)) = v \quad \text{fof}(\text{enc\_dec\_cancel, axiom})$   
 $\forall u, v: \text{enc}(u, \text{enc}(i(u), v)) = v \quad \text{fof}(\text{dec\_enc\_cancel, axiom})$   
 $\forall u: i(i(u)) = u \quad \text{fof}(\text{double\_inverse\_cancel, axiom})$   
 $\forall u: (p(u) \Rightarrow p(i(u))) \quad \text{fof}(\text{keys\_are\_symmetric, axiom})$   
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{tmk}, \text{enc}(i(\text{enc}(i(\text{zcmk}), v)), u)))) \quad \text{fof}(\text{key\_translate\_from\_ZCMK\_to\_TMK, axiom})$   
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(i(\text{enc}(i(\text{zcmk}), v)), \text{enc}(i(\text{tmk}), u)))) \quad \text{fof}(\text{key\_translate\_from\_TMK\_to\_ZCMK, axiom})$   
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{wk}, \text{enc}(i(\text{tmk}), u)))) \quad \text{fof}(\text{receive\_working\_key\_from\_switch, axiom})$   
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{enc}(i(\text{tmk}), v), \text{enc}(i(\text{tmk}), u)))) \quad \text{fof}(\text{encrypt\_a\_PIN\_derivation\_key\_under\_a\_PIN, axiom})$   
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{enc}(i(\text{tmk}), v), \text{enc}(i(\text{tc}), u)))) \quad \text{fof}(\text{encrypt\_a\_stored\_comms\_key, axiom})$   
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{tc}, u))) \quad \text{fof}(\text{encrypt\_clear\_key\_as\_Tcomms\_key, axiom})$   
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{enc}(i(\text{tc}), u), v))) \quad \text{fof}(\text{data\_encrypt, axiom})$   
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(i(\text{enc}(i(\text{tc}), u)), v))) \quad \text{fof}(\text{data\_decrypt, axiom})$   
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{enc}(i(\text{wk}), w), \text{enc}(i(\text{enc}(i(\text{tmk}), v)), u)))) \quad \text{fof}(\text{data\_translate\_PIN\_from\_local\_to\_remote, conjecture})$

$\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{enc}(i(\text{wk}), w), \text{enc}(i(\text{enc}(i(\text{wk}), v)), u))))$     fof(data\_translate\_between\_interch.  
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{enc}(i(\text{wk}), v), \text{enc}(i(\text{lp}), u))))$     fof(data\_translate\_PIN\_from\_local\_storage\_to.i  
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(u, v)))$     fof(attacker\_can\_encrypt, axiom)  
 $p(\text{enc}(\text{tmk}, \text{pp}))$     fof(intruder\_knows<sub>1</sub>, axiom)  
 $p(\text{enc}(\text{wk}, w))$     fof(intruder\_knows<sub>2</sub>, axiom)  
 $p(\text{enc}(w, t_1))$     fof(intruder\_knows<sub>3</sub>, axiom)  
 $p(\text{enc}(\text{lp}, t_2))$     fof(intruder\_knows<sub>4</sub>, axiom)  
 $p(\text{enc}(\text{tc}, k))$     fof(intruder\_knows<sub>5</sub>, axiom)  
 $p(\text{kk})$     fof(intruder\_knows<sub>6</sub>, axiom)  
 $p(i(\text{kk}))$     fof(intruder\_knows<sub>7</sub>, axiom)  
 $p(a)$     fof(intruder\_knows<sub>8</sub>, axiom)  
 $p(\text{enc}(\text{pp}, a))$     fof(co<sub>1</sub>, conjecture)

### SWV238+1.p Visa Security Module (VSM) attack denied

This file models the API of the Visa Security Module (VSM). In this version, the command that Visa removed to try to prevent Bond's attack has been commented out. So the problem is now to prove the attack is not possible.

$\forall u, v: \text{enc}(i(u), \text{enc}(u, v)) = v$     fof(enc\_dec\_cancel, axiom)  
 $\forall u, v: \text{enc}(u, \text{enc}(i(u), v)) = v$     fof(dec\_enc\_cancel, axiom)  
 $\forall u: i(i(u)) = u$     fof(double\_inverse\_cancel, axiom)  
 $\forall u: (p(u) \Rightarrow p(i(u)))$     fof(keys\_are\_symmetric, axiom)  
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{tmk}, \text{enc}(i(\text{enc}(i(\text{zcmk}), v)), u))))$     fof(key\_translate\_from\_ZCMK\_to\_TMK, a  
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(i(\text{enc}(i(\text{zcmk}), v)), \text{enc}(i(\text{tmk}), u))))$     fof(key\_translate\_from\_TMK\_to\_ZCMK  
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{wk}, \text{enc}(i(\text{tmk}), u))))$     fof(receive\_working\_key\_from\_switch, axiom)  
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{enc}(i(\text{tmk}), v), \text{enc}(i(\text{tmk}), u))))$     fof(encrypt\_a\_PIN\_derivation\_key\_under\_a.  
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{enc}(i(\text{tmk}), v), \text{enc}(i(\text{tc}), u))))$     fof(encrypt\_a\_stored\_comms\_key, axiom)  
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{enc}(i(\text{tc}), u), v)))$     fof(data\_encrypt, axiom)  
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(i(\text{enc}(i(\text{tc}), u), v))))$     fof(data\_decrypt, axiom)  
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{enc}(i(\text{wk}), w), \text{enc}(i(\text{enc}(i(\text{tmk}), v)), u))))$     fof(data\_translate\_PIN\_from\_local  
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{enc}(i(\text{wk}), w), \text{enc}(i(\text{enc}(i(\text{wk}), v)), u))))$     fof(data\_translate\_between\_interch  
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(\text{enc}(i(\text{wk}), v), \text{enc}(i(\text{lp}), u))))$     fof(data\_translate\_PIN\_from\_local\_storage\_to.i  
 $\forall u, v, w: ((p(u) \text{ and } p(v) \text{ and } p(w)) \Rightarrow p(\text{enc}(u, v)))$     fof(attacker\_can\_encrypt, axiom)  
 $p(\text{enc}(\text{tmk}, \text{pp}))$     fof(intruder\_knows<sub>1</sub>, axiom)  
 $p(\text{enc}(\text{wk}, w))$     fof(intruder\_knows<sub>2</sub>, axiom)  
 $p(\text{enc}(w, t_1))$     fof(intruder\_knows<sub>3</sub>, axiom)  
 $p(\text{enc}(\text{lp}, t_2))$     fof(intruder\_knows<sub>4</sub>, axiom)  
 $p(\text{enc}(\text{tc}, k))$     fof(intruder\_knows<sub>5</sub>, axiom)  
 $p(\text{kk})$     fof(intruder\_knows<sub>6</sub>, axiom)  
 $p(i(\text{kk}))$     fof(intruder\_knows<sub>7</sub>, axiom)  
 $p(a)$     fof(intruder\_knows<sub>8</sub>, axiom)  
 $p(\text{enc}(\text{pp}, a))$     fof(co<sub>1</sub>, conjecture)

### SWV239-1.p Cryptographic protocol problem for messages

include('Axioms/MS001-0.ax')  
include('Axioms/MS001-2.ax')  
include('Axioms/SWV004-0.ax')  
(c\_lessequals(c\_Message\_Oanalz(v\_H), c\_Message\_Oanalz(v\_H\_H), tc\_set(tc\_Message\_Omsg)) and c\_lessequals(c\_Message\_Oanalz(v\_G, v\_H, tc\_Message\_Omsg), c\_Message\_Oanalz(c\_union(v\_G\_H, v\_H\_H, tc\_Message\_Omsg)), c\_Message\_Oanalz(c\_union(v\_G\_H, v\_H\_H, tc\_Message\_Omsg))) and c\_in(v\_X, c\_Message\_Osynth(c\_Message\_Osynth(v\_H)), tc\_Message\_Omsg)  $\Rightarrow$  c\_in(v\_X, c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) and  $\neg$  c\_lessequals(c\_Message\_Oanalz(c\_union(c\_Message\_Oanalz(v\_G), v\_H, tc\_Message\_Omsg), c\_Message\_Oanalz(c\_union(v\_G, v\_H, tc\_Message\_Omsg))), c\_Message\_Oanalz(c\_union(v\_G, v\_H, tc\_Message\_Omsg)))

### SWV239-2.p Cryptographic protocol problem for messages

$\neg$  c\_lessequals(c\_Message\_Oanalz(c\_union(c\_Message\_Oanalz(v\_G), v\_H, tc\_Message\_Omsg), c\_Message\_Oanalz(c\_union(v\_G, v\_H, tc\_Message\_Omsg))), c\_Message\_Oanalz(c\_union(v\_G, v\_H, tc\_Message\_Omsg))) and c\_in(v\_X, c\_Message\_Oanalz(c\_Message\_Oanalz(v\_H)), tc\_Message\_Omsg)  $\Rightarrow$  c\_in(v\_X, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) and (c\_lessequals(c\_Message\_Oanalz(v\_H), c\_Message\_Oanalz(v\_H\_H), tc\_set(tc\_Message\_Omsg)) and c\_lessequals(c\_Message\_Oanalz(v\_G, v\_H, tc\_Message\_Omsg), c\_Message\_Oanalz(c\_union(v\_G\_H, v\_H\_H, tc\_Message\_Omsg)), c\_Message\_Oanalz(c\_union(v\_G\_H, v\_H\_H, tc\_Message\_Omsg))) and c\_in(c\_Main\_OsubsetI<sub>1</sub>(v\_A, v\_B, t\_a), v\_A, t\_a) or c\_lessequals(v\_A, v\_B, tc\_set(t\_a))    cnf(cls\_Set\_OsubsetI<sub>0</sub>, axiom)  
c\_in(c\_Main\_OsubsetI<sub>1</sub>(v\_A, v\_B, t\_a), v\_B, t\_a)  $\Rightarrow$  c\_lessequals(v\_A, v\_B, tc\_set(t\_a))    cnf(cls\_Set\_OsubsetI<sub>1</sub>, axiom)  
c\_lessequals(v\_A, v\_A, tc\_set(t\_a))    cnf(cls\_Set\_Osubset\_refl<sub>0</sub>, axiom)

### SWV240-1.p Cryptographic protocol problem for messages

include('Axioms/MS001-0.ax')

```

include('Axioms/MSC001-2.ax')
include('Axioms/SWV004-0.ax')
(c_lessequals(c_Message_Oanalz(v_H), c_Message_Oanalz(v_H_H), tc_set(tc_Message_Omsg)) and c_lessequals(c_Message_Oanalz(v_G), c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg)), c_Message_Oanalz(c_union(v_G_H, v_H_H, tc_Message_Omsg))) and c_in(v_X, c_Message_Osynth(c_Message_Osynth(v_H)), tc_Message_Omsg)  $\Rightarrow$  c_in(v_X, c_Message_Osynth(v_H), tc_Message_Omsg) and  $\neg$  c_lessequals(c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg)), c_Message_Oanalz(c_union(c_Message_Oanalz(v_G), v_H, tc_Message_Omsg)))

```

**SWV240-2.p** Cryptographic protocol problem for messages

```

 $\neg$  c_lessequals(c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg)), c_Message_Oanalz(c_union(c_Message_Oanalz(v_G), v_H, tc_Message_Omsg))) and c_in(v_X, v_H, tc_Message_Omsg)  $\Rightarrow$  c_in(v_X, c_Message_Oanalz(v_H), tc_Message_Omsg)   cnf(cls_Message_Oanalz_OInj_0, axiom)
(c_lessequals(c_Message_Oanalz(v_H), c_Message_Oanalz(v_H_H), tc_set(tc_Message_Omsg)) and c_lessequals(c_Message_Oanalz(v_G), c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg)), c_Message_Oanalz(c_union(v_G_H, v_H_H, tc_Message_Omsg))) and c_in(c_Main_OsubsetI_1(v_A, v_B, t_a), v_A, t_a) or c_lessequals(v_A, v_B, tc_set(t_a))   cnf(cls_Set_OsubsetI_0, axiom)
c_in(c_Main_OsubsetI_1(v_A, v_B, t_a), v_B, t_a)  $\Rightarrow$  c_lessequals(v_A, v_B, tc_set(t_a))   cnf(cls_Set_OsubsetI_1, axiom)
c_lessequals(v_A, v_A, tc_set(t_a))   cnf(cls_Set_Osubset_refl_0, axiom)

```

**SWV241-2.p** Cryptographic protocol problem for messages

```

c_in(v_X, v_H, tc_Message_Omsg)  $\Rightarrow$  c_in(v_X, c_Message_Oanalz(v_H), tc_Message_Omsg)   cnf(cls_Message_Oanalz_OInj_0, axiom)
(c_in(v_X, c_Message_Oanalz(v_G), tc_Message_Omsg) and c_lessequals(v_G, c_Message_Oanalz(v_H), tc_set(tc_Message_Omsg))) and c_in(v_X, c_Message_Oanalz(v_H), tc_Message_Omsg)   cnf(cls_Message_Oanalz_trans_0, axiom)
c_in(v_a, c_insert(v_b, v_A, t_a), t_a)  $\Rightarrow$  (c_in(v_a, v_A, t_a) or v_a = v_b)   cnf(cls_Set_OinsertE_0, axiom)
c_in(c_Main_OsubsetI_1(v_A, v_B, t_a), v_A, t_a) or c_lessequals(v_A, v_B, tc_set(t_a))   cnf(cls_Set_OsubsetI_0, axiom)
c_in(c_Main_OsubsetI_1(v_A, v_B, t_a), v_B, t_a)  $\Rightarrow$  c_lessequals(v_A, v_B, tc_set(t_a))   cnf(cls_Set_OsubsetI_1, axiom)
c_in(v_Y, c_Message_Oanalz(c_insert(v_X, v_H, tc_Message_Omsg)), tc_Message_Omsg)   cnf(cls_conjecture_0, negated_conjecture)
c_in(v_X, c_Message_Oanalz(v_H), tc_Message_Omsg)   cnf(cls_conjecture_1, negated_conjecture)
 $\neg$  c_in(v_Y, c_Message_Oanalz(v_H), tc_Message_Omsg)   cnf(cls_conjecture_2, negated_conjecture)

```

**SWV242-2.p** Cryptographic protocol problem for messages

```

c_lessequals(v_G, c_Message_Oanalz(v_G_H), tc_set(tc_Message_Omsg))   cnf(cls_conjecture_0, negated_conjecture)
c_lessequals(v_H, c_Message_Oanalz(v_H_H), tc_set(tc_Message_Omsg))   cnf(cls_conjecture_1, negated_conjecture)
c_lessequals(v_H, c_Message_Oanalz(c_union(v_G_H, v_H_H, tc_Message_Omsg)), tc_set(tc_Message_Omsg))  $\Rightarrow$   $\neg$  c_lessequals(v_G, c_Message_Oanalz(v_H), tc_set(tc_Message_Omsg))
c_lessequals(v_G, v_H, tc_set(tc_Message_Omsg))  $\Rightarrow$  c_lessequals(c_Message_Oanalz(v_G), c_Message_Oanalz(v_H), tc_set(tc_Message_Omsg))
c_lessequals(v_A, c_union(v_A, v_B, t_a), tc_set(t_a))   cnf(cls_Set_OUn_upper1_0, axiom)
c_lessequals(v_B, c_union(v_A, v_B, t_a), tc_set(t_a))   cnf(cls_Set_OUn_upper2_0, axiom)
(c_lessequals(v_B, v_C, tc_set(t_a)) and c_lessequals(v_A, v_B, tc_set(t_a)))  $\Rightarrow$  c_lessequals(v_A, v_C, tc_set(t_a))   cnf(cls_Set_OUn_upper3_0, axiom)

```

**SWV243-1.p** Cryptographic protocol problem for messages

```

include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-1.ax')
include('Axioms/SWV005-0.ax')
include('Axioms/SWV005-1.ax')
c_Message_Oanalz(c_union(c_Message_Oanalz(v_G), v_H, tc_Message_Omsg)) = c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg))
c_Message_Oanalz(c_union(c_Message_Osynth(v_G), v_H, tc_Message_Omsg)) = c_union(c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg)), c_Message_Osynth(v_G, v_H, tc_Message_Omsg))
c_Message_Oparts(c_Message_Osynth(v_H)) = c_union(c_Message_Oparts(v_H), c_Message_Osynth(v_H), tc_Message_Omsg)
c_Message_Oanalz(c_Message_Osynth(v_H))  $\neq$  c_union(c_Message_Oanalz(v_H), c_Message_Osynth(v_H), tc_Message_Omsg)

```

**SWV243-2.p** Cryptographic protocol problem for messages

```

c_Message_Oanalz(c_Message_Osynth(v_H))  $\neq$  c_union(c_Message_Oanalz(v_H), c_Message_Osynth(v_H), tc_Message_Omsg)
c_Message_Oanalz(c_union(c_Message_Osynth(v_G), v_H, tc_Message_Omsg)) = c_union(c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg)), c_Message_Osynth(v_G, v_H, tc_Message_Omsg))
c_union(v_y, c_emptyset, t_a) = v_y   cnf(cls_Set_OUn_empty_right_0, axiom)

```

**SWV244-1.p** Cryptographic protocol problem for messages

```

include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-2.ax')
include('Axioms/SWV004-0.ax')
c_lessequals(v_G, v_H, tc_set(tc_Message_Omsg))  $\Rightarrow$  c_lessequals(c_Message_Oanalz(v_G), c_Message_Oanalz(v_H), tc_set(tc_Message_Omsg))
c_in(v_X, c_Message_Osynth(c_Message_Osynth(v_H)), tc_Message_Omsg)  $\Rightarrow$  c_in(v_X, c_Message_Osynth(v_H), tc_Message_Omsg)
(c_lessequals(v_B, v_C, tc_set(t_a)) and c_lessequals(v_A, v_C, tc_set(t_a)))  $\Rightarrow$  c_lessequals(c_union(v_A, v_B, t_a), v_C, tc_set(t_a))
c_in(v_X, c_union(c_Message_Osynth(v_G), v_H, tc_Message_Omsg), tc_Message_Omsg)   cnf(cls_conjecture_0, negated_conjecture)
 $\neg$  c_in(v_X, c_union(c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg)), c_Message_Osynth(v_G), tc_Message_Omsg), tc_Message_Omsg)

```

**SWV244-2.p** Cryptographic protocol problem for messages

```

c_in(v_X, c_union(c_Message_Osynth(v_G), v_H, tc_Message_Omsg), tc_Message_Omsg)   cnf(cls_conjecture_0, negated_conjecture)

```





$(c.in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg))$  and  $c.in(c\_Message\_Omsg\_OKey(c\_Message\_Oanalz(v\_X, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg))$   $cnf(cls\_Message\_Oanalz\_ODecrypt\_dest_0, axiom)$   
 $c.in(c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(c\_Message\_Omsg\_OKey(v\_K), v\_H, tc\_Message\_Omsg)$   
 $c.in(v\_X, v\_H, tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg)$   $cnf(cls\_Message\_Oanalz\_OInj_0, axiom)$   
 $c.in(v\_c, v\_B, t\_a) \Rightarrow c.in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a)$   $cnf(cls\_Set\_OUnCI_0, axiom)$   
 $c.in(v\_c, v\_A, t\_a) \Rightarrow c.in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a)$   $cnf(cls\_Set\_OUnCI_1, axiom)$   
 $c.in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a) \Rightarrow (c.in(v\_c, v\_B, t\_a) \text{ or } c.in(v\_c, v\_A, t\_a))$   $cnf(cls\_Set\_OUnE_0, axiom)$   
 $c.in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_union(c\_Message\_Oanalz(c\_union(v\_G, v\_H, tc\_Message\_Omsg)), c\_Message\_Osynth(v\_G), tc\_Message\_Omsg))$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Message\_OinvKey(v\_K)), c\_union(c\_Message\_Oanalz(c\_union(v\_G, v\_H, tc\_Message\_Omsg)), c\_Message\_Osynth(v\_G), tc\_Message\_Omsg))$   
 $\neg c.in(v\_X, c\_union(c\_Message\_Oanalz(c\_union(v\_G, v\_H, tc\_Message\_Omsg)), c\_Message\_Osynth(v\_G), tc\_Message\_Omsg), tc\_Message\_Omsg)$

**SWV248-1.p** Cryptographic protocol problem for messages

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-2.ax')$   
 $include('Axioms/SWV004-0.ax')$   
 $c.lessequals(v\_G, v\_H, tc.set(tc\_Message\_Omsg)) \Rightarrow c.lessequals(c\_Message\_Oanalz(v\_G), c\_Message\_Oanalz(v\_H), tc.set(tc\_Message\_Omsg))$   
 $c.in(v\_X, c\_Message\_Osynth(c\_Message\_Osynth(v\_H)), tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Osynth(v\_H), tc\_Message\_Omsg)$   
 $(c.lessequals(v\_B, v\_C, tc.set(t\_a)) \text{ and } c.lessequals(v\_A, v\_C, tc.set(t\_a))) \Rightarrow c.lessequals(c\_union(v\_A, v\_B, t\_a), v\_C, tc.set(t\_a))$   
 $\neg c.lessequals(c\_union(c\_Message\_Oanalz(c\_union(v\_G, v\_H, tc\_Message\_Omsg)), c\_Message\_Osynth(v\_G), tc\_Message\_Omsg), tc\_Message\_Omsg)$

**SWV248-2.p** Cryptographic protocol problem for messages

$\neg c.lessequals(c\_union(c\_Message\_Oanalz(c\_union(v\_G, v\_H, tc\_Message\_Omsg)), c\_Message\_Osynth(v\_G), tc\_Message\_Omsg), tc\_Message\_Omsg)$   
 $c.in(v\_X, v\_H, tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg)$   $cnf(cls\_Message\_Oanalz\_OInj_0, axiom)$   
 $c.lessequals(v\_G, v\_H, tc.set(tc\_Message\_Omsg)) \Rightarrow c.lessequals(c\_Message\_Oanalz(v\_G), c\_Message\_Oanalz(v\_H), tc.set(tc\_Message\_Omsg))$   
 $c.in(v\_X, v\_H, tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Osynth(v\_H), tc\_Message\_Omsg)$   $cnf(cls\_Message\_Osynth\_OInj_0, axiom)$   
 $c.in(v\_c, v\_B, t\_a) \Rightarrow c.in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a)$   $cnf(cls\_Set\_OUnCI_0, axiom)$   
 $c.in(v\_c, v\_A, t\_a) \Rightarrow c.in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a)$   $cnf(cls\_Set\_OUnCI_1, axiom)$   
 $(c.lessequals(v\_B, v\_C, tc.set(t\_a)) \text{ and } c.lessequals(v\_A, v\_C, tc.set(t\_a))) \Rightarrow c.lessequals(c\_union(v\_A, v\_B, t\_a), v\_C, tc.set(t\_a))$   
 $c.in(c\_Main\_OsubsetI\_1(v\_A, v\_B, t\_a), v\_A, t\_a) \text{ or } c.lessequals(v\_A, v\_B, tc.set(t\_a))$   $cnf(cls\_Set\_OsubsetI_0, axiom)$   
 $c.in(c\_Main\_OsubsetI\_1(v\_A, v\_B, t\_a), v\_B, t\_a) \Rightarrow c.lessequals(v\_A, v\_B, tc.set(t\_a))$   $cnf(cls\_Set\_OsubsetI_1, axiom)$

**SWV249-1.p** Cryptographic protocol problem for messages

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-1.ax')$   
 $include('Axioms/SWV005-0.ax')$   
 $include('Axioms/SWV005-1.ax')$   
 $c\_Message\_Oanalz(c\_union(c\_Message\_Oanalz(v\_G), v\_H, tc\_Message\_Omsg)) = c\_Message\_Oanalz(c\_union(v\_G, v\_H, tc\_Message\_Omsg))$   
 $c.lessequals(v\_G, v\_H, tc.set(tc\_Message\_Omsg)) \Rightarrow c.lessequals(c\_Message\_Oanalz(v\_G), c\_Message\_Oanalz(v\_H), tc.set(tc\_Message\_Omsg))$   
 $c\_Message\_Oanalz(c\_Message\_Osynth(v\_H)) = c\_union(c\_Message\_Oanalz(v\_H), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg)$   
 $c\_Message\_Oanalz(c\_union(c\_Message\_Osynth(v\_G), v\_H, tc\_Message\_Omsg)) = c\_union(c\_Message\_Oanalz(c\_union(v\_G, v\_H, tc\_Message\_Omsg)), c\_Message\_Osynth(v\_G), tc\_Message\_Omsg)$   
 $c\_Message\_Oparts(c\_Message\_Osynth(v\_H)) = c\_union(c\_Message\_Oparts(v\_H), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg)$   
 $c.lessequals(v\_G, v\_H, tc.set(tc\_Message\_Omsg)) \Rightarrow c.lessequals(c\_Message\_Osynth(v\_G), c\_Message\_Osynth(v\_H), tc.set(tc\_Message\_Omsg))$   
 $c.in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(v\_G)), tc\_Message\_Omsg)$   $cnf(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c.lessequals(c\_Message\_Oanalz(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), c\_union(c\_Message\_Osynth(c\_Message\_Oanalz(v\_G)), tc\_Message\_Omsg))$

**SWV249-2.p** Cryptographic protocol problem for messages

$c.in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(v\_G)), tc\_Message\_Omsg)$   $cnf(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c.lessequals(c\_Message\_Oanalz(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), c\_union(c\_Message\_Osynth(c\_Message\_Oanalz(v\_G)), tc\_Message\_Omsg))$   
 $c\_Message\_Oanalz(c\_union(c\_Message\_Oanalz(v\_G), v\_H, tc\_Message\_Omsg)) = c\_Message\_Oanalz(c\_union(v\_G, v\_H, tc\_Message\_Omsg))$   
 $c.lessequals(v\_G, v\_H, tc.set(tc\_Message\_Omsg)) \Rightarrow c.lessequals(c\_Message\_Oanalz(v\_G), c\_Message\_Oanalz(v\_H), tc.set(tc\_Message\_Omsg))$   
 $c\_Message\_Oanalz(c\_union(c\_Message\_Osynth(v\_G), v\_H, tc\_Message\_Omsg)) = c\_union(c\_Message\_Oanalz(c\_union(v\_G, v\_H, tc\_Message\_Omsg)), c\_Message\_Osynth(v\_G), tc\_Message\_Omsg)$   
 $class\_Orderings\_Oorder(t\_a) \Rightarrow c.lessequals(v\_x, v\_x, t\_a)$   $cnf(cls\_Orderings\_Oorder\_class\_Oaxioms\_1_0, axiom)$   
 $c\_union(c\_minus(v\_B, v\_A, tc.set(t\_a)), v\_A, t\_a) = c\_union(v\_B, v\_A, t\_a)$   $cnf(cls\_Set\_OUn\_Diff\_cancel2_0, axiom)$   
 $c\_union(v\_A, c\_minus(v\_B, v\_A, tc.set(t\_a)), t\_a) = c\_union(v\_A, v\_B, t\_a)$   $cnf(cls\_Set\_OUn\_Diff\_cancel_0, axiom)$   
 $c\_union(c\_insert(v\_a, v\_B, t\_a), v\_C, t\_a) = c\_insert(v\_a, c\_union(v\_B, v\_C, t\_a), t\_a)$   $cnf(cls\_Set\_OUn\_insert\_left_0, axiom)$   
 $c\_union(v\_A, c\_insert(v\_a, v\_B, t\_a), t\_a) = c\_insert(v\_a, c\_union(v\_A, v\_B, t\_a), t\_a)$   $cnf(cls\_Set\_OUn\_insert\_right_0, axiom)$   
 $c.lessequals(c\_union(v\_A, v\_B, t\_a), v\_C, tc.set(t\_a)) \Rightarrow c.lessequals(v\_A, v\_C, tc.set(t\_a))$   $cnf(cls\_Set\_OUn\_subset\_iff_0, axiom)$   
 $c.lessequals(c\_union(v\_A, v\_B, t\_a), v\_C, tc.set(t\_a)) \Rightarrow c.lessequals(v\_B, v\_C, tc.set(t\_a))$   $cnf(cls\_Set\_OUn\_subset\_iff_1, axiom)$   
 $(c.lessequals(v\_B, v\_C, tc.set(t\_a)) \text{ and } c.lessequals(v\_A, v\_C, tc.set(t\_a))) \Rightarrow c.lessequals(c\_union(v\_A, v\_B, t\_a), v\_C, tc.set(t\_a))$   
 $c.lessequals(c\_insert(v\_x, v\_A, t\_a), v\_B, tc.set(t\_a)) \Rightarrow c.lessequals(v\_A, v\_B, tc.set(t\_a))$   $cnf(cls\_Set\_Oinsert\_subset_1, axiom)$   
 $(c.in(v\_x, v\_B, t\_a) \text{ and } c.lessequals(v\_A, v\_B, tc.set(t\_a))) \Rightarrow c.lessequals(c\_insert(v\_x, v\_A, t\_a), v\_B, tc.set(t\_a))$   $cnf(cls\_Set\_Oinsert\_subset_1, axiom)$

$(c\_lessequals(v\_B, v\_A, tc\_set(t\_a)) \text{ and } c\_lessequals(v\_A, v\_B, tc\_set(t\_a))) \Rightarrow v\_A = v\_B$      $\text{cnf}(\text{cls\_Set\_Osubset\_antisym}_0, \text{class\_Orderings\_Oorder}(tc\_set(t_1)) \text{ cnf}(\text{clarity\_set}_2, \text{axiom}))$

**SWV250-1.p** Cryptographic protocol problem for messages

```
include('Axioms/MS001-0.ax')
include('Axioms/MS001-1.ax')
include('Axioms/SWV005-0.ax')
include('Axioms/SWV005-1.ax')
c_Message_Oanalz(c_union(c_Message_Oanalz(v_G), v_H, tc_Message_Omsg)) = c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg))
c_lessequals(v_G, v_H, tc_set(tc_Message_Omsg))  $\Rightarrow$  c_lessequals(c_Message_Oanalz(v_G), c_Message_Oanalz(v_H), tc_set(tc_Message_Omsg))
c_Message_Oanalz(c_Message_Osynth(v_H)) = c_union(c_Message_Oanalz(v_H), c_Message_Osynth(v_H), tc_Message_Omsg)
c_Message_Oanalz(c_union(c_Message_Osynth(v_G), v_H, tc_Message_Omsg)) = c_union(c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg)), c_Message_Osynth(v_H))
c_Message_Oparts(c_Message_Osynth(v_H)) = c_union(c_Message_Oparts(v_H), c_Message_Osynth(v_H), tc_Message_Omsg)
c_lessequals(v_G, v_H, tc_set(tc_Message_Omsg))  $\Rightarrow$  c_lessequals(c_Message_Osynth(v_G), c_Message_Osynth(v_H), tc_set(tc_Message_Omsg))
c_in(v_X, c_Message_Osynth(c_Message_Oanalz(v_G)), tc_Message_Omsg)     $\text{cnf}(\text{cls\_conjecture}_0, \text{negated\_conjecture})$ 
c_in(v_x, c_Message_Oanalz(c_insert(v_X, v_H, tc_Message_Omsg)), tc_Message_Omsg)     $\text{cnf}(\text{cls\_conjecture}_1, \text{negated\_conjecture})$ 
c_in(v_x, c_Message_Oanalz(c_union(c_Message_Osynth(c_Message_Oanalz(v_G)), v_H, tc_Message_Omsg)), tc_Message_Omsg)
 $\neg$  c_in(v_x, c_union(c_Message_Osynth(c_Message_Oanalz(v_G)), c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg)), tc_Message_Omsg))
```

**SWV250-2.p** Cryptographic protocol problem for messages

```
c_in(v_x, c_Message_Oanalz(c_union(c_Message_Osynth(c_Message_Oanalz(v_G)), v_H, tc_Message_Omsg)), tc_Message_Omsg)
 $\neg$  c_in(v_x, c_union(c_Message_Osynth(c_Message_Oanalz(v_G)), c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg)), tc_Message_Omsg))
c_Message_Oanalz(c_union(c_Message_Oanalz(v_G), v_H, tc_Message_Omsg)) = c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg))
c_Message_Oanalz(c_union(c_Message_Osynth(v_G), v_H, tc_Message_Omsg)) = c_union(c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg)), c_Message_Osynth(v_H))
c_in(v_c, c_union(v_A, v_B, t_a), t_a)  $\Rightarrow$  (c_in(v_c, v_B, t_a) or c_in(v_c, v_A, t_a))     $\text{cnf}(\text{cls\_Set\_OU\_iff}_0, \text{axiom})$ 
c_in(v_c, v_A, t_a)  $\Rightarrow$  c_in(v_c, c_union(v_A, v_B, t_a), t_a)     $\text{cnf}(\text{cls\_Set\_OU\_iff}_1, \text{axiom})$ 
c_in(v_c, v_B, t_a)  $\Rightarrow$  c_in(v_c, c_union(v_A, v_B, t_a), t_a)     $\text{cnf}(\text{cls\_Set\_OU\_iff}_2, \text{axiom})$ 
```

**SWV251-1.p** Cryptographic protocol problem for messages

```
include('Axioms/MS001-0.ax')
include('Axioms/MS001-1.ax')
include('Axioms/SWV005-0.ax')
include('Axioms/SWV005-1.ax')
c_Message_Oanalz(c_union(c_Message_Oanalz(v_G), v_H, tc_Message_Omsg)) = c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg))
c_lessequals(v_G, v_H, tc_set(tc_Message_Omsg))  $\Rightarrow$  c_lessequals(c_Message_Oanalz(v_G), c_Message_Oanalz(v_H), tc_set(tc_Message_Omsg))
c_Message_Oanalz(c_Message_Osynth(v_H)) = c_union(c_Message_Oanalz(v_H), c_Message_Osynth(v_H), tc_Message_Omsg)
c_Message_Oanalz(c_union(c_Message_Osynth(v_G), v_H, tc_Message_Omsg)) = c_union(c_Message_Oanalz(c_union(v_G, v_H, tc_Message_Omsg)), c_Message_Osynth(v_H))
c_Message_Oparts(c_Message_Osynth(v_H)) = c_union(c_Message_Oparts(v_H), c_Message_Osynth(v_H), tc_Message_Omsg)
c_lessequals(v_G, v_H, tc_set(tc_Message_Omsg))  $\Rightarrow$  c_lessequals(c_Message_Osynth(v_G), c_Message_Osynth(v_H), tc_set(tc_Message_Omsg))
c_in(v_X, c_Message_Osynth(c_Message_Oanalz(v_G)), tc_Message_Omsg)     $\text{cnf}(\text{cls\_conjecture}_0, \text{negated\_conjecture})$ 
c_in(v_x, c_Message_Oanalz(c_insert(v_X, v_H, tc_Message_Omsg)), tc_Message_Omsg)     $\text{cnf}(\text{cls\_conjecture}_1, \text{negated\_conjecture})$ 
 $\neg$  c_in(v_x, c_Message_Oanalz(c_union(c_Message_Osynth(c_Message_Oanalz(v_G)), v_H, tc_Message_Omsg)), tc_Message_Omsg)
```

**SWV251-2.p** Cryptographic protocol problem for messages

```
c_lessequals(v_G, v_H, tc_set(tc_Message_Omsg))  $\Rightarrow$  c_lessequals(c_Message_Oanalz(v_G), c_Message_Oanalz(v_H), tc_set(tc_Message_Omsg))
c_union(c_minus(v_B, v_A, tc_set(t_a)), v_A, t_a) = c_union(v_B, v_A, t_a)     $\text{cnf}(\text{cls\_Set\_OU\_Diff\_cancel}_2, \text{axiom})$ 
c_union(v_A, c_minus(v_B, v_A, tc_set(t_a)), t_a) = c_union(v_A, v_B, t_a)     $\text{cnf}(\text{cls\_Set\_OU\_Diff\_cancel}_0, \text{axiom})$ 
c_lessequals(c_union(v_A, v_B, t_a), v_C, tc_set(t_a))  $\Rightarrow$  c_lessequals(v_A, v_C, tc_set(t_a))     $\text{cnf}(\text{cls\_Set\_OU\_subset\_iff}_0, \text{axiom})$ 
c_lessequals(c_union(v_A, v_B, t_a), v_C, tc_set(t_a))  $\Rightarrow$  c_lessequals(v_B, v_C, tc_set(t_a))     $\text{cnf}(\text{cls\_Set\_OU\_subset\_iff}_1, \text{axiom})$ 
(c_lessequals(v_B, v_C, tc_set(t_a)) and c_lessequals(v_A, v_C, tc_set(t_a)))  $\Rightarrow$  c_lessequals(c_union(v_A, v_B, t_a), v_C, tc_set(t_a))
c_in(v_x, v_B, t_a)  $\Rightarrow$  c_minus(c_insert(v_x, v_A, t_a), v_B, tc_set(t_a)) = c_minus(v_A, v_B, tc_set(t_a))     $\text{cnf}(\text{cls\_Set\_Oinsert}, \text{axiom})$ 
(c_in(v_c, v_A, t_a) and c_lessequals(v_A, v_B, tc_set(t_a)))  $\Rightarrow$  c_in(v_c, v_B, t_a)     $\text{cnf}(\text{cls\_Set\_Osubset}_D, \text{axiom})$ 
(c_lessequals(v_B, v_A, tc_set(t_a)) and c_lessequals(v_A, v_B, tc_set(t_a)))  $\Rightarrow$  v_A = v_B     $\text{cnf}(\text{cls\_Set\_Osubset\_antisym}_0, \text{axiom})$ 
c_lessequals(v_A, v_A, tc_set(t_a))     $\text{cnf}(\text{cls\_Set\_Osubset\_refl}_0, \text{axiom})$ 
c_in(v_X, c_Message_Osynth(c_Message_Oanalz(v_G)), tc_Message_Omsg)     $\text{cnf}(\text{cls\_conjecture}_0, \text{negated\_conjecture})$ 
c_in(v_x, c_Message_Oanalz(c_insert(v_X, v_H, tc_Message_Omsg)), tc_Message_Omsg)     $\text{cnf}(\text{cls\_conjecture}_1, \text{negated\_conjecture})$ 
 $\neg$  c_in(v_x, c_Message_Oanalz(c_union(c_Message_Osynth(c_Message_Oanalz(v_G)), v_H, tc_Message_Omsg)), tc_Message_Omsg)
```

**SWV252-1.p** Cryptographic protocol problem for messages

```
include('Axioms/MS001-0.ax')
include('Axioms/MS001-1.ax')
include('Axioms/SWV005-0.ax')
```

include('Axioms/SWV005-1.ax')

$c\_Message\_Oanalz(c\_union(c\_Message\_Oanalz(v\_G), v\_H, tc\_Message\_Omsg)) = c\_Message\_Oanalz(c\_union(v\_G, v\_H, tc\_Message\_Omsg))$   
 $c\_Message\_Oanalz(c\_Message\_OSynth(v\_H)) = c\_union(c\_Message\_Oanalz(v\_H), c\_Message\_OSynth(v\_H), tc\_Message\_Omsg)$   
 $c\_Message\_Oanalz(c\_union(c\_Message\_OSynth(v\_G), v\_H, tc\_Message\_Omsg)) = c\_union(c\_Message\_Oanalz(c\_union(v\_G, v\_H, tc\_Message\_Omsg)), c\_Message\_OSynth(v\_H))$   
 $c\_in(v\_X, v\_G, tc\_Message\_Omsg) \Rightarrow c\_lessequals(c\_Message\_Oparts(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), c\_union(c\_Message\_Oanalz(v\_G), v\_H, tc\_Message\_Omsg))$   
 $c\_Message\_Oparts(c\_Message\_OSynth(v\_H)) = c\_union(c\_Message\_Oparts(v\_H), c\_Message\_OSynth(v\_H), tc\_Message\_Omsg)$   
 $c\_in(v\_X, c\_Message\_OSynth(c\_Message\_Oanalz(v\_H)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c\_lessequals(c\_Message\_Oparts(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), c\_union(c\_Message\_OSynth(c\_Message\_Oanalz(v\_H)), tc\_Message\_Omsg))$

**SWV252-2.p** Cryptographic protocol problem for messages

$c\_in(v\_X, c\_Message\_OSynth(c\_Message\_Oanalz(v\_H)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c\_lessequals(c\_Message\_Oparts(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), c\_union(c\_Message\_OSynth(c\_Message\_Oanalz(v\_H)), tc\_Message\_Omsg))$   
 $c\_Message\_Oanalz(c\_Message\_Oparts(v\_H)) = c\_Message\_Oparts(v\_H) \quad cnf(cls\_Message\_Oanalz\_parts_0, axiom)$   
 $c\_lessequals(c\_Message\_Oanalz(v\_G), c\_Message\_Oanalz(v\_H), tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(v\_G, c\_Message\_Oanalz(v\_H))$   
 $c\_Message\_Oparts(c\_Message\_Oanalz(v\_H)) = c\_Message\_Oparts(v\_H) \quad cnf(cls\_Message\_Oparts\_analz_0, axiom)$   
 $c\_lessequals(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(v\_G, c\_Message\_Oparts(v\_H))$   
 $c\_lessequals(v\_G, c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H))$   
 $c\_Message\_Oparts(c\_Message\_OSynth(v\_H)) = c\_union(c\_Message\_Oparts(v\_H), c\_Message\_OSynth(v\_H), tc\_Message\_Omsg)$   
 $class\_Orderings\_Oorder(t\_a) \Rightarrow c\_lessequals(v\_x, v\_x, t\_a) \quad cnf(cls\_Orderings\_Oorder\_class\_Oaxioms\_1_0, axiom)$   
 $c\_union(c\_minus(v\_B, v\_A, tc\_set(t\_a)), v\_A, t\_a) = c\_union(v\_B, v\_A, t\_a) \quad cnf(cls\_Set\_OU\_Diff\_cancel2_0, axiom)$   
 $c\_union(v\_A, c\_minus(v\_B, v\_A, tc\_set(t\_a)), t\_a) = c\_union(v\_A, v\_B, t\_a) \quad cnf(cls\_Set\_OU\_Diff\_cancel_0, axiom)$   
 $c\_lessequals(c\_union(v\_A, v\_B, t\_a), v\_C, tc\_set(t\_a)) \Rightarrow c\_lessequals(v\_A, v\_C, tc\_set(t\_a)) \quad cnf(cls\_Set\_OU\_subset\_iff_0, axiom)$   
 $c\_lessequals(c\_union(v\_A, v\_B, t\_a), v\_C, tc\_set(t\_a)) \Rightarrow c\_lessequals(v\_B, v\_C, tc\_set(t\_a)) \quad cnf(cls\_Set\_OU\_subset\_iff_1, axiom)$   
 $(c\_lessequals(v\_B, v\_C, tc\_set(t\_a)) \text{ and } c\_lessequals(v\_A, v\_C, tc\_set(t\_a))) \Rightarrow c\_lessequals(c\_union(v\_A, v\_B, t\_a), v\_C, tc\_set(t\_a))$   
 $c\_lessequals(c\_insert(v\_x, v\_A, t\_a), v\_B, tc\_set(t\_a)) \Rightarrow c\_in(v\_x, v\_B, t\_a) \quad cnf(cls\_Set\_Oinsert\_subset_0, axiom)$   
 $c\_lessequals(c\_insert(v\_x, v\_A, t\_a), v\_B, tc\_set(t\_a)) \Rightarrow c\_lessequals(v\_A, v\_B, tc\_set(t\_a)) \quad cnf(cls\_Set\_Oinsert\_subset_1, axiom)$   
 $(c\_in(v\_x, v\_B, t\_a) \text{ and } c\_lessequals(v\_A, v\_B, tc\_set(t\_a))) \Rightarrow c\_lessequals(c\_insert(v\_x, v\_A, t\_a), v\_B, tc\_set(t\_a)) \quad cnf(cls\_Set\_Oinsert\_subset\_2, axiom)$   
 $(c\_lessequals(v\_B, v\_A, tc\_set(t\_a)) \text{ and } c\_lessequals(v\_A, v\_B, tc\_set(t\_a))) \Rightarrow v\_A = v\_B \quad cnf(cls\_Set\_Osubset\_antisym_0, axiom)$   
 $class\_Orderings\_Oorder(tc\_set(t_1)) \quad cnf(cls\_arity\_set_2, axiom)$

**SWV253-2.p** Cryptographic protocol problem for messages

$v\_K = v\_K\_H \Rightarrow c\_Message\_OinvKey(v\_K) \neq c\_Message\_OinvKey(v\_K\_H) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c\_Message\_OinvKey(v\_K) = c\_Message\_OinvKey(v\_K\_H) \text{ or } v\_K = v\_K\_H \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c\_Message\_OinvKey(c\_Message\_OinvKey(v\_y)) = v\_y \quad cnf(cls\_Message\_OinvKey\_A\_InvKey\_Ay\_J\_A.61.61\_Ay_0, axiom)$

**SWV254-2.p** Cryptographic protocol problem for messages

$(class\_Orderings\_Oorder(t\_a) \text{ and } c\_lessequals(v\_n, v\_m, t\_a)) \Rightarrow c\_SetInterval\_OatLeastLessThan(v\_m, v\_n, t\_a) = c\_emptyset$   
 $cnf(cls\_SetInterval\_OatLeastLessThan\_empty_0, axiom)$   
 $c\_SetInterval\_OatLeastLessThan(v\_m, c\_Suc(v\_m), tc\_nat) = c\_insert(v\_m, c\_emptyset, tc\_nat) \quad cnf(cls\_SetInterval\_OatLeastLessThan\_Suc_0, axiom)$   
 $c\_emptyset \neq c\_insert(v\_a, v\_A, t\_a) \quad cnf(cls\_Set\_Oempty\_not\_insert_0, axiom)$   
 $c\_lessequals(v\_U, v\_x(v\_U), tc\_nat) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $v\_x(v\_U) = v\_nat \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $class\_Orderings\_Oorder(tc\_nat) \quad cnf(cls\_arity\_nat_3, axiom)$

**SWV255-2.p** Cryptographic protocol problem for messages

$c\_lessequals(v\_U, v\_xb(v\_U), tc\_nat) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_ONonce(v\_U), c\_Message\_Oparts(c\_insert(v\_msg_1, c\_emptyset, tc\_Message\_Omsg)), tc\_Message\_Omsg) = c\_emptyset$   
 $\neg c\_lessequals(v\_x, v\_U, tc\_nat) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_ONonce(v\_U), c\_Message\_Oparts(c\_insert(v\_msg_2, c\_emptyset, tc\_Message\_Omsg)), tc\_Message\_Omsg) = c\_emptyset$   
 $\neg c\_lessequals(v\_xa, v\_U, tc\_nat) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_ONonce(v\_xb(v\_U)), c\_Message\_Oparts(c\_insert(v\_msg_2, c\_emptyset, tc\_Message\_Omsg)), tc\_Message\_Omsg) = c\_emptyset$   
 $c\_lessequals(c\_plus(v\_m, v\_k, tc\_nat), v\_n, tc\_nat) \Rightarrow c\_lessequals(v\_k, v\_n, tc\_nat) \quad cnf(cls\_Nat\_Oadd\_leE_0, axiom)$   
 $c\_lessequals(c\_plus(v\_m, v\_k, tc\_nat), v\_n, tc\_nat) \Rightarrow c\_lessequals(v\_m, v\_n, tc\_nat) \quad cnf(cls\_Nat\_Oadd\_leE_1, axiom)$

**SWV256-2.p** Cryptographic protocol problem for messages

$\neg c\_lessequals(c\_Message\_Oparts(c\_Message\_Oanalz(v\_H)), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c\_lessequals(c\_Message\_Oanalz(v\_H), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_Message\_Oanalz\_subset_0, axiom)$   
 $c\_lessequals(v\_G, c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg))$

**SWV257-2.p** Cryptographic protocol problem for messages

$\neg c\_lessequals(c\_Message\_Oparts(v\_H), c\_Message\_Oparts(c\_Message\_Oanalz(v\_H)), tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c\_lessequals(v\_H, c\_Message\_Oanalz(v\_H), tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_Message\_Oanalz\_increasing_0, axiom)$   
 $c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg))$

**SWV258-1.p** Cryptographic protocol problem for messages

include('Axioms/MSC001-0.ax')

include('Axioms/MSC001-1.ax')

include('Axioms/SWV005-0.ax')

$c.in(v.c, c.Message\_Oparts(c.union(v.G, v.H, tc.Message\_Omsg)), tc.Message\_Omsg) \Rightarrow (c.in(v.c, c.Message\_Oparts(v.H), tc.Message\_Omsg) \vee c.in(c.Message\_Omsg\_OCrypt(v.K, v.X), c.Message\_Oparts(v.H), tc.Message\_Omsg) \Rightarrow c.in(v.X, c.Message\_Oparts(v.H), tc.Message\_Omsg))$   
 $c.Message\_Oparts(c.Message\_Oparts(v.H)) = c.Message\_Oparts(v.H) \quad \text{cnf}(cls\_Message\_Oparts\_idem_0, axiom)$   
 $c.in(v.X, c.Message\_Oparts(c.Message\_Oparts(v.H)), tc.Message\_Omsg) \Rightarrow c.in(v.X, c.Message\_Oparts(v.H), tc.Message\_Omsg)$   
 $c.lessequals(c.Message\_Oparts(v.G), c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg)) \Rightarrow c.lessequals(v.G, c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg))$   
 $c.lessequals(v.G, c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg)) \Rightarrow c.lessequals(c.Message\_Oparts(v.G), c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg))$   
 $c.in(v.X, c.Message\_Oparts(v.H), tc.Message\_Omsg) \quad \text{cnf}(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c.lessequals(c.Message\_Oparts(c.insert(v.X, v.H, tc.Message\_Omsg)), c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg))$

**SWV258-2.p** Cryptographic protocol problem for messages

$c.in(v.X, c.Message\_Oparts(v.H), tc.Message\_Omsg) \quad \text{cnf}(cls\_conjecture_0, negated\_conjecture)$

$\neg c.lessequals(c.Message\_Oparts(c.insert(v.X, v.H, tc.Message\_Omsg)), c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg))$

$c.lessequals(c.Message\_Oparts(v.G), c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg)) \Rightarrow c.lessequals(v.G, c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg))$

$c.lessequals(v.G, c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg)) \Rightarrow c.lessequals(c.Message\_Oparts(v.G), c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg))$

$(c.in(v.x, v.B, t.a) \text{ and } c.lessequals(v.A, v.B, tc.set(t.a))) \Rightarrow c.lessequals(c.insert(v.x, v.A, t.a), v.B, tc.set(t.a)) \quad \text{cnf}(cls\_Set\_Oinsert\_subset_1, axiom)$

$c.lessequals(v.A, v.A, tc.set(t.a)) \quad \text{cnf}(cls\_Set\_Osubset\_refl_0, axiom)$

**SWV259-1.p** Cryptographic protocol problem for messages

include('Axioms/MSC001-0.ax')

include('Axioms/MSC001-1.ax')

include('Axioms/SWV005-0.ax')

$c.in(v.c, c.Message\_Oparts(c.union(v.G, v.H, tc.Message\_Omsg)), tc.Message\_Omsg) \Rightarrow (c.in(v.c, c.Message\_Oparts(v.H), tc.Message\_Omsg) \vee c.in(c.Message\_Omsg\_OCrypt(v.K, v.X), c.Message\_Oparts(v.H), tc.Message\_Omsg) \Rightarrow c.in(v.X, c.Message\_Oparts(v.H), tc.Message\_Omsg))$

$c.Message\_Oparts(c.Message\_Oparts(v.H)) = c.Message\_Oparts(v.H) \quad \text{cnf}(cls\_Message\_Oparts\_idem_0, axiom)$

$c.in(v.X, c.Message\_Oparts(c.Message\_Oparts(v.H)), tc.Message\_Omsg) \Rightarrow c.in(v.X, c.Message\_Oparts(v.H), tc.Message\_Omsg)$

$c.lessequals(c.Message\_Oparts(v.G), c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg)) \Rightarrow c.lessequals(v.G, c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg))$

$c.lessequals(v.G, c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg)) \Rightarrow c.lessequals(c.Message\_Oparts(v.G), c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg))$

$c.in(v.X, c.Message\_Oparts(v.H), tc.Message\_Omsg) \quad \text{cnf}(cls\_conjecture_0, negated\_conjecture)$

$\neg c.lessequals(c.Message\_Oparts(v.H), c.Message\_Oparts(c.insert(v.X, v.H, tc.Message\_Omsg)), tc.set(tc.Message\_Omsg))$

**SWV259-2.p** Cryptographic protocol problem for messages

$\neg c.lessequals(c.Message\_Oparts(v.H), c.Message\_Oparts(c.insert(v.X, v.H, tc.Message\_Omsg)), tc.set(tc.Message\_Omsg))$

$c.lessequals(c.Message\_Oparts(v.G), c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg)) \Rightarrow c.lessequals(v.G, c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg))$

$c.lessequals(v.G, c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg)) \Rightarrow c.lessequals(c.Message\_Oparts(v.G), c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg))$

$c.lessequals(c.insert(v.x, v.A, t.a), v.B, tc.set(t.a)) \Rightarrow c.lessequals(v.A, v.B, tc.set(t.a)) \quad \text{cnf}(cls\_Set\_Oinsert\_subset_1, axiom)$

$c.lessequals(v.A, v.A, tc.set(t.a)) \quad \text{cnf}(cls\_Set\_Osubset\_refl_0, axiom)$

**SWV260-2.p** Cryptographic protocol problem for messages

$c.in(v.Y, c.Message\_Oparts(c.insert(v.X, v.G, tc.Message\_Omsg)), tc.Message\_Omsg) \quad \text{cnf}(cls\_conjecture_0, negated\_conjecture)$

$c.in(v.X, c.Message\_Oparts(v.H), tc.Message\_Omsg) \quad \text{cnf}(cls\_conjecture_1, negated\_conjecture)$

$\neg c.in(v.Y, c.Message\_Oparts(c.union(v.G, v.H, tc.Message\_Omsg)), tc.Message\_Omsg) \quad \text{cnf}(cls\_conjecture_2, negated\_conjecture)$

$c.in(v.X, v.H, tc.Message\_Omsg) \Rightarrow c.in(v.X, c.Message\_Oparts(v.H), tc.Message\_Omsg) \quad \text{cnf}(cls\_Message\_Oparts\_OInj_0, axiom)$

$c.in(v.c, v.B, t.a) \Rightarrow c.in(v.c, c.union(v.A, v.B, t.a), t.a) \quad \text{cnf}(cls\_Set\_OUncI_0, axiom)$

$c.in(v.c, v.A, t.a) \Rightarrow c.in(v.c, c.union(v.A, v.B, t.a), t.a) \quad \text{cnf}(cls\_Set\_OUncI_1, axiom)$

$c.in(v.a, c.insert(v.b, v.A, t.a), t.a) \Rightarrow (c.in(v.a, v.A, t.a) \text{ or } v.a = v.b) \quad \text{cnf}(cls\_Set\_OinsertE_0, axiom)$

$c.in(c\_Main\_OsubsetI_{-1}(v.A, v.B, t.a), v.A, t.a) \text{ or } c.lessequals(v.A, v.B, tc.set(t.a)) \quad \text{cnf}(cls\_Set\_OsubsetI_0, axiom)$

$c.in(c\_Main\_OsubsetI_{-1}(v.A, v.B, t.a), v.B, t.a) \Rightarrow c.lessequals(v.A, v.B, tc.set(t.a)) \quad \text{cnf}(cls\_Set\_OsubsetI_1, axiom)$

$(c.in(v.X, c.Message\_Oparts(v.G), tc.Message\_Omsg) \text{ and } c.lessequals(v.G, c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg))) \Rightarrow c.in(v.X, c.Message\_Oparts(v.H), tc.Message\_Omsg) \quad \text{cnf}(cls\_Message\_Oparts\_trans_0, axiom)$

**SWV261-1.p** Cryptographic protocol problem for messages

include('Axioms/MSC001-0.ax')

include('Axioms/MSC001-2.ax')

include('Axioms/SWV004-0.ax')

$c.lessequals(c.Message\_Oparts(c.union(v.G, v.H, tc.Message\_Omsg)), c.union(c.Message\_Oparts(v.G), c.Message\_Oparts(v.H), tc.Message\_Omsg))$

$c.lessequals(v.G, v.H, tc.set(tc.Message\_Omsg)) \Rightarrow c.lessequals(c.Message\_Oparts(v.G), c.Message\_Oparts(v.H), tc.set(tc.Message\_Omsg))$

$c.in(v.X, c.Message\_Osynth(c.Message\_Osynth(v.H)), tc.Message\_Omsg) \Rightarrow c.in(v.X, c.Message\_Osynth(v.H), tc.Message\_Omsg)$

$(c.lessequals(v.B, v.C, tc.set(t.a)) \text{ and } c.lessequals(v.A, v.B, tc.set(t.a))) \Rightarrow c.lessequals(v.A, v.C, tc.set(t.a)) \quad \text{cnf}(cls\_Set\_OsubsetI_1, axiom)$

$c\_in(v\_X, v\_G, tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c\_lessequals(c\_Message\_Oparts(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), c\_union(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H)))$

**SWV261-2.p** Cryptographic protocol problem for messages

$c\_in(v\_X, v\_G, tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c\_lessequals(c\_Message\_Oparts(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), c\_union(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H)))$   
 $c\_lessequals(c\_Message\_Oparts(c\_union(v\_G, v\_H, tc\_Message\_Omsg)), c\_union(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H)))$   
 $c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg))$   
 $c\_in(v\_c, v\_B, t\_a) \Rightarrow c\_in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a) \quad cnf(cls\_Set\_OUncI_0, axiom)$   
 $c\_in(v\_c, v\_A, t\_a) \Rightarrow c\_in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a) \quad cnf(cls\_Set\_OUncI_1, axiom)$   
 $c\_in(v\_a, c\_insert(v\_b, v\_A, t\_a), t\_a) \Rightarrow (c\_in(v\_a, v\_A, t\_a) \text{ or } v\_a = v\_b) \quad cnf(cls\_Set\_OinsertE_0, axiom)$   
 $c\_in(c\_Main\_OsubsetI\_1(v\_A, v\_B, t\_a), v\_A, t\_a) \text{ or } c\_lessequals(v\_A, v\_B, tc\_set(t\_a)) \quad cnf(cls\_Set\_OsubsetI_0, axiom)$   
 $c\_in(c\_Main\_OsubsetI\_1(v\_A, v\_B, t\_a), v\_B, t\_a) \Rightarrow c\_lessequals(v\_A, v\_B, tc\_set(t\_a)) \quad cnf(cls\_Set\_OsubsetI_1, axiom)$   
 $(c\_lessequals(v\_B, v\_C, tc\_set(t\_a)) \text{ and } c\_lessequals(v\_A, v\_B, tc\_set(t\_a))) \Rightarrow c\_lessequals(v\_A, v\_C, tc\_set(t\_a)) \quad cnf(cls\_Set\_OtransI, axiom)$

**SWV262-1.p** Cryptographic protocol problem for messages

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-1.ax')$   
 $include('Axioms/SWV005-0.ax')$   
 $c\_in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $c\_Message\_Oparts(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)) = c\_union(c\_Message\_Oparts(c\_insert(v\_X, c\_emptyset, tc\_Message\_Omsg)), c\_Message\_Oparts(v\_H))$   
 $c\_union(c\_union(v\_A, v\_B, t\_a), v\_C, t\_a) = c\_union(v\_A, c\_union(v\_B, v\_C, t\_a), t\_a) \quad cnf(cls\_Set\_OUncAssoc_0, axiom)$   
 $c\_Message\_Oparts(c\_insert(v\_X, c\_insert(v\_Y, v\_H, tc\_Message\_Omsg), tc\_Message\_Omsg)) \neq c\_union(c\_union(c\_Message\_Oparts(v\_X), c\_Message\_Oparts(v\_Y)), c\_Message\_Oparts(v\_H))$

**SWV262-2.p** Cryptographic protocol problem for messages

$c\_Message\_Oparts(c\_insert(v\_X, c\_insert(v\_Y, v\_H, tc\_Message\_Omsg), tc\_Message\_Omsg)) \neq c\_union(c\_union(c\_Message\_Oparts(v\_X), c\_Message\_Oparts(v\_Y)), c\_Message\_Oparts(v\_H))$   
 $c\_Message\_Oparts(c\_union(v\_G, v\_H, tc\_Message\_Omsg)) = c\_union(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $c\_union(c\_emptyset, v\_y, t\_a) = v\_y \quad cnf(cls\_Set\_OUncEmpty\_left_0, axiom)$   
 $c\_union(c\_insert(v\_a, v\_B, t\_a), v\_C, t\_a) = c\_insert(v\_a, c\_union(v\_B, v\_C, t\_a), t\_a) \quad cnf(cls\_Set\_OUncInsert\_left_0, axiom)$

**SWV263-1.p** Cryptographic protocol problem for messages

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-2.ax')$   
 $c\_Message\_Oagent\_OServer \neq c\_Message\_Oagent\_OFriend(v\_nat\_H) \quad cnf(cls\_Message\_Oagent\_Odistinguish\_1\_iff1_0, axiom)$   
 $c\_Message\_Oagent\_OFriend(v\_nat\_H) \neq c\_Message\_Oagent\_OServer \quad cnf(cls\_Message\_Oagent\_Odistinguish\_2\_iff1_0, axiom)$   
 $c\_Message\_Oagent\_OServer \neq c\_Message\_Oagent\_OSpy \quad cnf(cls\_Message\_Oagent\_Odistinguish\_3\_iff1_0, axiom)$   
 $c\_Message\_Oagent\_OSpy \neq c\_Message\_Oagent\_OServer \quad cnf(cls\_Message\_Oagent\_Odistinguish\_4\_iff1_0, axiom)$   
 $c\_Message\_Oagent\_OFriend(v\_nat) \neq c\_Message\_Oagent\_OSpy \quad cnf(cls\_Message\_Oagent\_Odistinguish\_5\_iff1_0, axiom)$   
 $c\_Message\_Oagent\_OSpy \neq c\_Message\_Oagent\_OFriend(v\_nat) \quad cnf(cls\_Message\_Oagent\_Odistinguish\_6\_iff1_0, axiom)$   
 $c\_Message\_Oagent\_OFriend(v\_nat) = c\_Message\_Oagent\_OFriend(v\_nat\_H) \Rightarrow v\_nat = v\_nat\_H \quad cnf(cls\_Message\_Oagent\_OIdentify, axiom)$   
 $c\_Message\_Omsg\_OAgent(v\_agent) = c\_Message\_Omsg\_OAgent(v\_agent\_H) \Rightarrow v\_agent = v\_agent\_H \quad cnf(cls\_Message\_Omsg\_OIdentify, axiom)$   
 $c\_Message\_Omsg\_ONumber(v\_nat) = c\_Message\_Omsg\_ONumber(v\_nat\_H) \Rightarrow v\_nat = v\_nat\_H \quad cnf(cls\_Message\_Omsg\_OIdentify, axiom)$   
 $c\_Message\_Omsg\_ONonce(v\_nat) = c\_Message\_Omsg\_ONonce(v\_nat\_H) \Rightarrow v\_nat = v\_nat\_H \quad cnf(cls\_Message\_Omsg\_OIdentify, axiom)$   
 $c\_Message\_Omsg\_OKey(v\_nat) = c\_Message\_Omsg\_OKey(v\_nat\_H) \Rightarrow v\_nat = v\_nat\_H \quad cnf(cls\_Message\_Omsg\_OIdentify, axiom)$   
 $c\_Message\_Omsg\_OHash(v\_msg) = c\_Message\_Omsg\_OHash(v\_msg\_H) \Rightarrow v\_msg = v\_msg\_H \quad cnf(cls\_Message\_Omsg\_OIdentify, axiom)$   
 $c\_Message\_Omsg\_OMPair(v\_msg_1, v\_msg_2) = c\_Message\_Omsg\_OMPair(v\_msg1\_H, v\_msg2\_H) \Rightarrow v\_msg_1 = v\_msg1\_H \quad cnf(cls\_Message\_Omsg\_OIdentify, axiom)$   
 $c\_Message\_Omsg\_OMPair(v\_msg_1, v\_msg_2) = c\_Message\_Omsg\_OMPair(v\_msg1\_H, v\_msg2\_H) \Rightarrow v\_msg_2 = v\_msg2\_H \quad cnf(cls\_Message\_Omsg\_OIdentify, axiom)$   
 $c\_Message\_Omsg\_OCrypt(v\_nat, v\_msg) = c\_Message\_Omsg\_OCrypt(v\_nat\_H, v\_msg\_H) \Rightarrow v\_nat = v\_nat\_H \quad cnf(cls\_Message\_Omsg\_OIdentify, axiom)$   
 $c\_Message\_Omsg\_OCrypt(v\_nat, v\_msg) = c\_Message\_Omsg\_OCrypt(v\_nat\_H, v\_msg\_H) \Rightarrow v\_msg = v\_msg\_H \quad cnf(cls\_Message\_Omsg\_OIdentify, axiom)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $c\_in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $c\_in(v\_X, v\_H, tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oparts\_OInj_0, axiom)$   
 $c\_in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_Y, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c\_in(v\_X, v\_G, tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_2, negated\_conjecture)$

**SWV263-2.p** Cryptographic protocol problem for messages

$c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c\_in(v\_X, v\_G, tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c\_in(v\_X, v\_H, tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oparts\_OInj_0, axiom)$





$\neg c\_in(v\_X, c\_union(c\_Message\_Oparts(v\_H), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture_0)$

**SWV272-2.p** Cryptographic protocol problem for messages

$c\_in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_union(c\_Message\_Oparts(v\_H), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture_0)$   
 $\neg c\_in(v\_X, c\_union(c\_Message\_Oparts(v\_H), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture_0)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \Rightarrow (c\_in(v\_X, c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \wedge c\_in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oparts\_OInj_0, axiom)$   
 $c\_in(v\_X, v\_H, tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oparts\_OInj_0, axiom)$   
 $c\_in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a) \Rightarrow (c\_in(v\_c, v\_B, t\_a) \vee c\_in(v\_c, v\_A, t\_a)) \quad cnf(cls\_Set\_OU\_iff_0, axiom)$   
 $c\_in(v\_c, v\_A, t\_a) \Rightarrow c\_in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a) \quad cnf(cls\_Set\_OU\_iff_1, axiom)$   
 $c\_in(v\_c, v\_B, t\_a) \Rightarrow c\_in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a) \quad cnf(cls\_Set\_OU\_iff_2, axiom)$

**SWV273-1.p** Cryptographic protocol problem for messages

include('Axioms/MS001-0.ax')  
include('Axioms/MS001-1.ax')  
include('Axioms/SWV005-0.ax')  
include('Axioms/SWV005-1.ax')  
 $c\_in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture_0)$   
 $c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_Message\_Oparts\_OInj_0, axiom)$   
 $c\_lessequals(v\_H, c\_Message\_Osynth(v\_H), tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_Message\_Osynth\_increasing_0, axiom)$   
 $\neg c\_lessequals(c\_union(c\_Message\_Oparts(v\_H), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg), c\_Message\_Oparts(c\_Message\_Osynth(v\_H), tc\_set(tc\_Message\_Omsg))) \quad cnf(cls\_conjecture_0, negated\_conjecture_0)$

**SWV273-2.p** Cryptographic protocol problem for messages

$\neg c\_lessequals(c\_union(c\_Message\_Oparts(v\_H), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg), c\_Message\_Oparts(c\_Message\_Osynth(v\_H), tc\_set(tc\_Message\_Omsg))) \quad cnf(cls\_conjecture_0, negated\_conjecture_0)$   
 $c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_Message\_Oparts\_OInj_0, axiom)$   
 $c\_lessequals(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(v\_G, c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_Message\_Oparts\_OInj_0, axiom)$   
 $c\_lessequals(v\_H, c\_Message\_Osynth(v\_H), tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_Message\_Osynth\_increasing_0, axiom)$   
 $(c\_lessequals(v\_B, v\_C, tc\_set(t\_a)) \wedge c\_lessequals(v\_A, v\_C, tc\_set(t\_a))) \Rightarrow c\_lessequals(c\_union(v\_A, v\_B, t\_a), v\_C, tc\_set(t\_a)) \quad cnf(cls\_Set\_Osubset\_refl_0, axiom)$   
 $c\_lessequals(v\_A, v\_A, tc\_set(t\_a)) \quad cnf(cls\_Set\_Osubset\_refl_0, axiom)$

**SWV274-1.p** Cryptographic protocol problem for messages

include('Axioms/MS001-0.ax')  
include('Axioms/MS001-2.ax')  
include('Axioms/SWV004-0.ax')  
 $c\_in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture_0)$   
 $c\_in(v\_X, c\_Message\_Osynth(c\_Message\_Osynth(v\_H)), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture_0)$   
 $(c\_in(v\_X, c\_Message\_Osynth(v\_G), tc\_Message\_Omsg) \wedge c\_lessequals(v\_G, c\_Message\_Osynth(v\_H), tc\_set(tc\_Message\_Omsg))) \Rightarrow c\_in(v\_X, c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Osynth\_trans_0, axiom)$   
 $c\_in(v\_Y, c\_Message\_Osynth(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture_0)$   
 $c\_in(v\_X, c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture_1)$   
 $\neg c\_in(v\_Y, c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_2, negated\_conjecture_2)$

**SWV274-2.p** Cryptographic protocol problem for messages

$c\_in(v\_X, v\_H, tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Osynth\_OInj_0, axiom)$   
 $(c\_in(v\_X, c\_Message\_Osynth(v\_G), tc\_Message\_Omsg) \wedge c\_lessequals(v\_G, c\_Message\_Osynth(v\_H), tc\_set(tc\_Message\_Omsg))) \Rightarrow c\_in(v\_X, c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Osynth\_trans_0, axiom)$   
 $c\_in(v\_a, c\_insert(v\_b, v\_A, t\_a), t\_a) \Rightarrow (c\_in(v\_a, v\_A, t\_a) \vee v\_a = v\_b) \quad cnf(cls\_Set\_OinsertE_0, axiom)$   
 $c\_in(c\_Main\_OsubsetI\_1(v\_A, v\_B, t\_a), v\_A, t\_a) \vee c\_lessequals(v\_A, v\_B, tc\_set(t\_a)) \quad cnf(cls\_Set\_OsubsetI_0, axiom)$   
 $c\_in(c\_Main\_OsubsetI\_1(v\_A, v\_B, t\_a), v\_B, t\_a) \Rightarrow c\_lessequals(v\_A, v\_B, tc\_set(t\_a)) \quad cnf(cls\_Set\_OsubsetI_1, axiom)$   
 $c\_in(v\_Y, c\_Message\_Osynth(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture_0)$   
 $c\_in(v\_X, c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture_1)$   
 $\neg c\_in(v\_Y, c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_2, negated\_conjecture_2)$

**SWV275-1.p** Cryptographic protocol problem for messages

include('Axioms/MS001-0.ax')  
include('Axioms/MS001-2.ax')  
include('Axioms/SWV004-0.ax')  
 $c\_in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture_0)$   
 $c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_Osynth(v\_G), c\_Message\_Osynth(v\_H), tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_Message\_Oparts\_OInj_0, axiom)$   
 $\neg c\_lessequals(c\_insert(v\_X, c\_Message\_Osynth(v\_H), tc\_Message\_Omsg), c\_Message\_Osynth(c\_insert(v\_X, v\_H, tc\_Message\_Omsg))) \quad cnf(cls\_conjecture_0, negated\_conjecture_0)$

**SWV275-2.p** Cryptographic protocol problem for messages

$c\_in(v\_X, v\_H, tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Osynth\_OInj_0, axiom)$



$c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_Osynth(v\_G), c\_Message\_Osynth(v\_H), tc\_set(tc\_Message\_Omsg))$   
 $c\_in(v\_a, v\_B, t\_a) \Rightarrow c\_in(v\_a, c\_insert(v\_b, v\_B, t\_a), t\_a) \quad cnf(cls\_Set\_OinsertCI_0, axiom)$   
 $c\_in(v\_x, c\_insert(v\_x, v\_B, t\_a), t\_a) \quad cnf(cls\_Set\_OinsertCI_1, axiom)$   
 $c\_in(v\_a, c\_insert(v\_b, v\_A, t\_a), t\_a) \Rightarrow (c\_in(v\_a, v\_A, t\_a) \text{ or } v\_a = v\_b) \quad cnf(cls\_Set\_OinsertE_0, axiom)$   
 $(c\_in(v\_c, v\_A, t\_a) \text{ and } c\_lessequals(v\_A, v\_B, tc\_set(t\_a))) \Rightarrow c\_in(v\_c, v\_B, t\_a) \quad cnf(cls\_Set\_OsubsetD_0, axiom)$   
 $c\_in(c\_Main\_OsubsetI_{-1}(v\_A, v\_B, t\_a), v\_A, t\_a) \text{ or } c\_lessequals(v\_A, v\_B, tc\_set(t\_a)) \quad cnf(cls\_Set\_OsubsetI_0, axiom)$   
 $c\_in(c\_Main\_OsubsetI_{-1}(v\_A, v\_B, t\_a), v\_B, t\_a) \Rightarrow c\_lessequals(v\_A, v\_B, tc\_set(t\_a)) \quad cnf(cls\_Set\_OsubsetI_1, axiom)$   
 $\neg c\_lessequals(c\_insert(v\_X, c\_Message\_Osynth(v\_H), tc\_Message\_Omsg), c\_Message\_Osynth(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)))$

**SWV276-1.p** Cryptographic protocol problem for events

include('Axioms/MSC001-0.ax')  
include('Axioms/MSC001-1.ax')  
include('Axioms/SWV005-0.ax')  
include('Axioms/SWV005-2.ax')  
 $c\_lessequals(c\_Message\_Oanalz(v\_H), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_Message\_Oanalz\_subset\_0, axiom)$   
 $c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_OkeysFor(v\_G), c\_Message\_OkeysFor(v\_H), tc\_set(tc\_Message\_Omsg))$   
 $c\_in(v\_X, v\_G, tc\_Message\_Omsg) \Rightarrow c\_lessequals(c\_Message\_Oparts(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), c\_union(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)))$   
 $c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg))$   
 $c\_in(v\_K, c\_Message\_OkeysFor(c\_Message\_Oparts(c\_insert(v\_X, v\_G, tc\_Message\_Omsg))), tc\_nat) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c\_in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(v\_H)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c\_in(v\_K, c\_Message\_OkeysFor(c\_Message\_Oparts(c\_union(v\_G, v\_H, tc\_Message\_Omsg))), tc\_nat) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $\neg c\_in(c\_Message\_Omsg\_OKey(c\_Message\_OinvKey(v\_K)), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_3, negated\_conjecture)$

**SWV276-2.p** Cryptographic protocol problem for events

$c\_in(v\_K, c\_Message\_OkeysFor(c\_Message\_Osynth(v\_H)), tc\_nat) \Rightarrow (c\_in(v\_K, c\_Message\_OkeysFor(v\_H), tc\_nat) \text{ or } c\_in(c\_Message\_Osynth(v\_H), tc\_nat))$   
 $c\_in(v\_K, c\_Message\_OkeysFor(c\_Message\_Osynth(v\_H)), tc\_nat) \Rightarrow (c\_in(v\_K, c\_Message\_OkeysFor(v\_H), tc\_nat) \text{ or } v\_K = c\_Message\_OinvKey(v\_sko\_uhi(v\_H, v\_K))) \quad cnf(cls\_Event\_OkeysFor\_synth\_H_1, axiom)$   
 $c\_in(v\_X, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oanalz\_subset\_0, axiom)$   
 $c\_lessequals(c\_Message\_Oanalz(v\_H), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_Message\_Oanalz\_subset\_0, axiom)$   
 $c\_Message\_OinvKey(c\_Message\_OinvKey(v\_y)) = v\_y \quad cnf(cls\_Message\_OinvKey\_A\_InvKey\_Ay\_JA.61.61\_Ay_0, axiom)$   
 $c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_OkeysFor(v\_G), c\_Message\_OkeysFor(v\_H), tc\_set(tc\_Message\_Omsg))$   
 $c\_Message\_OkeysFor(c\_union(v\_H, v\_H, tc\_Message\_Omsg)) = c\_union(c\_Message\_OkeysFor(v\_H), c\_Message\_OkeysFor(v\_H))$   
 $c\_Message\_Oparts(c\_Message\_Oanalz(v\_H)) = c\_Message\_Oparts(v\_H) \quad cnf(cls\_Message\_Oparts\_analz_0, axiom)$   
 $c\_in(v\_X, v\_G, tc\_Message\_Omsg) \Rightarrow c\_lessequals(c\_Message\_Oparts(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), c\_union(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)))$   
 $c\_Message\_Oparts(c\_Message\_Osynth(v\_H)) = c\_union(c\_Message\_Oparts(v\_H), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg)$   
 $c\_Message\_Oparts(c\_union(v\_G, v\_H, tc\_Message\_Omsg)) = c\_union(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg))$   
 $(c\_in(v\_c, v\_A, t\_a) \text{ and } c\_lessequals(v\_A, v\_B, tc\_set(t\_a))) \Rightarrow c\_in(v\_c, v\_B, t\_a) \quad cnf(cls\_Set\_OsubsetD_0, axiom)$   
 $c\_in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a) \Rightarrow (c\_in(v\_c, v\_B, t\_a) \text{ or } c\_in(v\_c, v\_A, t\_a)) \quad cnf(cls\_Set\_OU\_iff_0, axiom)$   
 $c\_in(v\_c, v\_A, t\_a) \Rightarrow c\_in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a) \quad cnf(cls\_Set\_OU\_iff_1, axiom)$   
 $c\_in(v\_c, v\_B, t\_a) \Rightarrow c\_in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a) \quad cnf(cls\_Set\_OU\_iff_2, axiom)$   
 $c\_in(v\_K, c\_Message\_OkeysFor(c\_Message\_Oparts(c\_insert(v\_X, v\_G, tc\_Message\_Omsg))), tc\_nat) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c\_in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(v\_H)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c\_in(v\_K, c\_Message\_OkeysFor(c\_Message\_Oparts(c\_union(v\_G, v\_H, tc\_Message\_Omsg))), tc\_nat) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $\neg c\_in(c\_Message\_Omsg\_OKey(c\_Message\_OinvKey(v\_K)), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_3, negated\_conjecture)$

**SWV277-1.p** Cryptographic protocol problem for events

include('Axioms/MSC001-0.ax')  
include('Axioms/MSC001-1.ax')  
include('Axioms/SWV005-0.ax')  
include('Axioms/SWV005-2.ax')  
 $c\_lessequals(c\_Message\_Oanalz(v\_H), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_Message\_Oanalz\_subset\_0, axiom)$   
 $c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_OkeysFor(v\_G), c\_Message\_OkeysFor(v\_H), tc\_set(tc\_Message\_Omsg))$   
 $c\_in(v\_X, v\_G, tc\_Message\_Omsg) \Rightarrow c\_lessequals(c\_Message\_Oparts(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), c\_union(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)))$   
 $c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg))$   
 $c\_in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(v\_H)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c\_in(c\_Message\_Omsg\_OKey(c\_Message\_OinvKey(v\_K)), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c\_in(v\_K, c\_Message\_OkeysFor(c\_Message\_Oparts(v\_H)), tc\_nat) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c\_in(v\_K, c\_Message\_OkeysFor(c\_Message\_Oanalz(v\_H)), tc\_nat) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $\neg c\_in(v\_K, c\_Message\_OkeysFor(c\_Message\_Oparts(v\_G)), tc\_nat) \quad cnf(cls\_conjecture_4, negated\_conjecture)$

**SWV277-2.p** Cryptographic protocol problem for events

$c\_lessequals(c\_Message\_Oanalz(v\_H), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_Message\_Oanalz\_subset\_)$   
 $c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_OkeysFor(v\_G), c\_Message\_OkeysFor(v\_H), tc\_set(tc\_Message\_Omsg))$   
 $(c\_in(v\_c, v\_A, t\_a) \text{ and } c\_lessequals(v\_A, v\_B, tc\_set(t\_a))) \Rightarrow c\_in(v\_c, v\_B, t\_a) \quad cnf(cls\_Set\_OsubsetD_0, axiom)$   
 $\neg c\_in(v\_K, c\_Message\_OkeysFor(c\_Message\_Oparts(v\_H)), tc\_nat) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c\_in(v\_K, c\_Message\_OkeysFor(c\_Message\_Oanalz(v\_H)), tc\_nat) \quad cnf(cls\_conjecture_3, negated\_conjecture)$

**SWV278-1.p** Cryptographic protocol problem for events

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-1.ax')$   
 $include('Axioms/SWV005-0.ax')$   
 $include('Axioms/SWV005-2.ax')$   
 $c\_lessequals(c\_Message\_Oanalz(v\_H), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)) \quad cnf(cls\_Message\_Oanalz\_subset\_)$   
 $c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_OkeysFor(v\_G), c\_Message\_OkeysFor(v\_H), tc\_set(tc\_Message\_Omsg))$   
 $c\_in(v\_X, v\_G, tc\_Message\_Omsg) \Rightarrow c\_lessequals(c\_Message\_Oparts(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), c\_union(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg)))$   
 $c\_lessequals(v\_G, v\_H, tc\_set(tc\_Message\_Omsg)) \Rightarrow c\_lessequals(c\_Message\_Oparts(v\_G), c\_Message\_Oparts(v\_H), tc\_set(tc\_Message\_Omsg))$   
 $c\_in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(v\_H)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c\_in(c\_Message\_Omsg\_OKey(c\_Message\_OinvKey(c\_Message\_OinvKey(v\_K\_H))), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $\neg c\_in(c\_Message\_OinvKey(v\_K\_H), c\_Message\_OkeysFor(c\_Message\_Oparts(v\_H)), tc\_nat) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_OKey(v\_K\_H), c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $\neg c\_in(c\_Message\_OinvKey(v\_K\_H), c\_Message\_OkeysFor(c\_Message\_Oparts(v\_G)), tc\_nat) \quad cnf(cls\_conjecture_4, negated\_conjecture)$

**SWV278-2.p** Cryptographic protocol problem for events

$\neg c\_in(c\_Message\_Omsg\_OKey(c\_Message\_OinvKey(c\_Message\_OinvKey(v\_K\_H))), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $c\_in(c\_Message\_Omsg\_OKey(v\_K\_H), c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c\_in(v\_X, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oanalz\_subset\_)$   
 $c\_Message\_OinvKey(c\_Message\_OinvKey(v\_y)) = v\_y \quad cnf(cls\_Message\_OinvKey\_A\_IinvKey\_Ay\_J\_A\_61\_61\_Ay_0, axiom)$

**SWV279-2.p** Cryptographic protocol problem for public

$c\_in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Event\_Oused(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c\_in(v\_Y, c\_Event\_Oused(v\_H), tc\_Message\_Omsg) \Rightarrow \neg c\_in(v\_X, c\_Event\_Oused(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_Y, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $c\_in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $c\_in(v\_X, v\_H, tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oparts\_OInj_0, axiom)$   
 $c\_in(v\_X, c\_Event\_Oused(v\_evs), tc\_Message\_Omsg) \Rightarrow c\_lessequals(c\_Message\_Oparts(c\_insert(v\_X, c\_emptyset, tc\_Message\_Omsg)), c\_insert(v\_X, v\_A, t\_a), t\_a) \quad cnf(cls\_Set\_Oinsert\_iff_1, axiom)$   
 $(c\_in(v\_c, v\_A, t\_a) \text{ and } c\_lessequals(v\_A, v\_B, tc\_set(t\_a))) \Rightarrow c\_in(v\_c, v\_B, t\_a) \quad cnf(cls\_Set\_OsubsetD_0, axiom)$

**SWV280-1.p** Cryptographic protocol problem for public

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-1.ax')$   
 $include('Axioms/SWV005-0.ax')$   
 $include('Axioms/SWV005-2.ax')$   
 $include('Axioms/SWV005-3.ax')$   
 $c\_lessequals(v\_n, c\_plus(v\_n, v\_m, tc\_nat), tc\_nat) \quad cnf(cls\_Nat\_Ole\_add1_0, axiom)$   
 $c\_lessequals(v\_n, c\_plus(v\_m, v\_n, tc\_nat), tc\_nat) \quad cnf(cls\_Nat\_Ole\_add2_0, axiom)$   
 $c\_less(v\_m, c\_Suc(v\_n), tc\_nat) \Rightarrow c\_lessequals(v\_m, v\_n, tc\_nat) \quad cnf(cls\_Nat\_Oless\_Suc\_eq\_le_0, axiom)$   
 $c\_lessequals(v\_m, v\_n, tc\_nat) \Rightarrow c\_less(v\_m, c\_Suc(v\_n), tc\_nat) \quad cnf(cls\_Nat\_Oless\_Suc\_eq\_le_1, axiom)$   
 $c\_in(c\_Message\_Omsg\_ONonce(v\_U), c\_Event\_Oused(v\_evs), tc\_Message\_Omsg) \Rightarrow \neg c\_lessequals(v\_sko\_urX(v\_evs), v\_U, tc\_nat)$   
 $c\_in(c\_Message\_Omsg\_ONonce(v\_U), c\_Event\_Oused(v\_evs), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture)$

**SWV280-2.p** Cryptographic protocol problem for public

$c\_in(c\_Message\_Omsg\_ONonce(v\_U), c\_Event\_Oused(v\_evs), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c\_lessequals(v\_n, c\_plus(v\_n, v\_m, tc\_nat), tc\_nat) \quad cnf(cls\_Nat\_Ole\_add1_0, axiom)$   
 $c\_in(c\_Message\_Omsg\_ONonce(v\_U), c\_Event\_Oused(v\_evs), tc\_Message\_Omsg) \Rightarrow \neg c\_lessequals(v\_sko\_urX(v\_evs), v\_U, tc\_nat)$

**SWV281-1.p** Cryptographic protocol problem for public

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-1.ax')$   
 $include('Axioms/SWV005-0.ax')$   
 $include('Axioms/SWV005-2.ax')$   
 $include('Axioms/SWV005-3.ax')$   
 $c\_lessequals(v\_n, c\_plus(v\_n, v\_m, tc\_nat), tc\_nat) \quad cnf(cls\_Nat\_Ole\_add1_0, axiom)$   
 $c\_lessequals(v\_n, c\_plus(v\_m, v\_n, tc\_nat), tc\_nat) \quad cnf(cls\_Nat\_Ole\_add2_0, axiom)$

$c\_less(v\_m, c\_Suc(v\_n), tc\_nat) \Rightarrow c\_lessequals(v\_m, v\_n, tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Oless\_Suc\_eq\_le}_0, \text{axiom})$   
 $c\_lessequals(v\_m, v\_n, tc\_nat) \Rightarrow c\_less(v\_m, c\_Suc(v\_n), tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Oless\_Suc\_eq\_le}_1, \text{axiom})$   
 $c\_in(c\_Message\_Omsg\_ONonce(v\_U), c\_Event\_Oused(v\_evs), tc\_Message\_Omsg) \Rightarrow \neg c\_lessequals(v\_sko\_urX(v\_evs), v\_U, tc\_nat)$   
 $v\_U = v\_V \text{ or } c\_in(c\_Message\_Omsg\_ONonce(v\_V), c\_Event\_Oused(v\_evs\_H), tc\_Message\_Omsg) \text{ or } c\_in(c\_Message\_Omsg\_ONonce(v\_U), c\_Event\_Oused(v\_evs\_H), tc\_Message\_Omsg)$

**SWV281-2.p** Cryptographic protocol problem for public

$v\_U = v\_V \text{ or } c\_in(c\_Message\_Omsg\_ONonce(v\_V), c\_Event\_Oused(v\_evs\_H), tc\_Message\_Omsg) \text{ or } c\_in(c\_Message\_Omsg\_ONonce(v\_U), c\_Event\_Oused(v\_evs\_H), tc\_Message\_Omsg)$   
 $c\_List\_Olist\_ONil \neq c\_List\_Olist\_OCons(v\_a\_H, v\_list\_H, t\_a) \quad \text{cnf}(\text{cls\_List\_Olist\_Odistinct\_l}_0, \text{axiom})$   
 $c\_lessequals(v\_n, c\_plus(v\_m, v\_n, tc\_nat), tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Ole\_add}_2, \text{axiom})$   
 $c\_plus(v\_m, v\_k, tc\_nat) = c\_plus(v\_n, v\_k, tc\_nat) \Rightarrow v\_m = v\_n \quad \text{cnf}(\text{cls\_Nat\_Onat\_add\_right\_cancel}_0, \text{axiom})$   
 $c\_plus(c_0, v\_y, tc\_nat) = v\_y \quad \text{cnf}(\text{cls\_Nat\_Oop\_A\_L\_Oadd\_l}_0, \text{axiom})$   
 $c\_in(c\_Message\_Omsg\_ONonce(v\_U), c\_Event\_Oused(v\_evs), tc\_Message\_Omsg) \Rightarrow \neg c\_lessequals(v\_sko\_urX(v\_evs), v\_U, tc\_nat)$

**SWV282-1.p** Cryptographic protocol problem for public

$\text{include('Axioms/MS001-0.ax')}$   
 $\text{include('Axioms/MS001-1.ax')}$   
 $\text{include('Axioms/SWV005-0.ax')}$   
 $\text{include('Axioms/SWV005-2.ax')}$   
 $\text{include('Axioms/SWV005-3.ax')}$   
 $c\_lessequals(v\_n, c\_plus(v\_n, v\_m, tc\_nat), tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Ole\_add}_1, \text{axiom})$   
 $c\_lessequals(v\_n, c\_plus(v\_m, v\_n, tc\_nat), tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Ole\_add}_2, \text{axiom})$   
 $c\_less(v\_m, c\_Suc(v\_n), tc\_nat) \Rightarrow c\_lessequals(v\_m, v\_n, tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Oless\_Suc\_eq\_le}_0, \text{axiom})$   
 $c\_lessequals(v\_m, v\_n, tc\_nat) \Rightarrow c\_less(v\_m, c\_Suc(v\_n), tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Oless\_Suc\_eq\_le}_1, \text{axiom})$   
 $c\_in(c\_Message\_Omsg\_ONonce(v\_U), c\_Event\_Oused(v\_evs), tc\_Message\_Omsg) \Rightarrow \neg c\_lessequals(v\_sko\_urX(v\_evs), v\_U, tc\_nat)$   
 $v\_U = v\_W \text{ or } v\_V = v\_W \text{ or } v\_U = v\_V \text{ or } c\_in(c\_Message\_Omsg\_ONonce(v\_W), c\_Event\_Oused(v\_evs\_H), tc\_Message\_Omsg)$

**SWV282-2.p** Cryptographic protocol problem for public

$v\_U = v\_W \text{ or } v\_V = v\_W \text{ or } v\_U = v\_V \text{ or } c\_in(c\_Message\_Omsg\_ONonce(v\_W), c\_Event\_Oused(v\_evs\_H), tc\_Message\_Omsg)$   
 $c\_Binomial\_Obinomial(v\_y, c\_Suc(c_0)) = v\_y \quad \text{cnf}(\text{cls\_Binomial\_Obinomial\_l}_0, \text{axiom})$   
 $c\_Binomial\_Obinomial(c\_Suc(v\_n), c\_Suc(v\_k)) = c\_plus(c\_Binomial\_Obinomial(v\_n, v\_k), c\_Binomial\_Obinomial(v\_n, c\_Suc(v\_l)))$   
 $c\_Binomial\_Obinomial(v\_n, c_0) = c_1 \quad \text{cnf}(\text{cls\_Binomial\_Obinomial\_n\_l}_0, \text{axiom})$   
 $c_1 = c\_Suc(c_0) \quad \text{cnf}(\text{cls\_Nat\_OOne\_nat\_def}_0, \text{axiom})$   
 $c\_minus(v\_m, v\_n, tc\_nat) = c_0 \Rightarrow c\_lessequals(v\_m, v\_n, tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Odiff\_is\_l}_0\_eq_0, \text{axiom})$   
 $c\_minus(v\_m, v\_m, tc\_nat) = c_0 \quad \text{cnf}(\text{cls\_Nat\_Odiff\_self\_eq\_l}_0, \text{axiom})$   
 $c\_lessequals(v\_n, c\_plus(v\_n, v\_m, tc\_nat), tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Ole\_add}_1, \text{axiom})$   
 $c\_less(v\_n, c\_Suc(v\_n), tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_OlessI}_0, \text{axiom})$   
 $c\_lessequals(v\_m, v\_n, tc\_nat) \Rightarrow c\_less(v\_m, c\_Suc(v\_n), tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Oless\_Suc\_eq\_le}_1, \text{axiom})$   
 $c\_lessequals(c\_plus(v\_k, v\_m, tc\_nat), c\_plus(v\_k, v\_n, tc\_nat), tc\_nat) \Rightarrow c\_lessequals(v\_m, v\_n, tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Onat\_add\_cancel}_0, \text{axiom})$   
 $\neg c\_less(c\_plus(v\_j, v\_i, tc\_nat), v\_i, tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Onot\_add\_less}_2, \text{axiom})$   
 $c\_in(c\_Message\_Omsg\_ONonce(v\_U), c\_Event\_Oused(v\_evs), tc\_Message\_Omsg) \Rightarrow \neg c\_lessequals(v\_sko\_urX(v\_evs), v\_U, tc\_nat)$   
 $c\_Finite\_Set\_Ocard(c\_SetInterval\_OatMost(v\_u, tc\_nat), tc\_nat) = c\_Suc(v\_u) \quad \text{cnf}(\text{cls\_SetInterval\_Ocard\_atMost}_0, \text{axiom})$

**SWV283-2.p** Cryptographic protocol problem for public

$c\_in(c\_Message\_Omsg\_ONonce(v\_U), c\_Message\_Oparts(c\_insert(v\_msg, c\_emptyset, tc\_Message\_Omsg)), tc\_Message\_Omsg) \Rightarrow \neg c\_lessequals(v\_sko\_upX(v\_msg), v\_U, tc\_nat) \quad \text{cnf}(\text{cls\_Message\_Omsg\_Nonce\_supply}_0, \text{axiom})$   
 $c\_lessequals(c\_plus(v\_m, v\_k, tc\_nat), v\_n, tc\_nat) \Rightarrow c\_lessequals(v\_k, v\_n, tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Oadd\_leE}_0, \text{axiom})$   
 $c\_lessequals(c\_plus(v\_m, v\_k, tc\_nat), v\_n, tc\_nat) \Rightarrow c\_lessequals(v\_m, v\_n, tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Oadd\_leE}_1, \text{axiom})$   
 $c\_in(c\_Message\_Omsg\_ONonce(v\_U), c\_Event\_Oused(v\_list), tc\_Message\_Omsg) \Rightarrow \neg c\_lessequals(v\_x, v\_U, tc\_nat) \quad \text{cnf}(\text{cls\_Message\_Omsg\_Nonce\_supply}_1, \text{axiom})$   
 $c\_lessequals(v\_W, v\_xd(v\_W), tc\_nat) \text{ or } c\_lessequals(v\_U, v\_xd(v\_U), tc\_nat) \quad \text{cnf}(\text{cls\_conjecture}_4, \text{negated\_conjecture})$   
 $c\_in(c\_Message\_Omsg\_ONonce(v\_xd(v\_X)), c\_Event\_Oused(v\_list), tc\_Message\_Omsg) \text{ or } c\_in(c\_Message\_Omsg\_ONonce(v\_xd(v\_X)), c\_Event\_Oused(v\_list), tc\_Message\_Omsg)$

**SWV284-1.p** Cryptographic protocol problem for shared

$\text{include('Axioms/MS001-0.ax')}$   
 $\text{include('Axioms/MS001-2.ax')}$   
 $\text{include('Axioms/SWV006-0.ax')}$   
 $c\_in(c\_Message\_Omsg\_ONonce(v\_U), c\_Message\_Oparts(c\_insert(v\_msg, c\_emptyset, tc\_Message\_Omsg)), tc\_Message\_Omsg) \Rightarrow \neg c\_lessequals(v\_sko\_upX(v\_msg), v\_U, tc\_nat) \quad \text{cnf}(\text{cls\_Message\_Omsg\_Nonce\_supply}_0, \text{axiom})$   
 $c\_lessequals(c\_plus(v\_m, v\_k, tc\_nat), v\_n, tc\_nat) \Rightarrow c\_lessequals(v\_k, v\_n, tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Oadd\_leE}_0, \text{axiom})$   
 $c\_lessequals(c\_plus(v\_m, v\_k, tc\_nat), v\_n, tc\_nat) \Rightarrow c\_lessequals(v\_m, v\_n, tc\_nat) \quad \text{cnf}(\text{cls\_Nat\_Oadd\_leE}_1, \text{axiom})$   
 $\neg c\_in(c\_Message\_Omsg\_ONonce(v\_N), c\_Message\_Oparts(c\_Event\_OinitState(v\_B)), tc\_Message\_Omsg) \quad \text{cnf}(\text{cls\_Shared\_ONonce}, \text{axiom})$   
 $c\_in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow c\_in(c\_Message\_Omsg\_OKey(c\_Shared\_OshrK(v\_A)), c\_Event\_Oknows(c\_Message\_Oagent), tc\_Message\_Oagent)$   
 $c\_Shared\_OshrK(v\_x) = c\_Shared\_OshrK(v\_y) \Rightarrow v\_x = v\_y \quad \text{cnf}(\text{cls\_Shared\_O91\_124\_AshrK\_Ax\_A\_61\_AshrK\_Ay\_59\_Ax}, \text{axiom})$

```
(c.in(c_Message.Omsg.OCrypt(v_K, v_X), c_Message.Oanalz(v_H), tc_Message.Omsg) and c.in(c_Message.Omsg.OKey(v_K),
c.in(v_X, c_Message.Oanalz(v_H), tc_Message.Omsg)    cnf(cls_Shared.Oanalz_DeCrypt_H_dest0, axiom)
c.in(c_Message.Omsg.OKey(c_Shared.OshrK(v_A)), c_Event.OinitState(v_A), tc_Message.Omsg)    cnf(cls_Shared.OshrK_...
c.in(c_Message.Omsg.OKey(c_Shared.OshrK(v_A)), c_Event.Oused(v_ews), tc_Message.Omsg)    cnf(cls_Shared.OshrK_in_...
c.lessequals(v_U, v_x(v_U), tc_nat)    cnf(cls_conjecture0, negated_conjecture)
c.in(c_Message.Omsg.ONonce(v_U), c_Event.Oused(v_list), tc_Message.Omsg)  $\Rightarrow$   $\neg$ c.lessequals(v_N, v_U, tc_nat)    cnf(cls_...
c.in(c_Message.Omsg.ONonce(v_x(v_U)), c_Event.Oused(v_list), tc_Message.Omsg) or c.in(c_Message.Omsg.ONonce(v_x(v_U)...
```

**SWV284-2.p** Cryptographic protocol problem for shared

```
c.lessequals(v_U, v_x(v_U), tc_nat)    cnf(cls_conjecture0, negated_conjecture)
c.in(c_Message.Omsg.ONonce(v_U), c_Event.Oused(v_list), tc_Message.Omsg)  $\Rightarrow$   $\neg$ c.lessequals(v_N, v_U, tc_nat)    cnf(cls_...
c.in(c_Message.Omsg.ONonce(v_x(v_U)), c_Event.Oused(v_list), tc_Message.Omsg) or c.in(c_Message.Omsg.ONonce(v_x(v_U)...)
c.in(c_Message.Omsg.ONonce(v_U), c_Message.Oparts(c_insert(v_msg, c_emptyset, tc_Message.Omsg)), tc_Message.Omsg)  $\Rightarrow$ 
 $\neg$ c.lessequals(v_sko_upX(v_msg), v_U, tc_nat)    cnf(cls_Message.Omsg_Nonce_supply0, axiom)
c.lessequals(c_plus(v_m, v_k, tc_nat), v_n, tc_nat)  $\Rightarrow$  c.lessequals(v_k, v_n, tc_nat)    cnf(cls_Nat.Oadd_leE0, axiom)
c.lessequals(c_plus(v_m, v_k, tc_nat), v_n, tc_nat)  $\Rightarrow$  c.lessequals(v_m, v_n, tc_nat)    cnf(cls_Nat.Oadd_leE1, axiom)
```

**SWV287-2.p** Cryptographic protocol problem for Otway Rees

```
c.in(c_Event.Oevent.OSays(v_A, v_B, c_Message.Omsg.OMPair(v_NA, c_Message.Omsg.OMPair(c_Message.Omsg.OAgent(v_A, v_B,
c.in(c_Event.Oevent.OSays(v_B_H, v_A, c_Message.Omsg.OMPair(v_NA, c_Message.Omsg.OCrypt(c_Public.OshrK(v_A), c_Message.Omsg_...
 $\neg$ c.in(c_Event.Oevent.ONotes(c_Message.Oagent.OSpy, c_Message.Omsg.OMPair(v_NA, c_Message.Omsg.OMPair(v_U, c_Message.Omsg_...
 $\neg$ c.in(v_A, c_Event.Obad, tc_Message.Oagent)    cnf(cls_conjecture3, negated_conjecture)
 $\neg$ c.in(v_B, c_Event.Obad, tc_Message.Oagent)    cnf(cls_conjecture4, negated_conjecture)
c.in(v_ews, c_OtwayRees.Ootway, tc_List.Olist(tc_Event.Oevent))    cnf(cls_conjecture5, negated_conjecture)
c.in(c_Message.Omsg.OKey(v_K), c_Message.Oanalz(c_Event.Oknows(c_Message.Oagent.OSpy, v_ews)), tc_Message.Omsg)
(c.in(v_ews, c_OtwayRees.Ootway, tc_List.Olist(tc_Event.Oevent)) and c.in(c_Event.Oevent.OSays(v_B_H, v_A, c_Message.Omsg_...
(c.in(v_A, c_Event.Obad, tc_Message.Oagent) or c.in(c_Event.Oevent.OSays(c_Message.Oagent.OServer, v_B, c_Message.Omsg_...
(c.in(v_ews, c_OtwayRees.Ootway, tc_List.Olist(tc_Event.Oevent)) and c.in(c_Event.Oevent.OSays(c_Message.Oagent.OServe...
(c.in(v_B, c_Event.Obad, tc_Message.Oagent) or c.in(v_A, c_Event.Obad, tc_Message.Oagent) or c.in(c_Event.Oevent.ONotes...
```

**SWV288-1.p** Cryptographic protocol problem for Otway Rees

```
include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-2.ax')
include('Axioms/SWV006-0.ax')
include('Axioms/SWV006-2.ax')
(c.in(v_ews, c_OtwayRees.Ootway, tc_List.Olist(tc_Event.Oevent)) and c.in(c_Event.Oevent.OSays(v_A, v_B, c_Message.Omsg_...
(c.in(v_A, c_Event.Obad, tc_Message.Oagent) or c.in(c_Event.Oevent.OSays(c_Message.Oagent.OServer, v_B, c_Message.Omsg_...
(c.in(v_ews, c_OtwayRees.Ootway, tc_List.Olist(tc_Event.Oevent)) and c.in(c_Message.Omsg.OKey(c_Public.OshrK(v_A)), c_...
c.in(v_A, c_Event.Obad, tc_Message.Oagent)    cnf(cls_OtwayRees.OSpy_see_shrK_D_dest0, axiom)
c.in(c_Event.Oevent.OSays(v_A, v_B, c_Message.Omsg.OMPair(v_NA, c_Message.Omsg.OMPair(c_Message.Omsg.OAgent(v_A, v_B,
c.in(c_Event.Oevent.OSays(v_B_H, v_A, c_Message.Omsg.OMPair(v_NA, c_Message.Omsg.OCrypt(c_Public.OshrK(v_A), c_Message.Omsg_...
 $\neg$ c.in(v_A, c_Event.Obad, tc_Message.Oagent)    cnf(cls_conjecture2, negated_conjecture)
c.in(v_ews, c_OtwayRees.Ootway, tc_List.Olist(tc_Event.Oevent))    cnf(cls_conjecture3, negated_conjecture)
 $\neg$ c.in(c_Event.Oevent.OSays(c_Message.Oagent.OServer, v_B, c_Message.Omsg.OMPair(v_NA, c_Message.Omsg.OMPair(c_...
```

**SWV288-2.p** Cryptographic protocol problem for Otway Rees

```
c.in(c_Event.Oevent.OSays(v_A, v_B, c_Message.Omsg.OMPair(v_NA, c_Message.Omsg.OMPair(c_Message.Omsg.OAgent(v_A, v_B,
c.in(c_Event.Oevent.OSays(v_B_H, v_A, c_Message.Omsg.OMPair(v_NA, c_Message.Omsg.OCrypt(c_Public.OshrK(v_A), c_Message.Omsg_...
 $\neg$ c.in(v_A, c_Event.Obad, tc_Message.Oagent)    cnf(cls_conjecture2, negated_conjecture)
c.in(v_ews, c_OtwayRees.Ootway, tc_List.Olist(tc_Event.Oevent))    cnf(cls_conjecture3, negated_conjecture)
 $\neg$ c.in(c_Event.Oevent.OSays(c_Message.Oagent.OServer, v_B, c_Message.Omsg.OMPair(v_NA, c_Message.Omsg.OMPair(c_...
c.in(c_Event.Oevent.OSays(v_A, v_B, v_X), c_List.Oset(v_ews, tc_Event.Oevent), tc_Event.Oevent)  $\Rightarrow$  c.in(v_X, c_Message.O...
c.in(c_Message.Omsg.OMPair(v_X, v_Y), c_Message.Oparts(v_H), tc_Message.Omsg)  $\Rightarrow$  c.in(v_Y, c_Message.Oparts(v_H), tc_...
c.in(v_c, c_Message.Oanalz(v_H), tc_Message.Omsg)  $\Rightarrow$  c.in(v_c, c_Message.Oparts(v_H), tc_Message.Omsg)    cnf(cls_Mess_...
(c.in(v_ews, c_OtwayRees.Ootway, tc_List.Olist(tc_Event.Oevent)) and c.in(c_Event.Oevent.OSays(v_A, v_B, c_Message.Omsg_...
(c.in(v_A, c_Event.Obad, tc_Message.Oagent) or c.in(c_Event.Oevent.OSays(c_Message.Oagent.OServer, v_B, c_Message.Omsg_...
```

**SWV291-1.p** Cryptographic protocol problem for Otway Rees

```
include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-2.ax')
include('Axioms/SWV006-0.ax')
include('Axioms/SWV006-2.ax')
```

$(c.in(v\_evs, c.OtwayRees.Ootway, tc.List.Olist(tc.Event.Oevent)))$  and  $c.in(c.Message.Omsg.OKey(c.Public.OshrK(v\_A)), c.in(v\_A, c.Event.Obad, tc.Message.Oagent) \quad cnf(cls.OtwayRees.OSpy\_see\_shrK\_D\_dest_0, axiom)$   
 $\neg c.in(v\_A, c.Event.Obad, tc.Message.Oagent) \quad cnf(cls.conjecture_0, negated.conjecture)$   
 $c.in(v\_evsf, c.OtwayRees.Ootway, tc.List.Olist(tc.Event.Oevent)) \quad cnf(cls.conjecture_1, negated.conjecture)$   
 $c.in(v\_X, c.Message.Osynth(c.Message.Oanalz(c.Event.OKnows(c.Message.Oagent.OSpy, v\_evsf))), tc.Message.Omsg) \quad cr$   
 $c.in(c.Message.Omsg.OCrypt(c.Public.OshrK(v\_A), c.Message.Omsg.OMPair(v\_NA, c.Message.Omsg.OMPair(c.Message.O$   
 $\neg c.in(c.Event.Oevent.OSays(v\_A, v\_B, c.Message.Omsg.OMPair(v\_NA, c.Message.Omsg.OMPair(c.Message.Omsg.OAgent$   
 $c.in(c.Message.Omsg.OCrypt(c.Public.OshrK(v\_A), c.Message.Omsg.OMPair(v\_NA, c.Message.Omsg.OMPair(c.Message.O$   
 $c.in(c.Event.Oevent.OSays(v\_A, v\_B, c.Message.Omsg.OMPair(v\_NA, c.Message.Omsg.OMPair(c.Message.Omsg.OAgent(v$   
 $(c.Message.Omsg.OMPair(v\_NA, c.Message.Omsg.OMPair(c.Message.Omsg.OAgent(v\_A), c.Message.Omsg.OMPair(c.Mes$   
 $v\_X$  and  $v\_B = v\_Ba) \Rightarrow v\_A \neq c.Message.Oagent.OSpy \quad cnf(cls.conjecture_6, negated.conjecture)$

**SWV291-2.p** Cryptographic protocol problem for Otway Rees

$\neg c.in(v\_A, c.Event.Obad, tc.Message.Oagent) \quad cnf(cls.conjecture_0, negated.conjecture)$   
 $c.in(v\_evsf, c.OtwayRees.Ootway, tc.List.Olist(tc.Event.Oevent)) \quad cnf(cls.conjecture_1, negated.conjecture)$   
 $c.in(v\_X, c.Message.Osynth(c.Message.Oanalz(c.Event.OKnows(c.Message.Oagent.OSpy, v\_evsf))), tc.Message.Omsg) \quad cr$   
 $c.in(c.Message.Omsg.OCrypt(c.Public.OshrK(v\_A), c.Message.Omsg.OMPair(v\_NA, c.Message.Omsg.OMPair(c.Message.O$   
 $\neg c.in(c.Event.Oevent.OSays(v\_A, v\_B, c.Message.Omsg.OMPair(v\_NA, c.Message.Omsg.OMPair(c.Message.Omsg.OAgent$   
 $c.in(c.Message.Omsg.OCrypt(c.Public.OshrK(v\_A), c.Message.Omsg.OMPair(v\_NA, c.Message.Omsg.OMPair(c.Message.O$   
 $c.in(c.Event.Oevent.OSays(v\_A, v\_B, c.Message.Omsg.OMPair(v\_NA, c.Message.Omsg.OMPair(c.Message.Omsg.OAgent(v$   
 $c.in(c.Message.Omsg.OCrypt(v\_K, v\_X), c.Message.Osynth(v\_H), tc.Message.Omsg) \Rightarrow (c.in(c.Message.Omsg.OCrypt(v\_K$   
 $(c.in(v\_Z, c.Message.Oparts(c.insert(v\_X, v\_H, tc.Message.Omsg)), tc.Message.Omsg) and  $c.in(v\_X, c.Message.Osynth(c.Mes$   
 $c.in(v\_Z, c.union(c.Message.Osynth(c.Message.Oanalz(v\_H)), c.Message.Oparts(v\_H), tc.Message.Omsg), tc.Message.Omsg)$   
 $c.in(v\_c, c.Message.Oanalz(v\_H), tc.Message.Omsg) \Rightarrow c.in(v\_c, c.Message.Oparts(v\_H), tc.Message.Omsg) \quad cnf(cls.Mess$   
 $(c.in(v\_evs, c.OtwayRees.Ootway, tc.List.Olist(tc.Event.Oevent)))$  and  $c.in(c.Message.Omsg.OKey(c.Public.OshrK(v\_A)), c.$   
 $c.in(v\_A, c.Event.Obad, tc.Message.Oagent) \quad cnf(cls.OtwayRees.OSpy\_see\_shrK\_D\_dest_0, axiom)$   
 $c.in(v\_c, c.union(v\_A, v\_B, t\_a), t\_a) \Rightarrow (c.in(v\_c, v\_B, t\_a) or c.in(v\_c, v\_A, t\_a)) \quad cnf(cls.Set.OUnE_0, axiom)$$

**SWV293-1.p** Cryptographic protocol problem for Otway Rees

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-2.ax')$   
 $include('Axioms/SWV006-0.ax')$   
 $include('Axioms/SWV006-2.ax')$   
 $(c.in(v\_evs, c.OtwayRees.Ootway, tc.List.Olist(tc.Event.Oevent)))$  and  $c.in(c.Message.Omsg.OCrypt(c.Public.OshrK(v\_A), c$   
 $(c.in(v\_A, c.Event.Obad, tc.Message.Oagent) or c.in(c.Event.Oevent.OSays(v\_A, v\_B, c.Message.Omsg.OMPair(v\_NA, c.Me$   
 $(c.in(v\_evs, c.OtwayRees.Ootway, tc.List.Olist(tc.Event.Oevent)))$  and  $c.in(c.Message.Omsg.OKey(c.Public.OshrK(v\_A)), c.$   
 $c.in(v\_A, c.Event.Obad, tc.Message.Oagent) \quad cnf(cls.OtwayRees.OSpy\_see\_shrK\_D\_dest_0, axiom)$   
 $c.in(c.Event.Oevent.OGets(v\_B, c.Message.Omsg.OMPair(v\_NA, c.Message.Omsg.OMPair(c.Message.Omsg.OAgent(v\_A),$   
 $\neg c.in(v\_A, c.Event.Obad, tc.Message.Oagent) \quad cnf(cls.conjecture_1, negated.conjecture)$   
 $c.in(v\_evs, c.OtwayRees.Ootway, tc.List.Olist(tc.Event.Oevent)) \quad cnf(cls.conjecture_2, negated.conjecture)$   
 $\neg c.in(c.Event.Oevent.OSays(v\_A, v\_B, c.Message.Omsg.OMPair(v\_NA, c.Message.Omsg.OMPair(c.Message.Omsg.OAgent$

**SWV293-2.p** Cryptographic protocol problem for Otway Rees

$c.in(c.Event.Oevent.OGets(v\_B, c.Message.Omsg.OMPair(v\_NA, c.Message.Omsg.OMPair(c.Message.Omsg.OAgent(v\_A),$   
 $\neg c.in(v\_A, c.Event.Obad, tc.Message.Oagent) \quad cnf(cls.conjecture_1, negated.conjecture)$   
 $c.in(v\_evs, c.OtwayRees.Ootway, tc.List.Olist(tc.Event.Oevent)) \quad cnf(cls.conjecture_2, negated.conjecture)$   
 $\neg c.in(c.Event.Oevent.OSays(v\_A, v\_B, c.Message.Omsg.OMPair(v\_NA, c.Message.Omsg.OMPair(c.Message.Omsg.OAgent$   
 $c.in(c.Message.Omsg.OMPair(v\_X, v\_Y), c.Message.Oparts(v\_H), tc.Message.Omsg) \Rightarrow c.in(v\_Y, c.Message.Oparts(v\_H), tc$   
 $c.in(v\_c, c.Message.Oanalz(v\_H), tc.Message.Omsg) \Rightarrow c.in(v\_c, c.Message.Oparts(v\_H), tc.Message.Omsg) \quad cnf(cls.Mess$   
 $(c.in(v\_evs, c.OtwayRees.Ootway, tc.List.Olist(tc.Event.Oevent)))$  and  $c.in(c.Message.Omsg.OCrypt(c.Public.OshrK(v\_A), c$   
 $(c.in(v\_A, c.Event.Obad, tc.Message.Oagent) or c.in(c.Event.Oevent.OSays(v\_A, v\_B, c.Message.Omsg.OMPair(v\_NA, c.Me$   
 $(c.in(v\_evs, c.OtwayRees.Ootway, tc.List.Olist(tc.Event.Oevent)))$  and  $c.in(c.Event.Oevent.OGets(v\_B, v\_X), c.List.Oset(v.e$   
 $c.in(c.Event.Oevent.OSays(v\_sko\_usf(v\_B, v\_X, v\_evs), v\_B, v\_X), c.List.Oset(v\_evs, tc.Event.Oevent), tc.Event.Oevent) \quad$   
 $c.in(c.Event.Oevent.OSays(v\_A, v\_B, v\_X), c.List.Oset(v\_evs, tc.Event.Oevent), tc.Event.Oevent) \Rightarrow c.in(v\_X, c.Message.O$

**SWV295-2.p** Cryptographic protocol problem for Otway Rees

$c.in(c.Message.Omsg.OCrypt(c.Public.OshrK(v\_Aa), c.Message.Omsg.OMPair(c.Message.Omsg.ONonce(v\_NAa), c.Messag$   
 $\neg c.in(c.Message.Omsg.ONonce(v\_NAa), c.Event.Oused(v\_evs_1), tc.Message.Omsg) \quad cnf(cls.conjecture_2, negated.conjecture)$   
 $v\_NA = c.Message.Omsg.ONonce(v\_NAa) \quad cnf(cls.conjecture_5, negated.conjecture)$   
 $c.in(v\_c, c.Message.Oparts(c.Event.OKnows(c.Message.Oagent.OSpy, v\_evs)), tc.Message.Omsg) \Rightarrow c.in(v\_c, c.Event.Oused$   
 $c.in(c.Message.Omsg.OMPair(v\_X, v\_Y), c.Message.Oparts(v\_H), tc.Message.Omsg) \Rightarrow c.in(v\_X, c.Message.Oparts(v\_H), tc$



$(c.in(v\_evs, c.OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)))$  and  $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_OtwayRees\_OSpy\_see\_shrK\_D\_dest_0, axiom)$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c.in(v\_evsf, c.OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c.in(v\_X, c\_Message\_OSynth(c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg) \quad cr$   
 $c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA, c\_Message\_Omsg\_OMPair(c\_Message\_O$   
 $c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA\_H, c\_Message\_Omsg\_OMPair(v\_NA, c\_M$   
 $c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA\_H, c\_Message\_Omsg\_OMPair(v\_NA, c\_M$   
 $\neg c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA, c\_Message\_Omsg\_OMPair(c\_Message$

**SWV305-2.p** Cryptographic protocol problem for Otway Rees

$\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c.in(v\_evsf, c.OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c.in(v\_X, c\_Message\_OSynth(c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg) \quad cr$   
 $c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA, c\_Message\_Omsg\_OMPair(c\_Message\_O$   
 $c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA\_H, c\_Message\_Omsg\_OMPair(v\_NA, c\_M$   
 $c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA\_H, c\_Message\_Omsg\_OMPair(v\_NA, c\_M$   
 $\neg c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA, c\_Message\_Omsg\_OMPair(c\_Message$   
 $c.in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_OSynth(v\_H), tc\_Message\_Omsg) \Rightarrow (c.in(c\_Message\_Omsg\_OCrypt(v\_K$   
 $(c.in(v\_Z, c\_Message\_Oparts(c.insert(v\_X, v\_H, tc\_Message\_Omsg)), tc\_Message\_Omsg) and  $c.in(v\_X, c\_Message\_OSynth(c\_Mes$   
 $c.in(v\_Z, c\_union(c\_Message\_OSynth(c\_Message\_Oanalz(v\_H)), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg)$   
 $c.in(v\_c, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_c, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Mess$   
 $(c.in(v\_evs, c.OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)))$  and  $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c.$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_OtwayRees\_OSpy\_see\_shrK\_D\_dest_0, axiom)$   
 $c.in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a) \Rightarrow (c.in(v\_c, v\_B, t\_a) or c.in(v\_c, v\_A, t\_a)) \quad cnf(cls\_Set\_OUne_0, axiom)$$

**SWV306-1.p** Cryptographic protocol problem for Otway Rees

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-2.ax')$   
 $include('Axioms/SWV006-0.ax')$   
 $include('Axioms/SWV006-2.ax')$   
 $(c.in(v\_evs, c.OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)))$  and  $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c.$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_OtwayRees\_OSpy\_see\_shrK\_D\_dest_0, axiom)$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c.in(v\_evs_1, c.OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c.in(c\_Message\_Omsg\_ONonce(v\_NAa), c\_Event\_Oused(v\_evs_1), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $v\_A = v\_Aa \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $v\_NA = c\_Message\_Omsg\_ONonce(v\_NAa) \quad cnf(cls\_conjecture_4, negated\_conjecture)$   
 $v\_A = v\_Aa \quad cnf(cls\_conjecture_5, negated\_conjecture)$   
 $v\_B = v\_Ba \quad cnf(cls\_conjecture_6, negated\_conjecture)$   
 $c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_Aa), c\_Message\_Omsg\_OMPair(v\_NA\_H, c\_Message\_Omsg\_OMPair(c\_Message$   
 $c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA\_H, c\_Message\_Omsg\_OMPair(v\_NA, c\_M$   
 $\neg c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA, c\_Message\_Omsg\_OMPair(c\_Message$

**SWV306-2.p** Cryptographic protocol problem for Otway Rees

$\neg c.in(c\_Message\_Omsg\_ONonce(v\_NAa), c\_Event\_Oused(v\_evs_1), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $v\_NA = c\_Message\_Omsg\_ONonce(v\_NAa) \quad cnf(cls\_conjecture_4, negated\_conjecture)$   
 $c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_Aa), c\_Message\_Omsg\_OMPair(v\_NA\_H, c\_Message\_Omsg\_OMPair(c\_Message$   
 $c.in(v\_c, c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) \Rightarrow c.in(v\_c, c\_Event\_Oused$   
 $c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_Y, c\_Message\_Oparts(v\_H), tc$   
 $c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc$   
 $c.in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc$

**SWV307-1.p** Cryptographic protocol problem for Otway Rees

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-2.ax')$   
 $include('Axioms/SWV006-0.ax')$   
 $include('Axioms/SWV006-2.ax')$   
 $(c.in(v\_evs, c.OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)))$  and  $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c.$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_OtwayRees\_OSpy\_see\_shrK\_D\_dest_0, axiom)$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_0, negated\_conjecture)$





```

c.in(c_Event_Oevent_OSays(c_Message_Oagent_OServer, v_B, c_Message_Omsg_OMPair(v_NA, c_Message_Omsg_OMPair(c_M
- c.in(c_Event_Oevent_ONotes(c_Message_Oagent_OSpy, c_Message_Omsg_OMPair(v_NA, c_Message_Omsg_OMPair(v_NB, c_
- c.in(v_A, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_2, negated_conjecture)
- c.in(v_B, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_3, negated_conjecture)
c.in(v_ews, c_OtwayRees_Ootway, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture_4, negated_conjecture)
c.in(c_Message_Omsg_OKey(v_K), c_Event_Oknows(c_Message_Oagent_OSpy, v_ews), tc_Message_Omsg)    cnf(cls_conjecture

```

**SWV313-2.p** Cryptographic protocol problem for Otway Rees

```

c.in(c_Event_Oevent_OSays(c_Message_Oagent_OServer, v_B, c_Message_Omsg_OMPair(v_NA, c_Message_Omsg_OMPair(c_M
- c.in(c_Event_Oevent_ONotes(c_Message_Oagent_OSpy, c_Message_Omsg_OMPair(v_NA, c_Message_Omsg_OMPair(v_NB, c_
- c.in(v_A, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_2, negated_conjecture)
- c.in(v_B, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_3, negated_conjecture)
c.in(v_ews, c_OtwayRees_Ootway, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture_4, negated_conjecture)
c.in(c_Message_Omsg_OKey(v_K), c_Event_Oknows(c_Message_Oagent_OSpy, v_ews), tc_Message_Omsg)    cnf(cls_conjecture
c.in(v_X, v_H, tc_Message_Omsg) ⇒ c.in(v_X, c_Message_Oanalz(v_H), tc_Message_Omsg)    cnf(cls_Message_Oanalz_OInj_0,
(c.in(v_ews, c_OtwayRees_Ootway, tc_List_Olist(tc_Event_Oevent)) and c.in(c_Event_Oevent_OSays(c_Message_Oagent_OServ
(c.in(v_B, c_Event_Obad, tc_Message_Oagent) or c.in(v_A, c_Event_Obad, tc_Message_Oagent) or c.in(c_Event_Oevent_ONotes

```

**SWV314-1.p** Cryptographic protocol problem for Otway Rees

```

include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-2.ax')
include('Axioms/SWV006-0.ax')
include('Axioms/SWV006-2.ax')
(c.in(v_ews, c_OtwayRees_Ootway, tc_List_Olist(tc_Event_Oevent)) and c.in(c_Message_Omsg_OKey(c_Public_OshrK(v_A)), c_
c.in(v_A, c_Event_Obad, tc_Message_Oagent)    cnf(cls_OtwayRees_OSpy__see__shrK__D__dest_0, axiom)
(c.in(v_ews, c_OtwayRees_Ootway, tc_List_Olist(tc_Event_Oevent)) and c.in(c_Event_Oevent_OSays(c_Message_Oagent_OServ
(c.in(v_B, c_Event_Obad, tc_Message_Oagent) or c.in(v_A, c_Event_Obad, tc_Message_Oagent) or c.in(c_Event_Oevent_ONotes
c.in(c_Event_Oevent_OSays(c_Message_Oagent_OServer, v_B, c_Message_Omsg_OMPair(v_NA, c_Message_Omsg_OMPair(c_M
- c.in(c_Event_Oevent_ONotes(c_Message_Oagent_OSpy, c_Message_Omsg_OMPair(v_NA, c_Message_Omsg_OMPair(v_NB, c_
- c.in(v_A, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_2, negated_conjecture)
- c.in(v_B, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_3, negated_conjecture)
c.in(v_ews, c_OtwayRees_Ootway, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture_4, negated_conjecture)
c.in(c_Message_Omsg_OKey(v_K), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_ews)), tc_Message_Omsg)

```

**SWV314-2.p** Cryptographic protocol problem for Otway Rees

```

c.in(c_Event_Oevent_OSays(c_Message_Oagent_OServer, v_B, c_Message_Omsg_OMPair(v_NA, c_Message_Omsg_OMPair(c_M
- c.in(c_Event_Oevent_ONotes(c_Message_Oagent_OSpy, c_Message_Omsg_OMPair(v_NA, c_Message_Omsg_OMPair(v_NB, c_
- c.in(v_A, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_2, negated_conjecture)
- c.in(v_B, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_3, negated_conjecture)
c.in(v_ews, c_OtwayRees_Ootway, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture_4, negated_conjecture)
c.in(c_Message_Omsg_OKey(v_K), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_ews)), tc_Message_Omsg)
(c.in(v_ews, c_OtwayRees_Ootway, tc_List_Olist(tc_Event_Oevent)) and c.in(c_Event_Oevent_OSays(c_Message_Oagent_OServ
(c.in(v_B, c_Event_Obad, tc_Message_Oagent) or c.in(v_A, c_Event_Obad, tc_Message_Oagent) or c.in(c_Event_Oevent_ONotes

```

**SWV315-1.p** Cryptographic protocol problem for Otway Rees

```

include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-1.ax')
include('Axioms/SWV005-0.ax')
include('Axioms/SWV005-2.ax')
include('Axioms/SWV005-3.ax')
c.in(c_Event_Oevent_OSays(v_A, v_B, v_X), c_List_Oset(v_ews, tc_Event_Oevent), tc_Event_Oevent) ⇒ c.in(v_X, c_Message_Oa
(c.in(v_Z, c_Message_Oparts(c_insert(v_X, v_H, tc_Message_Omsg)), tc_Message_Omsg) and c.in(v_X, c_Message_Osynth(c_Mes
c.in(v_Z, c_union(c_Message_Osynth(c_Message_Oanalz(v_H)), c_Message_Oparts(v_H), tc_Message_Omsg), tc_Message_Omsg)
c.in(c_Message_Omsg_OCrypt(v_K, v_X), c_Message_Oparts(v_H), tc_Message_Omsg) ⇒ c.in(v_X, c_Message_Oparts(v_H), tc
(c.in(v_ews, c_OtwayRees_Ootway, tc_List_Olist(tc_Event_Oevent)) and c.in(c_Event_Oevent_OGets(v_B, v_X), c_List_Oset(v_e
c.in(c_Event_Oevent_OSays(v_sko__usf(v_B, v_X, v_ews), v_B, v_X), c_List_Oset(v_ews, tc_Event_Oevent), tc_Event_Oevent)
(c.in(v_ews, c_OtwayRees_Ootway, tc_List_Olist(tc_Event_Oevent)) and c.in(c_Event_Oevent_OGets(v_B, c_Message_Omsg_OM
c.in(v_c, c_Message_Oparts(c_Event_Oknows(c_Message_Oagent_OSpy, v_ews)), tc_Message_Omsg)    cnf(cls_OtwayRees_OO
c.in(v_ewsf, c_OtwayRees_Ootway, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture_0, negated_conjecture)
c.in(v_X, c_Message_Osynth(c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_ewsf))), tc_Message_Omsg)    cr

```

$c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow \neg c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg)$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_insert(v\_X, c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg)$

**SWV315-2.p** Cryptographic protocol problem for Otway Rees

$c.in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow \neg c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg)$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_insert(v\_X, c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg) \text{ and } c.in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg)$   
 $c.in(v\_Z, c\_union(c\_Message\_Osynth(c\_Message\_Oanalz(v\_H)), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg), tc\_Message\_Omsg)$   
 $c.in(c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(c\_Message\_Omsg\_OKey(v\_K), v\_H, tc\_Message\_Omsg), tc\_Message\_Omsg)$   
 $c.in(v\_X, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oparts\_OInj_0, axiom)$   
 $c.in(v\_X, v\_H, tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oparts\_OInj_0, axiom)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg)$   
 $c.in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a) \Rightarrow (c.in(v\_c, v\_B, t\_a) \text{ or } c.in(v\_c, v\_A, t\_a)) \quad cnf(cls\_Set\_OU\_iff_0, axiom)$   
 $c.in(v\_a, v\_A, t\_a) \Rightarrow c.in(v\_a, c\_insert(v\_b, v\_A, t\_a), t\_a) \quad cnf(cls\_Set\_Oinsert\_iff_2, axiom)$

**SWV317-2.p** Cryptographic protocol problem for Otway Rees

$\neg c.in(c\_Message\_Omsg\_OKey(v\_KAB), c\_Event\_Oused(v\_evs_3), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c\_Public\_OshrK(v\_A) = v\_KAB \text{ or } c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_7, negated\_conjecture)$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Event\_Oused(v\_evs), tc\_Message\_Omsg) \quad cnf(cls\_Public\_OshrK\_in\_evs, axiom)$

**SWV318-2.p** Cryptographic protocol problem for Otway Rees

$c.in(c\_Event\_Oevent\_OSays(v\_A, v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent) \Rightarrow c.in(v\_X, c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg)$   
 $c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_Y, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg)$   
 $c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg)$   
 $c.in(v\_X, v\_H, tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oparts\_OInj_0, axiom)$   
 $c\_Message\_Oparts(c\_Message\_Oanalz(v\_H)) = c\_Message\_Oparts(v\_H) \quad cnf(cls\_Message\_Oparts\_OInj_0, axiom)$   
 $c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(c\_insert(v\_X, v\_H, tc\_Message\_Omsg), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) = c\_Message\_Oparts(v\_H) \quad cnf(cls\_Message\_Oparts\_Ocut\_eq_0, axiom)$   
 $(c.in(v\_evs, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent))) \text{ and } c.in(c\_Event\_Oevent\_OGets(v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent)$   
 $c.in(c\_Event\_Oevent\_OSays(v\_sko\_usf(v\_B, v\_X, v\_evs), v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent) \Rightarrow c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg)$   
 $c.in(v\_a, v\_A, t\_a) \Rightarrow c.in(v\_a, c\_insert(v\_b, v\_A, t\_a), t\_a) \quad cnf(cls\_Set\_Oinsert\_iff_2, axiom)$   
 $c.in(v\_evs_4, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OGets(v\_B, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_ONonce(v\_NA), c\_Message\_Omsg\_OMPair(v\_X, v\_Y)), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg)$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_4))), tc\_Message\_Omsg)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_4, negated\_conjecture)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow \neg c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg)$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_insert(v\_X, c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg)$

**SWV319-1.p** Cryptographic protocol problem for Otway Rees

`include('Axioms/MS001-0.ax')`  
`include('Axioms/MS001-1.ax')`  
`include('Axioms/SWV005-0.ax')`  
`include('Axioms/SWV005-2.ax')`  
`include('Axioms/SWV005-3.ax')`  
 $c.in(c\_Event\_Oevent\_OSays(v\_A, v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent) \Rightarrow c.in(v\_X, c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg)$   
 $(c.in(v\_Z, c\_Message\_Oparts(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), tc\_Message\_Omsg) \text{ and } c.in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg))$   
 $c.in(v\_Z, c\_union(c\_Message\_Osynth(c\_Message\_Oanalz(v\_H)), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg), tc\_Message\_Omsg)$   
 $c.in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg)$   
 $(c.in(v\_evs, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent))) \text{ and } c.in(c\_Event\_Oevent\_OGets(v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent)$   
 $c.in(c\_Event\_Oevent\_OSays(v\_sko\_usf(v\_B, v\_X, v\_evs), v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent) \Rightarrow c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg)$   
 $(c.in(v\_evs, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent))) \text{ and } c.in(c\_Event\_Oevent\_OGets(v\_B, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_ONonce(v\_NA), c\_Message\_Omsg\_OMPair(v\_X, v\_Y))), tc\_Message\_Omsg)$   
 $c.in(v\_c, c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) \quad cnf(cls\_OtwayRees\_OO\_iff_0, axiom)$   
 $c.in(v\_evso, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$

$c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_OServer, v\_B, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_ONonce(v\_NA), c\_M$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evso)), tc$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Ev$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow c\_Public\_OshrK(v\_A) \neq v\_K \quad cnf(cls\_conjecture_5, negated\_conjecture)$   
 $c\_Public\_OshrK(v\_A) = v\_K \text{ or } c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_6, negated\_conjecture)$

**SWV319-2.p** Cryptographic protocol problem for Otway Rees

$c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_OServer, v\_B, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_ONonce(v\_NA), c\_M$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evso)), tc$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c\_Public\_OshrK(v\_A) = v\_K \text{ or } c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_6, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OSays(v\_A, v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent) \Rightarrow c.in(v\_X, c\_Message\_O$   
 $c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_Y, c\_Message\_Oanalz(v\_H), tc$   
 $c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_Y, c\_Message\_Oparts(v\_H), tc$   
 $c.in(v\_X, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Mes$   
 $c.in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc$

**SWV320-1.p** Cryptographic protocol problem for Otway Rees

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-1.ax')$   
 $include('Axioms/SWV005-0.ax')$   
 $include('Axioms/SWV005-2.ax')$   
 $include('Axioms/SWV005-3.ax')$   
 $c.in(c\_Event\_Oevent\_OSays(v\_A, v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent) \Rightarrow c.in(v\_X, c\_Message\_O$   
 $(c.in(v\_Z, c\_Message\_Oparts(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), tc\_Message\_Omsg) \text{ and } c.in(v\_X, c\_Message\_Osynth(c\_Mes$   
 $c.in(v\_Z, c\_union(c\_Message\_Osynth(c\_Message\_Oanalz(v\_H)), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg)$   
 $c.in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc$   
 $(c.in(v\_evs, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \text{ and } c.in(c\_Event\_Oevent\_OGets(v\_B, v\_X), c\_List\_Oset(v\_e$   
 $c.in(c\_Event\_Oevent\_OSays(v\_sko\_usf(v\_B, v\_X, v\_evs), v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent)$   
 $(c.in(v\_evs, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \text{ and } c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_OtwayRees\_OSpy\_analz\_shrK_0, axiom)$   
 $(c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \text{ and } c.in(v\_evs, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent))) \Rightarrow$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc$   
 $(c.in(v\_evs, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \text{ and } c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_OtwayRees\_OSpy\_see\_shrK_0, axiom)$   
 $(c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \text{ and } c.in(v\_evs, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent))) \Rightarrow$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc$   
 $c.in(v\_evs, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_2, negated\_conjecture)$

**SWV320-2.p** Cryptographic protocol problem for Otway Rees

$c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc$   
 $c.in(v\_evs, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $(c.in(v\_evs, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \text{ and } c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_OtwayRees\_OSpy\_see\_shrK_0, axiom)$

**SWV321-1.p** Cryptographic protocol problem for Otway Rees

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-2.ax')$   
 $include('Axioms/SWV006-0.ax')$   
 $include('Axioms/SWV006-2.ax')$   
 $c.in(v\_evsf, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c.in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg) \quad cn$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf)), tc$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Ev$

$c.in(v_A, c.Event\_Obad, tc\_Message\_Oagent) \Rightarrow \neg c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v_A)), c\_Message\_Oparts(c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v_A)), c\_Message\_Oparts(c.insert(v\_X, c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg))$

**SWV321-2.p** Cryptographic protocol problem for Otway Rees

$c.in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg) \wedge c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow \neg c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c.insert(v\_X, c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg))$   
 $(c.in(v\_Z, c\_Message\_Oparts(c.insert(v\_X, v\_H, tc\_Message\_Omsg)), tc\_Message\_Omsg) \wedge c.in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg) \wedge c.in(v\_Z, c\_union(c\_Message\_Osynth(c\_Message\_Oanalz(v\_H)), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg) \wedge c.in(c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(c\_Message\_Omsg\_OKey(v\_K), v\_H, tc.in(v\_c, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_c, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oparts\_OInj_0, negated\_conjecture)$   
 $c.in(v\_X, v\_H, tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oparts\_OInj_0, negated\_conjecture)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf)) \quad cnf(cls\_Set\_OUne_0, axiom)$   
 $c.in(v\_c, c\_union(v\_A, v\_B, t.a), t.a) \Rightarrow (c.in(v\_c, v\_B, t.a) \vee c.in(v\_c, v\_A, t.a)) \quad cnf(cls\_Set\_OUne_0, axiom)$   
 $c.in(v\_a, v\_B, t.a) \Rightarrow c.in(v\_a, c.insert(v\_b, v\_B, t.a), t.a) \quad cnf(cls\_Set\_OinsertCI_0, axiom)$

**SWV322-1.p** Cryptographic protocol problem for Otway Rees

`include('Axioms/MS001-0.ax')`  
`include('Axioms/MS001-2.ax')`  
`include('Axioms/SWV006-0.ax')`  
`include('Axioms/SWV006-2.ax')`  
 $c.in(v\_evs_3, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c.in(c\_Message\_Omsg\_OKey(v\_KAB), c\_Event\_Oused(v\_evs_3), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OGets(c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_ONonce(v\_NA), c\_Message\_Omsg\_OMPair(v\_X, v\_Y)), tc\_Message\_Omsg), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_3))), tc.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_4, negated\_conjecture)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_3))) \quad cnf(cls\_conjecture_5, negated\_conjecture)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow c\_Public\_OshrK(v\_A) \neq v\_KAB \quad cnf(cls\_conjecture_6, negated\_conjecture)$   
 $c\_Public\_OshrK(v\_A) = v\_KAB \vee c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_7, negated\_conjecture)$

**SWV322-2.p** Cryptographic protocol problem for Otway Rees

$\neg c.in(c\_Message\_Omsg\_OKey(v\_KAB), c\_Event\_Oused(v\_evs_3), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c\_Public\_OshrK(v\_A) = v\_KAB \vee c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_7, negated\_conjecture)$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Event\_Oused(v\_evs), tc\_Message\_Omsg) \quad cnf(cls\_Public\_OshrK\_in\_1, negated\_conjecture)$

**SWV323-1.p** Cryptographic protocol problem for Otway Rees

`include('Axioms/MS001-0.ax')`  
`include('Axioms/MS001-2.ax')`  
`include('Axioms/SWV006-0.ax')`  
`include('Axioms/SWV006-2.ax')`  
 $c.in(v\_evs_4, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $v\_B \neq c\_Message\_Oagent\_OServer \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OSays(v\_B, c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_ONonce(v\_NA), c\_Message\_Omsg\_OMPair(v\_X, v\_Y)), tc\_Message\_Omsg), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OGets(v\_B, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_ONonce(v\_NA), c\_Message\_Omsg\_OMPair(v\_X, v\_Y)), tc\_Message\_Omsg), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_4))), tc.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_4, negated\_conjecture)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_4))) \quad cnf(cls\_conjecture_5, negated\_conjecture)$   
 $c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow \neg c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c.in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c.insert(v\_X, c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg)) \quad cnf(cls\_conjecture_6, negated\_conjecture)$

**SWV324-1.p** Cryptographic protocol problem for Otway Rees

`include('Axioms/MS001-0.ax')`  
`include('Axioms/MS001-2.ax')`  
`include('Axioms/SWV006-0.ax')`  
`include('Axioms/SWV006-2.ax')`  
 $c.in(v\_evso, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_OServer, v\_B, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_ONonce(v\_NA), c\_Message\_Omsg\_OMPair(v\_X, v\_Y)), tc\_Message\_Omsg), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_2, negated\_conjecture)$

$c\_in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evso))), tc\_Message\_Oagent) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c\_in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow c\_in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evso))), tc\_Message\_Oagent)$   
 $c\_in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \Rightarrow c\_Public\_OshrK(v\_A) \neq v\_K \quad cnf(cls\_conjecture_5, negated\_conjecture)$   
 $c\_Public\_OshrK(v\_A) = v\_K \text{ or } c\_in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_6, negated\_conjecture)$

**SWV324-2.p** Cryptographic protocol problem for Otway Rees

$c\_in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_OServer, v\_B, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_ONonce(v\_NA), c\_Message\_Omsg\_OMPair(v\_X, v\_Y))), tc\_Message\_Oagent) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evso))), tc\_Message\_Oagent) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c\_in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c\_Public\_OshrK(v\_A) = v\_K \text{ or } c\_in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_6, negated\_conjecture)$   
 $c\_in(c\_Event\_Oevent\_OSays(v\_A, v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_Y, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $c\_in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_Y, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $c\_in(v\_c, c\_Message\_Oanlz(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_c, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_7, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$

**SWV325-1.p** Cryptographic protocol problem for Otway Rees

`include('Axioms/MS001-0.ax')`  
`include('Axioms/MS001-2.ax')`  
`include('Axioms/SWV006-0.ax')`  
`include('Axioms/SWV006-2.ax')`  
 $(c\_in(v\_evs, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent))) \text{ and } c\_in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg) \quad cnf(cls\_OtwayRees\_OSpy\_see\_shrK\_D\_dest_0, axiom)$   
 $\neg c\_in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c\_in(v\_evsf, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c\_in(v\_X, c\_Message\_Osynth(c\_Message\_Oanlz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OMPair(v\_X, v\_Y))), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OMPair(v\_X, v\_Y))), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $v\_B \neq v\_C \quad cnf(cls\_conjecture_5, negated\_conjecture)$   
 $(c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OMPair(v\_X, v\_Y))), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $v\_B = v\_C \quad cnf(cls\_conjecture_6, negated\_conjecture)$

**SWV325-2.p** Cryptographic protocol problem for Otway Rees

$\neg c\_in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c\_in(v\_evsf, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c\_in(v\_X, c\_Message\_Osynth(c\_Message\_Oanlz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OMPair(v\_X, v\_Y))), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OMPair(v\_X, v\_Y))), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $v\_B \neq v\_C \quad cnf(cls\_conjecture_5, negated\_conjecture)$   
 $(c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OMPair(v\_X, v\_Y))), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $v\_B = v\_C \quad cnf(cls\_conjecture_6, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \Rightarrow (c\_in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_Z, c\_Message\_Oparts(c\_insert(v\_X, v\_H, tc\_Message\_Omsg)), tc\_Message\_Omsg) \text{ and } c\_in(v\_X, c\_Message\_Osynth(c\_Message\_Oanlz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg))$   
 $c\_in(v\_Z, c\_union(c\_Message\_Osynth(c\_Message\_Oanlz(v\_H)), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg) \Rightarrow c\_in(v\_Z, c\_union(c\_Message\_Osynth(c\_Message\_Oanlz(v\_H)), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg)$   
 $c\_in(v\_c, c\_Message\_Oanlz(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_c, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_7, negated\_conjecture)$   
 $(c\_in(v\_evs, c\_OtwayRees\_Ootway, tc\_List\_Olist(tc\_Event\_Oevent))) \text{ and } c\_in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evso))), tc\_Message\_Oagent) \quad cnf(cls\_OtwayRees\_OSpy\_see\_shrK\_D\_dest_0, axiom)$   
 $c\_in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_OtwayRees\_OSpy\_see\_shrK\_D\_dest_0, axiom)$   
 $c\_in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a) \Rightarrow (c\_in(v\_c, v\_B, t\_a) \text{ or } c\_in(v\_c, v\_A, t\_a)) \quad cnf(cls\_Set\_OUne_0, axiom)$

**SWV326-2.p** Cryptographic protocol problem for Otway Rees

$c\_in(v\_c, c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) \Rightarrow c\_in(v\_c, c\_Event\_Oused(v\_evs_1), tc\_Message\_Omsg)$   
 $c\_in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $\neg c\_in(c\_Message\_Omsg\_ONonce(v\_NAa), c\_Event\_Oused(v\_evs_1), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_OMPair(v\_NA, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OMPair(v\_X, v\_Y))), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $v\_Ba \quad cnf(cls\_conjecture_{21}, negated\_conjecture)$   
 $v\_A = v\_Aa \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $v\_Ba = v\_C \Rightarrow c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_Aa), c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_ONonce(v\_NAa), c\_Message\_Omsg\_ONonce(v\_NAa))), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg)$   
 $v\_NA = c\_Message\_Omsg\_ONonce(v\_NAa) \quad cnf(cls\_conjecture_5, negated\_conjecture)$

**SWV327-1.p** Cryptographic protocol problem for Otway Rees

```

include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-2.ax')
include('Axioms/SWV006-0.ax')
include('Axioms/SWV006-2.ax')
(c.in(v_evs, c.OtwayRees_Ootway, tc.List_Olist(tc_Event_Oevent)) and c.in(c.Message_Omsg_OKey(c.Public_OshrK(v_A)), c.
c.in(v_A, c.Event_Obad, tc.Message_Oagent)   cnf(cls.OtwayRees_OSpy__see__shrK__D__dest0, axiom)
¬ c.in(v_A, c.Event_Obad, tc.Message_Oagent)   cnf(cls.conjecture0, negated_conjecture)
c.in(v_evs4, c.OtwayRees_Ootway, tc.List_Olist(tc_Event_Oevent))   cnf(cls.conjecture1, negated_conjecture)
v_Ba ≠ c.Message_Oagent_OServer   cnf(cls.conjecture2, negated_conjecture)
c.in(c.Event_Oevent_OSays(v_Ba, c.Message_Oagent_OServer, c.Message_Omsg_OMPair(c.Message_Omsg_ONonce(v_NAa), c.
c.in(c.Event_Oevent_OGets(v_Ba, c.Message_Omsg_OMPair(c.Message_Omsg_ONonce(v_NAa), c.Message_Omsg_OMPair(v_
c.in(c.Message_Omsg_OCrypt(c.Public_OshrK(v_A), c.Message_Omsg_OMPair(v_NA, c.Message_Omsg_OMPair(c.Message_O
c.in(c.Message_Omsg_OCrypt(c.Public_OshrK(v_A), c.Message_Omsg_OMPair(v_NA, c.Message_Omsg_OMPair(c.Message_O
v_B ≠ v_C   cnf(cls.conjecture7, negated_conjecture)
(c.in(c.Message_Omsg_OCrypt(c.Public_OshrK(v_A), c.Message_Omsg_OMPair(v_NA, c.Message_Omsg_OMPair(c.Message_
v_B = v_C   cnf(cls.conjecture8, negated_conjecture)

```

**SWV328-1.p** Cryptographic protocol problem for Yahalom

```

include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-1.ax')
include('Axioms/SWV005-0.ax')
include('Axioms/SWV005-2.ax')
include('Axioms/SWV005-3.ax')
include('Axioms/SWV005-4.ax')
include('Axioms/SWV005-5.ax')
include('Axioms/SWV005-6.ax')
c.in(v_evsf, c.Yahalom_Oyahalom, tc.List_Olist(tc_Event_Oevent))   cnf(cls.conjecture0, negated_conjecture)
c.in(v_X, c.Message_Osynth(c.Message_Oanalz(c.Event_Oknows(c.Message_Oagent_OSpy, v_evsf))), tc.Message_Omsg)   cr
¬ c.in(c.Message_Omsg_OKey(v_K), c.Message_Oanalz(c.Event_Oknows(c.Message_Oagent_OSpy, v_evsf)), tc.Message_Omsg)
c.in(c.Message_Omsg_OCrypt(v_K, c.Message_Omsg_ONonce(v_NB)), c.Message_Oparts(c.insert(v_X, c.Event_Oknows(c.Me
c.in(c.Message_Omsg_OCrypt(c.Public_OshrK(v_B), c.Message_Omsg_OMPair(c.Message_Omsg_OAgent(v_A), c.Message_O
¬ c.in(v_B, c.Event_Obad, tc.Message_Oagent)   cnf(cls.conjecture5, negated_conjecture)
¬ c.in(c.Message_Omsg_OCrypt(v_K, c.Message_Omsg_ONonce(v_NB)), c.Message_Oparts(c.Event_Oknows(c.Message_Oager
¬ c.in(c.Event_Oevent_OSays(v_A, v_B, c.Message_Omsg_OMPair(v_U, c.Message_Omsg_OCrypt(v_K, c.Message_Omsg_ONor
(c.Message_Omsg_OMPair(v_U, c.Message_Omsg_OCrypt(v_K, c.Message_Omsg_ONonce(v_NB))) = v_X and v_B =
v_Ba) ⇒ v_A ≠ c.Message_Oagent_OSpy   cnf(cls.conjecture8, negated_conjecture)

```

**SWV328-2.p** Cryptographic protocol problem for Yahalom

```

c.in(v_X, c.Message_Osynth(c.Message_Oanalz(c.Event_Oknows(c.Message_Oagent_OSpy, v_evsf))), tc.Message_Omsg)   cr
¬ c.in(c.Message_Omsg_OKey(v_K), c.Message_Oanalz(c.Event_Oknows(c.Message_Oagent_OSpy, v_evsf)), tc.Message_Omsg)
c.in(c.Message_Omsg_OCrypt(v_K, c.Message_Omsg_ONonce(v_NB)), c.Message_Oparts(c.insert(v_X, c.Event_Oknows(c.Me
¬ c.in(c.Message_Omsg_OCrypt(v_K, c.Message_Omsg_ONonce(v_NB)), c.Message_Oparts(c.Event_Oknows(c.Message_Oager
c.in(c.Message_Omsg_OCrypt(v_K, v_X), c.Message_Osynth(v_H), tc.Message_Omsg) ⇒ (c.in(c.Message_Omsg_OCrypt(v_K
(c.in(v_Z, c.Message_Oparts(c.insert(v_X, v_H, tc.Message_Omsg)), tc.Message_Omsg) and c.in(v_X, c.Message_Osynth(c.Me
c.in(v_Z, c.union(c.Message_Osynth(c.Message_Oanalz(v_H)), c.Message_Oparts(v_H), tc.Message_Omsg), tc.Message_Omsg)
c.in(v_X, c.Message_Oanalz(v_H), tc.Message_Omsg) ⇒ c.in(v_X, c.Message_Oparts(v_H), tc.Message_Omsg)   cnf(cls.Me
c.in(v_c, c.union(v_A, v_B, t_a), t_a) ⇒ (c.in(v_c, v_B, t_a) or c.in(v_c, v_A, t_a))   cnf(cls.Set_OUn_iff0, axiom)

```

**SWV329-1.p** Cryptographic protocol problem for Yahalom

```

include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-1.ax')
include('Axioms/SWV005-0.ax')
include('Axioms/SWV005-2.ax')
include('Axioms/SWV005-3.ax')
include('Axioms/SWV005-4.ax')
include('Axioms/SWV005-5.ax')
include('Axioms/SWV005-6.ax')
c.in(v_evsf, c.Yahalom_Oyahalom, tc.List_Olist(tc_Event_Oevent))   cnf(cls.conjecture0, negated_conjecture)
c.in(v_X, c.Message_Osynth(c.Message_Oanalz(c.Event_Oknows(c.Message_Oagent_OSpy, v_evsf))), tc.Message_Omsg)   cr
¬ c.in(c.Message_Omsg_OKey(v_K), c.Message_Oanalz(c.Event_Oknows(c.Message_Oagent_OSpy, v_evsf)), tc.Message_Omsg)
c.in(c.Message_Omsg_OCrypt(v_K, c.Message_Omsg_ONonce(v_NB)), c.Message_Oparts(c.insert(v_X, c.Event_Oknows(c.Me

```

$c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_B), c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_A), c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Omsg\_ONonce(v\_NB))), c\_Message\_Omsg\_OAgent(v\_A), c\_Message\_Omsg\_OAgent(v\_A))$   
 $\neg c\_in(v\_B, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_5, negated\_conjecture)$   
 $\neg c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_B), c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_A), c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Omsg\_ONonce(v\_NB))), c\_Message\_Omsg\_OAgent(v\_A), c\_Message\_Omsg\_OAgent(v\_A))$   
 $\neg c\_in(c\_Event\_Oevent\_OSays(v\_A, v\_B, c\_Message\_Omsg\_OMPair(v\_U, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB))), c\_Message\_Omsg\_OMPair(v\_U, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB)))) = v\_X \text{ and } v\_B = v\_Ba) \Rightarrow v\_A \neq c\_Message\_Oagent\_OSpy \quad cnf(cls\_conjecture_8, negated\_conjecture)$

**SWV329-2.p** Cryptographic protocol problem for Yahalom

$c\_in(v\_evsf, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c\_in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_B), c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_A), c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Omsg\_ONonce(v\_NB))), c\_Message\_Omsg\_OAgent(v\_A), c\_Message\_Omsg\_OAgent(v\_A))$   
 $\neg c\_in(v\_B, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_5, negated\_conjecture)$   
 $\neg c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_B), c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_A), c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Omsg\_ONonce(v\_NB))), c\_Message\_Omsg\_OAgent(v\_A), c\_Message\_Omsg\_OAgent(v\_A))$   
 $c\_in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \Rightarrow (c\_in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Osynth(v\_H), tc\_Message\_Omsg) \text{ and } c\_in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf)), tc\_Message\_Omsg))$   
 $c\_in(v\_Z, c\_union(c\_Message\_Osynth(c\_Message\_Oanalz(v\_H)), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg) \text{ and } c\_in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf)), tc\_Message\_Omsg))$   
 $c\_in(v\_Z, c\_union(c\_Message\_Osynth(c\_Message\_Oanalz(v\_H)), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg), tc\_Message\_Omsg) \text{ and } c\_in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf)), tc\_Message\_Omsg))$   
 $c\_in(v\_X, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c\_in(v\_c, c\_union(v\_A, v\_B, t\_a), t\_a) \Rightarrow (c\_in(v\_c, v\_B, t\_a) \text{ or } c\_in(v\_c, v\_A, t\_a)) \quad cnf(cls\_Set\_OU\_iff_0, axiom)$   
 $(c\_in(v\_evs, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \text{ and } c\_in(c\_Message\_Omsg\_OKey(c\_Public\_OshrK(v\_A)), c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Omsg\_ONonce(v\_NB)))$   
 $c\_in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_Yahalom\_OSpy\_analz\_shrK_0, axiom)$

**SWV330-1.p** Cryptographic protocol problem for Yahalom

$include('Axioms/MSC001-0.ax')$   
 $include('Axioms/MSC001-1.ax')$   
 $include('Axioms/SWV005-0.ax')$   
 $include('Axioms/SWV005-2.ax')$   
 $include('Axioms/SWV005-3.ax')$   
 $include('Axioms/SWV005-4.ax')$   
 $include('Axioms/SWV005-5.ax')$   
 $include('Axioms/SWV005-6.ax')$   
 $c\_in(v\_evsf, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c\_in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c\_in(c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB)), c\_Message\_Oparts(c\_insert(v\_X, c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf)), tc\_Message\_Omsg))$   
 $c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_B), c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_A), c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Omsg\_ONonce(v\_NB))), c\_Message\_Omsg\_OAgent(v\_A), c\_Message\_Omsg\_OAgent(v\_A))$   
 $\neg c\_in(v\_B, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_5, negated\_conjecture)$   
 $c\_in(c\_Event\_Oevent\_OSays(v\_A, v\_B, c\_Message\_Omsg\_OMPair(v\_Xa, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB))), c\_Message\_Omsg\_OMPair(v\_Xa, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB))))$   
 $\neg c\_in(c\_Event\_Oevent\_OSays(v\_A, v\_B, c\_Message\_Omsg\_OMPair(v\_U, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB))), c\_Message\_Omsg\_OMPair(v\_U, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB)))) = v\_X \text{ and } v\_B = v\_Ba) \Rightarrow v\_A \neq c\_Message\_Oagent\_OSpy \quad cnf(cls\_conjecture_8, negated\_conjecture)$

**SWV330-2.p** Cryptographic protocol problem for Yahalom

$c\_in(c\_Event\_Oevent\_OSays(v\_A, v\_B, c\_Message\_Omsg\_OMPair(v\_Xa, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB))), c\_Message\_Omsg\_OMPair(v\_Xa, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB))))$   
 $\neg c\_in(c\_Event\_Oevent\_OSays(v\_A, v\_B, c\_Message\_Omsg\_OMPair(v\_U, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB))), c\_Message\_Omsg\_OMPair(v\_U, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB))))$

**SWV331-1.p** Cryptographic protocol problem for Yahalom

$include('Axioms/MSC001-0.ax')$   
 $include('Axioms/MSC001-1.ax')$   
 $include('Axioms/SWV005-0.ax')$   
 $include('Axioms/SWV005-2.ax')$   
 $include('Axioms/SWV005-3.ax')$   
 $include('Axioms/SWV005-4.ax')$   
 $include('Axioms/SWV005-5.ax')$   
 $include('Axioms/SWV005-6.ax')$   
 $c\_in(v\_evs_3, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c\_in(c\_Message\_Omsg\_OKey(v\_K), c\_Event\_Oused(v\_evs_3), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c\_in(v\_K, c\_Message\_OsymKeys, tc\_nat) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c\_in(c\_Event\_Oevent\_OGets(c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_B), c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Omsg\_ONonce(v\_NB))), c\_Message\_Omsg\_OMPair(v\_U, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB))))$   
 $\neg c\_in(c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_3)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_3), tc\_Message\_Omsg))$   
 $\neg c\_in(v\_B, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_6, negated\_conjecture)$

$\neg c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_B), c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_A), c\_Message\_Omsg\_ONonce(v\_U)), c\_Message\_Omsg\_ONonce(v\_U), c\_Event\_Oevent\_OSays(v\_A, v\_B, c\_Message\_Omsg\_OMPair(v\_U, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_U))), tc\_nat))$   
 $\neg c\_in(c\_Event\_Oevent\_OSays(v\_A, v\_B, c\_Message\_Omsg\_OMPair(v\_U, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_U))), tc\_nat))$

**SWV331-2.p** Cryptographic protocol problem for Yahalom

$c\_in(v\_evs_3, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c\_in(c\_Message\_Omsg\_OKey(v\_K), c\_Event\_Oused(v\_evs_3), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c\_in(v\_K, c\_Message\_OsymKeys, tc\_nat) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent(v\_A), c\_Message\_Omsg\_ONonce(v\_U)), tc\_Message\_Omsg)) \Rightarrow c\_in(v\_K, c\_Message\_OkeyFor(c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent(v\_A), c\_Message\_Omsg\_ONonce(v\_U))), tc\_nat))$   
 $c\_in(c\_Message\_Omsg\_OKey(v\_K), c\_Event\_Oused(v\_evs), tc\_Message\_Omsg) \quad cnf(cls\_Yahalom\_Onew\_keys\_not\_used_0, ax)$

**SWV332-1.p** Cryptographic protocol problem for Yahalom

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-1.ax')$   
 $include('Axioms/SWV005-0.ax')$   
 $include('Axioms/SWV005-2.ax')$   
 $include('Axioms/SWV005-3.ax')$   
 $include('Axioms/SWV005-4.ax')$   
 $include('Axioms/SWV005-5.ax')$   
 $include('Axioms/SWV005-6.ax')$   
 $c\_in(v\_evs_4, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $v\_Aa \neq c\_Message\_Oagent\_OServer \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c\_in(c\_Event\_Oevent\_OSays(v\_A, v\_B, c\_Message\_Omsg\_OMPair(v\_U, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_U)), tc\_Message\_Omsg)) \Rightarrow v\_A \neq v\_Aa \quad cnf(cls\_conjecture_{11}, negated\_conjecture)$   
 $c\_in(v\_K, c\_Message\_OsymKeys, tc\_nat) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c\_in(c\_Event\_Oevent\_OGets(v\_Aa, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_Aa), c\_Message\_Omsg\_ONonce(v\_U)), tc\_Message\_Omsg)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c\_in(c\_Event\_Oevent\_OSays(v\_Aa, v\_Ba, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_Aa), c\_Message\_Omsg\_ONonce(v\_U)), tc\_Message\_Omsg)) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent(v\_Aa), c\_Message\_Omsg\_ONonce(v\_U)), tc\_Message\_Omsg)) \quad cnf(cls\_conjecture_5, negated\_conjecture)$   
 $\neg c\_in(c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent(v\_Aa), c\_Message\_Omsg\_ONonce(v\_U)), tc\_Message\_Omsg)) \quad cnf(cls\_conjecture_6, negated\_conjecture)$   
 $\neg c\_in(c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent(v\_Aa), c\_Message\_Omsg\_ONonce(v\_U)), tc\_Message\_Omsg)) \quad cnf(cls\_conjecture_7, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_B), c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_A), c\_Message\_Omsg\_ONonce(v\_U))), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_8, negated\_conjecture)$   
 $\neg c\_in(v\_B, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_9, negated\_conjecture)$

**SWV333-1.p** Cryptographic protocol problem for Yahalom

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-1.ax')$   
 $include('Axioms/SWV005-0.ax')$   
 $include('Axioms/SWV005-2.ax')$   
 $include('Axioms/SWV005-3.ax')$   
 $include('Axioms/SWV005-4.ax')$   
 $include('Axioms/SWV005-5.ax')$   
 $include('Axioms/SWV005-6.ax')$   
 $c\_in(v\_evs_4, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $v\_Aa \neq c\_Message\_Oagent\_OServer \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c\_in(c\_Event\_Oevent\_OSays(v\_A, v\_B, c\_Message\_Omsg\_OMPair(v\_U, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_U)), tc\_Message\_Omsg)) \Rightarrow v\_A \neq v\_Aa \quad cnf(cls\_conjecture_{11}, negated\_conjecture)$   
 $c\_in(v\_K, c\_Message\_OsymKeys, tc\_nat) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c\_in(c\_Event\_Oevent\_OGets(v\_Aa, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_Aa), c\_Message\_Omsg\_ONonce(v\_U)), tc\_Message\_Omsg)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c\_in(c\_Event\_Oevent\_OSays(v\_Aa, v\_Ba, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_Aa), c\_Message\_Omsg\_ONonce(v\_U)), tc\_Message\_Omsg)) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent(v\_Aa), c\_Message\_Omsg\_ONonce(v\_U)), tc\_Message\_Omsg)) \quad cnf(cls\_conjecture_5, negated\_conjecture)$   
 $\neg c\_in(c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent(v\_Aa), c\_Message\_Omsg\_ONonce(v\_U)), tc\_Message\_Omsg)) \quad cnf(cls\_conjecture_6, negated\_conjecture)$   
 $c\_in(c\_Event\_Oevent\_OSays(v\_A, v\_B, c\_Message\_Omsg\_OMPair(v\_Xa, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_U))), tc\_Message\_Omsg)) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent(v\_Aa), c\_Message\_Omsg\_ONonce(v\_U)), tc\_Message\_Omsg)) \quad cnf(cls\_conjecture_7, negated\_conjecture)$   
 $c\_in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_B), c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_A), c\_Message\_Omsg\_ONonce(v\_U))), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_8, negated\_conjecture)$   
 $\neg c\_in(v\_B, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_9, negated\_conjecture)$

**SWV333-2.p** Cryptographic protocol problem for Yahalom

$\neg c\_in(c\_Event\_Oevent\_OSays(v\_A, v\_B, c\_Message\_Omsg\_OMPair(v\_U, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_U))), tc\_Message\_Omsg)) \Rightarrow v\_A \neq v\_Aa \quad cnf(cls\_conjecture_{11}, negated\_conjecture)$   
 $c\_in(c\_Event\_Oevent\_OSays(v\_A, v\_B, c\_Message\_Omsg\_OMPair(v\_Xa, c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_U))), tc\_Message\_Omsg)) \Rightarrow c\_in(v\_X, c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent(v\_Aa), c\_Message\_Omsg\_ONonce(v\_U)), tc\_Message\_Omsg)) \quad cnf(cls\_conjecture_7, negated\_conjecture)$

**SWV334-1.p** Cryptographic protocol problem for Yahalom

$include('Axioms/MS001-0.ax')$



```

include('Axioms/MSC001-1.ax')
include('Axioms/SWV005-0.ax')
include('Axioms/SWV005-2.ax')
include('Axioms/SWV005-3.ax')
include('Axioms/SWV005-4.ax')
include('Axioms/SWV005-5.ax')
include('Axioms/SWV005-6.ax')
c.in(v_evs4, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture0, negated_conjecture)
v_Aa ≠ c_Message_Oagent_OServer    cnf(cls_conjecture1, negated_conjecture)
¬ c.in(v_B, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture10, negated_conjecture)
¬ c.in(c_Event_Oevent_OSays(v_A, v_B, c_Message_Omsg_OMPair(v_U, c_Message_Omsg_OCrypt(v_K, c_Message_Omsg_ONonce(v_NB = v_NBa and v_K = v_Ka and v_U = v_X and v_B = v_Ba)) ⇒ v_A ≠ v_Aa    cnf(cls_conjecture12, negated_conjecture)
c.in(v_Ka, c_Message_OsymKeys, tc_nat)    cnf(cls_conjecture2, negated_conjecture)
c.in(c_Event_Oevent_OGets(v_Aa, c_Message_Omsg_OMPair(c_Message_Omsg_OCrypt(c_Public_OshrK(v_Aa), c_Message_Omsg_ONonce(v_NB = v_NBa and v_K = v_Ka and v_U = v_X and v_B = v_Ba)), c_Message_Omsg_ONonce(v_NB = v_NBa and v_K = v_Ka and v_U = v_X and v_B = v_Ba))) ⇒ v_A ≠ v_Aa    cnf(cls_conjecture12, negated_conjecture)
c.in(c_Event_Oevent_OSays(v_Aa, v_Ba, c_Message_Omsg_OMPair(c_Message_Omsg_OAgent(v_Aa), c_Message_Omsg_ONonce(v_NB = v_NBa and v_K = v_Ka and v_U = v_X and v_B = v_Ba))) ⇒ v_A ≠ v_Aa    cnf(cls_conjecture12, negated_conjecture)
c.in(v_X, c_Message_Oparts(c_Event_Oknows(c_Message_Oagent_OSpy, v_evs4)), tc_Message_Omsg)    cnf(cls_conjecture5, negated_conjecture)
¬ c.in(c_Message_Omsg_OKey(v_K), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evs4)), tc_Message_Omsg)    cnf(cls_conjecture5, negated_conjecture)
c.in(c_Event_Oevent_OSays(v_A, v_B, c_Message_Omsg_OMPair(v_Xa, c_Message_Omsg_OCrypt(v_K, c_Message_Omsg_ONonce(v_NB = v_NBa and v_K = v_Ka and v_U = v_X and v_B = v_Ba))) ⇒ v_A ≠ v_Aa    cnf(cls_conjecture12, negated_conjecture)
c.in(c_Message_Omsg_OCrypt(v_K, c_Message_Omsg_ONonce(v_NB)), c_Message_Oparts(c_Event_Oknows(c_Message_Oagent_OSpy, v_evs4)), tc_Message_Omsg)    cnf(cls_conjecture5, negated_conjecture)
c.in(c_Message_Omsg_OCrypt(c_Public_OshrK(v_B), c_Message_Omsg_OMPair(c_Message_Omsg_OAgent(v_A), c_Message_Omsg_ONonce(v_NB = v_NBa and v_K = v_Ka and v_U = v_X and v_B = v_Ba))) ⇒ v_A ≠ v_Aa    cnf(cls_conjecture12, negated_conjecture)

```

### SWV334-2.p Cryptographic protocol problem for Yahalom

```

¬ c.in(c_Event_Oevent_OSays(v_A, v_B, c_Message_Omsg_OMPair(v_U, c_Message_Omsg_OCrypt(v_K, c_Message_Omsg_ONonce(v_NB = v_NBa and v_K = v_Ka and v_U = v_X and v_B = v_Ba))) ⇒ v_A ≠ v_Aa    cnf(cls_conjecture12, negated_conjecture)
c.in(c_Event_Oevent_OSays(v_A, v_B, c_Message_Omsg_OMPair(v_Xa, c_Message_Omsg_OCrypt(v_K, c_Message_Omsg_ONonce(v_NB = v_NBa and v_K = v_Ka and v_U = v_X and v_B = v_Ba))) ⇒ v_A ≠ v_Aa    cnf(cls_conjecture12, negated_conjecture)

```

### SWV335-1.p Cryptographic protocol problem for Yahalom

```

include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-2.ax')
include('Axioms/SWV006-0.ax')
include('Axioms/SWV006-3.ax')
c.in(v_evsf, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture0, negated_conjecture)
c.in(v_X, c_Message_Osynth(c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evsf))), tc_Message_Omsg)    cnf(cls_conjecture5, negated_conjecture)
¬ c.in(c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evsf)), tc_Message_Omsg)    cnf(cls_conjecture5, negated_conjecture)
c.in(c_Message_Omsg_OCrypt(v_K, c_Message_Omsg_ONonce(v_NB)), c_Message_Oparts(c_insert(v_X, c_Event_Oknows(c_Message_Oagent_OSpy, v_evsf))), tc_Message_Omsg)    cnf(cls_conjecture5, negated_conjecture)
¬ c.in(c_Message_Omsg_OCrypt(v_K, c_Message_Omsg_ONonce(v_NB)), c_Message_Oparts(c_Event_Oknows(c_Message_Oagent_OSpy, v_evsf)), tc_Message_Omsg)    cnf(cls_conjecture5, negated_conjecture)
¬ c.in(c_Event_Oevent_OSays(c_Message_Oagent_OServer, v_U, c_Message_Omsg_OMPair(c_Message_Omsg_OCrypt(c_Public_OshrK(v_B), c_Message_Omsg_OMPair(v_Xa, c_Message_Omsg_OCrypt(v_K, c_Message_Omsg_ONonce(v_NB = v_NBa and v_K = v_Ka and v_U = v_X and v_B = v_Ba))), c_Message_Omsg_ONonce(v_NB = v_NBa and v_K = v_Ka and v_U = v_X and v_B = v_Ba))) ⇒ v_A ≠ v_Aa    cnf(cls_conjecture12, negated_conjecture)

```

### SWV335-2.p Cryptographic protocol problem for Yahalom

```

c.in(v_X, c_Message_Osynth(c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evsf))), tc_Message_Omsg)    cnf(cls_conjecture5, negated_conjecture)
¬ c.in(c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evsf)), tc_Message_Omsg)    cnf(cls_conjecture5, negated_conjecture)
c.in(c_Message_Omsg_OCrypt(v_K, c_Message_Omsg_ONonce(v_NB)), c_Message_Oparts(c_insert(v_X, c_Event_Oknows(c_Message_Oagent_OSpy, v_evsf))), tc_Message_Omsg)    cnf(cls_conjecture5, negated_conjecture)
¬ c.in(c_Message_Omsg_OCrypt(v_K, c_Message_Omsg_ONonce(v_NB)), c_Message_Oparts(c_Event_Oknows(c_Message_Oagent_OSpy, v_evsf)), tc_Message_Omsg)    cnf(cls_conjecture5, negated_conjecture)
c.in(c_Message_Omsg_OCrypt(v_K, v_X), c_Message_Osynth(v_H), tc_Message_Omsg) ⇒ (c.in(v_X, c_Message_Osynth(v_H), tc_Message_Omsg) and (c.in(v_Z, c_Message_Oparts(c_insert(v_X, v_H, tc_Message_Omsg)), tc_Message_Omsg) and c.in(v_X, c_Message_Osynth(c_Message_Oanalz(v_H), c_Message_Oparts(v_H), tc_Message_Omsg), tc_Message_Omsg)))
c.in(v_Z, c_union(c_Message_Osynth(c_Message_Oanalz(v_H), c_Message_Oparts(v_H), tc_Message_Omsg), tc_Message_Omsg), tc_Message_Omsg) and c.in(v_X, c_Message_Osynth(c_Message_Oanalz(v_H), c_Message_Oparts(v_H), tc_Message_Omsg), tc_Message_Omsg) ⇒ c.in(v_Z, c_union(c_Message_Osynth(c_Message_Oanalz(v_H), c_Message_Oparts(v_H), tc_Message_Omsg), tc_Message_Omsg), tc_Message_Omsg) and c.in(v_X, c_Message_Osynth(c_Message_Oanalz(v_H), c_Message_Oparts(v_H), tc_Message_Omsg), tc_Message_Omsg)
c.in(c_Message_Omsg_ONonce(v_n), c_Message_Osynth(v_H), tc_Message_Omsg) ⇒ c.in(c_Message_Omsg_ONonce(v_n), v_H, tc_Message_Omsg) and c.in(v_c, c_Message_Oanalz(v_H), tc_Message_Omsg) ⇒ c.in(v_c, c_Message_Oparts(v_H), tc_Message_Omsg)    cnf(cls_Message_Oanalz, axiom)
c.in(v_c, c_union(v_A, v_B, t_a), t_a) ⇒ (c.in(v_c, v_B, t_a) or c.in(v_c, v_A, t_a))    cnf(cls_Set_OUnE0, axiom)

```

### SWV336-1.p Cryptographic protocol problem for Yahalom

```

include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-2.ax')
include('Axioms/SWV006-0.ax')
include('Axioms/SWV006-3.ax')
c.in(v_evs3, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture0, negated_conjecture)
¬ c.in(c_Message_Omsg_OKey(v_KAB), c_Event_Oused(v_evs3), tc_Message_Omsg)    cnf(cls_conjecture1, negated_conjecture)
c.in(v_KAB, c_Message_OsymKeys, tc_nat)    cnf(cls_conjecture2, negated_conjecture)
c.in(c_Event_Oevent_OGets(c_Message_Oagent_OServer, c_Message_Omsg_OMPair(c_Message_Omsg_OAgent(v_B), c_Message_Omsg_ONonce(v_NB = v_NBa and v_K = v_Ka and v_U = v_X and v_B = v_Ba))), c_Message_Omsg_ONonce(v_NB = v_NBa and v_K = v_Ka and v_U = v_X and v_B = v_Ba)) ⇒ v_A ≠ v_Aa    cnf(cls_conjecture12, negated_conjecture)
¬ c.in(c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evs3)), tc_Message_Omsg)    cnf(cls_conjecture5, negated_conjecture)
c.in(c_Message_Omsg_OCrypt(v_K, c_Message_Omsg_ONonce(v_NB)), c_Message_Oparts(c_Event_Oknows(c_Message_Oagent_OSpy, v_evs3)), tc_Message_Omsg)    cnf(cls_conjecture5, negated_conjecture)
c.in(c_Event_Oevent_OSays(c_Message_Oagent_OServer, v_Aa, c_Message_Omsg_OMPair(c_Message_Omsg_OCrypt(c_Public_OshrK(v_B), c_Message_Omsg_OMPair(v_Xa, c_Message_Omsg_OCrypt(v_K, c_Message_Omsg_ONonce(v_NB = v_NBa and v_K = v_Ka and v_U = v_X and v_B = v_Ba))), c_Message_Omsg_ONonce(v_NB = v_NBa and v_K = v_Ka and v_U = v_X and v_B = v_Ba))) ⇒ v_A ≠ v_Aa    cnf(cls_conjecture12, negated_conjecture)

```

$\neg c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_OServer, v\_U, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), v\_NB, v\_W, v\_K, v\_V))) \Rightarrow v\_U \neq v\_A \quad \text{cnf}(cls\_conjecture_8, \text{negated\_conjecture})$

**SWV336-2.p** Cryptographic protocol problem for Yahalom

$c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_OServer, v\_Aa, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), v\_NB, v\_W, v\_K, v\_V))) \wedge$   
 $\neg c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_OServer, v\_U, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), v\_NB, v\_W, v\_K, v\_V)))$

**SWV337-1.p** Cryptographic protocol problem for Yahalom

include('Axioms/MS001-0.ax')

include('Axioms/MS001-2.ax')

include('Axioms/SWV006-0.ax')

include('Axioms/SWV006-3.ax')

$c.in(v\_evs_4, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad \text{cnf}(cls\_conjecture_0, \text{negated\_conjecture})$

$v\_A \neq c\_Message\_Oagent\_OServer \quad \text{cnf}(cls\_conjecture_1, \text{negated\_conjecture})$

$c.in(v\_K, c\_Message\_OsymKeys, tc\_nat) \quad \text{cnf}(cls\_conjecture_2, \text{negated\_conjecture})$

$c.in(c\_Event\_Oevent\_OGets(v\_A, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_ONonce(v\_NB), v\_W, v\_K, v\_V)))$

$c.in(c\_Event\_Oevent\_OSays(v\_A, v\_B, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_A), c\_Message\_Omsg\_ONonce(v\_NB), v\_W, v\_K, v\_V)))$

$c.in(v\_X, c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_4)), tc\_Message\_Omsg) \quad \text{cnf}(cls\_conjecture_5, \text{negated\_conjecture})$

$\neg c.in(c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_4)), tc\_Message\_Omsg)$

$\neg c.in(c\_Message\_Omsg\_OCrypt(v\_K, c\_Message\_Omsg\_ONonce(v\_NB)), c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_4)), tc\_Message\_Omsg)$

$\neg c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_OServer, v\_U, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), v\_NB, v\_W, v\_K, v\_V)))$

**SWV337-2.p** Cryptographic protocol problem for Yahalom

$c.in(v\_evs_4, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad \text{cnf}(cls\_conjecture_0, \text{negated\_conjecture})$

$c.in(c\_Event\_Oevent\_OGets(v\_A, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), c\_Message\_Omsg\_ONonce(v\_NB), v\_W, v\_K, v\_V)))$

$\neg c.in(c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_4)), tc\_Message\_Omsg)$

$\neg c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_OServer, v\_U, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), v\_NB, v\_W, v\_K, v\_V)))$

$c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_Y, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg)$

$c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg)$

$c.in(v\_c, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_c, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad \text{cnf}(cls\_Message\_Oparts, \text{negated\_conjecture})$

$(c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \wedge c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), v\_X), c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg))$

$c.in(v\_X, c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) \quad \text{cnf}(cls\_Public\_OCrypt, \text{negated\_conjecture})$

$(c.in(v\_evs, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \wedge c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), v\_X), c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg))$

$(c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \vee c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_OServer, v\_A, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), v\_NB, v\_W, v\_K, v\_V)))$

$(c.in(v\_evs, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \wedge c.in(c\_Event\_Oevent\_OGets(v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent)))$

$c.in(v\_X, c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) \quad \text{cnf}(cls\_Yahalom\_OGets, \text{negated\_conjecture})$

**SWV338-1.p** Cryptographic protocol problem for Yahalom

include('Axioms/MS001-0.ax')

include('Axioms/MS001-1.ax')

include('Axioms/SWV005-0.ax')

include('Axioms/SWV005-2.ax')

include('Axioms/SWV005-3.ax')

include('Axioms/SWV005-4.ax')

$(c.in(v\_K, c\_Message\_OkeysFor(c\_Message\_Oparts(c\_insert(v\_X, v\_G, tc\_Message\_Omsg))), tc\_nat) \wedge c.in(v\_X, c\_Message\_Oparts(c\_insert(v\_X, v\_G, tc\_Message\_Omsg))), tc\_nat) \wedge$

$(c.in(v\_K, c\_Message\_OkeysFor(c\_Message\_Oparts(c\_union(v\_G, v\_H, tc\_Message\_Omsg))), tc\_nat) \vee c.in(c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Oparts(c\_insert(v\_X, v\_G, tc\_Message\_Omsg))), tc\_nat)$

$c.in(v\_K, c\_Message\_OsymKeys, tc\_nat) \quad \text{cnf}(cls\_conjecture_0, \text{negated\_conjecture})$

$c.in(v\_evsf, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad \text{cnf}(cls\_conjecture_1, \text{negated\_conjecture})$

$c.in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg) \quad \text{cnf}(cls\_Message\_OSynth, \text{negated\_conjecture})$

$\neg c.in(c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Oparts(c\_insert(v\_X, c\_emptyset, tc\_Message\_Omsg))), tc\_Message\_Omsg) \quad \text{cnf}(cls\_Message\_OKey, \text{negated\_conjecture})$

$\neg c.in(c\_Message\_Omsg\_OKey(v\_K), c\_Event\_Oused(v\_evsf), tc\_Message\_Omsg) \quad \text{cnf}(cls\_conjecture_4, \text{negated\_conjecture})$

$c.in(v\_K, c\_Message\_OkeysFor(c\_Message\_Oparts(c\_insert(v\_X, c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg) \quad \text{cnf}(cls\_Message\_OkeysFor, \text{negated\_conjecture})$

$c.in(v\_K, c\_Message\_OkeysFor(c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_nat) \Rightarrow c.in(c\_Message\_Oparts(c\_insert(v\_X, v\_G, tc\_Message\_Omsg))), tc\_nat)$

**SWV338-2.p** Cryptographic protocol problem for Yahalom

$c.in(v\_c, c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) \Rightarrow c.in(v\_c, c\_Event\_Oused(v\_evs), tc\_Message\_Omsg)$

$(c.in(v\_K, c\_Message\_OkeysFor(c\_Message\_Oparts(c\_insert(v\_X, v\_G, tc\_Message\_Omsg))), tc\_nat) \wedge c.in(v\_X, c\_Message\_Oparts(c\_insert(v\_X, v\_G, tc\_Message\_Omsg))), tc\_nat) \wedge$

$(c.in(v\_K, c\_Message\_OkeysFor(c\_Message\_Oparts(c\_union(v\_G, v\_H, tc\_Message\_Omsg))), tc\_nat) \vee c.in(c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Oparts(c\_insert(v\_X, v\_G, tc\_Message\_Omsg))), tc\_nat)$

$c.in(v\_y, c\_Message\_OsymKeys, tc\_nat) \Rightarrow c\_Message\_OinvKey(v\_y) = v\_y \quad \text{cnf}(cls\_Public\_OinvKey\_K_0, \text{axiom})$

$c.union(v\_y, v\_y, t\_a) = v\_y \quad \text{cnf}(cls\_Set\_OUn\_absorb_0, \text{axiom})$

$c.in(v\_K, c\_Message\_OsymKeys, tc\_nat) \quad \text{cnf}(cls\_conjecture_0, \text{negated\_conjecture})$

$c.in(v\_X, c\_Message\_Osynth(c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evsf))), tc\_Message\_Omsg) \quad \text{cnf}(cls\_Message\_OSynth, \text{negated\_conjecture})$



(c.in(v\_evs, c.Yahalom\_Oyahalom, tc.List\_Olist(tc\_Event\_Oevent)) and c.in(c\_Event\_Oevent\_OGets(v\_B, v\_X), c.List\_Oset(v\_evs, c.in(v\_X, c.Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) cnf(cls\_Yahalom\_OGets

**SWV341-2.p** Cryptographic protocol problem for Yahalom

¬ c.in(c\_Message\_Omsg\_OKey(v\_K), c\_Event\_Oused(v\_evs<sub>3</sub>), tc\_Message\_Omsg) cnf(cls\_conjecture<sub>1</sub>, negated\_conjecture)  
 c.in(c\_Message\_Omsg\_OKey(v\_K), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs<sub>3</sub>)), tc\_Message\_Omsg)  
 c.in(v\_c, c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) ⇒ c.in(v\_c, c\_Event\_Oused  
 c.in(v\_X, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) ⇒ c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) cnf(cls\_Mes

**SWV342-2.p** Cryptographic protocol problem for Yahalom

¬ c.in(c\_Message\_Omsg\_OKey(v\_K), c\_Event\_Oused(v\_evs<sub>3</sub>), tc\_Message\_Omsg) cnf(cls\_conjecture<sub>3</sub>, negated\_conjecture)  
 c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_Oserver, v\_A, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_O  
 c.in(c\_Event\_Oevent\_OSays(v\_A, v\_B, v\_X), c.List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent) ⇒ c.in(v\_X, c\_Message\_Oa  
 c.in(v\_c, c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) ⇒ c.in(v\_c, c\_Event\_Oused  
 c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) ⇒ c.in(v\_Y, c\_Message\_Oanalz(v\_H), tc  
 c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) ⇒ c.in(v\_Y, c\_Message\_Oparts(v\_H), tc  
 c.in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) ⇒ c.in(v\_X, c\_Message\_Oparts(v\_H), tc  
 c.in(v\_X, v\_H, tc\_Message\_Omsg) ⇒ c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) cnf(cls\_Message\_Oparts\_OInj<sub>0</sub>,  
 c\_Message\_Oparts(c\_Message\_Oanalz(v\_H)) = c\_Message\_Oparts(v\_H) cnf(cls\_Message\_Oparts\_\_analz<sub>0</sub>, axiom)

**SWV343-2.p** Cryptographic protocol problem for Yahalom

c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_Oserver, v\_A, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_O  
 ¬ c.in(c\_Message\_Omsg\_OKey(v\_K), c\_Event\_Oused(v\_evs<sub>3</sub>), tc\_Message\_Omsg) cnf(cls\_conjecture<sub>3</sub>, negated\_conjecture)  
 c.in(c\_Event\_Oevent\_OSays(v\_A, v\_B, v\_X), c.List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent) ⇒ c.in(v\_X, c\_Message\_Oa  
 c.in(v\_c, c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) ⇒ c.in(v\_c, c\_Event\_Oused  
 c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) ⇒ c.in(v\_Y, c\_Message\_Oanalz(v\_H), tc  
 c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) ⇒ c.in(v\_Y, c\_Message\_Oparts(v\_H), tc  
 c.in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) ⇒ c.in(v\_X, c\_Message\_Oparts(v\_H), tc  
 c.in(v\_X, v\_H, tc\_Message\_Omsg) ⇒ c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) cnf(cls\_Message\_Oparts\_OInj<sub>0</sub>,  
 c\_Message\_Oparts(c\_Message\_Oanalz(v\_H)) = c\_Message\_Oparts(v\_H) cnf(cls\_Message\_Oparts\_\_analz<sub>0</sub>, axiom)

**SWV344-2.p** Cryptographic protocol problem for Yahalom

¬ c.in(c\_Message\_Omsg\_OKey(v\_K), c\_Event\_Oused(v\_evs<sub>3</sub>), tc\_Message\_Omsg) cnf(cls\_conjecture<sub>3</sub>, negated\_conjecture)  
 c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_Oserver, v\_A, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_O  
 c.in(c\_Event\_Oevent\_OSays(v\_A, v\_B, v\_X), c.List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent) ⇒ c.in(v\_X, c\_Message\_Oa  
 c.in(v\_c, c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) ⇒ c.in(v\_c, c\_Event\_Oused  
 c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) ⇒ c.in(v\_Y, c\_Message\_Oanalz(v\_H), tc  
 c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) ⇒ c.in(v\_Y, c\_Message\_Oparts(v\_H), tc  
 c.in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) ⇒ c.in(v\_X, c\_Message\_Oparts(v\_H), tc  
 c.in(v\_X, v\_H, tc\_Message\_Omsg) ⇒ c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) cnf(cls\_Message\_Oparts\_OInj<sub>0</sub>,  
 c\_Message\_Oparts(c\_Message\_Oanalz(v\_H)) = c\_Message\_Oparts(v\_H) cnf(cls\_Message\_Oparts\_\_analz<sub>0</sub>, axiom)

**SWV345-2.p** Cryptographic protocol problem for Yahalom

(c.in(v\_evs, c.Yahalom\_Oyahalom, tc.List\_Olist(tc\_Event\_Oevent)) and c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_OServ  
 v\_nb = v\_nb\_H cnf(cls\_Yahalom\_Ounique\_\_session\_\_keys\_\_dest<sub>3</sub>, axiom)  
 c.in(v\_evso, c.Yahalom\_Oyahalom, tc.List\_Olist(tc\_Event\_Oevent)) cnf(cls\_conjecture<sub>2</sub>, negated\_conjecture)  
 c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_Oserver, v\_Aa, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_O  
 c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_Oserver, v\_A, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_O  
 v\_nb ≠ c\_Message\_Omsg\_ONonce(v\_NB) cnf(cls\_conjecture<sub>7</sub>, negated\_conjecture)

**SWV346-2.p** Cryptographic protocol problem for Yahalom

(c.in(v\_evs, c.Yahalom\_Oyahalom, tc.List\_Olist(tc\_Event\_Oevent)) and c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_OServ  
 v\_na = v\_na\_H cnf(cls\_Yahalom\_Ounique\_\_session\_\_keys\_\_dest<sub>2</sub>, axiom)  
 c.in(v\_evso, c.Yahalom\_Oyahalom, tc.List\_Olist(tc\_Event\_Oevent)) cnf(cls\_conjecture<sub>2</sub>, negated\_conjecture)  
 c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_Oserver, v\_Aa, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_O  
 c.in(c\_Event\_Oevent\_OSays(c\_Message\_Oagent\_Oserver, v\_A, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_O  
 v\_na ≠ c\_Message\_Omsg\_ONonce(v\_NA) cnf(cls\_conjecture<sub>7</sub>, negated\_conjecture)

**SWV347-1.p** Cryptographic protocol problem for Yahalom

include('Axioms/MSC001-0.ax')  
 include('Axioms/MSC001-1.ax')  
 include('Axioms/SWV005-0.ax')  
 include('Axioms/SWV005-2.ax')

```

include('Axioms/SWV005-3.ax')
include('Axioms/SWV005-4.ax')
include('Axioms/SWV005-5.ax')
include('Axioms/SWV005-7.ax')
- c.in(v_A, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_0, negated_conjecture)
- c.in(v_B, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_1, negated_conjecture)
c.in(v_Aa, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_11, negated_conjecture)
c.in(v_evs_3, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture_2, negated_conjecture)
- c.in(c_Message_Omsg_OKey(v_KAB), c_Event_Oused(v_evs_3), tc_Message_Omsg)    cnf(cls_conjecture_3, negated_conjecture)
c.in(v_KAB, c_Message_OsymKeys, tc_nat)    cnf(cls_conjecture_4, negated_conjecture)
c.in(c_Event_Oevent_OGets(c_Message_Oagent_OServer, c_Message_Omsg_OMPair(c_Message_Omsg_OAgent(v_Ba), c_Message_Omsg_ONonce(v_NA), c_Message_Omsg_OKey(v_KAB)))
- c.in(c_Event_Oevent_ONotes(c_Message_Oagent_OSpy, c_Message_Omsg_OMPair(c_Message_Omsg_ONonce(v_NA), c_Message_Omsg_OKey(v_KAB)))
c.in(c_Event_Oevent_OSays(v_B, c_Message_Oagent_OServer, c_Message_Omsg_OMPair(c_Message_Omsg_OAgent(v_B), c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evs_3))), tc_Message_Omsg)
- c.in(c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evs_3))), tc_Message_Omsg)
c.in(v_Aa, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_9, negated_conjecture)

```

#### SWV347-2.p Cryptographic protocol problem for Yahalom

```

(c.in(v_evs, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent)) and c.in(c_Event_Oevent_OGets(v_S_H, c_Message_Omsg_OMPair(c_Message_Omsg_OAgent(v_Ba), c_Message_Omsg_ONonce(v_NA), c_Message_Omsg_OKey(v_KAB)))
(c.in(v_nb, c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evs)), tc_Message_Omsg) or v_A_H = v_A)    cnf(cls_conjecture_10, negated_conjecture)
- c.in(v_A, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_0, negated_conjecture)
c.in(v_Aa, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_11, negated_conjecture)
c.in(v_evs_3, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture_2, negated_conjecture)
c.in(c_Event_Oevent_OGets(c_Message_Oagent_OServer, c_Message_Omsg_OMPair(c_Message_Omsg_OAgent(v_Ba), c_Message_Omsg_ONonce(v_NA), c_Message_Omsg_OKey(v_KAB)))
c.in(c_Event_Oevent_OSays(v_B, c_Message_Oagent_OServer, c_Message_Omsg_OMPair(c_Message_Omsg_OAgent(v_B), c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evs_3))), tc_Message_Omsg)
- c.in(c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evs_3))), tc_Message_Omsg)

```

#### SWV348-1.p Cryptographic protocol problem for Yahalom

```

include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-1.ax')
include('Axioms/SWV005-0.ax')
include('Axioms/SWV005-2.ax')
include('Axioms/SWV005-3.ax')
include('Axioms/SWV005-4.ax')
include('Axioms/SWV005-5.ax')
include('Axioms/SWV005-7.ax')
- c.in(v_A, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_0, negated_conjecture)
- c.in(v_B, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_1, negated_conjecture)
- c.in(c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evs_4))), tc_Message_Omsg)
c.in(c_Message_Omsg_OKey(v_K), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evs_4))), tc_Message_Omsg)
c.in(v_evs_4, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture_2, negated_conjecture)
v_Aa ≠ c_Message_Oagent_OServer    cnf(cls_conjecture_3, negated_conjecture)
c.in(v_K, c_Message_OsymKeys, tc_nat)    cnf(cls_conjecture_4, negated_conjecture)
c.in(c_Event_Oevent_OGets(v_Aa, c_Message_Omsg_OMPair(c_Message_Omsg_OCrypt(c_Public_OshrK(v_Aa), c_Message_Omsg_ONonce(v_NB), c_Message_Omsg_OKey(v_K)))
c.in(c_Event_Oevent_OSays(v_Aa, v_Ba, c_Message_Omsg_OMPair(c_Message_Omsg_OAgent(v_Aa), c_Message_Omsg_ONonce(v_NB), c_Message_Omsg_OKey(v_K)))
c.in(v_X, c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evs_4))), tc_Message_Omsg)    cnf(cls_conjecture_7, negated_conjecture)
- c.in(c_Event_Oevent_ONotes(c_Message_Oagent_OSpy, c_Message_Omsg_OMPair(c_Message_Omsg_ONonce(v_NA), c_Message_Omsg_OKey(v_K)))
c.in(c_Event_Oevent_OSays(v_B, c_Message_Oagent_OServer, c_Message_Omsg_OMPair(c_Message_Omsg_OAgent(v_B), c_Message_Omsg_ONonce(v_NB), c_Message_Omsg_OKey(v_K)))

```

#### SWV349-1.p Cryptographic protocol problem for Yahalom

```

include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-1.ax')
include('Axioms/SWV005-0.ax')
include('Axioms/SWV005-2.ax')
include('Axioms/SWV005-3.ax')
include('Axioms/SWV005-4.ax')
include('Axioms/SWV005-5.ax')
include('Axioms/SWV005-7.ax')
- c.in(v_A, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_0, negated_conjecture)
- c.in(v_B, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_1, negated_conjecture)
c.in(v_evso, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture_2, negated_conjecture)
c.in(c_Event_Oevent_OSays(c_Message_Oagent_OServer, v_Aa, c_Message_Omsg_OMPair(c_Message_Omsg_OCrypt(c_Public_OshrK(v_Aa), c_Message_Omsg_ONonce(v_NB), c_Message_Omsg_OKey(v_K)))

```



```

- c.in(v_A, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_0, negated_conjecture)
- c.in(v_B, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_1, negated_conjecture)
c.in(v_evso, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture_2, negated_conjecture)
c.in(c_Event_Oevent_OSays(c_Message_Oagent_OServer, v_Aa, c_Message_Omsg_OMPair(c_Message_Omsg_OCrypt(c_Public_
- c.in(c_Event_Oevent_ONotes(c_Message_Oagent_OSpy, c_Message_Omsg_OMPair(c_Message_Omsg_ONonce(v_NA), c_Messa
c.in(c_Event_Oevent_OSays(v_B, c_Message_Oagent_OServer, c_Message_Omsg_OMPair(c_Message_Omsg_OAgent(v_B), c_Mes
- c.in(c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evso)), tc_Message_O
(v_U = c_Message_Omsg_OKey(v_K) and v_NA = v_NB) ⇒ v_NB ≠ v_NBa    cnf(cls_conjecture_8, negated_conjecture)

```

**SWV353-1.p** Cryptographic protocol problem for Yahalom

```

include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-1.ax')
include('Axioms/SWV005-0.ax')
include('Axioms/SWV005-2.ax')
include('Axioms/SWV005-3.ax')
include('Axioms/SWV005-4.ax')
include('Axioms/SWV005-5.ax')
include('Axioms/SWV005-7.ax')
- c.in(v_A, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_0, negated_conjecture)
- c.in(v_B, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_1, negated_conjecture)
c.in(v_evso, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture_2, negated_conjecture)
c.in(c_Event_Oevent_OSays(c_Message_Oagent_OServer, v_Aa, c_Message_Omsg_OMPair(c_Message_Omsg_OCrypt(c_Public_
- c.in(c_Event_Oevent_ONotes(c_Message_Oagent_OSpy, c_Message_Omsg_OMPair(c_Message_Omsg_ONonce(v_NA), c_Messa
c.in(c_Event_Oevent_OSays(v_B, c_Message_Oagent_OServer, c_Message_Omsg_OMPair(c_Message_Omsg_OAgent(v_B), c_Mes
- c.in(c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evso)), tc_Message_O
v_U = c_Message_Omsg_OKey(v_K) ⇒ v_NA ≠ v_NAa    cnf(cls_conjecture_8, negated_conjecture)

```

**SWV353-2.p** Cryptographic protocol problem for Yahalom

```

c.in(v_evso, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture_2, negated_conjecture)
c.in(c_Event_Oevent_OSays(c_Message_Oagent_OServer, v_Aa, c_Message_Omsg_OMPair(c_Message_Omsg_OCrypt(c_Public_
c.in(c_Event_Oevent_OSays(v_B, c_Message_Oagent_OServer, c_Message_Omsg_OMPair(c_Message_Omsg_OAgent(v_B), c_Mes
- c.in(c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evso)), tc_Message_O
v_U = c_Message_Omsg_OKey(v_K) ⇒ v_NA ≠ v_NAa    cnf(cls_conjecture_8, negated_conjecture)
(c.in(v_evs, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent)) and c.in(c_Event_Oevent_OSays(c_Message_Oagent_OServ
c.in(c_Event_Oevent_OGets(c_Message_Oagent_OServer, c_Message_Omsg_OMPair(c_Message_Omsg_OAgent(v_B), c_Message
(c.in(v_evs, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent)) and c.in(c_Event_Oevent_OGets(v_S_H, c_Message_Omsg_
(c.in(v_nb, c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evs)), tc_Message_Omsg) or v_NA_H = v_NA)

```

**SWV354-1.p** Cryptographic protocol problem for Yahalom

```

include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-1.ax')
include('Axioms/SWV005-0.ax')
include('Axioms/SWV005-2.ax')
include('Axioms/SWV005-3.ax')
include('Axioms/SWV005-4.ax')
include('Axioms/SWV005-5.ax')
include('Axioms/SWV005-7.ax')
- c.in(v_A, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_0, negated_conjecture)
- c.in(v_B, c_Event_Obad, tc_Message_Oagent)    cnf(cls_conjecture_1, negated_conjecture)
c.in(v_evso, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent))    cnf(cls_conjecture_2, negated_conjecture)
c.in(c_Event_Oevent_OSays(c_Message_Oagent_OServer, v_Aa, c_Message_Omsg_OMPair(c_Message_Omsg_OCrypt(c_Public_
- c.in(c_Event_Oevent_ONotes(c_Message_Oagent_OSpy, c_Message_Omsg_OMPair(c_Message_Omsg_ONonce(v_NA), c_Messa
c.in(c_Event_Oevent_OSays(v_B, c_Message_Oagent_OServer, c_Message_Omsg_OMPair(c_Message_Omsg_OAgent(v_B), c_Mes
- c.in(c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_evso)), tc_Message_O
c.in(c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_insert(c_Message_Omsg_OKey(v_K), c_Event_Oknows(c_Message_
(v_U = c_Message_Omsg_OKey(v_K) and v_NA = v_NAa) ⇒ v_NB ≠ v_NBa    cnf(cls_conjecture_9, negated_conjecture)

```

**SWV355-1.p** Cryptographic protocol problem for Yahalom

```

include('Axioms/MSC001-0.ax')
include('Axioms/MSC001-1.ax')
include('Axioms/SWV005-0.ax')

```





$\neg c.in(c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_2)), tc\_Message\_Oagent)$   
 $c.in(c\_Event\_Oevent\_OSays(v\_B, c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_B), c\_Message\_Oagent))$   
 $c.in(v\_Ba, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_8, negated\_conjecture)$

**SWV357-2.p** Cryptographic protocol problem for Yahalom

$c.in(v\_evs_2, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OGets(v\_Ba, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_Aa), c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oagent))$   
 $\neg c.in(c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_2)), tc\_Message\_Oagent)$   
 $c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_Y, c\_Message\_Oanalz(v\_H), tc\_Message\_Oagent)$   
 $(c.in(v\_evs, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \text{ and } c.in(c\_Event\_Oevent\_OGets(v\_B, v\_X), c\_List\_Oset(v\_Ba, v\_X),$   
 $c.in(v\_X, c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) \quad cnf(cls\_Yahalom\_OGets, negated\_conjecture)$

**SWV358-1.p** Cryptographic protocol problem for Yahalom

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-1.ax')$   
 $include('Axioms/SWV005-0.ax')$   
 $include('Axioms/SWV005-2.ax')$   
 $include('Axioms/SWV005-3.ax')$   
 $include('Axioms/SWV005-4.ax')$   
 $include('Axioms/SWV005-5.ax')$   
 $include('Axioms/SWV005-7.ax')$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c.in(v\_B, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c.in(v\_evs_2, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $\neg c.in(c\_Message\_Omsg\_ONonce(v\_NB), c\_Event\_Oused(v\_evs_2), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OGets(v\_Ba, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_Aa), c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oagent))$   
 $\neg c.in(c\_Event\_Oevent\_ONotes(c\_Message\_Oagent\_OSpy, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_ONonce(v\_NA), c\_Message\_Oagent))$   
 $\neg c.in(c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_2)), tc\_Message\_Oagent)$   
 $c.in(c\_Event\_Oevent\_OSays(v\_B, c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_B), c\_Message\_Oagent))$   
 $c.in(v\_Ba, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_8, negated\_conjecture)$

**SWV358-2.p** Cryptographic protocol problem for Yahalom

$c.in(c\_Event\_Oevent\_OSays(v\_A, v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent) \Rightarrow c.in(v\_X, c\_Event\_Oknows(v\_A, v\_B, v\_X),$   
 $c.in(v\_c, c\_Message\_Oparts(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) \Rightarrow c.in(v\_c, c\_Event\_Oused(v\_evs, v\_c),$   
 $c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_Y, c\_Message\_Oparts(v\_H), tc\_Message\_Oagent)$   
 $c.in(c\_Message\_Omsg\_OCrypt(v\_K, v\_X), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Oagent)$   
 $c.in(v\_X, v\_H, tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oparts\_OInj_0, negated\_conjecture)$   
 $\neg c.in(c\_Message\_Omsg\_ONonce(v\_NB), c\_Event\_Oused(v\_evs_2), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OSays(v\_B, c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_B), c\_Message\_Oagent))$

**SWV359-1.p** Cryptographic protocol problem for Yahalom

$include('Axioms/MS001-0.ax')$   
 $include('Axioms/MS001-1.ax')$   
 $include('Axioms/SWV005-0.ax')$   
 $include('Axioms/SWV005-2.ax')$   
 $include('Axioms/SWV005-3.ax')$   
 $include('Axioms/SWV005-4.ax')$   
 $include('Axioms/SWV005-5.ax')$   
 $include('Axioms/SWV005-7.ax')$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c.in(v\_B, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c.in(v\_Aa, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_{11}, negated\_conjecture)$   
 $c.in(v\_evs_3, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $\neg c.in(c\_Message\_Omsg\_OKey(v\_KAB), c\_Event\_Oused(v\_evs_3), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c.in(v\_KAB, c\_Message\_OsymKeys, tc\_nat) \quad cnf(cls\_conjecture_4, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OGets(c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_Ba), c\_Message\_Oagent))$   
 $\neg c.in(c\_Event\_Oevent\_ONotes(c\_Message\_Oagent\_OSpy, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_ONonce(v\_NA), c\_Message\_Oagent))$   
 $c.in(c\_Event\_Oevent\_OSays(v\_B, c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_B), c\_Message\_Oagent))$   
 $\neg c.in(c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_3)), tc\_Message\_Oagent)$   
 $c.in(v\_Ba, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_9, negated\_conjecture)$

**SWV359-2.p** Cryptographic protocol problem for Yahalom

```

c.in(c_Event_Oevent_OSays(v_A, v_B, v_X), c_List_Oset(v_ews, tc_Event_Oevent), tc_Event_Oevent) ⇒ c.in(v_X, c_Event_Oknows(v_ews, tc_Event_Oevent))
c.in(c_Message_Omsg_OMPair(v_X, v_Y), c_Message_Oparts(v_H), tc_Message_Omsg) ⇒ c.in(v_Y, c_Message_Oparts(v_H), tc_Message_Omsg)
c.in(v_X, v_H, tc_Message_Omsg) ⇒ c.in(v_X, c_Message_Oparts(v_H), tc_Message_Omsg)   cnf(cls_Message_Oparts_OInj0, axiom)
c_Message_Oparts(c_Message_Oanalz(v_H)) = c_Message_Oparts(v_H)   cnf(cls_Message_Oparts__analz0, axiom)
(c.in(v_ews, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent)) and c.in(c_Event_Oevent_OGets(v_B, v_X), c_List_Oset(v_ews, tc_Event_Oevent))) ⇒ c.in(v_X, c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_ews)), tc_Message_Omsg)   cnf(cls_Yahalom_OGets, axiom)
(c.in(v_ews, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent)) and c.in(c_Message_Omsg_OCrypt(c_Public_OshrK(v_B), c_Message_Omsg), tc_Message_Omsg)) ⇒ c.in(v_ews, c_Message_Omsg, tc_Message_Omsg)   cnf(cls_Message_Omsg_OCrypt, axiom)
c.in(c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_ews)), tc_Message_Omsg) ⇒ c.in(v_ews, c_Message_Omsg, tc_Message_Omsg)   cnf(cls_Message_Omsg_ONonce, axiom)
c.in(v_ews3, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent))   cnf(cls_conjecture2, negated_conjecture)
c.in(c_Event_Oevent_OGets(c_Message_Oagent_Oserver, c_Message_Omsg_OMPair(c_Message_Omsg_Oagent(v_Ba), c_Message_Omsg_Oagent(v_B)), tc_Message_Omsg)) ⇒ c.in(v_B, c_Message_Oagent(v_B), tc_Message_Oagent(v_B))   cnf(cls_Message_Oagent_Oserver, axiom)
c.in(c_Event_Oevent_OSays(v_B, c_Message_Oagent_Oserver, c_Message_Omsg_OMPair(c_Message_Omsg_Oagent(v_B), c_Message_Omsg_Oagent(v_B)), tc_Message_Omsg)) ⇒ c.in(v_B, c_Message_Oagent(v_B), tc_Message_Oagent(v_B))   cnf(cls_Message_Oagent_OSays, axiom)
¬ c.in(c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_ews3)), tc_Message_Omsg)   cnf(cls_conjecture9, negated_conjecture)

```

**SWV360-1.p** Cryptographic protocol problem for Yahalom

```

include('Axioms/MS001-0.ax')
include('Axioms/MS001-1.ax')
include('Axioms/SWV005-0.ax')
include('Axioms/SWV005-2.ax')
include('Axioms/SWV005-3.ax')
include('Axioms/SWV005-4.ax')
include('Axioms/SWV005-5.ax')
include('Axioms/SWV005-7.ax')
¬ c.in(v_A, c_Event_Obad, tc_Message_Oagent)   cnf(cls_conjecture0, negated_conjecture)
¬ c.in(v_B, c_Event_Obad, tc_Message_Oagent)   cnf(cls_conjecture1, negated_conjecture)
c.in(v_Aa, c_Event_Obad, tc_Message_Oagent)   cnf(cls_conjecture11, negated_conjecture)
c.in(v_ews3, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent))   cnf(cls_conjecture2, negated_conjecture)
¬ c.in(c_Message_Omsg_OKey(v_KAB), c_Event_Oused(v_ews3), tc_Message_Omsg)   cnf(cls_conjecture3, negated_conjecture)
c.in(v_KAB, c_Message_OsymKeys, tc_nat)   cnf(cls_conjecture4, negated_conjecture)
c.in(c_Event_Oevent_OGets(c_Message_Oagent_Oserver, c_Message_Omsg_OMPair(c_Message_Omsg_Oagent(v_Ba), c_Message_Omsg_Oagent(v_B)), tc_Message_Omsg)) ⇒ c.in(v_B, c_Message_Oagent(v_B), tc_Message_Oagent(v_B))   cnf(cls_Message_Oagent_Oserver, axiom)
¬ c.in(c_Event_Oevent_ONotes(c_Message_Oagent_OSpy, c_Message_Omsg_OMPair(c_Message_Omsg_ONonce(v_NA), c_Message_Omsg_Oagent(v_B)), tc_Message_Omsg)) ⇒ c.in(v_NA, c_Message_Oagent(v_B), tc_Message_Oagent(v_B))   cnf(cls_Message_Oagent_OSpy, axiom)
c.in(c_Event_Oevent_OSays(v_B, c_Message_Oagent_Oserver, c_Message_Omsg_OMPair(c_Message_Omsg_Oagent(v_B), c_Message_Omsg_Oagent(v_B)), tc_Message_Omsg)) ⇒ c.in(v_B, c_Message_Oagent(v_B), tc_Message_Oagent(v_B))   cnf(cls_Message_Oagent_OSays, axiom)
¬ c.in(c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_ews3)), tc_Message_Omsg)   cnf(cls_conjecture9, negated_conjecture)
c.in(v_Ba, c_Event_Obad, tc_Message_Oagent)   cnf(cls_conjecture9, negated_conjecture)

```

**SWV360-2.p** Cryptographic protocol problem for Yahalom

```

(c.in(v_ews, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent)) and c.in(c_Event_Oevent_OGets(v_S_H, c_Message_Omsg_Oagent(v_B), tc_Message_Oagent(v_B)), tc_Message_Oagent(v_B))) ⇒ c.in(v_S_H, c_Message_Omsg_Oagent(v_B), tc_Message_Oagent(v_B))   cnf(cls_Yahalom_OGets, axiom)
(c.in(v_nb, c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_ews)), tc_Message_Omsg) or v_B_H = v_B)   cnf(cls_Message_Oanalz, axiom)
¬ c.in(v_B, c_Event_Obad, tc_Message_Oagent)   cnf(cls_conjecture1, negated_conjecture)
c.in(v_ews3, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent))   cnf(cls_conjecture2, negated_conjecture)
c.in(c_Event_Oevent_OGets(c_Message_Oagent_Oserver, c_Message_Omsg_OMPair(c_Message_Omsg_Oagent(v_Ba), c_Message_Omsg_Oagent(v_B)), tc_Message_Omsg)) ⇒ c.in(v_B, c_Message_Oagent(v_B), tc_Message_Oagent(v_B))   cnf(cls_Message_Oagent_Oserver, axiom)
c.in(c_Event_Oevent_OSays(v_B, c_Message_Oagent_Oserver, c_Message_Omsg_OMPair(c_Message_Omsg_Oagent(v_B), c_Message_Omsg_Oagent(v_B)), tc_Message_Omsg)) ⇒ c.in(v_B, c_Message_Oagent(v_B), tc_Message_Oagent(v_B))   cnf(cls_Message_Oagent_OSays, axiom)
¬ c.in(c_Message_Omsg_ONonce(v_NB), c_Message_Oanalz(c_Event_Oknows(c_Message_Oagent_OSpy, v_ews3)), tc_Message_Omsg)   cnf(cls_conjecture9, negated_conjecture)
c.in(v_Ba, c_Event_Obad, tc_Message_Oagent)   cnf(cls_conjecture9, negated_conjecture)

```

**SWV361-1.p** Cryptographic protocol problem for Yahalom

```

include('Axioms/MS001-0.ax')
include('Axioms/MS001-1.ax')
include('Axioms/SWV005-0.ax')
include('Axioms/SWV005-2.ax')
include('Axioms/SWV005-3.ax')
include('Axioms/SWV005-4.ax')
include('Axioms/SWV005-5.ax')
include('Axioms/SWV005-7.ax')
¬ c.in(v_A, c_Event_Obad, tc_Message_Oagent)   cnf(cls_conjecture0, negated_conjecture)
¬ c.in(v_B, c_Event_Obad, tc_Message_Oagent)   cnf(cls_conjecture1, negated_conjecture)
¬ c.in(v_Ba, c_Event_Obad, tc_Message_Oagent)   cnf(cls_conjecture11, negated_conjecture)
c.in(v_ews3, c_Yahalom_Oyahalom, tc_List_Olist(tc_Event_Oevent))   cnf(cls_conjecture2, negated_conjecture)
¬ c.in(c_Message_Omsg_OKey(v_KAB), c_Event_Oused(v_ews3), tc_Message_Omsg)   cnf(cls_conjecture3, negated_conjecture)
c.in(v_KAB, c_Message_OsymKeys, tc_nat)   cnf(cls_conjecture4, negated_conjecture)
c.in(c_Event_Oevent_OGets(c_Message_Oagent_Oserver, c_Message_Omsg_OMPair(c_Message_Omsg_Oagent(v_Ba), c_Message_Omsg_Oagent(v_B)), tc_Message_Omsg)) ⇒ c.in(v_B, c_Message_Oagent(v_B), tc_Message_Oagent(v_B))   cnf(cls_Message_Oagent_Oserver, axiom)
¬ c.in(c_Event_Oevent_ONotes(c_Message_Oagent_OSpy, c_Message_Omsg_OMPair(c_Message_Omsg_ONonce(v_NA), c_Message_Omsg_Oagent(v_B)), tc_Message_Omsg)) ⇒ c.in(v_NA, c_Message_Oagent(v_B), tc_Message_Oagent(v_B))   cnf(cls_Message_Oagent_OSpy, axiom)

```

$c.in(c\_Event\_Oevent\_OSays(v\_B, c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_B), c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_3))), tc\_Message\_Oagent(v\_Aa, c\_Event\_Obad, tc\_Message\_Oagent)) \quad cnf(cls\_conjecture_9, negated\_conjecture)$

**SWV361-2.p** Cryptographic protocol problem for Yahalom

$c.in(c\_Event\_Oevent\_OSays(v\_A, v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent) \Rightarrow c.in(v\_X, c\_Event\_Oknows(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_Y, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_X, v\_H, tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oparts\_OInj_0, c\_Message\_Oparts(c\_Message\_Oanalz(v\_H)) = c\_Message\_Oparts(v\_H) \quad cnf(cls\_Message\_Oparts\_Oanalz_0, axiom)$   
 $(c.in(v\_evs, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \text{ and } c.in(c\_Event\_Oevent\_OGets(v\_B, v\_X), c\_List\_Oset(v\_evs, c.in(v\_X, c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs))), tc\_Message\_Omsg) \quad cnf(cls\_Yahalom\_OGets(v\_B, v\_X, c.in(v\_evs, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \text{ and } c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_B), c.in(v\_evs, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OGets(c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_Ba), c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs))), tc\_Message\_Oagent(v\_Ba, c\_Event\_Obad, tc\_Message\_Oagent)) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OSays(v\_B, c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_B), c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_3))), tc\_Message\_Oagent(v\_Aa, c\_Event\_Obad, tc\_Message\_Oagent)) \quad cnf(cls\_conjecture_9, negated\_conjecture)$

**SWV362-1.p** Cryptographic protocol problem for Yahalom

$include('Axioms/MSC001-0.ax')$   
 $include('Axioms/MSC001-1.ax')$   
 $include('Axioms/SWV005-0.ax')$   
 $include('Axioms/SWV005-2.ax')$   
 $include('Axioms/SWV005-3.ax')$   
 $include('Axioms/SWV005-4.ax')$   
 $include('Axioms/SWV005-5.ax')$   
 $include('Axioms/SWV005-7.ax')$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c.in(v\_B, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c.in(v\_Ba, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_{11}, negated\_conjecture)$   
 $c.in(v\_evs_3, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $\neg c.in(c\_Message\_Omsg\_OKey(v\_KAB), c\_Event\_Oused(v\_evs_3), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c.in(v\_KAB, c\_Message\_OsymKeys, tc\_nat) \quad cnf(cls\_conjecture_4, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OGets(c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_Ba), c\_Message\_Omsg\_ONonce(v\_NA), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs))), tc\_Message\_Oagent(v\_Ba, c\_Event\_Obad, tc\_Message\_Oagent)) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $\neg c.in(c\_Event\_Oevent\_ONotes(c\_Message\_Oagent\_OSpy, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_ONonce(v\_NA), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs))), tc\_Message\_Oagent(v\_Ba, c\_Event\_Obad, tc\_Message\_Oagent)) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OSays(v\_B, c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_B), c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_3))), tc\_Message\_Oagent(v\_Ba, c\_Event\_Obad, tc\_Message\_Oagent)) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $\neg c.in(c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_3))), tc\_Message\_Oagent(v\_Ba, c\_Event\_Obad, tc\_Message\_Oagent)) \quad cnf(cls\_conjecture_9, negated\_conjecture)$   
 $c.in(v\_Aa, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_9, negated\_conjecture)$

**SWV362-2.p** Cryptographic protocol problem for Yahalom

$(c.in(v\_evs, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \text{ and } c.in(c\_Event\_Oevent\_OGets(v\_S\_H, c\_Message\_Omsg\_OAgent(v\_S\_H, c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs))), tc\_Message\_Omsg) \text{ or } v\_A.H = v\_A) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c.in(v\_evs_3, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OGets(c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_Ba), c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs))), tc\_Message\_Oagent(v\_Ba, c\_Event\_Obad, tc\_Message\_Oagent)) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OSays(v\_B, c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_B), c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_3))), tc\_Message\_Oagent(v\_Ba, c\_Event\_Obad, tc\_Message\_Oagent)) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $\neg c.in(c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_3))), tc\_Message\_Oagent(v\_Ba, c\_Event\_Obad, tc\_Message\_Oagent)) \quad cnf(cls\_conjecture_9, negated\_conjecture)$   
 $c.in(v\_Aa, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_9, negated\_conjecture)$

**SWV363-1.p** Cryptographic protocol problem for Yahalom

$include('Axioms/MSC001-0.ax')$   
 $include('Axioms/MSC001-1.ax')$   
 $include('Axioms/SWV005-0.ax')$   
 $include('Axioms/SWV005-2.ax')$   
 $include('Axioms/SWV005-3.ax')$   
 $include('Axioms/SWV005-4.ax')$   
 $include('Axioms/SWV005-5.ax')$   
 $include('Axioms/SWV005-7.ax')$   
 $\neg c.in(v\_A, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_0, negated\_conjecture)$   
 $\neg c.in(v\_B, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c.in(v\_Aa, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_{11}, negated\_conjecture)$

$c.in(v\_evs_3, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $\neg c.in(c\_Message\_Omsg\_OKey(v\_KAB), c\_Event\_Oused(v\_evs_3), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c.in(v\_KAB, c\_Message\_OsymKeys, tc\_nat) \quad cnf(cls\_conjecture_4, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OGets(c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_Ba), c\_Message\_Omsg\_ONonce(v\_NA), c\_Message\_Omsg\_Oanalz(v\_H))), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_5, negated\_conjecture)$   
 $\neg c.in(c\_Event\_Oevent\_ONotes(c\_Message\_Oagent\_OSpy, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_ONonce(v\_NA), c\_Message\_Omsg\_Oanalz(v\_H))), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_6, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OSays(v\_B, c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_B), c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Omsg\_Oanalz(v\_H))), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_7, negated\_conjecture)$   
 $\neg c.in(c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_3)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_8, negated\_conjecture)$   
 $c.in(v\_Aa, c\_Event\_Obad, tc\_Message\_Oagent) \quad cnf(cls\_conjecture_9, negated\_conjecture)$

**SWV363-2.p** Cryptographic protocol problem for Yahalom

$c.in(c\_Event\_Oevent\_OSays(v\_A, v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent) \Rightarrow c.in(v\_X, c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_Y, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oparts\_OInj_0, negated\_conjecture)$   
 $c.in(v\_X, v\_H, tc\_Message\_Omsg) \Rightarrow c.in(v\_X, c\_Message\_Oparts(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oparts\_Oanalz_0, axiom)$   
 $(c.in(v\_evs, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \text{ and } c.in(c\_Event\_Oevent\_OGets(v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent)) \Rightarrow c.in(v\_X, c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) \quad cnf(cls\_Yahalom\_OGets, negated\_conjecture)$   
 $(c.in(v\_evs, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \text{ and } c.in(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_B), v\_X), c\_Message\_Omsg)) \Rightarrow c.in(v\_X, c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) \quad cnf(cls\_Yahalom\_OCrypt, negated\_conjecture)$   
 $c.in(v\_evs_3, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OGets(c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_Ba), c\_Message\_Omsg\_ONonce(v\_NA), c\_Message\_Omsg\_Oanalz(v\_H))), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_3, negated\_conjecture)$   
 $c.in(c\_Event\_Oevent\_OSays(v\_B, c\_Message\_Oagent\_OServer, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OAgent(v\_B), c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Omsg\_Oanalz(v\_H))), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_4, negated\_conjecture)$   
 $\neg c.in(c\_Message\_Omsg\_ONonce(v\_NB), c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs_3)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_5, negated\_conjecture)$

**SWV364-2.p** Cryptographic protocol problem for Yahalom

$c.in(c\_Event\_Oevent\_OGets(v\_A, c\_Message\_Omsg\_OMPair(c\_Message\_Omsg\_OCrypt(c\_Public\_OshrK(v\_A), v\_Y), v\_X)), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent) \Rightarrow c.in(v\_X, c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_1, negated\_conjecture)$   
 $\neg c.in(v\_X, c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) \quad cnf(cls\_conjecture_2, negated\_conjecture)$   
 $c.in(c\_Message\_Omsg\_OMPair(v\_X, v\_Y), c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \Rightarrow c.in(v\_Y, c\_Message\_Oanalz(v\_H), tc\_Message\_Omsg) \quad cnf(cls\_Message\_Oparts\_OInj_0, axiom)$   
 $(c.in(v\_evs, c\_Yahalom\_Oyahalom, tc\_List\_Olist(tc\_Event\_Oevent)) \text{ and } c.in(c\_Event\_Oevent\_OGets(v\_B, v\_X), c\_List\_Oset(v\_evs, tc\_Event\_Oevent), tc\_Event\_Oevent)) \Rightarrow c.in(v\_X, c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) \quad cnf(cls\_Yahalom\_OGets, negated\_conjecture)$   
 $c.in(v\_X, c\_Message\_Oanalz(c\_Event\_Oknows(c\_Message\_Oagent\_OSpy, v\_evs)), tc\_Message\_Omsg) \quad cnf(cls\_Yahalom\_OCrypt, negated\_conjecture)$

**SWV365+1.p** Priority queue checker: lemma.Ls base

$include('Axioms/SWV007+0.ax')$   
 $include('Axioms/SWV007+1.ax')$   
 $include('Axioms/SWV007+2.ax')$   
 $include('Axioms/SWV007+3.ax')$   
 $include('Axioms/SWV007+4.ax')$   
 $\forall u, v, x, y: i(triple(u, create\_slb, x)) = i(triple(v, create\_slb, y)) \quad fof(l1\_co, conjecture)$

**SWV366+1.p** Priority queue checker: lemma.Ls induction

$include('Axioms/SWV007+0.ax')$   
 $include('Axioms/SWV007+1.ax')$   
 $include('Axioms/SWV007+2.ax')$   
 $include('Axioms/SWV007+3.ax')$   
 $include('Axioms/SWV007+4.ax')$   
 $\forall u: (\forall v, w, x, y: i(triple(v, u, x)) = i(triple(w, u, y)) \Rightarrow \forall z, x_1, x_2, x_3, x_4, x_5: i(triple(z, insert\_slb(u, pair(x_4, x_5)), x_2)) = i(triple(x_1, insert\_slb(u, pair(x_4, x_5)), x_3))) \quad fof(l2\_co, conjecture)$

**SWV367+1.p** Priority queue checker: lemma.contains\_s.I.remove base

$include('Axioms/SWV007+0.ax')$   
 $include('Axioms/SWV007+1.ax')$   
 $include('Axioms/SWV007+2.ax')$   
 $include('Axioms/SWV007+3.ax')$   
 $include('Axioms/SWV007+4.ax')$   
 $\forall u, v, w: (contains\_pq(i(triple(u, create\_slb, v)), w)) \Rightarrow i(remove\_cpq(triple(u, create\_slb, v), w)) = remove\_pq(i(triple(u, create\_slb, v), w)) \quad fof(l3\_co, conjecture)$

**SWV368+1.p** Priority queue checker: lemma.contains\_s.I.remove induction

$include('Axioms/SWV007+0.ax')$   
 $include('Axioms/SWV007+1.ax')$   
 $include('Axioms/SWV007+2.ax')$   
 $include('Axioms/SWV007+3.ax')$   
 $include('Axioms/SWV007+4.ax')$   
 $\forall u, v, w, x: (contains\_cpq(triple(u, v, w), x) \iff contains\_pq(i(triple(u, v, w)), x)) \quad fof(l3\_li56, lemma)$

$\forall u: (\forall v, w, x: (\text{contains\_pq}(i(\text{triple}(v, u, w)), x) \Rightarrow i(\text{remove\_cpq}(\text{triple}(v, u, w), x)) = \text{remove\_pq}(i(\text{triple}(v, u, w)), x)) \Rightarrow$   
 $\forall y, z, x_1, x_2, x_3: (\text{contains\_pq}(i(\text{triple}(y, \text{insert\_slb}(u, \text{pair}(x_2, x_3)), z)), x_1) \Rightarrow i(\text{remove\_cpq}(\text{triple}(y, \text{insert\_slb}(u, \text{pair}(x_2, x_3))), z))$   
 $\text{remove\_pq}(i(\text{triple}(y, \text{insert\_slb}(u, \text{pair}(x_2, x_3))), z)), x_1))) \quad \text{fof}(l4\_co, \text{conjecture})$

**SWV369+1.p** Priority queue checker: lemma\_contains\_s\_I base

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+1.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

include('Axioms/SWV007+4.ax')

$\forall u, v, w: (\text{contains\_cpq}(\text{triple}(u, \text{create\_slb}(v), w) \iff \text{contains\_pq}(i(\text{triple}(u, \text{create\_slb}(v)), w)) \quad \text{fof}(l5\_co, \text{conjecture})$

**SWV370+1.p** Priority queue checker: lemma\_contains\_s\_I induction

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+1.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

include('Axioms/SWV007+4.ax')

$\forall u: (\forall v, w, x: (\text{contains\_cpq}(\text{triple}(v, u, w), x) \iff \text{contains\_pq}(i(\text{triple}(v, u, w)), x)) \Rightarrow \forall y, z, x_1, x_2, x_3: (\text{contains\_cpq}(\text{triple}(y, \text{insert\_slb}(u, \text{pair}(x_1, x_2)), z)), x_3))$   
 $\text{contains\_pq}(i(\text{triple}(y, \text{insert\_slb}(u, \text{pair}(x_1, x_2)), z)), x_3))) \quad \text{fof}(l6\_co, \text{conjecture})$

**SWV371+1.p** Priority queue checker: lemma\_pi\_min\_elem

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+1.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

include('Axioms/SWV007+4.ax')

$\forall u, v, w: (\text{phi}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))) \Rightarrow \text{contains\_pq}(i(\text{triple}(u, v, w)), \text{findmin\_cpq\_res}(\text{triple}(u, v, w)))) \quad \text{fof}(l7\_l8, \text{lemma})$

$\forall u, v, w: (\text{phi}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))) \Rightarrow \text{issmallestelement\_pq}(i(\text{triple}(u, v, w)), \text{findmin\_cpq\_res}(\text{triple}(u, v, w)))) \quad \text{fof}(l7\_l8, \text{lemma})$

$\forall u, v, w: (\text{phi}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))) \Rightarrow \text{pi\_sharp\_find\_min}(i(\text{triple}(u, v, w)), \text{findmin\_cpq\_res}(\text{triple}(u, v, w)))) \quad \text{fof}(l7\_l8, \text{lemma})$

**SWV372+1.p** Priority queue checker: lemma\_contains\_cpq\_min\_elem

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+1.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

include('Axioms/SWV007+4.ax')

$\forall u, v, w, x: (\text{contains\_cpq}(\text{triple}(u, v, w), x) \iff \text{contains\_pq}(i(\text{triple}(u, v, w)), x)) \quad \text{fof}(l8\_li56, \text{lemma})$

$\forall u, v, w: (\neg \text{contains\_cpq}(\text{triple}(u, v, w), \text{findmin\_cpq\_res}(\text{triple}(u, v, w))) \Rightarrow \neg \text{ok}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w)))) \quad \text{fof}(l8\_li56, \text{lemma})$

$\forall u, v, w: (\neg \text{ok}(\text{triple}(u, v, w)) \Rightarrow \neg \text{phi}(\text{triple}(u, v, w))) \quad \text{fof}(l8\_lX, \text{lemma})$

$\forall u, v, w: (\text{phi}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))) \Rightarrow \text{contains\_pq}(i(\text{triple}(u, v, w)), \text{findmin\_cpq\_res}(\text{triple}(u, v, w)))) \quad \text{fof}(l8\_li56, \text{lemma})$

**SWV372+2.p** Priority queue checker: lemma\_contains\_cpq\_min\_elem

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+1.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

include('Axioms/SWV007+4.ax')

$\forall u, v, w, x: (\text{contains\_cpq}(\text{triple}(u, v, w), x) \iff \text{contains\_pq}(i(\text{triple}(u, v, w)), x)) \quad \text{fof}(l8\_li56, \text{lemma})$

$\forall u, v, w: (\text{ok}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))) \Rightarrow (v \neq \text{create\_slb} \text{ and } \text{contains\_slb}(v, \text{findmin\_cpq\_res}(u)) \text{ and } \text{lookup\_slb}(v, \text{findmin\_cpq\_res}(u)))) \quad \text{fof}(l9\_l10, \text{lemma})$

$\forall u, v, w: (\neg \text{ok}(\text{triple}(u, v, w)) \Rightarrow \forall x, y, z: (\text{succ\_cpq}(\text{triple}(u, v, w), \text{triple}(x, y, z)) \Rightarrow \neg \text{ok}(\text{triple}(x, y, z)))) \quad \text{fof}(l11\_l12, \text{lemma})$

$\forall u, v, w: (\text{phi}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))) \Rightarrow \text{contains\_pq}(i(\text{triple}(u, v, w)), \text{findmin\_cpq\_res}(\text{triple}(u, v, w)))) \quad \text{fof}(l8\_li56, \text{lemma})$

**SWV373+1.p** Priority queue checker: lemma\_not\_contains\_min\_not\_ok

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w: (\text{ok}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))) \Rightarrow (v \neq \text{create\_slb} \text{ and } \text{contains\_slb}(v, \text{findmin\_cpq\_res}(u)) \text{ and } \text{lookup\_slb}(v, \text{findmin\_cpq\_res}(u)))) \quad \text{fof}(l9\_l10, \text{lemma})$

$\forall u, v, w: (\neg \text{contains\_cpq}(\text{triple}(u, v, w), \text{findmin\_cpq\_res}(\text{triple}(u, v, w))) \Rightarrow \neg \text{ok}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w)))) \quad \text{fof}(l9\_l10, \text{lemma})$

**SWV374+1.p** Priority queue checker: lemma\_ok\_find\_min

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w: (\text{ok}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))) \Rightarrow (v \neq \text{create\_slb} \text{ and } \text{contains\_slb}(v, \text{findmin\_pqp\_res}(u)) \text{ and } \text{lookup\_slb}(v, \text{findmin\_pqp\_res}(u))))$  fof(l10\_co, conjecture)

**SWV375+1.p** Priority queue checker: lemma\_not\_ok\_not\_phi

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+1.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

include('Axioms/SWV007+4.ax')

$\forall u, v, w: (\neg \text{ok}(\text{triple}(u, v, w)) \Rightarrow \forall x, y, z: (\text{succ\_cpq}(\text{triple}(u, v, w), \text{triple}(x, y, z)) \Rightarrow \neg \text{ok}(\text{triple}(x, y, z))))$  fof(l11\_l12, lemma)

$\forall u, v, w: (\neg \text{ok}(\text{triple}(u, v, w)) \Rightarrow \neg \text{phi}(\text{triple}(u, v, w)))$  fof(l11\_co, conjecture)

**SWV376+1.p** Priority queue checker: lemma\_not\_ok\_persistence

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w, x, y, z: (\text{succ\_cpq}(\text{triple}(u, v, w), \text{triple}(x, y, z)) \Rightarrow (\neg \text{ok}(\text{triple}(x, y, z)) \Rightarrow \neg \text{ok}(\text{im\_succ\_cpq}(\text{triple}(x, y, z)))) \Rightarrow$

$\forall x_1, x_2, x_3: (\neg \text{ok}(\text{triple}(x_1, x_2, x_3)) \Rightarrow \forall x_4, x_5, x_6: (\text{succ\_cpq}(\text{triple}(x_1, x_2, x_3), \text{triple}(x_4, x_5, x_6)) \Rightarrow \neg \text{ok}(\text{triple}(x_4, x_5, x_6))))$

$\forall u, v, w: (\neg \text{ok}(\text{triple}(u, v, w)) \Rightarrow \neg \text{ok}(\text{im\_succ\_cpq}(\text{triple}(u, v, w))))$  fof(l12\_l13, lemma)

$\forall u, v, w: (\neg \text{ok}(\text{triple}(u, v, w)) \Rightarrow \forall x, y, z: (\text{succ\_cpq}(\text{triple}(u, v, w), \text{triple}(x, y, z)) \Rightarrow \neg \text{ok}(\text{triple}(x, y, z))))$  fof(l12\_co, conjecture)

**SWV377+1.p** Priority queue checker: lemma\_not\_ok\_persistence\_induction step 1

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w, x: (\neg \text{ok}(\text{triple}(u, v, w)) \Rightarrow \neg \text{ok}(\text{insert\_cpq}(\text{triple}(u, v, w), x)))$  fof(l13\_co, conjecture)

**SWV378+1.p** Priority queue checker: lemma\_not\_ok\_persistence\_induction step 2

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w, x: (\neg \text{ok}(\text{triple}(u, v, w)) \Rightarrow \neg \text{ok}(\text{remove\_cpq}(\text{triple}(u, v, w), x)))$  fof(l14\_co, conjecture)

**SWV379+1.p** Priority queue checker: lemma\_not\_ok\_persistence\_induction step 3

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w: (\neg \text{ok}(\text{triple}(u, v, w)) \Rightarrow \neg \text{ok}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))))$  fof(l15\_co, conjecture)

**SWV380+1.p** Priority queue checker: lemma\_not\_ok\_persistence\_induction step 4

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w, x: (\neg \text{ok}(\text{triple}(u, v, w)) \Rightarrow \neg \text{ok}(\text{remove\_cpq}(\text{triple}(u, v, w), x)))$  fof(l16\_l14, lemma)

$\forall u, v, w: (\neg \text{ok}(\text{triple}(u, v, w)) \Rightarrow \neg \text{ok}(\text{removemin\_cpq\_eff}(\text{triple}(u, v, w))))$  fof(l16\_co, conjecture)

**SWV381+1.p** Priority queue checker: lemma\_min\_elem\_smallest

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+1.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

include('Axioms/SWV007+4.ax')

$\forall u, v, w, x: (\text{contains\_cpq}(\text{triple}(u, v, w), x) \iff \text{contains\_pq}(i(\text{triple}(u, v, w)), x))$  fof(l17\_li56, lemma)

$\forall u, v, w: (\exists x: (\text{contains\_cpq}(\text{triple}(u, v, w), x) \text{ and } \text{strictly\_less\_than}(x, \text{findmin\_cpq\_res}(\text{triple}(u, v, w)))) \Rightarrow \neg \text{phi}(\text{findmin\_cpq\_res}(\text{triple}(u, v, w))))$

$\forall u, v, w: (\text{phi}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))) \Rightarrow \text{issmallestelement\_pq}(i(\text{triple}(u, v, w)), \text{findmin\_cpq\_res}(\text{triple}(u, v, w))))$

**SWV381+2.p** Priority queue checker: lemma\_min\_elem\_smallest

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+1.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

include('Axioms/SWV007+4.ax')

$\forall u, v, w, x: (\text{contains\_cpq}(\text{triple}(u, v, w), x) \iff \text{contains\_pq}(i(\text{triple}(u, v, w)), x)) \quad \text{fof}(\text{117\_li56}, \text{lemma})$

$\forall u, v, w: ((\neg \text{check\_cpq}(\text{triple}(u, v, w)) \text{ or } \neg \text{ok}(\text{triple}(u, v, w))) \Rightarrow \forall x, y, z: (\text{succ\_cpq}(\text{triple}(u, v, w), \text{triple}(x, y, z)) \Rightarrow (\neg \text{ok}(\text{triple}(x, y, z)) \text{ or } \neg \text{check\_cpq}(\text{triple}(x, y, z)))))) \quad \text{fof}(\text{119\_l20}, \text{lemma})$

$\forall u, v: (\text{contains\_slb}(u, v) \Rightarrow \exists w: \text{pair\_in\_list}(u, v, w)) \quad \text{fof}(\text{145\_li4647}, \text{lemma})$

$\forall u, v, w, x: ((\text{pair\_in\_list}(u, v, w) \text{ and } \text{strictly\_less\_than}(v, x) \text{ and } \text{strictly\_less\_than}(w, x)) \Rightarrow \text{pair\_in\_list}(\text{update\_slb}(u, x), v, x))$

$\forall u, v, w, x: ((\text{pair\_in\_list}(u, v, w) \text{ and } \text{strictly\_less\_than}(v, x) \text{ and } x < w) \Rightarrow \exists y: (\text{pair\_in\_list}(\text{update\_slb}(u, x), v, y) \text{ and } x < y)) \quad \text{fof}(\text{145\_l49}, \text{lemma})$

$\forall u, v, w: (\text{check\_cpq}(\text{triple}(u, v, w)) \iff \forall x, y: (\text{pair\_in\_list}(v, x, y) \Rightarrow y < x)) \quad \text{fof}(\text{143\_li4142}, \text{lemma})$

$\forall u, v, w: (\text{phi}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))) \Rightarrow \text{issmallestelement\_pq}(i(\text{triple}(u, v, w)), \text{findmin\_cpq\_res}(\text{triple}(u, v, w))))$

**SWV381+3.p** Priority queue checker: lemma\_min\_elem\_smallest

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+1.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

include('Axioms/SWV007+4.ax')

$\forall u, v, w, x: (\text{contains\_cpq}(\text{triple}(u, v, w), x) \iff \text{contains\_pq}(i(\text{triple}(u, v, w)), x)) \quad \text{fof}(\text{117\_li56}, \text{lemma})$

$\forall u, v, w: ((\neg \text{check\_cpq}(\text{triple}(u, v, w)) \text{ or } \neg \text{ok}(\text{triple}(u, v, w))) \Rightarrow \forall x, y, z: (\text{succ\_cpq}(\text{triple}(u, v, w), \text{triple}(x, y, z)) \Rightarrow (\neg \text{ok}(\text{triple}(x, y, z)) \text{ or } \neg \text{check\_cpq}(\text{triple}(x, y, z)))))) \quad \text{fof}(\text{119\_l20}, \text{lemma})$

$\forall u, v, w: ((\text{contains\_slb}(u, v) \text{ and } \text{strictly\_less\_than}(v, w)) \Rightarrow (\text{pair\_in\_list}(\text{update\_slb}(u, w), v, w) \text{ or } \exists x: (\text{pair\_in\_list}(\text{update\_slb}(u, w), v, x)))) \quad \text{fof}(\text{144\_l45}, \text{lemma})$

$\forall u, v, w: (\text{check\_cpq}(\text{triple}(u, v, w)) \iff \forall x, y: (\text{pair\_in\_list}(v, x, y) \Rightarrow y < x)) \quad \text{fof}(\text{143\_li4142}, \text{lemma})$

$\forall u, v, w: (\text{phi}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))) \Rightarrow \text{issmallestelement\_pq}(i(\text{triple}(u, v, w)), \text{findmin\_cpq\_res}(\text{triple}(u, v, w))))$

**SWV381+4.p** Priority queue checker: lemma\_min\_elem\_smallest

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+1.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

include('Axioms/SWV007+4.ax')

$\forall u, v, w, x: (\text{contains\_cpq}(\text{triple}(u, v, w), x) \iff \text{contains\_pq}(i(\text{triple}(u, v, w)), x)) \quad \text{fof}(\text{117\_li56}, \text{lemma})$

$\forall u, v, w: (\neg \text{check\_cpq}(\text{triple}(u, v, w)) \Rightarrow \forall x, y, z: (\text{succ\_cpq}(\text{triple}(u, v, w), \text{triple}(x, y, z)) \Rightarrow (\neg \text{ok}(\text{triple}(x, y, z)) \text{ or } \neg \text{check\_cpq}(\text{triple}(x, y, z))))$

$\forall u, v, w: (\exists x: (\text{contains\_cpq}(\text{triple}(u, v, w), x) \text{ and } \text{strictly\_less\_than}(x, \text{findmin\_cpq\_res}(\text{triple}(u, v, w)))) \Rightarrow \neg \text{check\_cpq}(\text{findmin\_cpq\_res}(\text{triple}(u, v, w))))$

$\forall u, v, w: (\text{phi}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))) \Rightarrow \text{issmallestelement\_pq}(i(\text{triple}(u, v, w)), \text{findmin\_cpq\_res}(\text{triple}(u, v, w))))$

**SWV382+1.p** Priority queue checker: lemma\_not\_min\_elem\_not\_phi

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+1.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

include('Axioms/SWV007+4.ax')

$\forall u, v, w: (\neg \text{check\_cpq}(\text{triple}(u, v, w)) \Rightarrow \forall x, y, z: (\text{succ\_cpq}(\text{triple}(u, v, w), \text{triple}(x, y, z)) \Rightarrow (\neg \text{ok}(\text{triple}(x, y, z)) \text{ or } \neg \text{check\_cpq}(\text{triple}(x, y, z))))$

$\forall u, v, w: (\exists x: (\text{contains\_cpq}(\text{triple}(u, v, w), x) \text{ and } \text{strictly\_less\_than}(x, \text{findmin\_cpq\_res}(\text{triple}(u, v, w)))) \Rightarrow \neg \text{check\_cpq}(\text{findmin\_cpq\_res}(\text{triple}(u, v, w))))$

$\forall u, v, w: (\exists x: (\text{contains\_cpq}(\text{triple}(u, v, w), x) \text{ and } \text{strictly\_less\_than}(x, \text{findmin\_cpq\_res}(\text{triple}(u, v, w)))) \Rightarrow \neg \text{phi}(\text{findmin\_cpq\_res}(\text{triple}(u, v, w))))$

**SWV383+1.p** Priority queue checker: lemma\_not\_check\_not\_phi

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w: ((\neg \text{check\_cpq}(\text{triple}(u, v, w)) \text{ or } \neg \text{ok}(\text{triple}(u, v, w))) \Rightarrow \forall x, y, z: (\text{succ\_cpq}(\text{triple}(u, v, w), \text{triple}(x, y, z)) \Rightarrow (\neg \text{ok}(\text{triple}(x, y, z)) \text{ or } \neg \text{check\_cpq}(\text{triple}(x, y, z)))))) \quad \text{fof}(\text{119\_l20}, \text{lemma})$

$\forall u, v, w: (\neg \text{check\_cpq}(\text{triple}(u, v, w)) \Rightarrow \forall x, y, z: (\text{succ\_cpq}(\text{triple}(u, v, w), \text{triple}(x, y, z)) \Rightarrow (\neg \text{ok}(\text{triple}(x, y, z)) \text{ or } \neg \text{check\_cpq}(\text{triple}(x, y, z))))$

**SWV384+1.p** Priority queue checker: lemma\_not\_min\_elem\_not\_check\_induction

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w, x, y, z: (\text{succ\_cpq}(\text{triple}(u, v, w), \text{triple}(x, y, z)) \Rightarrow ((\neg \text{check\_cpq}(\text{triple}(x, y, z)) \text{ or } \neg \text{ok}(\text{triple}(x, y, z))) \Rightarrow (\neg \text{check\_cpq}(\text{im\_succ\_cpq}(\text{triple}(x, y, z))) \text{ or } \neg \text{ok}(\text{im\_succ\_cpq}(\text{triple}(x, y, z)))))) \Rightarrow \forall x_1, x_2, x_3: ((\neg \text{check\_cpq}(\text{triple}(x_1, x_2, x_3)) \text{ or } \neg \text{ok}(\text{triple}(x_1, x_2, x_3))))$

$\forall x_4, x_5, x_6: (\text{succ\_cpq}(\text{triple}(x_1, x_2, x_3), \text{triple}(x_4, x_5, x_6)) \Rightarrow (\neg \text{ok}(\text{triple}(x_4, x_5, x_6)) \text{ or } \neg \text{check\_cpq}(\text{triple}(x_4, x_5, x_6))))$

$\forall u, v, w: ((\neg \text{check\_cpq}(\text{triple}(u, v, w)) \text{ or } \neg \text{ok}(\text{triple}(u, v, w))) \Rightarrow (\neg \text{check\_cpq}(\text{im\_succ\_cpq}(\text{triple}(u, v, w))) \text{ or } \neg \text{ok}(\text{im\_succ\_cpq}(\text{triple}(u, v, w))))$

$\forall u, v, w: ((\neg \text{check\_cpq}(\text{triple}(u, v, w)) \text{ or } \neg \text{ok}(\text{triple}(u, v, w))) \Rightarrow \forall x, y, z: (\text{succ\_cpq}(\text{triple}(u, v, w), \text{triple}(x, y, z)) \Rightarrow (\neg \text{ok}(\text{triple}(x, y, z)) \text{ or } \neg \text{check\_cpq}(\text{triple}(x, y, z))))))$  fof(l20\_co, conjecture)

**SWV385+1.p** Priority queue checker: lemma\_not\_min\_elem\_not\_check\_induction02

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w: (\neg \text{ok}(\text{triple}(u, v, w)) \Rightarrow \neg \text{ok}(\text{im\_succ\_cpq}(\text{triple}(u, v, w))))$  fof(l21\_li1316, lemma)

$\forall u, v, w: (\neg \text{check\_cpq}(\text{triple}(u, v, w)) \Rightarrow (\neg \text{check\_cpq}(\text{im\_succ\_cpq}(\text{triple}(u, v, w))) \text{ or } \neg \text{ok}(\text{im\_succ\_cpq}(\text{triple}(u, v, w))))))$

$\forall u, v, w: ((\neg \text{check\_cpq}(\text{triple}(u, v, w)) \text{ or } \neg \text{ok}(\text{triple}(u, v, w))) \Rightarrow (\neg \text{check\_cpq}(\text{im\_succ\_cpq}(\text{triple}(u, v, w))) \text{ or } \neg \text{ok}(\text{im\_succ\_cpq}(\text{triple}(u, v, w))))))$

**SWV386+1.p** Priority queue checker: lemma\_not\_min\_elem\_not\_check\_ind\_steps 1

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w: (\neg \text{check\_cpq}(\text{triple}(u, v, w)) \Rightarrow \forall x: \neg \text{check\_cpq}(\text{insert\_cpq}(\text{triple}(u, v, w), x)))$  fof(l22\_l26, lemma)

$\forall u, v, w: (\neg \text{check\_cpq}(\text{triple}(u, v, w)) \Rightarrow \forall x: (\neg \text{check\_cpq}(\text{insert\_cpq}(\text{triple}(u, v, w), x)) \text{ or } \neg \text{ok}(\text{insert\_cpq}(\text{triple}(u, v, w), x))))$

**SWV387+1.p** Priority queue checker: lemma\_not\_min\_elem\_not\_check\_ind\_steps 2

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w, x: ((\text{check\_cpq}(\text{remove\_cpq}(\text{triple}(u, v, w), x)) \text{ and } \text{ok}(\text{remove\_cpq}(\text{triple}(u, v, w), x))) \Rightarrow \text{check\_cpq}(\text{triple}(u, v, w)))$

$\forall u, v, w: (\neg \text{check\_cpq}(\text{triple}(u, v, w)) \Rightarrow \forall x: (\neg \text{check\_cpq}(\text{remove\_cpq}(\text{triple}(u, v, w), x)) \text{ or } \neg \text{ok}(\text{remove\_cpq}(\text{triple}(u, v, w), x))))$

**SWV388+1.p** Priority queue checker: lemma\_not\_min\_elem\_not\_check\_ind\_steps 3

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w: (\neg \text{check\_cpq}(\text{triple}(u, v, w)) \Rightarrow \neg \text{check\_cpq}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))))$  fof(l24\_l34, lemma)

$\forall u, v, w: (\neg \text{check\_cpq}(\text{triple}(u, v, w)) \Rightarrow (\neg \text{check\_cpq}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))) \text{ or } \neg \text{ok}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))))))$

**SWV389+1.p** Priority queue checker: lemma\_not\_min\_elem\_not\_check\_ind\_steps 4

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w: ((\text{check\_cpq}(\text{removemin\_cpq\_eff}(\text{triple}(u, v, w))) \text{ and } \text{ok}(\text{removemin\_cpq\_eff}(\text{triple}(u, v, w)))) \Rightarrow \text{check\_cpq}(\text{triple}(u, v, w)))$

$\forall u, v, w: (\neg \text{check\_cpq}(\text{triple}(u, v, w)) \Rightarrow (\neg \text{check\_cpq}(\text{removemin\_cpq\_eff}(\text{triple}(u, v, w))) \text{ or } \neg \text{ok}(\text{removemin\_cpq\_eff}(\text{triple}(u, v, w))))))$

**SWV390+1.p** Priority queue checker: tmp\_not\_check\_01

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w: (\text{check\_cpq}(\text{triple}(u, v, w)) \iff \forall x, y: (\text{pair\_in\_list}(v, x, y) \Rightarrow y < x))$  fof(l26\_li4142, lemma)

$\forall u, v, w: (\neg \text{check\_cpq}(\text{triple}(u, v, w)) \Rightarrow \forall x: \neg \text{check\_cpq}(\text{insert\_cpq}(\text{triple}(u, v, w), x)))$  fof(l26\_co, conjecture)

**SWV391+1.p** Priority queue checker: tmp\_not\_check\_02

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w: (\text{check\_cpq}(\text{triple}(u, v, w)) \iff \forall x, y: (\text{pair\_in\_list}(v, x, y) \Rightarrow y < x))$  fof(l27\_li4142, lemma)

$\forall u, v, w: (\text{pair\_in\_list}(u, v, w) \Rightarrow \forall x: (\text{contains\_slb}(u, x) \Rightarrow (\text{pair\_in\_list}(\text{remove\_slb}(u, x), v, w) \text{ or } v = x)))$  fof(l27\_li2829, lemma)

$\forall u, v, w, x: ((\text{check\_cpq}(\text{remove\_cpq}(\text{triple}(u, v, w), x)) \text{ and } \text{ok}(\text{remove\_cpq}(\text{triple}(u, v, w), x))) \Rightarrow \forall y: (\text{pair\_in\_list}(v, x, y) \Rightarrow y < x))$  fof(l27\_l30, lemma)

$\forall u, v, w, x: (\text{ok}(\text{remove\_cpq}(\text{triple}(u, v, w), x)) \Rightarrow \text{contains\_slb}(v, x))$  fof(l27\_l33, lemma)

$\forall u, v, w, x: ((\text{check\_cpq}(\text{remove\_cpq}(\text{triple}(u, v, w), x)) \text{ and } \text{ok}(\text{remove\_cpq}(\text{triple}(u, v, w), x))) \Rightarrow \text{check\_cpq}(\text{triple}(u, v, w)))$

**SWV392+1.p** Priority queue checker: tmp\_not\_check\_02\_1 base

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

$\forall u, v: (\text{pair\_in\_list}(\text{create\_slb}, u, v) \Rightarrow \forall w: (\text{contains\_slb}(\text{create\_slb}, w) \Rightarrow (\text{pair\_in\_list}(\text{remove\_slb}(\text{create\_slb}, w), u, v) \text{ or } u = w)))$  fof(l28\_co, conjecture)

**SWV393+1.p** Priority queue checker: tmp\_not\_check\_02\_1 step

include('Axioms/SWV007+0.ax')



include('Axioms/SWV007+2.ax')

$\forall u: (\forall v, w: (\text{pair\_in\_list}(u, v, w) \Rightarrow \forall x: (\text{contains\_slb}(u, x) \Rightarrow (\text{pair\_in\_list}(\text{remove\_slb}(u, x), v, w) \text{ or } v = x))) \Rightarrow$   
 $\forall y, z, x_1, x_2: (\text{pair\_in\_list}(\text{insert\_slb}(u, \text{pair}(x_1, x_2)), y, z) \Rightarrow \forall x_1: (\text{contains\_slb}(\text{insert\_slb}(u, \text{pair}(x_1, x_2)), x_1) \Rightarrow$   
 $(\text{pair\_in\_list}(\text{remove\_slb}(\text{insert\_slb}(u, \text{pair}(x_1, x_2)), x_1), y, z) \text{ or } y = x_1)))) \quad \text{fof}(129\_co, \text{conjecture})$

**SWV394+1.p** Priority queue checker: tmp\_not\_check\_02.2

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w: (\text{check\_cpq}(\text{triple}(u, v, w)) \iff \forall x, y: (\text{pair\_in\_list}(v, x, y) \Rightarrow y < x)) \quad \text{fof}(130\_li_{4142}, \text{lemma})$

$\forall u, v, w, x, y: ((\text{pair\_in\_list}(v, x, y) \text{ and } \text{strictly\_less\_than}(x, y) \text{ and } \text{ok}(\text{remove\_cpq}(\text{triple}(u, v, w), x))) \Rightarrow \text{pair\_in\_list}(\text{remove\_slb}(u, v, w), x, y))$

$\forall u, v, w, x: ((\text{check\_cpq}(\text{remove\_cpq}(\text{triple}(u, v, w), x)) \text{ and } \text{ok}(\text{remove\_cpq}(\text{triple}(u, v, w), x))) \Rightarrow \forall y: (\text{pair\_in\_list}(v, x, y) \Rightarrow y < x)) \quad \text{fof}(130\_co, \text{conjecture})$

**SWV395+1.p** Priority queue checker: tmp\_not\_check\_02.2.1 base

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w, x: ((\text{pair\_in\_list}(\text{create\_slb}, w, x) \text{ and } \text{strictly\_less\_than}(w, x) \text{ and } \text{ok}(\text{remove\_cpq}(\text{triple}(u, \text{create\_slb}, v), w))) \Rightarrow \text{pair\_in\_list}(\text{remove\_slb}(\text{create\_slb}, w), w, x)) \quad \text{fof}(131\_co, \text{conjecture})$

**SWV396+1.p** Priority queue checker: tmp\_not\_check\_02.2.1 step

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u: (\forall v, w, x, y: ((\text{pair\_in\_list}(u, x, y) \text{ and } \text{strictly\_less\_than}(x, y) \text{ and } \text{ok}(\text{remove\_cpq}(\text{triple}(v, u, w), x))) \Rightarrow \text{pair\_in\_list}(\text{remove\_slb}(u, v, w), x, y))$

$\forall z, x_1, x_2, x_3, x_4, x_5: ((\text{pair\_in\_list}(\text{insert\_slb}(u, \text{pair}(x_4, x_5)), x_2, x_3) \text{ and } \text{strictly\_less\_than}(x_2, x_3) \text{ and } \text{ok}(\text{remove\_cpq}(\text{triple}(z, \text{insert\_slb}(u, \text{pair}(x_4, x_5)), x_2), x_2, x_3))) \Rightarrow \text{pair\_in\_list}(\text{remove\_slb}(\text{insert\_slb}(u, \text{pair}(x_4, x_5)), x_2), x_2, x_3))) \quad \text{fof}(132\_co, \text{conjecture})$

**SWV397+1.p** Priority queue checker: tmp\_not\_check\_02.3

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w, x: (\text{ok}(\text{remove\_cpq}(\text{triple}(u, v, w), x)) \Rightarrow \text{contains\_slb}(v, x)) \quad \text{fof}(133\_co, \text{conjecture})$

**SWV398+1.p** Priority queue checker: tmp\_not\_check\_03

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w: (\text{check\_cpq}(\text{triple}(u, v, w)) \iff \forall x, y: (\text{pair\_in\_list}(v, x, y) \Rightarrow y < x)) \quad \text{fof}(126\_li_{4142}, \text{lemma})$

$\forall u: (\exists v, w: (\text{pair\_in\_list}(u, v, w) \text{ and } \text{strictly\_less\_than}(v, w)) \Rightarrow \forall x: \exists y, z: (\text{pair\_in\_list}(\text{update\_slb}(u, x), y, z) \text{ and } \text{strictly\_less\_than}(y, z)))$

$\forall u, v, w: (\neg \text{check\_cpq}(\text{triple}(u, v, w)) \Rightarrow \neg \text{check\_cpq}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w)))) \quad \text{fof}(124\_co, \text{conjecture})$

**SWV399+1.p** Priority queue checker: tmp\_not\_check\_03.1

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

$\forall u, v, w, x: ((\text{pair\_in\_list}(u, v, w) \text{ and } x < w) \Rightarrow \text{pair\_in\_list}(\text{update\_slb}(u, x), v, w)) \quad \text{fof}(135\_li_{3637}, \text{lemma})$

$\forall u, v, w, x: ((\text{pair\_in\_list}(u, v, w) \text{ and } \text{strictly\_less\_than}(w, x)) \Rightarrow \text{pair\_in\_list}(\text{update\_slb}(u, x), v, x)) \quad \text{fof}(135\_li_{3839}, \text{lemma})$

$\forall u: (\exists v, w: (\text{pair\_in\_list}(u, v, w) \text{ and } \text{strictly\_less\_than}(v, w)) \Rightarrow \forall x: \exists y, z: (\text{pair\_in\_list}(\text{update\_slb}(u, x), y, z) \text{ and } \text{strictly\_less\_than}(y, z)))$

**SWV400+1.p** Priority queue checker: tmp\_not\_check\_03.2 base

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

$\forall u, v, w, x: ((\text{pair\_in\_list}(\text{create\_slb}, v, w) \text{ and } x < w) \Rightarrow \text{pair\_in\_list}(\text{update\_slb}(\text{create\_slb}, x), v, w)) \quad \text{fof}(136\_co, \text{conjecture})$

**SWV401+1.p** Priority queue checker: tmp\_not\_check\_03.2 step

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

$\forall u: (\forall v, w, x: ((\text{pair\_in\_list}(u, v, w) \text{ and } x < w) \Rightarrow \text{pair\_in\_list}(\text{update\_slb}(u, x), v, w)) \Rightarrow \forall y, z, x_1, x_2, x_3: ((\text{pair\_in\_list}(\text{insert\_slb}(u, \text{pair}(x_2, x_3)), y, z) \text{ and } \text{strictly\_less\_than}(x_2, x_3) \text{ and } \text{ok}(\text{remove\_cpq}(\text{triple}(z, \text{insert\_slb}(u, \text{pair}(x_2, x_3)), x_1), y, z))) \Rightarrow \text{pair\_in\_list}(\text{update\_slb}(\text{insert\_slb}(u, \text{pair}(x_2, x_3)), x_1), y, z))) \quad \text{fof}(137\_co, \text{conjecture})$

**SWV402+1.p** Priority queue checker: tmp\_not\_check\_03.3 base

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

$\forall u, v, w, x: ((\text{pair\_in\_list}(\text{create\_slb}, v, w) \text{ and } \text{strictly\_less\_than}(w, x)) \Rightarrow \text{pair\_in\_list}(\text{update\_slb}(\text{create\_slb}, x), v, x)) \quad \text{fof}(138\_co, \text{conjecture})$

**SWV403+1.p** Priority queue checker: tmp\_not\_check\_03\_3 step

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

$\forall u: (\forall v, w, x: ((\text{pair\_in\_list}(u, v, w) \text{ and } \text{strictly\_less\_than}(w, x)) \Rightarrow \text{pair\_in\_list}(\text{update\_slb}(u, x), v, x)) \Rightarrow \forall y, z, x_1, x_2, x_3: ((\text{pair\_in\_list}(\text{update\_slb}(\text{insert\_slb}(u, \text{pair}(x_2, x_3)), x_1), y, x_1))) \text{ fof}(l39\_co, \text{conjecture}))$

**SWV404+1.p** Priority queue checker: tmp\_not\_check\_04

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w, x: ((\text{check\_cpq}(\text{remove\_cpq}(\text{triple}(u, v, w), x)) \text{ and } \text{ok}(\text{remove\_cpq}(\text{triple}(u, v, w), x))) \Rightarrow \text{check\_cpq}(\text{triple}(u, v, w)))$

$\forall u, v, w: (\neg \text{check\_cpq}(\text{triple}(u, v, w)) \Rightarrow \neg \text{check\_cpq}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w)))) \text{ fof}(l40\_l34, \text{lemma})$

$\forall u, v, w: ((\text{check\_cpq}(\text{removemin\_cpq\_eff}(\text{triple}(u, v, w))) \text{ and } \text{ok}(\text{removemin\_cpq\_eff}(\text{triple}(u, v, w)))) \Rightarrow \text{check\_cpq}(\text{triple}(u, v, w)))$

**SWV405+1.p** Priority queue checker: lemma\_check\_characterization base

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v: (\text{check\_cpq}(\text{triple}(u, \text{create\_slb}, v)) \iff \forall w, x: (\text{pair\_in\_list}(\text{create\_slb}, w, x) \Rightarrow x < w)) \text{ fof}(l41\_co, \text{conjecture})$

**SWV406+1.p** Priority queue checker: lemma\_check\_characterization step

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u: (\forall v, w: (\text{check\_cpq}(\text{triple}(v, u, w)) \iff \forall x, y: (\text{pair\_in\_list}(u, x, y) \Rightarrow y < x)) \Rightarrow \forall z, x_1, x_2, x_3: (\text{check\_cpq}(\text{triple}(z, \text{insert\_slb}(u, \text{pair}(x_2, x_3)), x_1)))) \text{ fof}(l42\_co, \text{conjecture}))$

$\forall x_4, x_5: (\text{pair\_in\_list}(\text{insert\_slb}(u, \text{pair}(x_2, x_3)), x_4, x_5) \Rightarrow x_5 < x_4)) \text{ fof}(l42\_co, \text{conjecture})$

**SWV407+1.p** Priority queue checker: lemma\_not\_min\_elem\_not\_check

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w: (\text{check\_cpq}(\text{triple}(u, v, w)) \iff \forall x, y: (\text{pair\_in\_list}(v, x, y) \Rightarrow y < x)) \text{ fof}(l43\_li4142, \text{lemma})$

$\forall u, v, w, x: ((\text{contains\_slb}(v, x) \text{ and } \text{strictly\_less\_than}(x, \text{findmin\_cpq\_res}(\text{triple}(u, v, w)))) \Rightarrow (\text{pair\_in\_list}(\text{update\_slb}(v, \text{findmin\_cpq\_res}(\text{triple}(u, v, w)), x)))) \text{ fof}(l43\_l44, \text{lemma})$

$\forall u, v, w: (\exists x: (\text{contains\_cpq}(\text{triple}(u, v, w), x) \text{ and } \text{strictly\_less\_than}(x, \text{findmin\_cpq\_res}(\text{triple}(u, v, w)))) \Rightarrow \neg \text{check\_cpq}(\text{findmin\_cpq\_res}(\text{triple}(u, v, w))))$

**SWV408+1.p** Priority queue checker: lemma\_not\_min\_elem\_pair

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v, w: ((\text{contains\_slb}(u, v) \text{ and } \text{strictly\_less\_than}(v, w)) \Rightarrow (\text{pair\_in\_list}(\text{update\_slb}(u, w), v, w) \text{ or } \exists x: (\text{pair\_in\_list}(\text{update\_slb}(u, w), x, v)))) \text{ fof}(l44\_l45, \text{lemma})$

$\forall u, v, w, x: ((\text{contains\_slb}(v, x) \text{ and } \text{strictly\_less\_than}(x, \text{findmin\_cpq\_res}(\text{triple}(u, v, w)))) \Rightarrow (\text{pair\_in\_list}(\text{update\_slb}(v, \text{findmin\_cpq\_res}(\text{triple}(u, v, w)), x)))) \text{ fof}(l44\_co, \text{conjecture})$

**SWV408+2.p** Priority queue checker: lemma\_not\_min\_elem\_pair

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

$\forall u, v: (\text{contains\_slb}(u, v) \Rightarrow \exists w: \text{pair\_in\_list}(u, v, w)) \text{ fof}(l45\_li4647, \text{lemma})$

$\forall u, v, w, x: ((\text{pair\_in\_list}(u, v, w) \text{ and } \text{strictly\_less\_than}(w, x)) \Rightarrow \text{pair\_in\_list}(\text{update\_slb}(u, x), v, x)) \text{ fof}(l48\_li3839, \text{lemma})$

$\forall u, v, w, x: ((\text{pair\_in\_list}(u, v, w) \text{ and } x < w) \Rightarrow \text{pair\_in\_list}(\text{update\_slb}(u, x), v, w)) \text{ fof}(l49\_li3637, \text{lemma})$

$\forall u, v, w, x: ((\text{contains\_slb}(v, x) \text{ and } \text{strictly\_less\_than}(x, \text{findmin\_cpq\_res}(\text{triple}(u, v, w)))) \Rightarrow (\text{pair\_in\_list}(\text{update\_slb}(v, \text{findmin\_cpq\_res}(\text{triple}(u, v, w)), x)))) \text{ fof}(l44\_co, \text{conjecture})$

**SWV409+1.p** Priority queue checker: lemma\_contains\_update

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

$\forall u, v: (\text{contains\_slb}(u, v) \Rightarrow \exists w: \text{pair\_in\_list}(u, v, w)) \text{ fof}(l45\_li4647, \text{lemma})$

$\forall u, v, w, x: ((\text{pair\_in\_list}(u, v, w) \text{ and } \text{strictly\_less\_than}(v, x) \text{ and } \text{strictly\_less\_than}(w, x)) \Rightarrow \text{pair\_in\_list}(\text{update\_slb}(u, x), v, x))$

$\forall u, v, w, x: ((\text{pair\_in\_list}(u, v, w) \text{ and } \text{strictly\_less\_than}(v, x) \text{ and } x < w) \Rightarrow \exists y: (\text{pair\_in\_list}(\text{update\_slb}(u, x), v, y) \text{ and } x < y)) \text{ fof}(l45\_l49, \text{lemma})$

$\forall u, v, w: ((\text{contains\_slb}(u, v) \text{ and } \text{strictly\_less\_than}(v, w)) \Rightarrow (\text{pair\_in\_list}(\text{update\_slb}(u, w), v, w) \text{ or } \exists x: (\text{pair\_in\_list}(\text{update\_slb}(u, w), v, w), x)))$  fof(145\_co, conjecture)

**SWV410+1.p** Priority queue checker: lemma\_contains\_pair base

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

$\forall u: (\text{contains\_slb}(\text{create\_slb}, u) \Rightarrow \exists v: \text{pair\_in\_list}(\text{create\_slb}, u, v))$  fof(146\_co, conjecture)

**SWV411+1.p** Priority queue checker: lemma\_contains\_pair step

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

$\forall u: (\forall v: (\text{contains\_slb}(u, v) \Rightarrow \exists w: \text{pair\_in\_list}(u, v, w)) \Rightarrow \forall x, y, z: (\text{contains\_slb}(\text{insert\_slb}(u, \text{pair}(y, z)), x) \Rightarrow \exists x_1: \text{pair\_in\_list}(\text{insert\_slb}(u, \text{pair}(y, z)), x, x_1)))$  fof(147\_co, conjecture)

**SWV412+1.p** Priority queue checker: lemma\_contains\_update\_01

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

$\forall u, v, w, x: ((\text{pair\_in\_list}(u, v, w) \text{ and } \text{strictly\_less\_than}(w, x)) \Rightarrow \text{pair\_in\_list}(\text{update\_slb}(u, x), v, x))$  fof(148\_li3839, lemma)

$\forall u, v, w, x: ((\text{pair\_in\_list}(u, v, w) \text{ and } \text{strictly\_less\_than}(v, x) \text{ and } \text{strictly\_less\_than}(w, x)) \Rightarrow \text{pair\_in\_list}(\text{update\_slb}(u, x), v, x))$

**SWV413+1.p** Priority queue checker: lemma\_contains\_update\_02

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+2.ax')

$\forall u, v, w, x: ((\text{pair\_in\_list}(u, v, w) \text{ and } x < w) \Rightarrow \text{pair\_in\_list}(\text{update\_slb}(u, x), v, w))$  fof(149\_li3637, lemma)

$\forall u, v, w, x: ((\text{pair\_in\_list}(u, v, w) \text{ and } \text{strictly\_less\_than}(v, x) \text{ and } x < w) \Rightarrow \exists y: (\text{pair\_in\_list}(\text{update\_slb}(u, x), v, y) \text{ and } x < y))$  fof(149\_co, conjecture)

**SWV414+1.p** Priority queue checker: Formula (12)

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+1.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

include('Axioms/SWV007+4.ax')

$\forall u: i(\text{triple}(\text{create\_pq}, \text{create\_slb}, u)) = \text{create\_pq}$  fof(co1, conjecture)

**SWV415+1.p** Priority queue checker: Formula (7)

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+1.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

include('Axioms/SWV007+4.ax')

$\forall u, v, w, x, y: i(\text{triple}(u, w, x)) = i(\text{triple}(v, w, y))$  fof(main2.li12, lemma)

$\forall u, v, w, x: i(\text{insert\_cpq}(\text{triple}(u, v, w), x)) = \text{insert\_pq}(i(\text{triple}(u, v, w)), x)$  fof(co2, conjecture)

**SWV415+2.p** Priority queue checker: Formula (7)

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+1.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

include('Axioms/SWV007+4.ax')

$(\forall u, v, w, x: i(\text{triple}(u, \text{create\_slb}, w)) = i(\text{triple}(v, \text{create\_slb}, x)) \text{ and } \forall y: (\forall z, x_1, x_2, x_3: i(\text{triple}(z, y, x_2)) = i(\text{triple}(x_1, y, x_3)))$

$\forall x_4, x_5, x_6, x_7, x_8, x_9: i(\text{triple}(x_4, \text{insert\_slb}(y, \text{pair}(x_8, x_9)), x_6)) = i(\text{triple}(x_5, \text{insert\_slb}(y, \text{pair}(x_8, x_9)), x_7)))) \Rightarrow$

$\forall x_{10}, x_{11}, x_{12}, x_{13}, x_{14}: i(\text{triple}(x_{10}, x_{12}, x_{13})) = i(\text{triple}(x_{11}, x_{12}, x_{14}))$  fof(big2.induction, axiom)

$\forall u, v, w, x: i(\text{insert\_cpq}(\text{triple}(u, v, w), x)) = \text{insert\_pq}(i(\text{triple}(u, v, w)), x)$  fof(co2, conjecture)

**SWV416+1.p** Priority queue checker: Formula (8)

include('Axioms/SWV007+0.ax')

include('Axioms/SWV007+1.ax')

include('Axioms/SWV007+2.ax')

include('Axioms/SWV007+3.ax')

include('Axioms/SWV007+4.ax')

$\forall u, v, w, x, y: i(\text{triple}(u, w, x)) = i(\text{triple}(v, w, y))$  fof(main3.li12, lemma)

$\forall u, v, w, x: (\text{contains\_pq}(i(\text{triple}(u, v, w)), x) \Rightarrow i(\text{remove\_cpq}(\text{triple}(u, v, w), x)) = \text{remove\_pq}(i(\text{triple}(u, v, w)), x))$  fof(m

$\forall u, v, w, x: (\text{pi\_remove}(\text{triple}(u, v, w), x) \Rightarrow (\text{phi}(\text{remove\_cpq}(\text{triple}(u, v, w), x)) \Rightarrow (\text{pi\_sharp\_remove}(i(\text{triple}(u, v, w)), x) \text{ and } \text{remove\_pq}(i(\text{triple}(u, v, w)), x)))) \quad \text{fof}(\text{co}_3, \text{conjecture})$

**SWV416+2.p** Priority queue checker: Formula (8)

```
include('Axioms/SWV007+0.ax')
include('Axioms/SWV007+1.ax')
include('Axioms/SWV007+2.ax')
include('Axioms/SWV007+3.ax')
include('Axioms/SWV007+4.ax')
 $\forall u, v, w, x: i(\text{triple}(u, \text{create\_slb}, w)) = i(\text{triple}(v, \text{create\_slb}, x)) \text{ and } \forall y: (\forall z, x_1, x_2, x_3: i(\text{triple}(z, y, x_2)) = i(\text{triple}(x_1, y, x_3)))$ 
 $\forall x_4, x_5, x_6, x_7, x_8, x_9: i(\text{triple}(x_4, \text{insert\_slb}(y, \text{pair}(x_8, x_9)), x_6)) = i(\text{triple}(x_5, \text{insert\_slb}(y, \text{pair}(x_8, x_9)), x_7))) \Rightarrow$ 
 $\forall x_{10}, x_{11}, x_{12}, x_{13}, x_{14}: i(\text{triple}(x_{10}, x_{12}, x_{13})) = i(\text{triple}(x_{11}, x_{12}, x_{14})) \quad \text{fof}(\text{big3\_induction}_1, \text{axiom})$ 
 $(\forall u, v, w: (\text{contains\_pq}(i(\text{triple}(u, \text{create\_slb}, v)), w) \Rightarrow i(\text{remove\_cpq}(\text{triple}(u, \text{create\_slb}, v), w)) = \text{remove\_pq}(i(\text{triple}(u, \text{create\_slb}, v)), w))$ 
 $i(\text{remove\_cpq}(\text{triple}(y, x, z), x_1)) = \text{remove\_pq}(i(\text{triple}(y, x, z), x_1)) \Rightarrow \forall x_2, x_3, x_4, x_5, x_6: (\text{contains\_pq}(i(\text{triple}(x_2, \text{insert\_slb}(x, \text{pair}(x_5, x_6)), x_3)), x_4)) = \text{remove\_pq}(i(\text{triple}(x_2, \text{insert\_slb}(x, \text{pair}(x_5, x_6)), x_3)), x_4))) \Rightarrow$ 
 $\forall x_7, x_8, x_9, x_{10}: (\text{contains\_pq}(i(\text{triple}(x_7, x_8, x_9)), x_{10}) \Rightarrow i(\text{remove\_cpq}(\text{triple}(x_7, x_8, x_9), x_{10})) = \text{remove\_pq}(i(\text{triple}(x_7, x_8, x_9)), x_{10}))) \Rightarrow$ 
 $(\forall u, v, w: (\text{contains\_cpq}(\text{triple}(u, \text{create\_slb}, v), w) \iff \text{contains\_pq}(i(\text{triple}(u, \text{create\_slb}, v)), w)) \text{ and } \forall x: (\forall y, z, x_1: (\text{contains\_cpq}(\text{triple}(x_2, \text{insert\_slb}(x, \text{pair}(x_4, x_5)), x_3), x_6) \iff \text{contains\_pq}(i(\text{triple}(x_2, \text{insert\_slb}(x, \text{pair}(x_4, x_5)), x_3)), x_6))) \Rightarrow \forall x_7, x_8, x_9, x_{10}: (\text{contains\_cpq}(\text{triple}(x_7, x_8, x_9), x_{10}) \iff \text{contains\_pq}(i(\text{triple}(x_7, x_8, x_9)), x_{10}))) \quad \text{fof}(\text{big3\_induction}_3, \text{axiom})$ 
 $\forall u, v, w, x: (\text{pi\_remove}(\text{triple}(u, v, w), x) \Rightarrow (\text{phi}(\text{remove\_cpq}(\text{triple}(u, v, w), x)) \Rightarrow (\text{pi\_sharp\_remove}(i(\text{triple}(u, v, w)), x) \text{ and } \text{remove\_pq}(i(\text{triple}(u, v, w)), x)))) \quad \text{fof}(\text{co}_3, \text{conjecture})$ 
```

**SWV417+1.p** Priority queue checker: Formula (9)

```
include('Axioms/SWV007+0.ax')
include('Axioms/SWV007+1.ax')
include('Axioms/SWV007+2.ax')
include('Axioms/SWV007+3.ax')
include('Axioms/SWV007+4.ax')
 $\forall u, v, w: (\text{phi}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))) \Rightarrow \text{pi\_sharp\_find\_min}(i(\text{triple}(u, v, w)), \text{findmin\_cpq\_res}(\text{triple}(u, v, w)))) \quad \text{fof}(\text{co}_4, \text{conjecture})$ 
 $\forall u, v, w: (\text{pi\_find\_min}(\text{triple}(u, v, w)) \Rightarrow (\text{phi}(\text{findmin\_cpq\_eff}(\text{triple}(u, v, w))) \Rightarrow \exists x: (\text{pi\_sharp\_find\_min}(i(\text{triple}(u, v, w)), x), \text{findmin\_pq\_res}(i(\text{triple}(u, v, w)), x)))) \quad \text{fof}(\text{co}_4, \text{conjecture})$ 
```

**SWV425^1.p** ICL logic mapping to modal logic implies 'unit'

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
s: $i → $o   thf(s, type)
a: $i → $o   thf(a, type)
iclval@(icl_impl@(icl_atom@s)@(icl_says@(icl_princ@a)@(icl_atom@s)))   thf(unit, conjecture)
```

**SWV425^2.p** ICL logic mapping to modal logic implies 'unit'

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
include('Axioms/SWV008^1.ax')
s: $i → $o   thf(s, type)
a: $i → $o   thf(a, type)
iclval@(icl_impl@(icl_atom@s)@(icl_says@(icl_princ@a)@(icl_atom@s)))   thf(unit, conjecture)
```

**SWV426^1.p** ICL logic mapping to modal logic implies 'cuc'

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
s: $i → $o   thf(s, type)
t: $i → $o   thf(t, type)
a: $i → $o   thf(a, type)
iclval@(icl_impl@(icl_says@(icl_princ@a)@(icl_impl@(icl_atom@s)@(icl_atom@t)))@(icl_impl@(icl_says@(icl_princ@a)@(icl_atom@s))))   thf(unit, conjecture)
```

**SWV426^2.p** ICL logic mapping to modal logic implies 'cuc'

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
include('Axioms/SWV008^1.ax')
s: $i → $o   thf(s, type)
t: $i → $o   thf(t, type)
a: $i → $o   thf(a, type)
```

iclval@(icl\_impl@(icl\_says@(icl\_princ@a)@(icl\_impl@(icl\_atom@s)@(icl\_atom@t)))@(icl\_impl@(icl\_says@(icl\_princ@a)@(icl\_atom@t)))

**SWV426^3.p** ICL $\wedge$ B logic mapping to modal logic implies 'cuc'

include('Axioms/LCL008^0.ax')

include('Axioms/SWV008^0.ax')

s:  $\$i \rightarrow \$o$  thf(s, type)

a:  $\$i \rightarrow \$o$  thf(a, type)

b:  $\$i \rightarrow \$o$  thf(b, type)

iclval@(icl\_impl@(icl\_says@(icl\_impl@(icl\_princ@a)@(icl\_princ@b))@(icl\_atom@s))@(icl\_impl@(icl\_says@(icl\_princ@a)@(icl\_atom@t)))

**SWV426^4.p** ICL $\wedge$ B logic mapping to modal logic implies 'cuc'

include('Axioms/LCL008^0.ax')

include('Axioms/SWV008^0.ax')

include('Axioms/SWV008^1.ax')

s:  $\$i \rightarrow \$o$  thf(s, type)

a:  $\$i \rightarrow \$o$  thf(a, type)

b:  $\$i \rightarrow \$o$  thf(b, type)

iclval@(icl\_impl@(icl\_says@(icl\_impl@(icl\_princ@a)@(icl\_princ@b))@(icl\_atom@s))@(icl\_impl@(icl\_says@(icl\_princ@a)@(icl\_atom@t)))

**SWV427^1.p** ICL logic mapping to modal logic implies 'idem'

include('Axioms/LCL008^0.ax')

include('Axioms/SWV008^0.ax')

s:  $\$i \rightarrow \$o$  thf(s, type)

a:  $\$i \rightarrow \$o$  thf(a, type)

iclval@(icl\_impl@(icl\_says@(icl\_princ@a)@(icl\_says@(icl\_princ@a)@(icl\_atom@s)))@(icl\_says@(icl\_princ@a)@(icl\_atom@s)))

**SWV427^2.p** ICL logic mapping to modal logic implies 'idem'

include('Axioms/LCL008^0.ax')

include('Axioms/SWV008^0.ax')

include('Axioms/SWV008^1.ax')

s:  $\$i \rightarrow \$o$  thf(s, type)

a:  $\$i \rightarrow \$o$  thf(a, type)

iclval@(icl\_impl@(icl\_says@(icl\_princ@a)@(icl\_says@(icl\_princ@a)@(icl\_atom@s)))@(icl\_says@(icl\_princ@a)@(icl\_atom@s)))

**SWV428^1.p** ICL logic mapping to modal logic K implies that Example 1 holds

include('Axioms/LCL008^0.ax')

include('Axioms/SWV008^0.ax')

admin:  $\$i \rightarrow \$o$  thf(admin, type)

bob:  $\$i \rightarrow \$o$  thf(bob, type)

deletefile<sub>1</sub>:  $\$i \rightarrow \$o$  thf(deletefile<sub>1</sub>, type)

iclval@(icl\_impl@(icl\_says@(icl\_princ@admin)@(icl\_atom@deletefile<sub>1</sub>))@(icl\_atom@deletefile<sub>1</sub>)) thf(ax<sub>1</sub>, axiom)

iclval@(icl\_says@(icl\_princ@admin)@(icl\_impl@(icl\_says@(icl\_princ@bob)@(icl\_atom@deletefile<sub>1</sub>))@(icl\_atom@deletefile<sub>1</sub>)))

iclval@(icl\_says@(icl\_princ@bob)@(icl\_atom@deletefile<sub>1</sub>)) thf(ax<sub>3</sub>, axiom)

iclval@(icl\_atom@deletefile<sub>1</sub>) thf(ex<sub>1</sub>, conjecture)

**SWV428^2.p** ICL logic mapping to modal logic S4 implies 'Ex1'

include('Axioms/LCL008^0.ax')

include('Axioms/SWV008^0.ax')

include('Axioms/SWV008^1.ax')

admin:  $\$i \rightarrow \$o$  thf(admin, type)

bob:  $\$i \rightarrow \$o$  thf(bob, type)

deletefile<sub>1</sub>:  $\$i \rightarrow \$o$  thf(deletefile<sub>1</sub>, type)

iclval@(icl\_impl@(icl\_says@(icl\_princ@admin)@(icl\_atom@deletefile<sub>1</sub>))@(icl\_atom@deletefile<sub>1</sub>)) thf(ax<sub>1</sub>, axiom)

iclval@(icl\_says@(icl\_princ@admin)@(icl\_impl@(icl\_says@(icl\_princ@bob)@(icl\_atom@deletefile<sub>1</sub>))@(icl\_atom@deletefile<sub>1</sub>)))

iclval@(icl\_says@(icl\_princ@bob)@(icl\_atom@deletefile<sub>1</sub>)) thf(ax<sub>3</sub>, axiom)

iclval@(icl\_atom@deletefile<sub>1</sub>) thf(ex<sub>1</sub>, conjecture)

**SWV429^1.p** ICL $\wedge$ => logic mapping to modal logic implies 'refl'

include('Axioms/LCL008^0.ax')

include('Axioms/SWV008^0.ax')

include('Axioms/SWV008^2.ax')

a:  $\$i \rightarrow \$o$  thf(a, type)

iclval@(icl\_impl\_princ@(icl\_princ@a)@(icl\_princ@a)) thf(conj, conjecture)

**SWV429^2.p** ICL $\wedge$  $\Rightarrow$  logic mapping to modal logic implies 'refl'

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
include('Axioms/SWV008^1.ax')
include('Axioms/SWV008^2.ax')
a: $i  $\rightarrow$  $o   thf(a, type)
iclval@(icl_impl_princ@(icl_princ@a))@(icl_princ@a))   thf(conj, conjecture)
```

**SWV430^1.p** ICL $\wedge$  $\Rightarrow$  logic mapping to modal logic implies 'trans'

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
include('Axioms/SWV008^2.ax')
a: $i  $\rightarrow$  $o   thf(a, type)
b: $i  $\rightarrow$  $o   thf(b, type)
c: $i  $\rightarrow$  $o   thf(c, type)
iclval@(icl_impl@(icl_impl_princ@(icl_princ@a))@(icl_princ@b))@(icl_impl@(icl_impl_princ@(icl_princ@b))@(icl_princ@c))@(icl_princ@c))
```

**SWV430^2.p** ICL $\wedge$  $\Rightarrow$  logic mapping to modal logic implies 'trans'

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
include('Axioms/SWV008^1.ax')
include('Axioms/SWV008^2.ax')
a: $i  $\rightarrow$  $o   thf(a, type)
b: $i  $\rightarrow$  $o   thf(b, type)
c: $i  $\rightarrow$  $o   thf(c, type)
iclval@(icl_impl@(icl_impl_princ@(icl_princ@a))@(icl_princ@b))@(icl_impl@(icl_impl_princ@(icl_princ@b))@(icl_princ@c))@(icl_princ@c))
```

**SWV431^1.p** ICL $\wedge$  $\Rightarrow$  logic mapping to modal logic implies 'speaking\_for'

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
include('Axioms/SWV008^2.ax')
a: $i  $\rightarrow$  $o   thf(a, type)
b: $i  $\rightarrow$  $o   thf(b, type)
s: $i  $\rightarrow$  $o   thf(s, type)
iclval@(icl_impl@(icl_impl_princ@(icl_princ@a))@(icl_princ@b))@(icl_impl@(icl_says@(icl_princ@a))@(icl_atom@s))@(icl_says@)
```

**SWV431^2.p** ICL $\wedge$  $\Rightarrow$  logic mapping to modal logic implies 'speaking\_for'

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
include('Axioms/SWV008^1.ax')
include('Axioms/SWV008^2.ax')
a: $i  $\rightarrow$  $o   thf(a, type)
b: $i  $\rightarrow$  $o   thf(b, type)
s: $i  $\rightarrow$  $o   thf(s, type)
iclval@(icl_impl@(icl_impl_princ@(icl_princ@a))@(icl_princ@b))@(icl_impl@(icl_says@(icl_princ@a))@(icl_atom@s))@(icl_says@)
```

**SWV432^1.p** ICL $\wedge$  $\Rightarrow$  logic mapping to modal logic implies 'handoff'

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
include('Axioms/SWV008^2.ax')
a: $i  $\rightarrow$  $o   thf(a, type)
b: $i  $\rightarrow$  $o   thf(b, type)
iclval@(icl_impl@(icl_says@(icl_princ@b))@(icl_impl_princ@(icl_princ@a))@(icl_princ@b))@(icl_impl_princ@(icl_princ@a))@(icl_princ@)
```

**SWV432^2.p** ICL $\wedge$  $\Rightarrow$  logic mapping to modal logic implies 'handoff'

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
include('Axioms/SWV008^1.ax')
include('Axioms/SWV008^2.ax')
a: $i  $\rightarrow$  $o   thf(a, type)
b: $i  $\rightarrow$  $o   thf(b, type)
iclval@(icl_impl@(icl_says@(icl_princ@b))@(icl_impl_princ@(icl_princ@a))@(icl_princ@b))@(icl_impl_princ@(icl_princ@a))@(icl_princ@)
```

**SWV433<sup>1.p</sup>** ICL<sup>∧</sup>⇒ logic mapping to modal logic implies that Example 2 holds

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
include('Axioms/SWV008^2.ax')
admin: $i → $o    thf(admin, type)
bob: $i → $o     thf(bob, type)
alice: $i → $o   thf(alice, type)
deletfile1: $i → $o    thf(deletfile1, type)
iclval@(icl_impl@(icl_says@(icl_princ@admin)@(icl_atom@deletfile1))@(icl_atom@deletfile1))    thf(ax1, axiom)
iclval@(icl_says@(icl_princ@admin)@(icl_impl@(icl_says@(icl_princ@bob)@(icl_atom@deletfile1))@(icl_atom@deletfile1)))
iclval@(icl_says@(icl_princ@bob)@(icl_impl_princ@(icl_princ@alice)@(icl_princ@bob)))    thf(ax3, axiom)
iclval@(icl_says@(icl_princ@alice)@(icl_atom@deletfile1))    thf(ax4, axiom)
iclval@(icl_atom@deletfile1)    thf(conj, conjecture)
```

**SWV433<sup>2.p</sup>** ICL<sup>∧</sup>⇒ logic mapping to modal logic implies that Example 2 holds

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
include('Axioms/SWV008^1.ax')
include('Axioms/SWV008^2.ax')
admin: $i → $o    thf(admin, type)
bob: $i → $o     thf(bob, type)
alice: $i → $o   thf(alice, type)
deletfile1: $i → $o    thf(deletfile1, type)
iclval@(icl_impl@(icl_says@(icl_princ@admin)@(icl_atom@deletfile1))@(icl_atom@deletfile1))    thf(ax1, axiom)
iclval@(icl_says@(icl_princ@admin)@(icl_impl@(icl_says@(icl_princ@bob)@(icl_atom@deletfile1))@(icl_atom@deletfile1)))
iclval@(icl_says@(icl_princ@bob)@(icl_impl_princ@(icl_princ@alice)@(icl_princ@bob)))    thf(ax3, axiom)
iclval@(icl_says@(icl_princ@alice)@(icl_atom@deletfile1))    thf(ax4, axiom)
iclval@(icl_atom@deletfile1)    thf(conj, conjecture)
```

**SWV434<sup>3.p</sup>** ICL<sup>∧</sup>∧ logic mapping to modal logic implies 'trust'

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
s: $i → $o    thf(s, type)
iclval@(icl_impl@(icl_says@icl_false@(icl_atom@s))@(icl_atom@s))    thf(trust, conjecture)
```

**SWV434<sup>4.p</sup>** ICL<sup>∧</sup>∧ logic mapping to modal logic implies 'trust'

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
include('Axioms/SWV008^1.ax')
s: $i → $o    thf(s, type)
iclval@(icl_impl@(icl_says@icl_false@(icl_atom@s))@(icl_atom@s))    thf(trust, conjecture)
```

**SWV435<sup>3.p</sup>** ICL<sup>∧</sup>∧ logic mapping to modal logic implies 'untrust'

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
a: $i → $o    thf(a, type)
(icl_princ@a) = icl_true    thf(ax1, axiom)
iclval@(icl_says@(icl_princ@a)@icl_false)    thf(untrust, conjecture)
```

**SWV435<sup>4.p</sup>** ICL<sup>∧</sup>∧ logic mapping to modal logic implies 'untrust'

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
include('Axioms/SWV008^1.ax')
a: $i → $o    thf(a, type)
(icl_princ@a) = icl_true    thf(ax1, axiom)
iclval@(icl_says@(icl_princ@a)@icl_false)    thf(untrust, conjecture)
```

**SWV436<sup>3.p</sup>** ICL<sup>∧</sup>∧ logic mapping to modal logic implies that Example 3 holds

```
include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
admin: $i → $o    thf(admin, type)
bob: $i → $o     thf(bob, type)
deletfile1: $i → $o    thf(deletfile1, type)
```

```

iclval@(icl_says@(icl_impl@(icl_princ@admin)@icl_false)@(icl_atom@deletfile1))    thf(ax1, axiom)
iclval@(icl_says@(icl_princ@admin)@(icl_says@(icl_impl@(icl_princ@bob)@(icl_princ@admin))@(icl_atom@deletfile1)))    thf(ax2, axiom)
iclval@(icl_says@(icl_princ@bob)@(icl_atom@deletfile1))    thf(ax3, axiom)
iclval@(icl_atom@deletfile1)    thf(ex3, conjecture)

```

**SWV436<sup>^</sup>4.p** ICL<sup>^</sup>B logic mapping to modal logic implies that Example 3 holds

```

include('Axioms/LCL008^0.ax')
include('Axioms/SWV008^0.ax')
include('Axioms/SWV008^1.ax')
admin: $i → $o    thf(admin, type)
bob: $i → $o    thf(bob, type)
deletfile1: $i → $o    thf(deletfile1, type)
iclval@(icl_says@(icl_impl@(icl_princ@admin)@icl_false)@(icl_atom@deletfile1))    thf(ax1, axiom)
iclval@(icl_says@(icl_princ@admin)@(icl_says@(icl_impl@(icl_princ@bob)@(icl_princ@admin))@(icl_atom@deletfile1)))    thf(ax2, axiom)
iclval@(icl_says@(icl_princ@bob)@(icl_atom@deletfile1))    thf(ax3, axiom)
iclval@(icl_atom@deletfile1)    thf(ex3, conjecture)

```

**SWV441<sup>^</sup>1.p** (K says (A => B)) => (K says A) => (K says B) in BL

```

include('Axioms/LCL008^0.ax')
include('Axioms/LCL009^0.ax')
include('Axioms/SWV010^0.ax')
∀k: individuals, a: $i → $o, b: $i → $o: (bl_valid@(bl_impl@(bl_says@k@(bl_impl@a@b))@(bl_impl@(bl_says@k@a)@(bl_says@k@a))))    thf(bl_id, conjecture)

```

**SWV442<sup>^</sup>1.p** A => A in BL

```

include('Axioms/LCL008^0.ax')
include('Axioms/LCL009^0.ax')
include('Axioms/SWV010^0.ax')
∀a: $i → $o: (bl_valid@(bl_impl@(bl_atom@a)@(bl_atom@a)))    thf(bl_id, conjecture)

```

**SWV443<sup>^</sup>1.p** (K says A) => (K says A) in BL

```

include('Axioms/LCL008^0.ax')
include('Axioms/LCL009^0.ax')
include('Axioms/SWV010^0.ax')
∀k: individuals, a: $i → $o: (bl_valid@(bl_impl@(bl_says@k@(bl_atom@a)@(bl_says@k@(bl_atom@a))))    thf(bl_id2, conjecture)

```

**SWV444<sup>^</sup>1.p** (loca says A) => (K says A) in BL

```

include('Axioms/LCL008^0.ax')
include('Axioms/LCL009^0.ax')
include('Axioms/SWV010^0.ax')
∀k: individuals, a: $i → $o: (bl_valid@(bl_impl@(bl_says@loca@(bl_atom@a)@(bl_says@k@(bl_atom@a))))    thf(bl_strength, conjecture)

```

**SWV445<sup>^</sup>1.p** (K says K says A) => (K says A) in BL

```

include('Axioms/LCL008^0.ax')
include('Axioms/LCL009^0.ax')
include('Axioms/SWV010^0.ax')
∀k: individuals, a: $i → $o: (bl_valid@(bl_impl@(bl_says@k@(bl_says@k@(bl_atom@a)@(bl_says@k@(bl_atom@a))))    thf(bl_id3, conjecture)

```

**SWV446<sup>^</sup>1.p** K says ((K says A) => A) in BL

```

include('Axioms/LCL008^0.ax')
include('Axioms/LCL009^0.ax')
include('Axioms/SWV010^0.ax')
∀k: individuals, a: $i → $o: (bl_valid@(bl_says@k@(bl_impl@(bl_says@k@(bl_atom@a)@(bl_atom@a))))    thf(bl_conceit, conjecture)

```

**SWV447<sup>^</sup>1.p** Nipkow's simple map-cons problem

```

nil: $i    thf(nil_type, type)
cons: $i → $i → $i    thf(cons_type, type)
map: ($i → $i) → $i → $i    thf(map_type, type)
∀f: $i → $i: (map@f@nil) = nil    thf(ax1, axiom)
∀f: $i → $i, x: $i, y: $i: (map@f@(cons@x@y)) = (cons@(f@x)@(map@f@y))    thf(ax2, axiom)
∀a: $i: (map@λx: $i: x@(cons@a@nil)) = (cons@a@nil)    thf(test, conjecture)

```

**SWV449+1.p** Establishing that there cannot be two leaders, part i26\_p30

```

include('Axioms/SWV011+0.ax')
∀v, w, x, y: ((∀z, pid0: (setIn(pid0, alive) ⇒ ¬elem(m_Down(pid0), queue(host(z)))) and ∀z, pid0: (elem(m_Down(pid0), queue(host(z))) ⇒ ¬setIn(pid0, alive)) and ∀z, pid0: (elem(m_Down(pid0), queue(host(z))) ⇒ host(pid0) ≠ host(z)) and ∀z, pid0: (elem(m_Halt(pid0), queue(host(z))) ⇒ ¬setIn(pid0, alive)))

```





$\text{cons}(\text{m\_Down}(y), v) \Rightarrow (\text{setIn}(x, \text{alive}) \Rightarrow (\neg \text{host}(x) \leq \text{host}(y) \Rightarrow (((\text{index}(\text{ldr}, \text{host}(x)) = \text{host}(y) \text{ and } \text{index}(\text{status}, \text{host}(x)) = \text{wait} \text{ and } \text{host}(y) = \text{host}(\text{index}(\text{elid}, \text{host}(x)))) \Rightarrow ((\forall z: (\text{host}(x) = \text{host}(z) \Rightarrow z \leq w) \text{ and } \neg \text{setIn}(w, \text{pids}) \text{ and } \text{host}(x) = \text{host}(w)) \Rightarrow (\text{host}(w) \neq s(0) \Rightarrow \forall z: (\text{host}(x) \neq \text{host}(z) \Rightarrow \forall x_0, y_0: (\text{host}(x) = \text{host}(y_0) \Rightarrow \forall z_0: (((z \neq x \text{ and } \text{setIn}(z, \text{alive})) \text{ or } z = w) \text{ and } ((y_0 \neq x \text{ and } \text{setIn}(y_0, \text{alive})) \text{ or } y_0 = w) \text{ and } \text{host}(y_0) \neq \text{host}(z) \text{ and } \text{host}(x_0) = \text{host}(z) \text{ and } \text{host}(z_0) = \text{host}(y_0)) \Rightarrow \neg \text{elem}(\text{m\_Down}(x_0), v) \text{ and } \text{elem}(\text{m\_Down}(z_0), v))))))))))$

**SWV454+1.p** Establishing that there cannot be two leaders, part i26\_p250

`include('Axioms/SWV011+0.ax')`

$\forall v, w, x, y: ((\forall z, \text{pid}_0: (\text{setIn}(\text{pid}_0, \text{alive}) \Rightarrow \neg \text{elem}(\text{m\_Down}(\text{pid}_0), \text{queue}(\text{host}(z)))) \text{ and } \forall z, \text{pid}_0: (\text{elem}(\text{m\_Down}(\text{pid}_0), \text{queue}(\text{host}(z))) \Rightarrow \neg \text{setIn}(\text{pid}_0, \text{alive})) \text{ and } \forall z, \text{pid}_0: (\text{elem}(\text{m\_Halt}(\text{pid}_0), \text{queue}(\text{host}(z))) \Rightarrow \neg \text{host}(z) \leq \text{host}(\text{pid}_0)) \text{ and } \forall z, \text{pid}_{20}, \text{pid}_0: (\text{elem}(\text{m\_Ack}(\text{pid}_0, z), \text{queue}(\text{host}(\text{pid}_{20}))) \Rightarrow \neg \text{host}(z) \leq \text{host}(\text{pid}_0)) \text{ and } \forall z, \text{pid}_0: (\text{elem}(\text{m\_Down}(\text{pid}_0), \text{queue}(\text{host}(z))) \Rightarrow \neg \text{setIn}(\text{pid}_0, \text{alive})) \text{ and } \forall z, \text{pid}_0: ((\text{pid}_0 \neq z \text{ and } \text{host}(\text{pid}_0) = \text{host}(z)) \Rightarrow (\neg \text{setIn}(z, \text{alive}) \text{ or } \neg \text{setIn}(\text{pid}_0, \text{alive}))) \text{ and } \forall z, \text{pid}_{30}, \text{pid}_{20}, \text{pid}_0: ((\text{host}(\text{pid}_{20}) \neq \text{host}(z) \text{ and } \text{setIn}(z, \text{alive}) \text{ and } \text{setIn}(\text{pid}_{20}, \text{alive}) \text{ and } \text{host}(\text{pid}_0) = \text{host}(\text{pid}_{20})) \Rightarrow \neg \text{elem}(\text{m\_Down}(\text{pid}_0), \text{queue}(\text{host}(z))) \text{ and } \text{elem}(\text{m\_Down}(\text{pid}_{30}), \text{queue}(\text{host}(\text{pid}_{20})))))) \Rightarrow (\text{setIn}(x, \text{alive}) \Rightarrow (\neg \text{host}(x) \leq \text{host}(y) \Rightarrow (\neg (\text{index}(\text{ldr}, \text{host}(x)) = \text{host}(y) \text{ and } \text{index}(\text{status}, \text{host}(x)) = \text{wait} \text{ and } \text{host}(y) = \text{host}(\text{index}(\text{elid}, \text{host}(x)))) \Rightarrow ((\forall z: ((\neg \text{host}(x) \leq z \text{ and } s(0) \leq z) \Rightarrow (\text{setIn}(z, \text{index}(\text{down}, \text{host}(x))) \text{ or } z = \text{host}(y))) \text{ and } \text{index}(\text{status}, \text{host}(x)) = \text{elec}_1) \Rightarrow (\neg \text{nbr\_proc} \leq \text{host}(x) \Rightarrow \forall z: (s(\text{host}(x)) \neq \text{host}(z) \Rightarrow (\text{host}(x) = \text{host}(z) \Rightarrow \forall w_0, x_0: (s(\text{host}(x)) \neq \text{host}(x_0) \Rightarrow (\text{host}(x) \neq \text{host}(x_0) \Rightarrow \forall y_0: ((\text{host}(x_0) \neq \text{host}(z) \text{ and } \text{setIn}(z, \text{alive}) \text{ and } \text{setIn}(x_0, \text{alive}) \text{ and } \text{host}(w_0) = \text{host}(z) \text{ and } \text{host}(y_0) = \text{host}(x_0)) \Rightarrow \neg \text{elem}(\text{m\_Down}(y_0), v) \text{ and } \text{elem}(\text{m\_Down}(w_0), \text{queue}(\text{host}(x_0)))))))))))))) \text{ fof}(\text{conj}, \text{conjecture})$

**SWV455+1.p** Establishing that there cannot be two leaders, part i26\_p257

`include('Axioms/SWV011+0.ax')`

$\forall v, w, x, y: ((\forall z, \text{pid}_0: (\text{setIn}(\text{pid}_0, \text{alive}) \Rightarrow \neg \text{elem}(\text{m\_Down}(\text{pid}_0), \text{queue}(\text{host}(z)))) \text{ and } \forall z, \text{pid}_0: (\text{elem}(\text{m\_Down}(\text{pid}_0), \text{queue}(\text{host}(z))) \Rightarrow \neg \text{setIn}(\text{pid}_0, \text{alive})) \text{ and } \forall z, \text{pid}_0: (\text{elem}(\text{m\_Halt}(\text{pid}_0), \text{queue}(\text{host}(z))) \Rightarrow \neg \text{host}(z) \leq \text{host}(\text{pid}_0)) \text{ and } \forall z, \text{pid}_{20}, \text{pid}_0: (\text{elem}(\text{m\_Ack}(\text{pid}_0, z), \text{queue}(\text{host}(\text{pid}_{20}))) \Rightarrow \neg \text{host}(z) \leq \text{host}(\text{pid}_0)) \text{ and } \forall z, \text{pid}_0: (\text{elem}(\text{m\_Down}(\text{pid}_0), \text{queue}(\text{host}(z))) \Rightarrow \neg \text{setIn}(\text{pid}_0, \text{alive})) \text{ and } \forall z, \text{pid}_0: ((\text{pid}_0 \neq z \text{ and } \text{host}(\text{pid}_0) = \text{host}(z)) \Rightarrow (\neg \text{setIn}(z, \text{alive}) \text{ or } \neg \text{setIn}(\text{pid}_0, \text{alive}))) \text{ and } \forall z, \text{pid}_{30}, \text{pid}_{20}, \text{pid}_0: ((\text{host}(\text{pid}_{20}) \neq \text{host}(z) \text{ and } \text{setIn}(z, \text{alive}) \text{ and } \text{setIn}(\text{pid}_{20}, \text{alive}) \text{ and } \text{host}(\text{pid}_0) = \text{host}(\text{pid}_{20})) \Rightarrow \neg \text{elem}(\text{m\_Down}(\text{pid}_0), \text{queue}(\text{host}(z))) \text{ and } \text{elem}(\text{m\_Down}(\text{pid}_{30}), \text{queue}(\text{host}(\text{pid}_{20})))))) \Rightarrow (\text{setIn}(x, \text{alive}) \Rightarrow (\neg \text{host}(x) \leq \text{host}(y) \Rightarrow (\neg (\text{index}(\text{ldr}, \text{host}(x)) = \text{host}(y) \text{ and } \text{index}(\text{status}, \text{host}(x)) = \text{wait} \text{ and } \text{host}(y) = \text{host}(\text{index}(\text{elid}, \text{host}(x)))) \Rightarrow (\neg \forall z: ((\neg \text{host}(x) \leq z \text{ and } s(0) \leq z) \Rightarrow (\text{setIn}(z, \text{index}(\text{down}, \text{host}(x))) \text{ or } z = \text{host}(y))) \text{ and } \text{index}(\text{status}, \text{host}(x)) = \text{elec}_1) \Rightarrow \forall z: (\text{host}(x) \neq \text{host}(z) \Rightarrow \forall w_0, x_0: (\text{host}(x) = \text{host}(x_0) \Rightarrow \forall y_0: ((\text{host}(x_0) \neq \text{host}(z) \text{ and } \text{setIn}(z, \text{alive}) \text{ and } \text{setIn}(x_0, \text{alive}) \text{ and } \text{host}(w_0) = \text{host}(z) \text{ and } \text{host}(y_0) = \text{host}(x_0)) \Rightarrow \neg \text{elem}(\text{m\_Down}(w_0), v) \text{ and } \text{elem}(\text{m\_Down}(y_0), \text{queue}(\text{host}(z)))))))))) \text{ fof}(\text{conj}, \text{conjecture})$

**SWV456+1.p** Establishing that there cannot be two leaders, part i27\_p134

`include('Axioms/SWV011+0.ax')`

$\forall v, w, x, y: ((\forall z, \text{pid}_0: (\text{elem}(\text{m\_Down}(\text{pid}_0), \text{queue}(\text{host}(z))) \Rightarrow \neg \text{setIn}(\text{pid}_0, \text{alive})) \text{ and } \forall z, \text{pid}_0: (\text{elem}(\text{m\_Down}(\text{pid}_0), \text{queue}(\text{host}(z))) \Rightarrow \text{host}(\text{pid}_0) \neq \text{host}(z)) \text{ and } \forall z, \text{pid}_0: (\text{elem}(\text{m\_Halt}(\text{pid}_0), \text{queue}(\text{host}(z))) \Rightarrow \neg \text{host}(z) \leq \text{host}(\text{pid}_0)) \text{ and } \forall z, \text{pid}_{20}, \text{pid}_0: (\text{elem}(\text{m\_Ack}(\text{pid}_0, z), \text{queue}(\text{host}(\text{pid}_{20}))) \Rightarrow \neg \text{host}(z) \leq \text{host}(\text{pid}_0)) \text{ and } \forall z, \text{pid}_0: ((\neg \text{setIn}(z, \text{alive}) \text{ and } \text{pid}_0 \leq z \text{ and } \text{host}(\text{pid}_0) = \text{host}(z)) \Rightarrow \neg \text{setIn}(\text{pid}_0, \text{alive})) \text{ and } \forall z, \text{pid}_0: ((\text{pid}_0 \neq z \text{ and } \text{host}(\text{pid}_0) = \text{host}(z)) \Rightarrow (\neg \text{setIn}(z, \text{alive}) \text{ or } \neg \text{setIn}(\text{pid}_0, \text{alive}))) \text{ and } \forall z, \text{pid}_{30}, \text{pid}_{20}, \text{pid}_0: ((\text{host}(\text{pid}_{20}) \neq \text{host}(z) \text{ and } \text{setIn}(z, \text{alive}) \text{ and } \text{setIn}(\text{pid}_{20}, \text{alive}) \text{ and } \text{host}(\text{pid}_{30}) = \text{host}(z) \text{ and } \text{host}(\text{pid}_0) = \text{host}(\text{pid}_{20})) \Rightarrow \neg \text{elem}(\text{m\_Down}(\text{pid}_0), \text{queue}(\text{host}(z))) \text{ and } \text{elem}(\text{m\_Down}(\text{pid}_{30}), \text{queue}(\text{host}(\text{pid}_{20})))))) \Rightarrow (\text{setIn}(x, \text{alive}) \Rightarrow (\neg \text{host}(x) \leq \text{host}(y) \Rightarrow (((\text{index}(\text{ldr}, \text{host}(x)) = \text{host}(y) \text{ and } \text{index}(\text{status}, \text{host}(x)) = \text{wait} \text{ and } \text{host}(y) = \text{host}(\text{index}(\text{elid}, \text{host}(x)))) \Rightarrow ((\forall z: (\text{host}(x) = \text{host}(z) \Rightarrow z \leq w) \text{ and } \neg \text{setIn}(w, \text{pids}) \text{ and } \text{host}(x) = \text{host}(w)) \Rightarrow (\text{host}(w) \neq s(0) \Rightarrow \forall z: (\text{host}(x) = \text{host}(z) \Rightarrow \forall x_0, y_0: (\text{host}(w) \neq \text{host}(y_0) \Rightarrow (\text{host}(x) \neq \text{host}(y_0) \Rightarrow \forall z_0: (((z \neq x \text{ and } \text{setIn}(z, \text{alive})) \text{ or } z = w) \text{ and } ((y_0 \neq x \text{ and } \text{setIn}(y_0, \text{alive})) \text{ or } y_0 = w) \text{ and } \text{host}(y_0) \neq \text{host}(z) \text{ and } \text{host}(x_0) = \text{host}(z) \text{ and } \text{host}(z_0) = \text{host}(y_0)) \Rightarrow \neg \text{elem}(\text{m\_Down}(z_0), v) \text{ and } \text{setIn}(\text{host}(x_0), \text{index}(\text{down}, \text{host}(y_0)))))))))) \text{ fof}(\text{conj}, \text{conjecture})$

**SWV486+1.p** Matrix is lower-triangular

$\forall i, j: (\text{int\_leq}(i, j) \iff (\text{int\_less}(i, j) \text{ or } i = j)) \quad \text{fof}(\text{int\_leq}, \text{axiom})$

$\forall i, j, k: ((\text{int\_less}(i, j) \text{ and } \text{int\_less}(j, k)) \Rightarrow \text{int\_less}(i, k)) \quad \text{fof}(\text{int\_less\_transitive}, \text{axiom})$

$\forall i, j: (\text{int\_less}(i, j) \Rightarrow i \neq j) \quad \text{fof}(\text{int\_less\_irreflexive}, \text{axiom})$

$\forall i, j: (\text{int\_less}(i, j) \text{ or } \text{int\_leq}(j, i)) \quad \text{fof}(\text{int\_less\_total}, \text{axiom})$

$\text{int\_less}(\text{int\_zero}, \text{int\_one}) \quad \text{fof}(\text{int\_zero\_one}, \text{axiom})$

$\forall i, j: i + j = j + i \quad \text{fof}(\text{plus\_commutative}, \text{axiom})$

$\forall i: i + \text{int\_zero} = i \quad \text{fof}(\text{plus\_zero}, \text{axiom})$

$\forall i_1, j_1, i_2, j_2: ((\text{int\_less}(i_1, j_1) \text{ and } \text{int\_leq}(i_2, j_2)) \Rightarrow \text{int\_leq}(i_1 + i_2, j_1 + j_2)) \quad \text{fof}(\text{plus\_and\_order}_1, \text{axiom})$

$\forall i, j: (\text{int\_less}(i, j) \iff \exists k: (i + k = j \text{ and } \text{int\_less}(\text{int\_zero}, k))) \quad \text{fof}(\text{plus\_and\_inverse}, \text{axiom})$

$\forall i: (\text{int\_less}(\text{int\_zero}, i) \iff \text{int\_leq}(\text{int\_one}, i)) \quad \text{fof}(\text{one\_successor\_of\_zero}, \text{axiom})$

















$a_{820} = \text{store}(a_{818}, i_1, e_{819}) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $a_{821} = \text{store}(a_{820}, i_1, e_{819}) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $a_{823} = \text{store}(a_{821}, i_5, e_{822}) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $a_{825} = \text{store}(a_{823}, i_2, e_{824}) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $a_{827} = \text{store}(a_{825}, i_5, e_{826}) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $a_{829} = \text{store}(a_{827}, i_2, e_{828}) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{782} = \text{select}(a_1, i_3) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{784} = \text{select}(a_1, i_4) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{786} = \text{select}(a_{785}, i_1) \quad \text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{788} = \text{select}(a_{785}, i_2) \quad \text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $e_{790} = \text{select}(a_{789}, i_5) \quad \text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $e_{792} = \text{select}(a_{789}, i_0) \quad \text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{794} = \text{select}(a_{793}, i_5) \quad \text{cnf}(\text{hyp}_{32}, \text{hypothesis})$   
 $e_{796} = \text{select}(a_{793}, i_2) \quad \text{cnf}(\text{hyp}_{33}, \text{hypothesis})$   
 $e_{798} = \text{select}(a_{797}, i_1) \quad \text{cnf}(\text{hyp}_{34}, \text{hypothesis})$   
 $e_{801} = \text{select}(a_{800}, i_2) \quad \text{cnf}(\text{hyp}_{35}, \text{hypothesis})$   
 $e_{803} = \text{select}(a_{800}, i_5) \quad \text{cnf}(\text{hyp}_{36}, \text{hypothesis})$   
 $e_{805} = \text{select}(a_{804}, i_2) \quad \text{cnf}(\text{hyp}_{37}, \text{hypothesis})$   
 $e_{807} = \text{select}(a_{804}, i_5) \quad \text{cnf}(\text{hyp}_{38}, \text{hypothesis})$   
 $e_{811} = \text{select}(a_{810}, i_0) \quad \text{cnf}(\text{hyp}_{39}, \text{hypothesis})$   
 $e_{813} = \text{select}(a_{810}, i_5) \quad \text{cnf}(\text{hyp}_{40}, \text{hypothesis})$   
 $e_{815} = \text{select}(a_{814}, i_2) \quad \text{cnf}(\text{hyp}_{41}, \text{hypothesis})$   
 $e_{817} = \text{select}(a_{814}, i_5) \quad \text{cnf}(\text{hyp}_{42}, \text{hypothesis})$   
 $e_{819} = \text{select}(a_{818}, i_1) \quad \text{cnf}(\text{hyp}_{43}, \text{hypothesis})$   
 $e_{822} = \text{select}(a_{821}, i_2) \quad \text{cnf}(\text{hyp}_{44}, \text{hypothesis})$   
 $e_{824} = \text{select}(a_{821}, i_5) \quad \text{cnf}(\text{hyp}_{45}, \text{hypothesis})$   
 $e_{826} = \text{select}(a_{825}, i_2) \quad \text{cnf}(\text{hyp}_{46}, \text{hypothesis})$   
 $e_{828} = \text{select}(a_{825}, i_5) \quad \text{cnf}(\text{hyp}_{47}, \text{hypothesis})$   
 $a_{808} \neq a_{829} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV534-1.004.p** Swap elements (t1\_np\_sf\_ai\_00004)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $a_{418} = \text{store}(a_1, i_1, e_{417}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{419} = \text{store}(a_{418}, i_1, e_{417}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{421} = \text{store}(a_{419}, i_0, e_{420}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{423} = \text{store}(a_{421}, i_3, e_{422}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{425} = \text{store}(a_{423}, i_3, e_{424}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{427} = \text{store}(a_{425}, i_2, e_{426}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{429} = \text{store}(a_{427}, i_2, e_{428}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{431} = \text{store}(a_{429}, i_0, e_{430}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{432} = \text{store}(a_{419}, i_3, e_{422}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{433} = \text{store}(a_{432}, i_0, e_{420}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{435} = \text{store}(a_{433}, i_3, e_{434}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{437} = \text{store}(a_{435}, i_2, e_{436}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{439} = \text{store}(a_{437}, i_0, e_{438}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{441} = \text{store}(a_{439}, i_3, e_{440}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{417} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{420} = \text{select}(a_{419}, i_3) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{422} = \text{select}(a_{419}, i_0) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{424} = \text{select}(a_{423}, i_2) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $e_{426} = \text{select}(a_{423}, i_3) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{428} = \text{select}(a_{427}, i_0) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{430} = \text{select}(a_{427}, i_2) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{434} = \text{select}(a_{433}, i_2) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{436} = \text{select}(a_{433}, i_3) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{438} = \text{select}(a_{437}, i_3) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{440} = \text{select}(a_{437}, i_0) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$

$a_{431} \neq a_{441}$        $\text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV534-1.007.p** Swap elements (t1\_np\_sf\_ai\_00007)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e$        $\text{cnf}(a_1, \text{axiom})$   
 $i = j$  or  $\text{select}(\text{store}(a, i, e), j) = \text{select}(a, j)$        $\text{cnf}(a_2, \text{axiom})$   
 $a_{785} = \text{store}(a_1, i_4, e_{784})$        $\text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{787} = \text{store}(a_{785}, i_3, e_{786})$        $\text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{789} = \text{store}(a_{787}, i_2, e_{788})$        $\text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{791} = \text{store}(a_{789}, i_1, e_{790})$        $\text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{793} = \text{store}(a_{791}, i_0, e_{792})$        $\text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{795} = \text{store}(a_{793}, i_5, e_{794})$        $\text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{797} = \text{store}(a_{795}, i_2, e_{796})$        $\text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{799} = \text{store}(a_{797}, i_5, e_{798})$        $\text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{801} = \text{store}(a_{799}, i_1, e_{800})$        $\text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{802} = \text{store}(a_{801}, i_1, e_{800})$        $\text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{804} = \text{store}(a_{802}, i_5, e_{803})$        $\text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{806} = \text{store}(a_{804}, i_2, e_{805})$        $\text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{808} = \text{store}(a_{806}, i_5, e_{807})$        $\text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{810} = \text{store}(a_{808}, i_2, e_{809})$        $\text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $a_{811} = \text{store}(a_{787}, i_1, e_{790})$        $\text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $a_{812} = \text{store}(a_{811}, i_2, e_{788})$        $\text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{814} = \text{store}(a_{812}, i_5, e_{813})$        $\text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_{816} = \text{store}(a_{814}, i_0, e_{815})$        $\text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $a_{818} = \text{store}(a_{816}, i_5, e_{817})$        $\text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{820} = \text{store}(a_{818}, i_2, e_{819})$        $\text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $a_{822} = \text{store}(a_{820}, i_1, e_{821})$        $\text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $a_{823} = \text{store}(a_{822}, i_1, e_{821})$        $\text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $a_{825} = \text{store}(a_{823}, i_5, e_{824})$        $\text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $a_{827} = \text{store}(a_{825}, i_2, e_{826})$        $\text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $a_{829} = \text{store}(a_{827}, i_6, e_{828})$        $\text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $a_{831} = \text{store}(a_{829}, i_2, e_{830})$        $\text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{784} = \text{select}(a_1, i_3)$        $\text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{786} = \text{select}(a_1, i_4)$        $\text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{788} = \text{select}(a_{787}, i_1)$        $\text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{790} = \text{select}(a_{787}, i_2)$        $\text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $e_{792} = \text{select}(a_{791}, i_5)$        $\text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $e_{794} = \text{select}(a_{791}, i_0)$        $\text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{796} = \text{select}(a_{795}, i_5)$        $\text{cnf}(\text{hyp}_{32}, \text{hypothesis})$   
 $e_{798} = \text{select}(a_{795}, i_2)$        $\text{cnf}(\text{hyp}_{33}, \text{hypothesis})$   
 $e_{800} = \text{select}(a_{799}, i_1)$        $\text{cnf}(\text{hyp}_{34}, \text{hypothesis})$   
 $e_{803} = \text{select}(a_{802}, i_2)$        $\text{cnf}(\text{hyp}_{35}, \text{hypothesis})$   
 $e_{805} = \text{select}(a_{802}, i_5)$        $\text{cnf}(\text{hyp}_{36}, \text{hypothesis})$   
 $e_{807} = \text{select}(a_{806}, i_2)$        $\text{cnf}(\text{hyp}_{37}, \text{hypothesis})$   
 $e_{809} = \text{select}(a_{806}, i_5)$        $\text{cnf}(\text{hyp}_{38}, \text{hypothesis})$   
 $e_{813} = \text{select}(a_{812}, i_0)$        $\text{cnf}(\text{hyp}_{39}, \text{hypothesis})$   
 $e_{815} = \text{select}(a_{812}, i_5)$        $\text{cnf}(\text{hyp}_{40}, \text{hypothesis})$   
 $e_{817} = \text{select}(a_{816}, i_2)$        $\text{cnf}(\text{hyp}_{41}, \text{hypothesis})$   
 $e_{819} = \text{select}(a_{816}, i_5)$        $\text{cnf}(\text{hyp}_{42}, \text{hypothesis})$   
 $e_{821} = \text{select}(a_{820}, i_1)$        $\text{cnf}(\text{hyp}_{43}, \text{hypothesis})$   
 $e_{824} = \text{select}(a_{823}, i_2)$        $\text{cnf}(\text{hyp}_{44}, \text{hypothesis})$   
 $e_{826} = \text{select}(a_{823}, i_5)$        $\text{cnf}(\text{hyp}_{45}, \text{hypothesis})$   
 $e_{828} = \text{select}(a_{827}, i_2)$        $\text{cnf}(\text{hyp}_{46}, \text{hypothesis})$   
 $e_{830} = \text{select}(a_{827}, i_6)$        $\text{cnf}(\text{hyp}_{47}, \text{hypothesis})$   
 $a_{810} \neq a_{831}$        $\text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV537-1.004.p** Swap elements (t1\_pp\_sf\_ai\_00004)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $a_{466} = \text{store}(a_1, i_1, e_{465}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{467} = \text{store}(a_{466}, i_1, e_{465}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{469} = \text{store}(a_{467}, i_0, e_{468}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{471} = \text{store}(a_{469}, i_3, e_{470}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{473} = \text{store}(a_{471}, i_3, e_{472}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{475} = \text{store}(a_{473}, i_2, e_{474}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{477} = \text{store}(a_{475}, i_2, e_{476}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{479} = \text{store}(a_{477}, i_0, e_{478}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{480} = \text{store}(a_{467}, i_3, e_{470}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{481} = \text{store}(a_{480}, i_0, e_{468}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{483} = \text{store}(a_{481}, i_3, e_{482}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{485} = \text{store}(a_{483}, i_2, e_{484}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{487} = \text{store}(a_{485}, i_0, e_{486}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{489} = \text{store}(a_{487}, i_2, e_{488}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{465} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{468} = \text{select}(a_{467}, i_3) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{470} = \text{select}(a_{467}, i_0) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{472} = \text{select}(a_{471}, i_2) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $e_{474} = \text{select}(a_{471}, i_3) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{476} = \text{select}(a_{475}, i_0) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{478} = \text{select}(a_{475}, i_2) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{482} = \text{select}(a_{481}, i_2) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{484} = \text{select}(a_{481}, i_3) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{486} = \text{select}(a_{485}, i_2) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{488} = \text{select}(a_{485}, i_0) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{491} = \text{select}(a_{479}, i_{490}) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{492} = \text{select}(a_{489}, i_{490}) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $i_{490} = \text{sk}(a_{479}, a_{489}) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{491} \neq e_{492} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV537-1.007.p** Swap elements (t1\_pp\_sf\_ai\_00007)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $a_{834} = \text{store}(a_1, i_4, e_{833}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{836} = \text{store}(a_{834}, i_3, e_{835}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{838} = \text{store}(a_{836}, i_2, e_{837}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{840} = \text{store}(a_{838}, i_1, e_{839}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{842} = \text{store}(a_{840}, i_0, e_{841}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{844} = \text{store}(a_{842}, i_5, e_{843}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{846} = \text{store}(a_{844}, i_2, e_{845}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{848} = \text{store}(a_{846}, i_5, e_{847}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{850} = \text{store}(a_{848}, i_1, e_{849}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{851} = \text{store}(a_{850}, i_1, e_{849}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{853} = \text{store}(a_{851}, i_5, e_{852}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{855} = \text{store}(a_{853}, i_2, e_{854}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{857} = \text{store}(a_{855}, i_5, e_{856}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{859} = \text{store}(a_{857}, i_2, e_{858}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $a_{860} = \text{store}(a_{836}, i_1, e_{839}) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $a_{861} = \text{store}(a_{860}, i_2, e_{837}) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{863} = \text{store}(a_{861}, i_5, e_{862}) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_{865} = \text{store}(a_{863}, i_0, e_{864}) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $a_{867} = \text{store}(a_{865}, i_5, e_{866}) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{869} = \text{store}(a_{867}, i_2, e_{868}) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $a_{871} = \text{store}(a_{869}, i_1, e_{870}) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $a_{872} = \text{store}(a_{871}, i_1, e_{870}) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $a_{874} = \text{store}(a_{872}, i_5, e_{873}) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$

$a_{876} = \text{store}(a_{874}, i_2, e_{875}) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $a_{878} = \text{store}(a_{876}, i_5, e_{877}) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $a_{880} = \text{store}(a_{878}, i_2, e_{879}) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{833} = \text{select}(a_1, i_3) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{835} = \text{select}(a_1, i_4) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{837} = \text{select}(a_{836}, i_1) \quad \text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{839} = \text{select}(a_{836}, i_2) \quad \text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $e_{841} = \text{select}(a_{840}, i_5) \quad \text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $e_{843} = \text{select}(a_{840}, i_0) \quad \text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{845} = \text{select}(a_{844}, i_5) \quad \text{cnf}(\text{hyp}_{32}, \text{hypothesis})$   
 $e_{847} = \text{select}(a_{844}, i_2) \quad \text{cnf}(\text{hyp}_{33}, \text{hypothesis})$   
 $e_{849} = \text{select}(a_{848}, i_1) \quad \text{cnf}(\text{hyp}_{34}, \text{hypothesis})$   
 $e_{852} = \text{select}(a_{851}, i_2) \quad \text{cnf}(\text{hyp}_{35}, \text{hypothesis})$   
 $e_{854} = \text{select}(a_{851}, i_5) \quad \text{cnf}(\text{hyp}_{36}, \text{hypothesis})$   
 $e_{856} = \text{select}(a_{855}, i_2) \quad \text{cnf}(\text{hyp}_{37}, \text{hypothesis})$   
 $e_{858} = \text{select}(a_{855}, i_5) \quad \text{cnf}(\text{hyp}_{38}, \text{hypothesis})$   
 $e_{862} = \text{select}(a_{861}, i_0) \quad \text{cnf}(\text{hyp}_{39}, \text{hypothesis})$   
 $e_{864} = \text{select}(a_{861}, i_5) \quad \text{cnf}(\text{hyp}_{40}, \text{hypothesis})$   
 $e_{866} = \text{select}(a_{865}, i_2) \quad \text{cnf}(\text{hyp}_{41}, \text{hypothesis})$   
 $e_{868} = \text{select}(a_{865}, i_5) \quad \text{cnf}(\text{hyp}_{42}, \text{hypothesis})$   
 $e_{870} = \text{select}(a_{869}, i_1) \quad \text{cnf}(\text{hyp}_{43}, \text{hypothesis})$   
 $e_{873} = \text{select}(a_{872}, i_2) \quad \text{cnf}(\text{hyp}_{44}, \text{hypothesis})$   
 $e_{875} = \text{select}(a_{872}, i_5) \quad \text{cnf}(\text{hyp}_{45}, \text{hypothesis})$   
 $e_{877} = \text{select}(a_{876}, i_2) \quad \text{cnf}(\text{hyp}_{46}, \text{hypothesis})$   
 $e_{879} = \text{select}(a_{876}, i_5) \quad \text{cnf}(\text{hyp}_{47}, \text{hypothesis})$   
 $e_{882} = \text{select}(a_{859}, i_{881}) \quad \text{cnf}(\text{hyp}_{48}, \text{hypothesis})$   
 $e_{883} = \text{select}(a_{880}, i_{881}) \quad \text{cnf}(\text{hyp}_{49}, \text{hypothesis})$   
 $i_{881} = \text{sk}(a_{859}, a_{880}) \quad \text{cnf}(\text{hyp}_{50}, \text{hypothesis})$   
 $e_{882} \neq e_{883} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

#### **SWV538-1.004.p** Swap elements (t1\_pp\_sf\_ai\_00004)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $a_{469} = \text{store}(a_1, i_1, e_{468}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{470} = \text{store}(a_{469}, i_1, e_{468}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{472} = \text{store}(a_{470}, i_0, e_{471}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{474} = \text{store}(a_{472}, i_3, e_{473}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{476} = \text{store}(a_{474}, i_3, e_{475}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{478} = \text{store}(a_{476}, i_2, e_{477}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{480} = \text{store}(a_{478}, i_2, e_{479}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{482} = \text{store}(a_{480}, i_0, e_{481}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{483} = \text{store}(a_{470}, i_3, e_{473}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{484} = \text{store}(a_{483}, i_0, e_{471}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{486} = \text{store}(a_{484}, i_3, e_{485}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{488} = \text{store}(a_{486}, i_2, e_{487}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{490} = \text{store}(a_{488}, i_0, e_{489}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{492} = \text{store}(a_{490}, i_3, e_{491}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{468} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{471} = \text{select}(a_{470}, i_3) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{473} = \text{select}(a_{470}, i_0) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{475} = \text{select}(a_{474}, i_2) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $e_{477} = \text{select}(a_{474}, i_3) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{479} = \text{select}(a_{478}, i_0) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{481} = \text{select}(a_{478}, i_2) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{485} = \text{select}(a_{484}, i_2) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{487} = \text{select}(a_{484}, i_3) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{489} = \text{select}(a_{488}, i_3) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{491} = \text{select}(a_{488}, i_0) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$

$e_{494} = \text{select}(a_{482}, i_{493}) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{495} = \text{select}(a_{492}, i_{493}) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $i_{493} = \text{sk}(a_{482}, a_{492}) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{494} \neq e_{495} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV538-1.007.p** Swap elements (t1\_pp\_sf\_ai\_00007)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $a_{836} = \text{store}(a_1, i_4, e_{835}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{838} = \text{store}(a_{836}, i_3, e_{837}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{840} = \text{store}(a_{838}, i_2, e_{839}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{842} = \text{store}(a_{840}, i_1, e_{841}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{844} = \text{store}(a_{842}, i_0, e_{843}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{846} = \text{store}(a_{844}, i_5, e_{845}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{848} = \text{store}(a_{846}, i_2, e_{847}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{850} = \text{store}(a_{848}, i_5, e_{849}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{852} = \text{store}(a_{850}, i_1, e_{851}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{853} = \text{store}(a_{852}, i_1, e_{851}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{855} = \text{store}(a_{853}, i_5, e_{854}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{857} = \text{store}(a_{855}, i_2, e_{856}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{859} = \text{store}(a_{857}, i_5, e_{858}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{861} = \text{store}(a_{859}, i_2, e_{860}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $a_{862} = \text{store}(a_{838}, i_1, e_{841}) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $a_{863} = \text{store}(a_{862}, i_2, e_{839}) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{865} = \text{store}(a_{863}, i_5, e_{864}) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_{867} = \text{store}(a_{865}, i_0, e_{866}) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $a_{869} = \text{store}(a_{867}, i_5, e_{868}) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{871} = \text{store}(a_{869}, i_2, e_{870}) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $a_{873} = \text{store}(a_{871}, i_1, e_{872}) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $a_{874} = \text{store}(a_{873}, i_1, e_{872}) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $a_{876} = \text{store}(a_{874}, i_5, e_{875}) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $a_{878} = \text{store}(a_{876}, i_2, e_{877}) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $a_{880} = \text{store}(a_{878}, i_6, e_{879}) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $a_{882} = \text{store}(a_{880}, i_2, e_{881}) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{835} = \text{select}(a_1, i_3) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{837} = \text{select}(a_1, i_4) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{839} = \text{select}(a_{838}, i_1) \quad \text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{841} = \text{select}(a_{838}, i_2) \quad \text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $e_{843} = \text{select}(a_{842}, i_5) \quad \text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $e_{845} = \text{select}(a_{842}, i_0) \quad \text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{847} = \text{select}(a_{846}, i_5) \quad \text{cnf}(\text{hyp}_{32}, \text{hypothesis})$   
 $e_{849} = \text{select}(a_{846}, i_2) \quad \text{cnf}(\text{hyp}_{33}, \text{hypothesis})$   
 $e_{851} = \text{select}(a_{850}, i_1) \quad \text{cnf}(\text{hyp}_{34}, \text{hypothesis})$   
 $e_{854} = \text{select}(a_{853}, i_2) \quad \text{cnf}(\text{hyp}_{35}, \text{hypothesis})$   
 $e_{856} = \text{select}(a_{853}, i_5) \quad \text{cnf}(\text{hyp}_{36}, \text{hypothesis})$   
 $e_{858} = \text{select}(a_{857}, i_2) \quad \text{cnf}(\text{hyp}_{37}, \text{hypothesis})$   
 $e_{860} = \text{select}(a_{857}, i_5) \quad \text{cnf}(\text{hyp}_{38}, \text{hypothesis})$   
 $e_{864} = \text{select}(a_{863}, i_0) \quad \text{cnf}(\text{hyp}_{39}, \text{hypothesis})$   
 $e_{866} = \text{select}(a_{863}, i_5) \quad \text{cnf}(\text{hyp}_{40}, \text{hypothesis})$   
 $e_{868} = \text{select}(a_{867}, i_2) \quad \text{cnf}(\text{hyp}_{41}, \text{hypothesis})$   
 $e_{870} = \text{select}(a_{867}, i_5) \quad \text{cnf}(\text{hyp}_{42}, \text{hypothesis})$   
 $e_{872} = \text{select}(a_{871}, i_1) \quad \text{cnf}(\text{hyp}_{43}, \text{hypothesis})$   
 $e_{875} = \text{select}(a_{874}, i_2) \quad \text{cnf}(\text{hyp}_{44}, \text{hypothesis})$   
 $e_{877} = \text{select}(a_{874}, i_5) \quad \text{cnf}(\text{hyp}_{45}, \text{hypothesis})$   
 $e_{879} = \text{select}(a_{878}, i_2) \quad \text{cnf}(\text{hyp}_{46}, \text{hypothesis})$   
 $e_{881} = \text{select}(a_{878}, i_6) \quad \text{cnf}(\text{hyp}_{47}, \text{hypothesis})$   
 $e_{884} = \text{select}(a_{861}, i_{883}) \quad \text{cnf}(\text{hyp}_{48}, \text{hypothesis})$   
 $e_{885} = \text{select}(a_{882}, i_{883}) \quad \text{cnf}(\text{hyp}_{49}, \text{hypothesis})$

$i_{883} = \text{sk}(a_{861}, a_{882}) \quad \text{cnf}(\text{hyp}_{50}, \text{hypothesis})$   
 $e_{884} \neq e_{885} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV540-1.004.p** Swap elements (t2\_np\_sf\_ai\_00004)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(a, i, \text{select}(a, i)) = a \quad \text{cnf}(a_3, \text{axiom})$   
 $\text{store}(\text{store}(a, i, e), i, f) = \text{store}(a, i, f) \quad \text{cnf}(a_4, \text{axiom})$   
 $i = j \text{ or } \text{store}(\text{store}(a, i, e), j, f) = \text{store}(\text{store}(a, j, f), i, e) \quad \text{cnf}(a_5, \text{axiom})$   
 $a_{417} = \text{store}(a_1, i_1, e_{416}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{418} = \text{store}(a_{417}, i_1, e_{416}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{420} = \text{store}(a_{418}, i_0, e_{419}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{422} = \text{store}(a_{420}, i_3, e_{421}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{424} = \text{store}(a_{422}, i_3, e_{423}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{426} = \text{store}(a_{424}, i_2, e_{425}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{428} = \text{store}(a_{426}, i_2, e_{427}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{430} = \text{store}(a_{428}, i_0, e_{429}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{431} = \text{store}(a_{418}, i_3, e_{421}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{432} = \text{store}(a_{431}, i_0, e_{419}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{434} = \text{store}(a_{432}, i_3, e_{433}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{436} = \text{store}(a_{434}, i_2, e_{435}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{438} = \text{store}(a_{436}, i_0, e_{437}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{440} = \text{store}(a_{438}, i_2, e_{439}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{416} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{419} = \text{select}(a_{418}, i_3) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{421} = \text{select}(a_{418}, i_0) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{423} = \text{select}(a_{422}, i_2) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $e_{425} = \text{select}(a_{422}, i_3) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{427} = \text{select}(a_{426}, i_0) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{429} = \text{select}(a_{426}, i_2) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{433} = \text{select}(a_{432}, i_2) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{435} = \text{select}(a_{432}, i_3) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{437} = \text{select}(a_{436}, i_2) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{439} = \text{select}(a_{436}, i_0) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $a_{430} \neq a_{440} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV540-1.007.p** Swap elements (t2\_np\_sf\_ai\_00007)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(a, i, \text{select}(a, i)) = a \quad \text{cnf}(a_3, \text{axiom})$   
 $\text{store}(\text{store}(a, i, e), i, f) = \text{store}(a, i, f) \quad \text{cnf}(a_4, \text{axiom})$   
 $i = j \text{ or } \text{store}(\text{store}(a, i, e), j, f) = \text{store}(\text{store}(a, j, f), i, e) \quad \text{cnf}(a_5, \text{axiom})$   
 $a_{783} = \text{store}(a_1, i_4, e_{782}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{785} = \text{store}(a_{783}, i_3, e_{784}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{787} = \text{store}(a_{785}, i_2, e_{786}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{789} = \text{store}(a_{787}, i_1, e_{788}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{791} = \text{store}(a_{789}, i_0, e_{790}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{793} = \text{store}(a_{791}, i_5, e_{792}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{795} = \text{store}(a_{793}, i_2, e_{794}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{797} = \text{store}(a_{795}, i_5, e_{796}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{799} = \text{store}(a_{797}, i_1, e_{798}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{800} = \text{store}(a_{799}, i_1, e_{798}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{802} = \text{store}(a_{800}, i_5, e_{801}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{804} = \text{store}(a_{802}, i_2, e_{803}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{806} = \text{store}(a_{804}, i_5, e_{805}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{808} = \text{store}(a_{806}, i_2, e_{807}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$

$a_{809} = \text{store}(a_{785}, i_1, e_{788}) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $a_{810} = \text{store}(a_{809}, i_2, e_{786}) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{812} = \text{store}(a_{810}, i_5, e_{811}) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_{814} = \text{store}(a_{812}, i_0, e_{813}) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $a_{816} = \text{store}(a_{814}, i_5, e_{815}) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{818} = \text{store}(a_{816}, i_2, e_{817}) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $a_{820} = \text{store}(a_{818}, i_1, e_{819}) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $a_{821} = \text{store}(a_{820}, i_1, e_{819}) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $a_{823} = \text{store}(a_{821}, i_5, e_{822}) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $a_{825} = \text{store}(a_{823}, i_2, e_{824}) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $a_{827} = \text{store}(a_{825}, i_5, e_{826}) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $a_{829} = \text{store}(a_{827}, i_2, e_{828}) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{782} = \text{select}(a_1, i_3) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{784} = \text{select}(a_1, i_4) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{786} = \text{select}(a_{785}, i_1) \quad \text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{788} = \text{select}(a_{785}, i_2) \quad \text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $e_{790} = \text{select}(a_{789}, i_5) \quad \text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $e_{792} = \text{select}(a_{789}, i_0) \quad \text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{794} = \text{select}(a_{793}, i_5) \quad \text{cnf}(\text{hyp}_{32}, \text{hypothesis})$   
 $e_{796} = \text{select}(a_{793}, i_2) \quad \text{cnf}(\text{hyp}_{33}, \text{hypothesis})$   
 $e_{798} = \text{select}(a_{797}, i_1) \quad \text{cnf}(\text{hyp}_{34}, \text{hypothesis})$   
 $e_{801} = \text{select}(a_{800}, i_2) \quad \text{cnf}(\text{hyp}_{35}, \text{hypothesis})$   
 $e_{803} = \text{select}(a_{800}, i_5) \quad \text{cnf}(\text{hyp}_{36}, \text{hypothesis})$   
 $e_{805} = \text{select}(a_{804}, i_2) \quad \text{cnf}(\text{hyp}_{37}, \text{hypothesis})$   
 $e_{807} = \text{select}(a_{804}, i_5) \quad \text{cnf}(\text{hyp}_{38}, \text{hypothesis})$   
 $e_{811} = \text{select}(a_{810}, i_0) \quad \text{cnf}(\text{hyp}_{39}, \text{hypothesis})$   
 $e_{813} = \text{select}(a_{810}, i_5) \quad \text{cnf}(\text{hyp}_{40}, \text{hypothesis})$   
 $e_{815} = \text{select}(a_{814}, i_2) \quad \text{cnf}(\text{hyp}_{41}, \text{hypothesis})$   
 $e_{817} = \text{select}(a_{814}, i_5) \quad \text{cnf}(\text{hyp}_{42}, \text{hypothesis})$   
 $e_{819} = \text{select}(a_{818}, i_1) \quad \text{cnf}(\text{hyp}_{43}, \text{hypothesis})$   
 $e_{822} = \text{select}(a_{821}, i_2) \quad \text{cnf}(\text{hyp}_{44}, \text{hypothesis})$   
 $e_{824} = \text{select}(a_{821}, i_5) \quad \text{cnf}(\text{hyp}_{45}, \text{hypothesis})$   
 $e_{826} = \text{select}(a_{825}, i_2) \quad \text{cnf}(\text{hyp}_{46}, \text{hypothesis})$   
 $e_{828} = \text{select}(a_{825}, i_5) \quad \text{cnf}(\text{hyp}_{47}, \text{hypothesis})$   
 $a_{808} \neq a_{829} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

#### SWV543-1.004.p Swap elements (t3\_np\_sf\_ai\_00004)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j)) \quad \text{cnf}(a_3, \text{axiom})$   
 $a_{417} = \text{store}(a_1, i_1, e_{416}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{418} = \text{store}(a_{417}, i_1, e_{416}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{420} = \text{store}(a_{418}, i_0, e_{419}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{422} = \text{store}(a_{420}, i_3, e_{421}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{424} = \text{store}(a_{422}, i_3, e_{423}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{426} = \text{store}(a_{424}, i_2, e_{425}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{428} = \text{store}(a_{426}, i_2, e_{427}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{430} = \text{store}(a_{428}, i_0, e_{429}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{431} = \text{store}(a_{418}, i_3, e_{421}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{432} = \text{store}(a_{431}, i_0, e_{419}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{434} = \text{store}(a_{432}, i_3, e_{433}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{436} = \text{store}(a_{434}, i_2, e_{435}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{438} = \text{store}(a_{436}, i_0, e_{437}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{440} = \text{store}(a_{438}, i_2, e_{439}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{416} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{419} = \text{select}(a_{418}, i_3) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{421} = \text{select}(a_{418}, i_0) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{423} = \text{select}(a_{422}, i_2) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$



$e_{425} = \text{select}(a_{422}, i_3)$        $\text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{427} = \text{select}(a_{426}, i_0)$        $\text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{429} = \text{select}(a_{426}, i_2)$        $\text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{433} = \text{select}(a_{432}, i_2)$        $\text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{435} = \text{select}(a_{432}, i_3)$        $\text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{437} = \text{select}(a_{436}, i_2)$        $\text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{439} = \text{select}(a_{436}, i_0)$        $\text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $a_{430} \neq a_{440}$        $\text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV543-1.007.p** Swap elements (t3\_np\_sf\_ai\_00007)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e$        $\text{cnf}(a_1, \text{axiom})$   
 $i = j$  or  $\text{select}(\text{store}(a, i, e), j) = \text{select}(a, j)$        $\text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j))$        $\text{cnf}(a_3, \text{axiom})$   
 $a_{783} = \text{store}(a_1, i_4, e_{782})$        $\text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{785} = \text{store}(a_{783}, i_3, e_{784})$        $\text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{787} = \text{store}(a_{785}, i_2, e_{786})$        $\text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{789} = \text{store}(a_{787}, i_1, e_{788})$        $\text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{791} = \text{store}(a_{789}, i_0, e_{790})$        $\text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{793} = \text{store}(a_{791}, i_5, e_{792})$        $\text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{795} = \text{store}(a_{793}, i_2, e_{794})$        $\text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{797} = \text{store}(a_{795}, i_5, e_{796})$        $\text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{799} = \text{store}(a_{797}, i_1, e_{798})$        $\text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{800} = \text{store}(a_{799}, i_1, e_{798})$        $\text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{802} = \text{store}(a_{800}, i_5, e_{801})$        $\text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{804} = \text{store}(a_{802}, i_2, e_{803})$        $\text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{806} = \text{store}(a_{804}, i_5, e_{805})$        $\text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{808} = \text{store}(a_{806}, i_2, e_{807})$        $\text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $a_{809} = \text{store}(a_{785}, i_1, e_{788})$        $\text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $a_{810} = \text{store}(a_{809}, i_2, e_{786})$        $\text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{812} = \text{store}(a_{810}, i_5, e_{811})$        $\text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_{814} = \text{store}(a_{812}, i_0, e_{813})$        $\text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $a_{816} = \text{store}(a_{814}, i_5, e_{815})$        $\text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{818} = \text{store}(a_{816}, i_2, e_{817})$        $\text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $a_{820} = \text{store}(a_{818}, i_1, e_{819})$        $\text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $a_{821} = \text{store}(a_{820}, i_1, e_{819})$        $\text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $a_{823} = \text{store}(a_{821}, i_5, e_{822})$        $\text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $a_{825} = \text{store}(a_{823}, i_2, e_{824})$        $\text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $a_{827} = \text{store}(a_{825}, i_5, e_{826})$        $\text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $a_{829} = \text{store}(a_{827}, i_2, e_{828})$        $\text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{782} = \text{select}(a_1, i_3)$        $\text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{784} = \text{select}(a_1, i_4)$        $\text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{786} = \text{select}(a_{785}, i_1)$        $\text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{788} = \text{select}(a_{785}, i_2)$        $\text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $e_{790} = \text{select}(a_{789}, i_5)$        $\text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $e_{792} = \text{select}(a_{789}, i_0)$        $\text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{794} = \text{select}(a_{793}, i_5)$        $\text{cnf}(\text{hyp}_{32}, \text{hypothesis})$   
 $e_{796} = \text{select}(a_{793}, i_2)$        $\text{cnf}(\text{hyp}_{33}, \text{hypothesis})$   
 $e_{798} = \text{select}(a_{797}, i_1)$        $\text{cnf}(\text{hyp}_{34}, \text{hypothesis})$   
 $e_{801} = \text{select}(a_{800}, i_2)$        $\text{cnf}(\text{hyp}_{35}, \text{hypothesis})$   
 $e_{803} = \text{select}(a_{800}, i_5)$        $\text{cnf}(\text{hyp}_{36}, \text{hypothesis})$   
 $e_{805} = \text{select}(a_{804}, i_2)$        $\text{cnf}(\text{hyp}_{37}, \text{hypothesis})$   
 $e_{807} = \text{select}(a_{804}, i_5)$        $\text{cnf}(\text{hyp}_{38}, \text{hypothesis})$   
 $e_{811} = \text{select}(a_{810}, i_0)$        $\text{cnf}(\text{hyp}_{39}, \text{hypothesis})$   
 $e_{813} = \text{select}(a_{810}, i_5)$        $\text{cnf}(\text{hyp}_{40}, \text{hypothesis})$   
 $e_{815} = \text{select}(a_{814}, i_2)$        $\text{cnf}(\text{hyp}_{41}, \text{hypothesis})$   
 $e_{817} = \text{select}(a_{814}, i_5)$        $\text{cnf}(\text{hyp}_{42}, \text{hypothesis})$   
 $e_{819} = \text{select}(a_{818}, i_1)$        $\text{cnf}(\text{hyp}_{43}, \text{hypothesis})$   
 $e_{822} = \text{select}(a_{821}, i_2)$        $\text{cnf}(\text{hyp}_{44}, \text{hypothesis})$

$e_{824} = \text{select}(a_{821}, i_5) \quad \text{cnf}(\text{hyp}_{45}, \text{hypothesis})$   
 $e_{826} = \text{select}(a_{825}, i_2) \quad \text{cnf}(\text{hyp}_{46}, \text{hypothesis})$   
 $e_{828} = \text{select}(a_{825}, i_5) \quad \text{cnf}(\text{hyp}_{47}, \text{hypothesis})$   
 $a_{808} \neq a_{829} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV544-1.004.p** Swap elements (t3\_np\_sf\_ai\_00004)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j)) \quad \text{cnf}(a_3, \text{axiom})$   
 $a_{418} = \text{store}(a_1, i_1, e_{417}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{419} = \text{store}(a_{418}, i_1, e_{417}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{421} = \text{store}(a_{419}, i_0, e_{420}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{423} = \text{store}(a_{421}, i_3, e_{422}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{425} = \text{store}(a_{423}, i_3, e_{424}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{427} = \text{store}(a_{425}, i_2, e_{426}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{429} = \text{store}(a_{427}, i_2, e_{428}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{431} = \text{store}(a_{429}, i_0, e_{430}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{432} = \text{store}(a_{419}, i_3, e_{422}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{433} = \text{store}(a_{432}, i_0, e_{420}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{435} = \text{store}(a_{433}, i_3, e_{434}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{437} = \text{store}(a_{435}, i_2, e_{436}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{439} = \text{store}(a_{437}, i_0, e_{438}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{441} = \text{store}(a_{439}, i_3, e_{440}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{417} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{420} = \text{select}(a_{419}, i_3) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{422} = \text{select}(a_{419}, i_0) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{424} = \text{select}(a_{423}, i_2) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $e_{426} = \text{select}(a_{423}, i_3) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{428} = \text{select}(a_{427}, i_0) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{430} = \text{select}(a_{427}, i_2) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{434} = \text{select}(a_{433}, i_2) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{436} = \text{select}(a_{433}, i_3) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{438} = \text{select}(a_{437}, i_3) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{440} = \text{select}(a_{437}, i_0) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $a_{431} \neq a_{441} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV544-1.007.p** Swap elements (t3\_np\_sf\_ai\_00007)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j)) \quad \text{cnf}(a_3, \text{axiom})$   
 $a_{785} = \text{store}(a_1, i_4, e_{784}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{787} = \text{store}(a_{785}, i_3, e_{786}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{789} = \text{store}(a_{787}, i_2, e_{788}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{791} = \text{store}(a_{789}, i_1, e_{790}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{793} = \text{store}(a_{791}, i_0, e_{792}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{795} = \text{store}(a_{793}, i_5, e_{794}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{797} = \text{store}(a_{795}, i_2, e_{796}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{799} = \text{store}(a_{797}, i_5, e_{798}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{801} = \text{store}(a_{799}, i_1, e_{800}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{802} = \text{store}(a_{801}, i_1, e_{800}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{804} = \text{store}(a_{802}, i_5, e_{803}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{806} = \text{store}(a_{804}, i_2, e_{805}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{808} = \text{store}(a_{806}, i_5, e_{807}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{810} = \text{store}(a_{808}, i_2, e_{809}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $a_{811} = \text{store}(a_{787}, i_1, e_{790}) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $a_{812} = \text{store}(a_{811}, i_2, e_{788}) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$

$a_{814} = \text{store}(a_{812}, i_5, e_{813}) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_{816} = \text{store}(a_{814}, i_0, e_{815}) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $a_{818} = \text{store}(a_{816}, i_5, e_{817}) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{820} = \text{store}(a_{818}, i_2, e_{819}) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $a_{822} = \text{store}(a_{820}, i_1, e_{821}) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $a_{823} = \text{store}(a_{822}, i_1, e_{821}) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $a_{825} = \text{store}(a_{823}, i_5, e_{824}) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $a_{827} = \text{store}(a_{825}, i_2, e_{826}) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $a_{829} = \text{store}(a_{827}, i_6, e_{828}) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $a_{831} = \text{store}(a_{829}, i_2, e_{830}) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{784} = \text{select}(a_1, i_3) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{786} = \text{select}(a_1, i_4) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{788} = \text{select}(a_{787}, i_1) \quad \text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{790} = \text{select}(a_{787}, i_2) \quad \text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $e_{792} = \text{select}(a_{791}, i_5) \quad \text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $e_{794} = \text{select}(a_{791}, i_0) \quad \text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{796} = \text{select}(a_{795}, i_5) \quad \text{cnf}(\text{hyp}_{32}, \text{hypothesis})$   
 $e_{798} = \text{select}(a_{795}, i_2) \quad \text{cnf}(\text{hyp}_{33}, \text{hypothesis})$   
 $e_{800} = \text{select}(a_{799}, i_1) \quad \text{cnf}(\text{hyp}_{34}, \text{hypothesis})$   
 $e_{803} = \text{select}(a_{802}, i_2) \quad \text{cnf}(\text{hyp}_{35}, \text{hypothesis})$   
 $e_{805} = \text{select}(a_{802}, i_5) \quad \text{cnf}(\text{hyp}_{36}, \text{hypothesis})$   
 $e_{807} = \text{select}(a_{806}, i_2) \quad \text{cnf}(\text{hyp}_{37}, \text{hypothesis})$   
 $e_{809} = \text{select}(a_{806}, i_5) \quad \text{cnf}(\text{hyp}_{38}, \text{hypothesis})$   
 $e_{813} = \text{select}(a_{812}, i_0) \quad \text{cnf}(\text{hyp}_{39}, \text{hypothesis})$   
 $e_{815} = \text{select}(a_{812}, i_5) \quad \text{cnf}(\text{hyp}_{40}, \text{hypothesis})$   
 $e_{817} = \text{select}(a_{816}, i_2) \quad \text{cnf}(\text{hyp}_{41}, \text{hypothesis})$   
 $e_{819} = \text{select}(a_{816}, i_5) \quad \text{cnf}(\text{hyp}_{42}, \text{hypothesis})$   
 $e_{821} = \text{select}(a_{820}, i_1) \quad \text{cnf}(\text{hyp}_{43}, \text{hypothesis})$   
 $e_{824} = \text{select}(a_{823}, i_2) \quad \text{cnf}(\text{hyp}_{44}, \text{hypothesis})$   
 $e_{826} = \text{select}(a_{823}, i_5) \quad \text{cnf}(\text{hyp}_{45}, \text{hypothesis})$   
 $e_{828} = \text{select}(a_{827}, i_2) \quad \text{cnf}(\text{hyp}_{46}, \text{hypothesis})$   
 $e_{830} = \text{select}(a_{827}, i_6) \quad \text{cnf}(\text{hyp}_{47}, \text{hypothesis})$   
 $a_{810} \neq a_{831} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV547-1.004.p** Swap elements (t3\_pp\_sf\_ai\_00004)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j)) \quad \text{cnf}(a_3, \text{axiom})$   
 $a_{466} = \text{store}(a_1, i_1, e_{465}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{467} = \text{store}(a_{466}, i_1, e_{465}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{469} = \text{store}(a_{467}, i_0, e_{468}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{471} = \text{store}(a_{469}, i_3, e_{470}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{473} = \text{store}(a_{471}, i_3, e_{472}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{475} = \text{store}(a_{473}, i_2, e_{474}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{477} = \text{store}(a_{475}, i_2, e_{476}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{479} = \text{store}(a_{477}, i_0, e_{478}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{480} = \text{store}(a_{467}, i_3, e_{470}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{481} = \text{store}(a_{480}, i_0, e_{468}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{483} = \text{store}(a_{481}, i_3, e_{482}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{485} = \text{store}(a_{483}, i_2, e_{484}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{487} = \text{store}(a_{485}, i_0, e_{486}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{489} = \text{store}(a_{487}, i_2, e_{488}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{465} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{468} = \text{select}(a_{467}, i_3) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{470} = \text{select}(a_{467}, i_0) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{472} = \text{select}(a_{471}, i_2) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $e_{474} = \text{select}(a_{471}, i_3) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{476} = \text{select}(a_{475}, i_0) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$

$e_{478} = \text{select}(a_{475}, i_2)$        $\text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{482} = \text{select}(a_{481}, i_2)$        $\text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{484} = \text{select}(a_{481}, i_3)$        $\text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{486} = \text{select}(a_{485}, i_2)$        $\text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{488} = \text{select}(a_{485}, i_0)$        $\text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{491} = \text{select}(a_{479}, i_{490})$        $\text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{492} = \text{select}(a_{489}, i_{490})$        $\text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $i_{490} = \text{sk}(a_{479}, a_{489})$        $\text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{491} \neq e_{492}$        $\text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV547-1.007.p** Swap elements (t3\_pp\_sf\_ai\_00007)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e$        $\text{cnf}(a_1, \text{axiom})$   
 $i = j$  or  $\text{select}(\text{store}(a, i, e), j) = \text{select}(a, j)$        $\text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j))$        $\text{cnf}(a_3, \text{axiom})$   
 $a_{834} = \text{store}(a_1, i_4, e_{833})$        $\text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{836} = \text{store}(a_{834}, i_3, e_{835})$        $\text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{838} = \text{store}(a_{836}, i_2, e_{837})$        $\text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{840} = \text{store}(a_{838}, i_1, e_{839})$        $\text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{842} = \text{store}(a_{840}, i_0, e_{841})$        $\text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{844} = \text{store}(a_{842}, i_5, e_{843})$        $\text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{846} = \text{store}(a_{844}, i_2, e_{845})$        $\text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{848} = \text{store}(a_{846}, i_5, e_{847})$        $\text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{850} = \text{store}(a_{848}, i_1, e_{849})$        $\text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{851} = \text{store}(a_{850}, i_1, e_{849})$        $\text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{853} = \text{store}(a_{851}, i_5, e_{852})$        $\text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{855} = \text{store}(a_{853}, i_2, e_{854})$        $\text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{857} = \text{store}(a_{855}, i_5, e_{856})$        $\text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{859} = \text{store}(a_{857}, i_2, e_{858})$        $\text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $a_{860} = \text{store}(a_{836}, i_1, e_{839})$        $\text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $a_{861} = \text{store}(a_{860}, i_2, e_{837})$        $\text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{863} = \text{store}(a_{861}, i_5, e_{862})$        $\text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_{865} = \text{store}(a_{863}, i_0, e_{864})$        $\text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $a_{867} = \text{store}(a_{865}, i_5, e_{866})$        $\text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{869} = \text{store}(a_{867}, i_2, e_{868})$        $\text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $a_{871} = \text{store}(a_{869}, i_1, e_{870})$        $\text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $a_{872} = \text{store}(a_{871}, i_1, e_{870})$        $\text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $a_{874} = \text{store}(a_{872}, i_5, e_{873})$        $\text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $a_{876} = \text{store}(a_{874}, i_2, e_{875})$        $\text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $a_{878} = \text{store}(a_{876}, i_5, e_{877})$        $\text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $a_{880} = \text{store}(a_{878}, i_2, e_{879})$        $\text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{833} = \text{select}(a_1, i_3)$        $\text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{835} = \text{select}(a_1, i_4)$        $\text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{837} = \text{select}(a_{836}, i_1)$        $\text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{839} = \text{select}(a_{836}, i_2)$        $\text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $e_{841} = \text{select}(a_{840}, i_5)$        $\text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $e_{843} = \text{select}(a_{840}, i_0)$        $\text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{845} = \text{select}(a_{844}, i_5)$        $\text{cnf}(\text{hyp}_{32}, \text{hypothesis})$   
 $e_{847} = \text{select}(a_{844}, i_2)$        $\text{cnf}(\text{hyp}_{33}, \text{hypothesis})$   
 $e_{849} = \text{select}(a_{848}, i_1)$        $\text{cnf}(\text{hyp}_{34}, \text{hypothesis})$   
 $e_{852} = \text{select}(a_{851}, i_2)$        $\text{cnf}(\text{hyp}_{35}, \text{hypothesis})$   
 $e_{854} = \text{select}(a_{851}, i_5)$        $\text{cnf}(\text{hyp}_{36}, \text{hypothesis})$   
 $e_{856} = \text{select}(a_{855}, i_2)$        $\text{cnf}(\text{hyp}_{37}, \text{hypothesis})$   
 $e_{858} = \text{select}(a_{855}, i_5)$        $\text{cnf}(\text{hyp}_{38}, \text{hypothesis})$   
 $e_{862} = \text{select}(a_{861}, i_0)$        $\text{cnf}(\text{hyp}_{39}, \text{hypothesis})$   
 $e_{864} = \text{select}(a_{861}, i_5)$        $\text{cnf}(\text{hyp}_{40}, \text{hypothesis})$   
 $e_{866} = \text{select}(a_{865}, i_2)$        $\text{cnf}(\text{hyp}_{41}, \text{hypothesis})$   
 $e_{868} = \text{select}(a_{865}, i_5)$        $\text{cnf}(\text{hyp}_{42}, \text{hypothesis})$   
 $e_{870} = \text{select}(a_{869}, i_1)$        $\text{cnf}(\text{hyp}_{43}, \text{hypothesis})$

$e_{873} = \text{select}(a_{872}, i_2) \quad \text{cnf}(\text{hyp}_{44}, \text{hypothesis})$   
 $e_{875} = \text{select}(a_{872}, i_5) \quad \text{cnf}(\text{hyp}_{45}, \text{hypothesis})$   
 $e_{877} = \text{select}(a_{876}, i_2) \quad \text{cnf}(\text{hyp}_{46}, \text{hypothesis})$   
 $e_{879} = \text{select}(a_{876}, i_5) \quad \text{cnf}(\text{hyp}_{47}, \text{hypothesis})$   
 $e_{882} = \text{select}(a_{859}, i_{881}) \quad \text{cnf}(\text{hyp}_{48}, \text{hypothesis})$   
 $e_{883} = \text{select}(a_{880}, i_{881}) \quad \text{cnf}(\text{hyp}_{49}, \text{hypothesis})$   
 $i_{881} = \text{sk}(a_{859}, a_{880}) \quad \text{cnf}(\text{hyp}_{50}, \text{hypothesis})$   
 $e_{882} \neq e_{883} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV548-1.004.p** Swap elements (t3\_pp\_sf\_ai\_00004)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j)) \quad \text{cnf}(a_3, \text{axiom})$   
 $a_{469} = \text{store}(a_1, i_1, e_{468}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{470} = \text{store}(a_{469}, i_1, e_{468}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{472} = \text{store}(a_{470}, i_0, e_{471}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{474} = \text{store}(a_{472}, i_3, e_{473}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{476} = \text{store}(a_{474}, i_3, e_{475}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{478} = \text{store}(a_{476}, i_2, e_{477}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{480} = \text{store}(a_{478}, i_2, e_{479}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{482} = \text{store}(a_{480}, i_0, e_{481}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{483} = \text{store}(a_{470}, i_3, e_{473}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{484} = \text{store}(a_{483}, i_0, e_{471}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{486} = \text{store}(a_{484}, i_3, e_{485}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{488} = \text{store}(a_{486}, i_2, e_{487}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{490} = \text{store}(a_{488}, i_0, e_{489}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{492} = \text{store}(a_{490}, i_3, e_{491}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{468} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{471} = \text{select}(a_{470}, i_3) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{473} = \text{select}(a_{470}, i_0) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{475} = \text{select}(a_{474}, i_2) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $e_{477} = \text{select}(a_{474}, i_3) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{479} = \text{select}(a_{478}, i_0) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{481} = \text{select}(a_{478}, i_2) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{485} = \text{select}(a_{484}, i_2) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{487} = \text{select}(a_{484}, i_3) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{489} = \text{select}(a_{488}, i_3) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{491} = \text{select}(a_{488}, i_0) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{494} = \text{select}(a_{482}, i_{493}) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{495} = \text{select}(a_{492}, i_{493}) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $i_{493} = \text{sk}(a_{482}, a_{492}) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{494} \neq e_{495} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV548-1.007.p** Swap elements (t3\_pp\_sf\_ai\_00007)

Swapping an element at position  $i1$  with an element at position  $i2$  is equivalent to swapping the element at position  $i2$  with the element at position  $i1$ .

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j)) \quad \text{cnf}(a_3, \text{axiom})$   
 $a_{836} = \text{store}(a_1, i_4, e_{835}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{838} = \text{store}(a_{836}, i_3, e_{837}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{840} = \text{store}(a_{838}, i_2, e_{839}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{842} = \text{store}(a_{840}, i_1, e_{841}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{844} = \text{store}(a_{842}, i_0, e_{843}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{846} = \text{store}(a_{844}, i_5, e_{845}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{848} = \text{store}(a_{846}, i_2, e_{847}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{850} = \text{store}(a_{848}, i_5, e_{849}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{852} = \text{store}(a_{850}, i_1, e_{851}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$

$a_{853} = \text{store}(a_{852}, i_1, e_{851})$        $\text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{855} = \text{store}(a_{853}, i_5, e_{854})$        $\text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{857} = \text{store}(a_{855}, i_2, e_{856})$        $\text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{859} = \text{store}(a_{857}, i_5, e_{858})$        $\text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{861} = \text{store}(a_{859}, i_2, e_{860})$        $\text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $a_{862} = \text{store}(a_{838}, i_1, e_{841})$        $\text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $a_{863} = \text{store}(a_{862}, i_2, e_{839})$        $\text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{865} = \text{store}(a_{863}, i_5, e_{864})$        $\text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_{867} = \text{store}(a_{865}, i_0, e_{866})$        $\text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $a_{869} = \text{store}(a_{867}, i_5, e_{868})$        $\text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{871} = \text{store}(a_{869}, i_2, e_{870})$        $\text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $a_{873} = \text{store}(a_{871}, i_1, e_{872})$        $\text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $a_{874} = \text{store}(a_{873}, i_1, e_{872})$        $\text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $a_{876} = \text{store}(a_{874}, i_5, e_{875})$        $\text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $a_{878} = \text{store}(a_{876}, i_2, e_{877})$        $\text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $a_{880} = \text{store}(a_{878}, i_6, e_{879})$        $\text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $a_{882} = \text{store}(a_{880}, i_2, e_{881})$        $\text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{835} = \text{select}(a_1, i_3)$        $\text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{837} = \text{select}(a_1, i_4)$        $\text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{839} = \text{select}(a_{838}, i_1)$        $\text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{841} = \text{select}(a_{838}, i_2)$        $\text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $e_{843} = \text{select}(a_{842}, i_5)$        $\text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $e_{845} = \text{select}(a_{842}, i_0)$        $\text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{847} = \text{select}(a_{846}, i_5)$        $\text{cnf}(\text{hyp}_{32}, \text{hypothesis})$   
 $e_{849} = \text{select}(a_{846}, i_2)$        $\text{cnf}(\text{hyp}_{33}, \text{hypothesis})$   
 $e_{851} = \text{select}(a_{850}, i_1)$        $\text{cnf}(\text{hyp}_{34}, \text{hypothesis})$   
 $e_{854} = \text{select}(a_{853}, i_2)$        $\text{cnf}(\text{hyp}_{35}, \text{hypothesis})$   
 $e_{856} = \text{select}(a_{853}, i_5)$        $\text{cnf}(\text{hyp}_{36}, \text{hypothesis})$   
 $e_{858} = \text{select}(a_{857}, i_2)$        $\text{cnf}(\text{hyp}_{37}, \text{hypothesis})$   
 $e_{860} = \text{select}(a_{857}, i_5)$        $\text{cnf}(\text{hyp}_{38}, \text{hypothesis})$   
 $e_{864} = \text{select}(a_{863}, i_0)$        $\text{cnf}(\text{hyp}_{39}, \text{hypothesis})$   
 $e_{866} = \text{select}(a_{863}, i_5)$        $\text{cnf}(\text{hyp}_{40}, \text{hypothesis})$   
 $e_{868} = \text{select}(a_{867}, i_2)$        $\text{cnf}(\text{hyp}_{41}, \text{hypothesis})$   
 $e_{870} = \text{select}(a_{867}, i_5)$        $\text{cnf}(\text{hyp}_{42}, \text{hypothesis})$   
 $e_{872} = \text{select}(a_{871}, i_1)$        $\text{cnf}(\text{hyp}_{43}, \text{hypothesis})$   
 $e_{875} = \text{select}(a_{874}, i_2)$        $\text{cnf}(\text{hyp}_{44}, \text{hypothesis})$   
 $e_{877} = \text{select}(a_{874}, i_5)$        $\text{cnf}(\text{hyp}_{45}, \text{hypothesis})$   
 $e_{879} = \text{select}(a_{878}, i_2)$        $\text{cnf}(\text{hyp}_{46}, \text{hypothesis})$   
 $e_{881} = \text{select}(a_{878}, i_6)$        $\text{cnf}(\text{hyp}_{47}, \text{hypothesis})$   
 $e_{884} = \text{select}(a_{861}, i_{883})$        $\text{cnf}(\text{hyp}_{48}, \text{hypothesis})$   
 $e_{885} = \text{select}(a_{882}, i_{883})$        $\text{cnf}(\text{hyp}_{49}, \text{hypothesis})$   
 $i_{883} = \text{sk}(a_{861}, a_{882})$        $\text{cnf}(\text{hyp}_{50}, \text{hypothesis})$   
 $e_{884} \neq e_{885}$        $\text{cnf}(\text{goal}, \text{negated\_conjecture})$

#### SWV549-1.004.p Store inverse (t1\_np\_nf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e$        $\text{cnf}(a_1, \text{axiom})$   
 $i = j$  or  $\text{select}(\text{store}(a, i, e), j) = \text{select}(a, j)$        $\text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(\text{store}(\text{store}(a_1, i_1, \text{select}(a_2, i_1)), i_2, \text{select}(\text{store}(a_2, i_1, \text{select}(a_1, i_1)), i_2)), i_3, \text{select}(\text{store}(\text{store}(a_2, i_1, \text{select}(a_1, i_1))), \text{store}(\text{store}(\text{store}(\text{store}(a_2, i_1, \text{select}(a_1, i_1)), i_2, \text{select}(\text{store}(a_1, i_1, \text{select}(a_2, i_1)), i_2)), i_3, \text{select}(\text{store}(\text{store}(a_1, i_1, \text{select}(a_2, i_1))), a_1 \neq a_2$        $\text{cnf}(\text{goal}, \text{negated\_conjecture})$

#### SWV550-1.004.p Store inverse (t1\_np\_nf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e$        $\text{cnf}(a_1, \text{axiom})$   
 $i = j$  or  $\text{select}(\text{store}(a, i, e), j) = \text{select}(a, j)$        $\text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(\text{store}(\text{store}(a_1, i_1, \text{select}(a_2, i_1)), i_2, \text{select}(\text{store}(a_2, i_1, \text{select}(a_1, i_1)), i_2)), i_3, \text{select}(\text{store}(\text{store}(a_2, i_1, \text{select}(a_1, i_1))), \text{store}(\text{store}(\text{store}(\text{store}(a_2, i_1, \text{select}(a_1, i_1)), i_2, \text{select}(\text{store}(a_1, i_1, \text{select}(a_2, i_1)), i_2)), i_3, \text{select}(\text{store}(\text{store}(a_1, i_1, \text{select}(a_2, i_1))),$

$a_1 \neq a_2$      $\text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV551-1.004.p** Store inverse (t1\_np\_sf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e$      $\text{cnf}(a_1, \text{axiom})$   
 $i = j$  or  $\text{select}(\text{store}(a, i, e), j) = \text{select}(a, j)$      $\text{cnf}(a_2, \text{axiom})$   
 $a_{17} = \text{store}(a_1, i_1, e_{16})$      $\text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{19} = \text{store}(a_2, i_1, e_{18})$      $\text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{21} = \text{store}(a_{17}, i_2, e_{20})$      $\text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{23} = \text{store}(a_{19}, i_2, e_{22})$      $\text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{25} = \text{store}(a_{21}, i_3, e_{24})$      $\text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{27} = \text{store}(a_{23}, i_3, e_{26})$      $\text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{29} = \text{store}(a_{25}, i_4, e_{28})$      $\text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{31} = \text{store}(a_{27}, i_4, e_{30})$      $\text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $e_{16} = \text{select}(a_2, i_1)$      $\text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $e_{18} = \text{select}(a_1, i_1)$      $\text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $e_{20} = \text{select}(a_{19}, i_2)$      $\text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $e_{22} = \text{select}(a_{17}, i_2)$      $\text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $e_{24} = \text{select}(a_{23}, i_3)$      $\text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $e_{26} = \text{select}(a_{21}, i_3)$      $\text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{28} = \text{select}(a_{27}, i_4)$      $\text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{30} = \text{select}(a_{25}, i_4)$      $\text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{29} = a_{31}$      $\text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_1 \neq a_2$      $\text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV551-1.007.p** Store inverse (t1\_np\_sf\_ai\_00007)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e$      $\text{cnf}(a_1, \text{axiom})$   
 $i = j$  or  $\text{select}(\text{store}(a, i, e), j) = \text{select}(a, j)$      $\text{cnf}(a_2, \text{axiom})$   
 $a_{29} = \text{store}(a_1, i_1, e_{28})$      $\text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{31} = \text{store}(a_2, i_1, e_{30})$      $\text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{33} = \text{store}(a_{29}, i_2, e_{32})$      $\text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{35} = \text{store}(a_{31}, i_2, e_{34})$      $\text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{37} = \text{store}(a_{33}, i_3, e_{36})$      $\text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{39} = \text{store}(a_{35}, i_3, e_{38})$      $\text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{41} = \text{store}(a_{37}, i_4, e_{40})$      $\text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{43} = \text{store}(a_{39}, i_4, e_{42})$      $\text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{45} = \text{store}(a_{41}, i_5, e_{44})$      $\text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{47} = \text{store}(a_{43}, i_5, e_{46})$      $\text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{49} = \text{store}(a_{45}, i_6, e_{48})$      $\text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{51} = \text{store}(a_{47}, i_6, e_{50})$      $\text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{53} = \text{store}(a_{49}, i_7, e_{52})$      $\text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{55} = \text{store}(a_{51}, i_7, e_{54})$      $\text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{28} = \text{select}(a_2, i_1)$      $\text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{30} = \text{select}(a_1, i_1)$      $\text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{32} = \text{select}(a_{31}, i_2)$      $\text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{34} = \text{select}(a_{29}, i_2)$      $\text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $e_{36} = \text{select}(a_{35}, i_3)$      $\text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{38} = \text{select}(a_{33}, i_3)$      $\text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{40} = \text{select}(a_{39}, i_4)$      $\text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{42} = \text{select}(a_{37}, i_4)$      $\text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{44} = \text{select}(a_{43}, i_5)$      $\text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{46} = \text{select}(a_{41}, i_5)$      $\text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{48} = \text{select}(a_{47}, i_6)$      $\text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{50} = \text{select}(a_{45}, i_6)$      $\text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{52} = \text{select}(a_{51}, i_7)$      $\text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{54} = \text{select}(a_{49}, i_7)$      $\text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $a_{53} = a_{55}$      $\text{cnf}(\text{hyp}_{28}, \text{hypothesis})$

$a_1 \neq a_2$      cnf(goal, negated\_conjecture)

**SWV551-1.010.p** Store inverse (t1\_np\_sf\_ai\_00010)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

select(store( $a, i, e$ ),  $i$ ) =  $e$      cnf( $a_1$ , axiom)  
 $i = j$  or select(store( $a, i, e$ ),  $j$ ) = select( $a, j$ )     cnf( $a_2$ , axiom)  
 $a_{41} = \text{store}(a_1, i_1, e_{40})$      cnf(hyp<sub>0</sub>, hypothesis)  
 $a_{43} = \text{store}(a_2, i_1, e_{42})$      cnf(hyp<sub>1</sub>, hypothesis)  
 $a_{45} = \text{store}(a_{41}, i_2, e_{44})$      cnf(hyp<sub>2</sub>, hypothesis)  
 $a_{47} = \text{store}(a_{43}, i_2, e_{46})$      cnf(hyp<sub>3</sub>, hypothesis)  
 $a_{49} = \text{store}(a_{45}, i_3, e_{48})$      cnf(hyp<sub>4</sub>, hypothesis)  
 $a_{51} = \text{store}(a_{47}, i_3, e_{50})$      cnf(hyp<sub>5</sub>, hypothesis)  
 $a_{53} = \text{store}(a_{49}, i_4, e_{52})$      cnf(hyp<sub>6</sub>, hypothesis)  
 $a_{55} = \text{store}(a_{51}, i_4, e_{54})$      cnf(hyp<sub>7</sub>, hypothesis)  
 $a_{57} = \text{store}(a_{53}, i_5, e_{56})$      cnf(hyp<sub>8</sub>, hypothesis)  
 $a_{59} = \text{store}(a_{55}, i_5, e_{58})$      cnf(hyp<sub>9</sub>, hypothesis)  
 $a_{61} = \text{store}(a_{57}, i_6, e_{60})$      cnf(hyp<sub>10</sub>, hypothesis)  
 $a_{63} = \text{store}(a_{59}, i_6, e_{62})$      cnf(hyp<sub>11</sub>, hypothesis)  
 $a_{65} = \text{store}(a_{61}, i_7, e_{64})$      cnf(hyp<sub>12</sub>, hypothesis)  
 $a_{67} = \text{store}(a_{63}, i_7, e_{66})$      cnf(hyp<sub>13</sub>, hypothesis)  
 $a_{69} = \text{store}(a_{65}, i_8, e_{68})$      cnf(hyp<sub>14</sub>, hypothesis)  
 $a_{71} = \text{store}(a_{67}, i_8, e_{70})$      cnf(hyp<sub>15</sub>, hypothesis)  
 $a_{73} = \text{store}(a_{69}, i_9, e_{72})$      cnf(hyp<sub>16</sub>, hypothesis)  
 $a_{75} = \text{store}(a_{71}, i_9, e_{74})$      cnf(hyp<sub>17</sub>, hypothesis)  
 $a_{77} = \text{store}(a_{73}, i_{10}, e_{76})$      cnf(hyp<sub>18</sub>, hypothesis)  
 $a_{79} = \text{store}(a_{75}, i_{10}, e_{78})$      cnf(hyp<sub>19</sub>, hypothesis)  
 $e_{40} = \text{select}(a_2, i_1)$      cnf(hyp<sub>20</sub>, hypothesis)  
 $e_{42} = \text{select}(a_1, i_1)$      cnf(hyp<sub>21</sub>, hypothesis)  
 $e_{44} = \text{select}(a_{43}, i_2)$      cnf(hyp<sub>22</sub>, hypothesis)  
 $e_{46} = \text{select}(a_{41}, i_2)$      cnf(hyp<sub>23</sub>, hypothesis)  
 $e_{48} = \text{select}(a_{47}, i_3)$      cnf(hyp<sub>24</sub>, hypothesis)  
 $e_{50} = \text{select}(a_{45}, i_3)$      cnf(hyp<sub>25</sub>, hypothesis)  
 $e_{52} = \text{select}(a_{51}, i_4)$      cnf(hyp<sub>26</sub>, hypothesis)  
 $e_{54} = \text{select}(a_{49}, i_4)$      cnf(hyp<sub>27</sub>, hypothesis)  
 $e_{56} = \text{select}(a_{55}, i_5)$      cnf(hyp<sub>28</sub>, hypothesis)  
 $e_{58} = \text{select}(a_{53}, i_5)$      cnf(hyp<sub>29</sub>, hypothesis)  
 $e_{60} = \text{select}(a_{59}, i_6)$      cnf(hyp<sub>30</sub>, hypothesis)  
 $e_{62} = \text{select}(a_{57}, i_6)$      cnf(hyp<sub>31</sub>, hypothesis)  
 $e_{64} = \text{select}(a_{63}, i_7)$      cnf(hyp<sub>32</sub>, hypothesis)  
 $e_{66} = \text{select}(a_{61}, i_7)$      cnf(hyp<sub>33</sub>, hypothesis)  
 $e_{68} = \text{select}(a_{67}, i_8)$      cnf(hyp<sub>34</sub>, hypothesis)  
 $e_{70} = \text{select}(a_{65}, i_8)$      cnf(hyp<sub>35</sub>, hypothesis)  
 $e_{72} = \text{select}(a_{71}, i_9)$      cnf(hyp<sub>36</sub>, hypothesis)  
 $e_{74} = \text{select}(a_{69}, i_9)$      cnf(hyp<sub>37</sub>, hypothesis)  
 $e_{76} = \text{select}(a_{75}, i_{10})$      cnf(hyp<sub>38</sub>, hypothesis)  
 $e_{78} = \text{select}(a_{73}, i_{10})$      cnf(hyp<sub>39</sub>, hypothesis)  
 $a_{77} = a_{79}$      cnf(hyp<sub>40</sub>, hypothesis)  
 $a_1 \neq a_2$      cnf(goal, negated\_conjecture)

**SWV552-1.004.p** Store inverse (t1\_np\_sf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

select(store( $a, i, e$ ),  $i$ ) =  $e$      cnf( $a_1$ , axiom)  
 $i = j$  or select(store( $a, i, e$ ),  $j$ ) = select( $a, j$ )     cnf( $a_2$ , axiom)  
 $a_{17} = \text{store}(a_1, i_1, e_{16})$      cnf(hyp<sub>0</sub>, hypothesis)  
 $a_{19} = \text{store}(a_2, i_1, e_{18})$      cnf(hyp<sub>1</sub>, hypothesis)  
 $a_{21} = \text{store}(a_{17}, i_2, e_{20})$      cnf(hyp<sub>2</sub>, hypothesis)  
 $a_{23} = \text{store}(a_{19}, i_2, e_{22})$      cnf(hyp<sub>3</sub>, hypothesis)  
 $a_{25} = \text{store}(a_{21}, i_3, e_{24})$      cnf(hyp<sub>4</sub>, hypothesis)



$a_{27} = \text{store}(a_{23}, i_3, e_{26}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{29} = \text{store}(a_{25}, i_1, e_{28}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{31} = \text{store}(a_{27}, i_4, e_{30}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $e_{16} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $e_{18} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $e_{20} = \text{select}(a_{19}, i_2) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $e_{22} = \text{select}(a_{17}, i_2) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $e_{24} = \text{select}(a_{23}, i_3) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $e_{26} = \text{select}(a_{21}, i_3) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{28} = \text{select}(a_{27}, i_4) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{30} = \text{select}(a_{25}, i_4) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{29} = a_{31} \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_1 \neq a_2 \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV552-1.007.p** Store inverse (t1\_np\_sf\_ai.00007)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $a_{29} = \text{store}(a_1, i_1, e_{28}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{31} = \text{store}(a_2, i_1, e_{30}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{33} = \text{store}(a_{29}, i_2, e_{32}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{35} = \text{store}(a_{31}, i_2, e_{34}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{37} = \text{store}(a_{33}, i_3, e_{36}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{39} = \text{store}(a_{35}, i_3, e_{38}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{41} = \text{store}(a_{37}, i_4, e_{40}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{43} = \text{store}(a_{39}, i_4, e_{42}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{45} = \text{store}(a_{41}, i_5, e_{44}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{47} = \text{store}(a_{43}, i_5, e_{46}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{49} = \text{store}(a_{45}, i_6, e_{48}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{51} = \text{store}(a_{47}, i_6, e_{50}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{53} = \text{store}(a_{49}, i_1, e_{52}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{55} = \text{store}(a_{51}, i_7, e_{54}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{28} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{30} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{32} = \text{select}(a_{31}, i_2) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{34} = \text{select}(a_{29}, i_2) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $e_{36} = \text{select}(a_{35}, i_3) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{38} = \text{select}(a_{33}, i_3) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{40} = \text{select}(a_{39}, i_4) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{42} = \text{select}(a_{37}, i_4) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{44} = \text{select}(a_{43}, i_5) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{46} = \text{select}(a_{41}, i_5) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{48} = \text{select}(a_{47}, i_6) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{50} = \text{select}(a_{45}, i_6) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{52} = \text{select}(a_{51}, i_7) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{54} = \text{select}(a_{49}, i_7) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $a_{53} = a_{55} \quad \text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $a_1 \neq a_2 \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV552-1.010.p** Store inverse (t1\_np\_sf\_ai.00010)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $a_{41} = \text{store}(a_1, i_1, e_{40}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{43} = \text{store}(a_2, i_1, e_{42}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{45} = \text{store}(a_{41}, i_2, e_{44}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{47} = \text{store}(a_{43}, i_2, e_{46}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{49} = \text{store}(a_{45}, i_3, e_{48}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$

$a_{51} = \text{store}(a_{47}, i_3, e_{50})$        $\text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{53} = \text{store}(a_{49}, i_4, e_{52})$        $\text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{55} = \text{store}(a_{51}, i_4, e_{54})$        $\text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{57} = \text{store}(a_{53}, i_5, e_{56})$        $\text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{59} = \text{store}(a_{55}, i_5, e_{58})$        $\text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{61} = \text{store}(a_{57}, i_6, e_{60})$        $\text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{63} = \text{store}(a_{59}, i_6, e_{62})$        $\text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{65} = \text{store}(a_{61}, i_7, e_{64})$        $\text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{67} = \text{store}(a_{63}, i_7, e_{66})$        $\text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $a_{69} = \text{store}(a_{65}, i_8, e_{68})$        $\text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $a_{71} = \text{store}(a_{67}, i_8, e_{70})$        $\text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{73} = \text{store}(a_{69}, i_9, e_{72})$        $\text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_{75} = \text{store}(a_{71}, i_9, e_{74})$        $\text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $a_{77} = \text{store}(a_{73}, i_1, e_{76})$        $\text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{79} = \text{store}(a_{75}, i_{10}, e_{78})$        $\text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{40} = \text{select}(a_2, i_1)$        $\text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{42} = \text{select}(a_1, i_1)$        $\text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{44} = \text{select}(a_{43}, i_2)$        $\text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{46} = \text{select}(a_{41}, i_2)$        $\text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{48} = \text{select}(a_{47}, i_3)$        $\text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{50} = \text{select}(a_{45}, i_3)$        $\text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{52} = \text{select}(a_{51}, i_4)$        $\text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{54} = \text{select}(a_{49}, i_4)$        $\text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{56} = \text{select}(a_{55}, i_5)$        $\text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{58} = \text{select}(a_{53}, i_5)$        $\text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $e_{60} = \text{select}(a_{59}, i_6)$        $\text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $e_{62} = \text{select}(a_{57}, i_6)$        $\text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{64} = \text{select}(a_{63}, i_7)$        $\text{cnf}(\text{hyp}_{32}, \text{hypothesis})$   
 $e_{66} = \text{select}(a_{61}, i_7)$        $\text{cnf}(\text{hyp}_{33}, \text{hypothesis})$   
 $e_{68} = \text{select}(a_{67}, i_8)$        $\text{cnf}(\text{hyp}_{34}, \text{hypothesis})$   
 $e_{70} = \text{select}(a_{65}, i_8)$        $\text{cnf}(\text{hyp}_{35}, \text{hypothesis})$   
 $e_{72} = \text{select}(a_{71}, i_9)$        $\text{cnf}(\text{hyp}_{36}, \text{hypothesis})$   
 $e_{74} = \text{select}(a_{69}, i_9)$        $\text{cnf}(\text{hyp}_{37}, \text{hypothesis})$   
 $e_{76} = \text{select}(a_{75}, i_{10})$        $\text{cnf}(\text{hyp}_{38}, \text{hypothesis})$   
 $e_{78} = \text{select}(a_{73}, i_{10})$        $\text{cnf}(\text{hyp}_{39}, \text{hypothesis})$   
 $a_{77} = a_{79}$        $\text{cnf}(\text{hyp}_{40}, \text{hypothesis})$   
 $a_1 \neq a_2$        $\text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV553-1.004.p** Store inverse (t1\_pp\_nf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e$        $\text{cnf}(a_1, \text{axiom})$   
 $i = j$  or  $\text{select}(\text{store}(a, i, e), j) = \text{select}(a, j)$        $\text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(\text{store}(\text{store}(a_1, i_1, \text{select}(a_2, i_1)), i_2, \text{select}(\text{store}(a_2, i_1, \text{select}(a_1, i_1)), i_2)), i_3, \text{select}(\text{store}(\text{store}(a_2, i_1, \text{select}(a_1, i_1))), \text{store}(\text{store}(\text{store}(\text{store}(a_2, i_1, \text{select}(a_1, i_1)), i_2, \text{select}(\text{store}(a_1, i_1, \text{select}(a_2, i_1)), i_2)), i_3, \text{select}(\text{store}(\text{store}(a_1, i_1, \text{select}(a_2, i_1))), \text{select}(a_1, \text{sk}(a_1, a_2))) \neq \text{select}(a_2, \text{sk}(a_1, a_2))$        $\text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV554-1.004.p** Store inverse (t1\_pp\_nf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e$        $\text{cnf}(a_1, \text{axiom})$   
 $i = j$  or  $\text{select}(\text{store}(a, i, e), j) = \text{select}(a, j)$        $\text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(\text{store}(\text{store}(a_1, i_1, \text{select}(a_2, i_1)), i_2, \text{select}(\text{store}(a_2, i_1, \text{select}(a_1, i_1)), i_2)), i_3, \text{select}(\text{store}(\text{store}(a_2, i_1, \text{select}(a_1, i_1))), \text{store}(\text{store}(\text{store}(\text{store}(a_2, i_1, \text{select}(a_1, i_1)), i_2, \text{select}(\text{store}(a_1, i_1, \text{select}(a_2, i_1)), i_2)), i_3, \text{select}(\text{store}(\text{store}(a_1, i_1, \text{select}(a_2, i_1))), \text{select}(a_1, \text{sk}(a_1, a_2))) \neq \text{select}(a_2, \text{sk}(a_1, a_2))$        $\text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV555-1.004.p** Store inverse (t1\_pp\_sf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e$        $\text{cnf}(a_1, \text{axiom})$   
 $i = j$  or  $\text{select}(\text{store}(a, i, e), j) = \text{select}(a, j)$        $\text{cnf}(a_2, \text{axiom})$

$a_{20} = \text{store}(a_1, i_1, e_{19}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{22} = \text{store}(a_2, i_1, e_{21}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{24} = \text{store}(a_{20}, i_2, e_{23}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{26} = \text{store}(a_{22}, i_2, e_{25}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{28} = \text{store}(a_{24}, i_3, e_{27}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{30} = \text{store}(a_{26}, i_3, e_{29}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{32} = \text{store}(a_{28}, i_4, e_{31}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{34} = \text{store}(a_{30}, i_4, e_{33}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $e_{19} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $e_{21} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $e_{23} = \text{select}(a_{22}, i_2) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $e_{25} = \text{select}(a_{20}, i_2) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $e_{27} = \text{select}(a_{26}, i_3) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $e_{29} = \text{select}(a_{24}, i_3) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{31} = \text{select}(a_{30}, i_4) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{33} = \text{select}(a_{28}, i_4) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{36} = \text{select}(a_1, i_{35}) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{37} = \text{select}(a_2, i_{35}) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $i_{35} = \text{sk}(a_1, a_2) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{32} = a_{34} \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{36} \neq e_{37} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

### SWV555-1.007.p Store inverse (t1\_pp\_sf\_ai\_00007)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $a_{32} = \text{store}(a_1, i_1, e_{31}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{34} = \text{store}(a_2, i_1, e_{33}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{36} = \text{store}(a_{32}, i_2, e_{35}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{38} = \text{store}(a_{34}, i_2, e_{37}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{40} = \text{store}(a_{36}, i_3, e_{39}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{42} = \text{store}(a_{38}, i_3, e_{41}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{44} = \text{store}(a_{40}, i_4, e_{43}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{46} = \text{store}(a_{42}, i_4, e_{45}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{48} = \text{store}(a_{44}, i_5, e_{47}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{50} = \text{store}(a_{46}, i_5, e_{49}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{52} = \text{store}(a_{48}, i_6, e_{51}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{54} = \text{store}(a_{50}, i_6, e_{53}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{56} = \text{store}(a_{52}, i_7, e_{55}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{58} = \text{store}(a_{54}, i_7, e_{57}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{31} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{33} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{35} = \text{select}(a_{34}, i_2) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{37} = \text{select}(a_{32}, i_2) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $e_{39} = \text{select}(a_{38}, i_3) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{41} = \text{select}(a_{36}, i_3) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{43} = \text{select}(a_{42}, i_4) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{45} = \text{select}(a_{40}, i_4) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{47} = \text{select}(a_{46}, i_5) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{49} = \text{select}(a_{44}, i_5) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{51} = \text{select}(a_{50}, i_6) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{53} = \text{select}(a_{48}, i_6) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{55} = \text{select}(a_{54}, i_7) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{57} = \text{select}(a_{52}, i_7) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{60} = \text{select}(a_1, i_{59}) \quad \text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{61} = \text{select}(a_2, i_{59}) \quad \text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $i_{59} = \text{sk}(a_1, a_2) \quad \text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $a_{56} = a_{58} \quad \text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{60} \neq e_{61} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV555-1.010.p** Store inverse (t1\_pp\_sf\_ai\_00010)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

```

select(store(a, i, e), i) = e      cnf(a1, axiom)
i = j or select(store(a, i, e), j) = select(a, j)      cnf(a2, axiom)
a44 = store(a1, i1, e43)      cnf(hyp0, hypothesis)
a46 = store(a2, i1, e45)      cnf(hyp1, hypothesis)
a48 = store(a44, i2, e47)      cnf(hyp2, hypothesis)
a50 = store(a46, i2, e49)      cnf(hyp3, hypothesis)
a52 = store(a48, i3, e51)      cnf(hyp4, hypothesis)
a54 = store(a50, i3, e53)      cnf(hyp5, hypothesis)
a56 = store(a52, i4, e55)      cnf(hyp6, hypothesis)
a58 = store(a54, i4, e57)      cnf(hyp7, hypothesis)
a60 = store(a56, i5, e59)      cnf(hyp8, hypothesis)
a62 = store(a58, i5, e61)      cnf(hyp9, hypothesis)
a64 = store(a60, i6, e63)      cnf(hyp10, hypothesis)
a66 = store(a62, i6, e65)      cnf(hyp11, hypothesis)
a68 = store(a64, i7, e67)      cnf(hyp12, hypothesis)
a70 = store(a66, i7, e69)      cnf(hyp13, hypothesis)
a72 = store(a68, i8, e71)      cnf(hyp14, hypothesis)
a74 = store(a70, i8, e73)      cnf(hyp15, hypothesis)
a76 = store(a72, i9, e75)      cnf(hyp16, hypothesis)
a78 = store(a74, i9, e77)      cnf(hyp17, hypothesis)
a80 = store(a76, i10, e79)      cnf(hyp18, hypothesis)
a82 = store(a78, i10, e81)      cnf(hyp19, hypothesis)
e43 = select(a2, i1)      cnf(hyp20, hypothesis)
e45 = select(a1, i1)      cnf(hyp21, hypothesis)
e47 = select(a46, i2)      cnf(hyp22, hypothesis)
e49 = select(a44, i2)      cnf(hyp23, hypothesis)
e51 = select(a50, i3)      cnf(hyp24, hypothesis)
e53 = select(a48, i3)      cnf(hyp25, hypothesis)
e55 = select(a54, i4)      cnf(hyp26, hypothesis)
e57 = select(a52, i4)      cnf(hyp27, hypothesis)
e59 = select(a58, i5)      cnf(hyp28, hypothesis)
e61 = select(a56, i5)      cnf(hyp29, hypothesis)
e63 = select(a62, i6)      cnf(hyp30, hypothesis)
e65 = select(a60, i6)      cnf(hyp31, hypothesis)
e67 = select(a66, i7)      cnf(hyp32, hypothesis)
e69 = select(a64, i7)      cnf(hyp33, hypothesis)
e71 = select(a70, i8)      cnf(hyp34, hypothesis)
e73 = select(a68, i8)      cnf(hyp35, hypothesis)
e75 = select(a74, i9)      cnf(hyp36, hypothesis)
e77 = select(a72, i9)      cnf(hyp37, hypothesis)
e79 = select(a78, i10)      cnf(hyp38, hypothesis)
e81 = select(a76, i10)      cnf(hyp39, hypothesis)
e84 = select(a1, i83)      cnf(hyp40, hypothesis)
e85 = select(a2, i83)      cnf(hyp41, hypothesis)
i83 = sk(a1, a2)      cnf(hyp42, hypothesis)
a80 = a82      cnf(hyp43, hypothesis)
e84 ≠ e85      cnf(goal, negated_conjecture)

```

**SWV556-1.004.p** Store inverse (t1\_pp\_sf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

```

select(store(a, i, e), i) = e      cnf(a1, axiom)
i = j or select(store(a, i, e), j) = select(a, j)      cnf(a2, axiom)
a20 = store(a1, i1, e19)      cnf(hyp0, hypothesis)
a22 = store(a2, i1, e21)      cnf(hyp1, hypothesis)
a24 = store(a20, i2, e23)      cnf(hyp2, hypothesis)
a26 = store(a22, i2, e25)      cnf(hyp3, hypothesis)

```

$a_{28} = \text{store}(a_{24}, i_3, e_{27}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{30} = \text{store}(a_{26}, i_3, e_{29}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{32} = \text{store}(a_{28}, i_1, e_{31}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{34} = \text{store}(a_{30}, i_4, e_{33}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $e_{19} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $e_{21} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $e_{23} = \text{select}(a_{22}, i_2) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $e_{25} = \text{select}(a_{20}, i_2) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $e_{27} = \text{select}(a_{26}, i_3) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $e_{29} = \text{select}(a_{24}, i_3) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{31} = \text{select}(a_{30}, i_4) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{33} = \text{select}(a_{28}, i_4) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{36} = \text{select}(a_1, i_{35}) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{37} = \text{select}(a_2, i_{35}) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $i_{35} = \text{sk}(a_1, a_2) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{32} = a_{34} \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{36} \neq e_{37} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV556-1.007.p** Store inverse (t1\_pp\_sf\_ai.00007)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $a_{32} = \text{store}(a_1, i_1, e_{31}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{34} = \text{store}(a_2, i_1, e_{33}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{36} = \text{store}(a_{32}, i_2, e_{35}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{38} = \text{store}(a_{34}, i_2, e_{37}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{40} = \text{store}(a_{36}, i_3, e_{39}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{42} = \text{store}(a_{38}, i_3, e_{41}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{44} = \text{store}(a_{40}, i_4, e_{43}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{46} = \text{store}(a_{42}, i_4, e_{45}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{48} = \text{store}(a_{44}, i_5, e_{47}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{50} = \text{store}(a_{46}, i_5, e_{49}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{52} = \text{store}(a_{48}, i_6, e_{51}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{54} = \text{store}(a_{50}, i_6, e_{53}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{56} = \text{store}(a_{52}, i_1, e_{55}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{58} = \text{store}(a_{54}, i_7, e_{57}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{31} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{33} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{35} = \text{select}(a_{34}, i_2) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{37} = \text{select}(a_{32}, i_2) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $e_{39} = \text{select}(a_{38}, i_3) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{41} = \text{select}(a_{36}, i_3) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{43} = \text{select}(a_{42}, i_4) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{45} = \text{select}(a_{40}, i_4) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{47} = \text{select}(a_{46}, i_5) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{49} = \text{select}(a_{44}, i_5) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{51} = \text{select}(a_{50}, i_6) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{53} = \text{select}(a_{48}, i_6) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{55} = \text{select}(a_{54}, i_7) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{57} = \text{select}(a_{52}, i_7) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{60} = \text{select}(a_1, i_{59}) \quad \text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{61} = \text{select}(a_2, i_{59}) \quad \text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $i_{59} = \text{sk}(a_1, a_2) \quad \text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $a_{56} = a_{58} \quad \text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{60} \neq e_{61} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV556-1.010.p** Store inverse (t1\_pp\_sf\_ai.00010)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

```

select(store(a, i, e), i) = e    cnf(a1, axiom)
i = j or select(store(a, i, e), j) = select(a, j)    cnf(a2, axiom)
a44 = store(a1, i1, e43)    cnf(hyp0, hypothesis)
a46 = store(a2, i1, e45)    cnf(hyp1, hypothesis)
a48 = store(a44, i2, e47)    cnf(hyp2, hypothesis)
a50 = store(a46, i2, e49)    cnf(hyp3, hypothesis)
a52 = store(a48, i3, e51)    cnf(hyp4, hypothesis)
a54 = store(a50, i3, e53)    cnf(hyp5, hypothesis)
a56 = store(a52, i4, e55)    cnf(hyp6, hypothesis)
a58 = store(a54, i4, e57)    cnf(hyp7, hypothesis)
a60 = store(a56, i5, e59)    cnf(hyp8, hypothesis)
a62 = store(a58, i5, e61)    cnf(hyp9, hypothesis)
a64 = store(a60, i6, e63)    cnf(hyp10, hypothesis)
a66 = store(a62, i6, e65)    cnf(hyp11, hypothesis)
a68 = store(a64, i7, e67)    cnf(hyp12, hypothesis)
a70 = store(a66, i7, e69)    cnf(hyp13, hypothesis)
a72 = store(a68, i8, e71)    cnf(hyp14, hypothesis)
a74 = store(a70, i8, e73)    cnf(hyp15, hypothesis)
a76 = store(a72, i9, e75)    cnf(hyp16, hypothesis)
a78 = store(a74, i9, e77)    cnf(hyp17, hypothesis)
a80 = store(a76, i1, e79)    cnf(hyp18, hypothesis)
a82 = store(a78, i10, e81)    cnf(hyp19, hypothesis)
e43 = select(a2, i1)    cnf(hyp20, hypothesis)
e45 = select(a1, i1)    cnf(hyp21, hypothesis)
e47 = select(a46, i2)    cnf(hyp22, hypothesis)
e49 = select(a44, i2)    cnf(hyp23, hypothesis)
e51 = select(a50, i3)    cnf(hyp24, hypothesis)
e53 = select(a48, i3)    cnf(hyp25, hypothesis)
e55 = select(a54, i4)    cnf(hyp26, hypothesis)
e57 = select(a52, i4)    cnf(hyp27, hypothesis)
e59 = select(a58, i5)    cnf(hyp28, hypothesis)
e61 = select(a56, i5)    cnf(hyp29, hypothesis)
e63 = select(a62, i6)    cnf(hyp30, hypothesis)
e65 = select(a60, i6)    cnf(hyp31, hypothesis)
e67 = select(a66, i7)    cnf(hyp32, hypothesis)
e69 = select(a64, i7)    cnf(hyp33, hypothesis)
e71 = select(a70, i8)    cnf(hyp34, hypothesis)
e73 = select(a68, i8)    cnf(hyp35, hypothesis)
e75 = select(a74, i9)    cnf(hyp36, hypothesis)
e77 = select(a72, i9)    cnf(hyp37, hypothesis)
e79 = select(a78, i10)    cnf(hyp38, hypothesis)
e81 = select(a76, i10)    cnf(hyp39, hypothesis)
e84 = select(a1, i83)    cnf(hyp40, hypothesis)
e85 = select(a2, i83)    cnf(hyp41, hypothesis)
i83 = sk(a1, a2)    cnf(hyp42, hypothesis)
a80 = a82    cnf(hyp43, hypothesis)
e84 ≠ e85    cnf(goal, negated_conjecture)

```

#### SWV557-1.004.p Store inverse (t2\_np\_nf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

```

select(store(a, i, e), i) = e    cnf(a1, axiom)
i = j or select(store(a, i, e), j) = select(a, j)    cnf(a2, axiom)
store(a, i, select(a, i)) = a    cnf(a3, axiom)
store(store(a, i, e), i, f) = store(a, i, f)    cnf(a4, axiom)
i = j or store(store(a, i, e), j, f) = store(store(a, j, f), i, e)    cnf(a5, axiom)
store(store(store(store(a1, i1, select(a2, i1)), i2, select(store(a2, i1, select(a1, i1)), i2)), i3, select(store(store(a2, i1, select(a1, i1)), store(store(store(store(a2, i1, select(a1, i1)), i2, select(store(a1, i1, select(a2, i1)), i2)), i3, select(store(store(a1, i1, select(a2, i1)), a1 ≠ a2    cnf(goal, negated_conjecture)

```

**SWV558-1.004.p** Store inverse (t2\_np\_sf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

```

select(store(a, i, e), i) = e      cnf(a1, axiom)
i = j or select(store(a, i, e), j) = select(a, j)      cnf(a2, axiom)
store(a, i, select(a, i)) = a      cnf(a3, axiom)
store(store(a, i, e), i, f) = store(a, i, f)      cnf(a4, axiom)
i = j or store(store(a, i, e), j, f) = store(store(a, j, f), i, e)      cnf(a5, axiom)
a17 = store(a1, i1, e16)      cnf(hyp0, hypothesis)
a19 = store(a2, i1, e18)      cnf(hyp1, hypothesis)
a21 = store(a17, i2, e20)      cnf(hyp2, hypothesis)
a23 = store(a19, i2, e22)      cnf(hyp3, hypothesis)
a25 = store(a21, i3, e24)      cnf(hyp4, hypothesis)
a27 = store(a23, i3, e26)      cnf(hyp5, hypothesis)
a29 = store(a25, i4, e28)      cnf(hyp6, hypothesis)
a31 = store(a27, i4, e30)      cnf(hyp7, hypothesis)
e16 = select(a2, i1)      cnf(hyp8, hypothesis)
e18 = select(a1, i1)      cnf(hyp9, hypothesis)
e20 = select(a19, i2)      cnf(hyp10, hypothesis)
e22 = select(a17, i2)      cnf(hyp11, hypothesis)
e24 = select(a23, i3)      cnf(hyp12, hypothesis)
e26 = select(a21, i3)      cnf(hyp13, hypothesis)
e28 = select(a27, i4)      cnf(hyp14, hypothesis)
e30 = select(a25, i4)      cnf(hyp15, hypothesis)
a29 = a31      cnf(hyp16, hypothesis)
a1 ≠ a2      cnf(goal, negated_conjecture)

```

**SWV558-1.007.p** Store inverse (t2\_np\_sf\_ai\_00007)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

```

select(store(a, i, e), i) = e      cnf(a1, axiom)
i = j or select(store(a, i, e), j) = select(a, j)      cnf(a2, axiom)
store(a, i, select(a, i)) = a      cnf(a3, axiom)
store(store(a, i, e), i, f) = store(a, i, f)      cnf(a4, axiom)
i = j or store(store(a, i, e), j, f) = store(store(a, j, f), i, e)      cnf(a5, axiom)
a29 = store(a1, i1, e28)      cnf(hyp0, hypothesis)
a31 = store(a2, i1, e30)      cnf(hyp1, hypothesis)
a33 = store(a29, i2, e32)      cnf(hyp2, hypothesis)
a35 = store(a31, i2, e34)      cnf(hyp3, hypothesis)
a37 = store(a33, i3, e36)      cnf(hyp4, hypothesis)
a39 = store(a35, i3, e38)      cnf(hyp5, hypothesis)
a41 = store(a37, i4, e40)      cnf(hyp6, hypothesis)
a43 = store(a39, i4, e42)      cnf(hyp7, hypothesis)
a45 = store(a41, i5, e44)      cnf(hyp8, hypothesis)
a47 = store(a43, i5, e46)      cnf(hyp9, hypothesis)
a49 = store(a45, i6, e48)      cnf(hyp10, hypothesis)
a51 = store(a47, i6, e50)      cnf(hyp11, hypothesis)
a53 = store(a49, i7, e52)      cnf(hyp12, hypothesis)
a55 = store(a51, i7, e54)      cnf(hyp13, hypothesis)
e28 = select(a2, i1)      cnf(hyp14, hypothesis)
e30 = select(a1, i1)      cnf(hyp15, hypothesis)
e32 = select(a31, i2)      cnf(hyp16, hypothesis)
e34 = select(a29, i2)      cnf(hyp17, hypothesis)
e36 = select(a35, i3)      cnf(hyp18, hypothesis)
e38 = select(a33, i3)      cnf(hyp19, hypothesis)
e40 = select(a39, i4)      cnf(hyp20, hypothesis)
e42 = select(a37, i4)      cnf(hyp21, hypothesis)
e44 = select(a43, i5)      cnf(hyp22, hypothesis)
e46 = select(a41, i5)      cnf(hyp23, hypothesis)
e48 = select(a47, i6)      cnf(hyp24, hypothesis)

```

$e_{50} = \text{select}(a_{45}, i_6) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{52} = \text{select}(a_{51}, i_7) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{54} = \text{select}(a_{49}, i_7) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $a_{53} = a_{55} \quad \text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $a_1 \neq a_2 \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV558-1.010.p** Store inverse (t2\_np\_sf\_ai\_00010)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(a, i, \text{select}(a, i)) = a \quad \text{cnf}(a_3, \text{axiom})$   
 $\text{store}(\text{store}(a, i, e), i, f) = \text{store}(a, i, f) \quad \text{cnf}(a_4, \text{axiom})$   
 $i = j \text{ or } \text{store}(\text{store}(a, i, e), j, f) = \text{store}(\text{store}(a, j, f), i, e) \quad \text{cnf}(a_5, \text{axiom})$   
 $a_{41} = \text{store}(a_1, i_1, e_{40}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{43} = \text{store}(a_2, i_1, e_{42}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{45} = \text{store}(a_{41}, i_2, e_{44}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{47} = \text{store}(a_{43}, i_2, e_{46}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{49} = \text{store}(a_{45}, i_3, e_{48}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{51} = \text{store}(a_{47}, i_3, e_{50}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{53} = \text{store}(a_{49}, i_4, e_{52}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{55} = \text{store}(a_{51}, i_4, e_{54}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{57} = \text{store}(a_{53}, i_5, e_{56}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{59} = \text{store}(a_{55}, i_5, e_{58}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{61} = \text{store}(a_{57}, i_6, e_{60}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{63} = \text{store}(a_{59}, i_6, e_{62}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{65} = \text{store}(a_{61}, i_7, e_{64}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{67} = \text{store}(a_{63}, i_7, e_{66}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $a_{69} = \text{store}(a_{65}, i_8, e_{68}) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $a_{71} = \text{store}(a_{67}, i_8, e_{70}) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{73} = \text{store}(a_{69}, i_9, e_{72}) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_{75} = \text{store}(a_{71}, i_9, e_{74}) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $a_{77} = \text{store}(a_{73}, i_{10}, e_{76}) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{79} = \text{store}(a_{75}, i_{10}, e_{78}) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{40} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{42} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{44} = \text{select}(a_{43}, i_2) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{46} = \text{select}(a_{41}, i_2) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{48} = \text{select}(a_{47}, i_3) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{50} = \text{select}(a_{45}, i_3) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{52} = \text{select}(a_{51}, i_4) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{54} = \text{select}(a_{49}, i_4) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{56} = \text{select}(a_{55}, i_5) \quad \text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{58} = \text{select}(a_{53}, i_5) \quad \text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $e_{60} = \text{select}(a_{59}, i_6) \quad \text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $e_{62} = \text{select}(a_{57}, i_6) \quad \text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{64} = \text{select}(a_{63}, i_7) \quad \text{cnf}(\text{hyp}_{32}, \text{hypothesis})$   
 $e_{66} = \text{select}(a_{61}, i_7) \quad \text{cnf}(\text{hyp}_{33}, \text{hypothesis})$   
 $e_{68} = \text{select}(a_{67}, i_8) \quad \text{cnf}(\text{hyp}_{34}, \text{hypothesis})$   
 $e_{70} = \text{select}(a_{65}, i_8) \quad \text{cnf}(\text{hyp}_{35}, \text{hypothesis})$   
 $e_{72} = \text{select}(a_{71}, i_9) \quad \text{cnf}(\text{hyp}_{36}, \text{hypothesis})$   
 $e_{74} = \text{select}(a_{69}, i_9) \quad \text{cnf}(\text{hyp}_{37}, \text{hypothesis})$   
 $e_{76} = \text{select}(a_{75}, i_{10}) \quad \text{cnf}(\text{hyp}_{38}, \text{hypothesis})$   
 $e_{78} = \text{select}(a_{73}, i_{10}) \quad \text{cnf}(\text{hyp}_{39}, \text{hypothesis})$   
 $a_{77} = a_{79} \quad \text{cnf}(\text{hyp}_{40}, \text{hypothesis})$   
 $a_1 \neq a_2 \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV559-1.004.p** Store inverse (t3\_np\_nf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.



$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j)) \quad \text{cnf}(a_3, \text{axiom})$   
 $\text{store}(\text{store}(\text{store}(\text{store}(a_1, i_1, \text{select}(a_2, i_1)), i_2, \text{select}(\text{store}(a_2, i_1, \text{select}(a_1, i_1)), i_2)), i_3, \text{select}(\text{store}(\text{store}(a_2, i_1, \text{select}(a_1, i_1))),$   
 $\text{store}(\text{store}(\text{store}(\text{store}(a_2, i_1, \text{select}(a_1, i_1)), i_2, \text{select}(\text{store}(a_1, i_1, \text{select}(a_2, i_1)), i_2)), i_3, \text{select}(\text{store}(\text{store}(a_1, i_1, \text{select}(a_2, i_1))),$   
 $a_1 \neq a_2 \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV560-1.004.p** Store inverse (t3\_np\_nf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j)) \quad \text{cnf}(a_3, \text{axiom})$   
 $\text{store}(\text{store}(\text{store}(\text{store}(a_1, i_1, \text{select}(a_2, i_1)), i_2, \text{select}(\text{store}(a_2, i_1, \text{select}(a_1, i_1)), i_2)), i_3, \text{select}(\text{store}(\text{store}(a_2, i_1, \text{select}(a_1, i_1))),$   
 $\text{store}(\text{store}(\text{store}(\text{store}(a_2, i_1, \text{select}(a_1, i_1)), i_2, \text{select}(\text{store}(a_1, i_1, \text{select}(a_2, i_1)), i_2)), i_3, \text{select}(\text{store}(\text{store}(a_1, i_1, \text{select}(a_2, i_1))),$   
 $a_1 \neq a_2 \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV561-1.004.p** Store inverse (t3\_np\_sf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j)) \quad \text{cnf}(a_3, \text{axiom})$   
 $a_{17} = \text{store}(a_1, i_1, e_{16}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{19} = \text{store}(a_2, i_1, e_{18}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{21} = \text{store}(a_{17}, i_2, e_{20}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{23} = \text{store}(a_{19}, i_2, e_{22}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{25} = \text{store}(a_{21}, i_3, e_{24}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{27} = \text{store}(a_{23}, i_3, e_{26}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{29} = \text{store}(a_{25}, i_4, e_{28}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{31} = \text{store}(a_{27}, i_4, e_{30}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $e_{16} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $e_{18} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $e_{20} = \text{select}(a_{19}, i_2) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $e_{22} = \text{select}(a_{17}, i_2) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $e_{24} = \text{select}(a_{23}, i_3) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $e_{26} = \text{select}(a_{21}, i_3) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{28} = \text{select}(a_{27}, i_4) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{30} = \text{select}(a_{25}, i_4) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{29} = a_{31} \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_1 \neq a_2 \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV561-1.007.p** Store inverse (t3\_np\_sf\_ai\_00007)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j)) \quad \text{cnf}(a_3, \text{axiom})$   
 $a_{29} = \text{store}(a_1, i_1, e_{28}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{31} = \text{store}(a_2, i_1, e_{30}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{33} = \text{store}(a_{29}, i_2, e_{32}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{35} = \text{store}(a_{31}, i_2, e_{34}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{37} = \text{store}(a_{33}, i_3, e_{36}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{39} = \text{store}(a_{35}, i_3, e_{38}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{41} = \text{store}(a_{37}, i_4, e_{40}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{43} = \text{store}(a_{39}, i_4, e_{42}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{45} = \text{store}(a_{41}, i_5, e_{44}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{47} = \text{store}(a_{43}, i_5, e_{46}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{49} = \text{store}(a_{45}, i_6, e_{48}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{51} = \text{store}(a_{47}, i_6, e_{50}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{53} = \text{store}(a_{49}, i_7, e_{52}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$

$a_{55} = \text{store}(a_{51}, i_7, e_{54}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{28} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{30} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{32} = \text{select}(a_{31}, i_2) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{34} = \text{select}(a_{29}, i_2) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $e_{36} = \text{select}(a_{35}, i_3) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{38} = \text{select}(a_{33}, i_3) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{40} = \text{select}(a_{39}, i_4) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{42} = \text{select}(a_{37}, i_4) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{44} = \text{select}(a_{43}, i_5) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{46} = \text{select}(a_{41}, i_5) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{48} = \text{select}(a_{47}, i_6) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{50} = \text{select}(a_{45}, i_6) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{52} = \text{select}(a_{51}, i_7) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{54} = \text{select}(a_{49}, i_7) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $a_{53} = a_{55} \quad \text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $a_1 \neq a_2 \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

### SWV561-1.010.p Store inverse (t3\_np\_sf\_ai\_00010)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j)) \quad \text{cnf}(a_3, \text{axiom})$   
 $a_{41} = \text{store}(a_1, i_1, e_{40}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{43} = \text{store}(a_2, i_1, e_{42}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{45} = \text{store}(a_{41}, i_2, e_{44}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{47} = \text{store}(a_{43}, i_2, e_{46}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{49} = \text{store}(a_{45}, i_3, e_{48}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{51} = \text{store}(a_{47}, i_3, e_{50}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{53} = \text{store}(a_{49}, i_4, e_{52}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{55} = \text{store}(a_{51}, i_4, e_{54}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{57} = \text{store}(a_{53}, i_5, e_{56}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{59} = \text{store}(a_{55}, i_5, e_{58}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{61} = \text{store}(a_{57}, i_6, e_{60}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{63} = \text{store}(a_{59}, i_6, e_{62}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{65} = \text{store}(a_{61}, i_7, e_{64}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{67} = \text{store}(a_{63}, i_7, e_{66}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $a_{69} = \text{store}(a_{65}, i_8, e_{68}) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $a_{71} = \text{store}(a_{67}, i_8, e_{70}) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{73} = \text{store}(a_{69}, i_9, e_{72}) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_{75} = \text{store}(a_{71}, i_9, e_{74}) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $a_{77} = \text{store}(a_{73}, i_{10}, e_{76}) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{79} = \text{store}(a_{75}, i_{10}, e_{78}) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{40} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{42} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{44} = \text{select}(a_{43}, i_2) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{46} = \text{select}(a_{41}, i_2) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{48} = \text{select}(a_{47}, i_3) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{50} = \text{select}(a_{45}, i_3) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{52} = \text{select}(a_{51}, i_4) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{54} = \text{select}(a_{49}, i_4) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{56} = \text{select}(a_{55}, i_5) \quad \text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{58} = \text{select}(a_{53}, i_5) \quad \text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $e_{60} = \text{select}(a_{59}, i_6) \quad \text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $e_{62} = \text{select}(a_{57}, i_6) \quad \text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{64} = \text{select}(a_{63}, i_7) \quad \text{cnf}(\text{hyp}_{32}, \text{hypothesis})$   
 $e_{66} = \text{select}(a_{61}, i_7) \quad \text{cnf}(\text{hyp}_{33}, \text{hypothesis})$   
 $e_{68} = \text{select}(a_{67}, i_8) \quad \text{cnf}(\text{hyp}_{34}, \text{hypothesis})$   
 $e_{70} = \text{select}(a_{65}, i_8) \quad \text{cnf}(\text{hyp}_{35}, \text{hypothesis})$

$e_{72} = \text{select}(a_{71}, i_9) \quad \text{cnf}(\text{hyp}_{36}, \text{hypothesis})$   
 $e_{74} = \text{select}(a_{69}, i_9) \quad \text{cnf}(\text{hyp}_{37}, \text{hypothesis})$   
 $e_{76} = \text{select}(a_{75}, i_{10}) \quad \text{cnf}(\text{hyp}_{38}, \text{hypothesis})$   
 $e_{78} = \text{select}(a_{73}, i_{10}) \quad \text{cnf}(\text{hyp}_{39}, \text{hypothesis})$   
 $a_{77} = a_{79} \quad \text{cnf}(\text{hyp}_{40}, \text{hypothesis})$   
 $a_1 \neq a_2 \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV562-1.004.p** Store inverse (t3\_np\_sf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j)) \quad \text{cnf}(a_3, \text{axiom})$   
 $a_{17} = \text{store}(a_1, i_1, e_{16}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{19} = \text{store}(a_2, i_1, e_{18}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{21} = \text{store}(a_{17}, i_2, e_{20}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{23} = \text{store}(a_{19}, i_2, e_{22}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{25} = \text{store}(a_{21}, i_3, e_{24}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{27} = \text{store}(a_{23}, i_3, e_{26}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{29} = \text{store}(a_{25}, i_1, e_{28}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{31} = \text{store}(a_{27}, i_4, e_{30}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $e_{16} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $e_{18} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $e_{20} = \text{select}(a_{19}, i_2) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $e_{22} = \text{select}(a_{17}, i_2) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $e_{24} = \text{select}(a_{23}, i_3) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $e_{26} = \text{select}(a_{21}, i_3) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{28} = \text{select}(a_{27}, i_4) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{30} = \text{select}(a_{25}, i_4) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{29} = a_{31} \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_1 \neq a_2 \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV562-1.007.p** Store inverse (t3\_np\_sf\_ai\_00007)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j)) \quad \text{cnf}(a_3, \text{axiom})$   
 $a_{29} = \text{store}(a_1, i_1, e_{28}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{31} = \text{store}(a_2, i_1, e_{30}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{33} = \text{store}(a_{29}, i_2, e_{32}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{35} = \text{store}(a_{31}, i_2, e_{34}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{37} = \text{store}(a_{33}, i_3, e_{36}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{39} = \text{store}(a_{35}, i_3, e_{38}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{41} = \text{store}(a_{37}, i_4, e_{40}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{43} = \text{store}(a_{39}, i_4, e_{42}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{45} = \text{store}(a_{41}, i_5, e_{44}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{47} = \text{store}(a_{43}, i_5, e_{46}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{49} = \text{store}(a_{45}, i_6, e_{48}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{51} = \text{store}(a_{47}, i_6, e_{50}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{53} = \text{store}(a_{49}, i_1, e_{52}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{55} = \text{store}(a_{51}, i_7, e_{54}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{28} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{30} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{32} = \text{select}(a_{31}, i_2) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{34} = \text{select}(a_{29}, i_2) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $e_{36} = \text{select}(a_{35}, i_3) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{38} = \text{select}(a_{33}, i_3) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{40} = \text{select}(a_{39}, i_4) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{42} = \text{select}(a_{37}, i_4) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$

$e_{44} = \text{select}(a_{43}, i_5)$        $\text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{46} = \text{select}(a_{41}, i_5)$        $\text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{48} = \text{select}(a_{47}, i_6)$        $\text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{50} = \text{select}(a_{45}, i_6)$        $\text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{52} = \text{select}(a_{51}, i_7)$        $\text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{54} = \text{select}(a_{49}, i_7)$        $\text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $a_{53} = a_{55}$        $\text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $a_1 \neq a_2$        $\text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV562-1.010.p** Store inverse (t3\_np\_sf\_ai\_00010)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e$        $\text{cnf}(a_1, \text{axiom})$   
 $i = j$  or  $\text{select}(\text{store}(a, i, e), j) = \text{select}(a, j)$        $\text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j))$        $\text{cnf}(a_3, \text{axiom})$   
 $a_{41} = \text{store}(a_1, i_1, e_{40})$        $\text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{43} = \text{store}(a_2, i_1, e_{42})$        $\text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{45} = \text{store}(a_{41}, i_2, e_{44})$        $\text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{47} = \text{store}(a_{43}, i_2, e_{46})$        $\text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{49} = \text{store}(a_{45}, i_3, e_{48})$        $\text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{51} = \text{store}(a_{47}, i_3, e_{50})$        $\text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{53} = \text{store}(a_{49}, i_4, e_{52})$        $\text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{55} = \text{store}(a_{51}, i_4, e_{54})$        $\text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{57} = \text{store}(a_{53}, i_5, e_{56})$        $\text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{59} = \text{store}(a_{55}, i_5, e_{58})$        $\text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{61} = \text{store}(a_{57}, i_6, e_{60})$        $\text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{63} = \text{store}(a_{59}, i_6, e_{62})$        $\text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{65} = \text{store}(a_{61}, i_7, e_{64})$        $\text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{67} = \text{store}(a_{63}, i_7, e_{66})$        $\text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $a_{69} = \text{store}(a_{65}, i_8, e_{68})$        $\text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $a_{71} = \text{store}(a_{67}, i_8, e_{70})$        $\text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{73} = \text{store}(a_{69}, i_9, e_{72})$        $\text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_{75} = \text{store}(a_{71}, i_9, e_{74})$        $\text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $a_{77} = \text{store}(a_{73}, i_{10}, e_{76})$        $\text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{79} = \text{store}(a_{75}, i_{10}, e_{78})$        $\text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{40} = \text{select}(a_2, i_1)$        $\text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{42} = \text{select}(a_1, i_1)$        $\text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{44} = \text{select}(a_{43}, i_2)$        $\text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{46} = \text{select}(a_{41}, i_2)$        $\text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{48} = \text{select}(a_{47}, i_3)$        $\text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{50} = \text{select}(a_{45}, i_3)$        $\text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{52} = \text{select}(a_{51}, i_4)$        $\text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{54} = \text{select}(a_{49}, i_4)$        $\text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{56} = \text{select}(a_{55}, i_5)$        $\text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{58} = \text{select}(a_{53}, i_5)$        $\text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $e_{60} = \text{select}(a_{59}, i_6)$        $\text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $e_{62} = \text{select}(a_{57}, i_6)$        $\text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{64} = \text{select}(a_{63}, i_7)$        $\text{cnf}(\text{hyp}_{32}, \text{hypothesis})$   
 $e_{66} = \text{select}(a_{61}, i_7)$        $\text{cnf}(\text{hyp}_{33}, \text{hypothesis})$   
 $e_{68} = \text{select}(a_{67}, i_8)$        $\text{cnf}(\text{hyp}_{34}, \text{hypothesis})$   
 $e_{70} = \text{select}(a_{65}, i_8)$        $\text{cnf}(\text{hyp}_{35}, \text{hypothesis})$   
 $e_{72} = \text{select}(a_{71}, i_9)$        $\text{cnf}(\text{hyp}_{36}, \text{hypothesis})$   
 $e_{74} = \text{select}(a_{69}, i_9)$        $\text{cnf}(\text{hyp}_{37}, \text{hypothesis})$   
 $e_{76} = \text{select}(a_{75}, i_{10})$        $\text{cnf}(\text{hyp}_{38}, \text{hypothesis})$   
 $e_{78} = \text{select}(a_{73}, i_{10})$        $\text{cnf}(\text{hyp}_{39}, \text{hypothesis})$   
 $a_{77} = a_{79}$        $\text{cnf}(\text{hyp}_{40}, \text{hypothesis})$   
 $a_1 \neq a_2$        $\text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV563-1.004.p** Store inverse (t3\_pp\_nf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

```

select(store(a, i, e), i) = e      cnf(a1, axiom)
i = j or select(store(a, i, e), j) = select(a, j)      cnf(a2, axiom)
store(store(a, i, select(a, j)), j, select(a, i)) = store(store(a, j, select(a, i)), i, select(a, j))      cnf(a3, axiom)
store(store(store(store(a1, i1, select(a2, i1)), i2, select(store(a2, i1, select(a1, i1)), i2)), i3, select(store(store(a2, i1, select(a1, i1)),
store(store(store(store(a2, i1, select(a1, i1)), i2, select(store(a1, i1, select(a2, i1)), i2)), i3, select(store(store(a1, i1, select(a2, i1)),
select(a1, sk(a1, a2)) ≠ select(a2, sk(a1, a2))      cnf(goal, negated_conjecture)

```

#### SWV564-1.004.p Store inverse (t3\_pp\_nf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

```

select(store(a, i, e), i) = e      cnf(a1, axiom)
i = j or select(store(a, i, e), j) = select(a, j)      cnf(a2, axiom)
store(store(a, i, select(a, j)), j, select(a, i)) = store(store(a, j, select(a, i)), i, select(a, j))      cnf(a3, axiom)
store(store(store(store(a1, i1, select(a2, i1)), i2, select(store(a2, i1, select(a1, i1)), i2)), i3, select(store(store(a2, i1, select(a1, i1)),
store(store(store(store(a2, i1, select(a1, i1)), i2, select(store(a1, i1, select(a2, i1)), i2)), i3, select(store(store(a1, i1, select(a2, i1)),
select(a1, sk(a1, a2)) ≠ select(a2, sk(a1, a2))      cnf(goal, negated_conjecture)

```

#### SWV565-1.004.p Store inverse (t3\_pp\_sf\_ai\_00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

```

select(store(a, i, e), i) = e      cnf(a1, axiom)
i = j or select(store(a, i, e), j) = select(a, j)      cnf(a2, axiom)
store(store(a, i, select(a, j)), j, select(a, i)) = store(store(a, j, select(a, i)), i, select(a, j))      cnf(a3, axiom)
a20 = store(a1, i1, e19)      cnf(hyp0, hypothesis)
a22 = store(a2, i1, e21)      cnf(hyp1, hypothesis)
a24 = store(a20, i2, e23)      cnf(hyp2, hypothesis)
a26 = store(a22, i2, e25)      cnf(hyp3, hypothesis)
a28 = store(a24, i3, e27)      cnf(hyp4, hypothesis)
a30 = store(a26, i3, e29)      cnf(hyp5, hypothesis)
a32 = store(a28, i4, e31)      cnf(hyp6, hypothesis)
a34 = store(a30, i4, e33)      cnf(hyp7, hypothesis)
e19 = select(a2, i1)      cnf(hyp8, hypothesis)
e21 = select(a1, i1)      cnf(hyp9, hypothesis)
e23 = select(a22, i2)      cnf(hyp10, hypothesis)
e25 = select(a20, i2)      cnf(hyp11, hypothesis)
e27 = select(a26, i3)      cnf(hyp12, hypothesis)
e29 = select(a24, i3)      cnf(hyp13, hypothesis)
e31 = select(a30, i4)      cnf(hyp14, hypothesis)
e33 = select(a28, i4)      cnf(hyp15, hypothesis)
e36 = select(a1, i35)      cnf(hyp16, hypothesis)
e37 = select(a2, i35)      cnf(hyp17, hypothesis)
i35 = sk(a1, a2)      cnf(hyp18, hypothesis)
a32 = a34      cnf(hyp19, hypothesis)
e36 ≠ e37      cnf(goal, negated_conjecture)

```

#### SWV565-1.007.p Store inverse (t3\_pp\_sf\_ai\_00007)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

```

select(store(a, i, e), i) = e      cnf(a1, axiom)
i = j or select(store(a, i, e), j) = select(a, j)      cnf(a2, axiom)
store(store(a, i, select(a, j)), j, select(a, i)) = store(store(a, j, select(a, i)), i, select(a, j))      cnf(a3, axiom)
a32 = store(a1, i1, e31)      cnf(hyp0, hypothesis)
a34 = store(a2, i1, e33)      cnf(hyp1, hypothesis)
a36 = store(a32, i2, e35)      cnf(hyp2, hypothesis)
a38 = store(a34, i2, e37)      cnf(hyp3, hypothesis)
a40 = store(a36, i3, e39)      cnf(hyp4, hypothesis)
a42 = store(a38, i3, e41)      cnf(hyp5, hypothesis)
a44 = store(a40, i4, e43)      cnf(hyp6, hypothesis)
a46 = store(a42, i4, e45)      cnf(hyp7, hypothesis)

```

$a_{48} = \text{store}(a_{44}, i_5, e_{47}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{50} = \text{store}(a_{46}, i_5, e_{49}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{52} = \text{store}(a_{48}, i_6, e_{51}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{54} = \text{store}(a_{50}, i_6, e_{53}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{56} = \text{store}(a_{52}, i_7, e_{55}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{58} = \text{store}(a_{54}, i_7, e_{57}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{31} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{33} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{35} = \text{select}(a_{34}, i_2) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{37} = \text{select}(a_{32}, i_2) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $e_{39} = \text{select}(a_{38}, i_3) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{41} = \text{select}(a_{36}, i_3) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{43} = \text{select}(a_{42}, i_4) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{45} = \text{select}(a_{40}, i_4) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{47} = \text{select}(a_{46}, i_5) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{49} = \text{select}(a_{44}, i_5) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{51} = \text{select}(a_{50}, i_6) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{53} = \text{select}(a_{48}, i_6) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{55} = \text{select}(a_{54}, i_7) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{57} = \text{select}(a_{52}, i_7) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{60} = \text{select}(a_1, i_{59}) \quad \text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{61} = \text{select}(a_2, i_{59}) \quad \text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $i_{59} = \text{sk}(a_1, a_2) \quad \text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $a_{56} = a_{58} \quad \text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{60} \neq e_{61} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV565-1.010.p** Store inverse (t3\_pp\_sf\_ai\_00010)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j)) \quad \text{cnf}(a_3, \text{axiom})$   
 $a_{44} = \text{store}(a_1, i_1, e_{43}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{46} = \text{store}(a_2, i_1, e_{45}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{48} = \text{store}(a_{44}, i_2, e_{47}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{50} = \text{store}(a_{46}, i_2, e_{49}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{52} = \text{store}(a_{48}, i_3, e_{51}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{54} = \text{store}(a_{50}, i_3, e_{53}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{56} = \text{store}(a_{52}, i_4, e_{55}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{58} = \text{store}(a_{54}, i_4, e_{57}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{60} = \text{store}(a_{56}, i_5, e_{59}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{62} = \text{store}(a_{58}, i_5, e_{61}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{64} = \text{store}(a_{60}, i_6, e_{63}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{66} = \text{store}(a_{62}, i_6, e_{65}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{68} = \text{store}(a_{64}, i_7, e_{67}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{70} = \text{store}(a_{66}, i_7, e_{69}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $a_{72} = \text{store}(a_{68}, i_8, e_{71}) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $a_{74} = \text{store}(a_{70}, i_8, e_{73}) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{76} = \text{store}(a_{72}, i_9, e_{75}) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_{78} = \text{store}(a_{74}, i_9, e_{77}) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $a_{80} = \text{store}(a_{76}, i_{10}, e_{79}) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{82} = \text{store}(a_{78}, i_{10}, e_{81}) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{43} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{45} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{47} = \text{select}(a_{46}, i_2) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{49} = \text{select}(a_{44}, i_2) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{51} = \text{select}(a_{50}, i_3) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{53} = \text{select}(a_{48}, i_3) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{55} = \text{select}(a_{54}, i_4) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{57} = \text{select}(a_{52}, i_4) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$

$e_{59} = \text{select}(a_{58}, i_5)$        $\text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{61} = \text{select}(a_{56}, i_5)$        $\text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $e_{63} = \text{select}(a_{62}, i_6)$        $\text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $e_{65} = \text{select}(a_{60}, i_6)$        $\text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{67} = \text{select}(a_{66}, i_7)$        $\text{cnf}(\text{hyp}_{32}, \text{hypothesis})$   
 $e_{69} = \text{select}(a_{64}, i_7)$        $\text{cnf}(\text{hyp}_{33}, \text{hypothesis})$   
 $e_{71} = \text{select}(a_{70}, i_8)$        $\text{cnf}(\text{hyp}_{34}, \text{hypothesis})$   
 $e_{73} = \text{select}(a_{68}, i_8)$        $\text{cnf}(\text{hyp}_{35}, \text{hypothesis})$   
 $e_{75} = \text{select}(a_{74}, i_9)$        $\text{cnf}(\text{hyp}_{36}, \text{hypothesis})$   
 $e_{77} = \text{select}(a_{72}, i_9)$        $\text{cnf}(\text{hyp}_{37}, \text{hypothesis})$   
 $e_{79} = \text{select}(a_{78}, i_{10})$        $\text{cnf}(\text{hyp}_{38}, \text{hypothesis})$   
 $e_{81} = \text{select}(a_{76}, i_{10})$        $\text{cnf}(\text{hyp}_{39}, \text{hypothesis})$   
 $e_{84} = \text{select}(a_1, i_{83})$        $\text{cnf}(\text{hyp}_{40}, \text{hypothesis})$   
 $e_{85} = \text{select}(a_2, i_{83})$        $\text{cnf}(\text{hyp}_{41}, \text{hypothesis})$   
 $i_{83} = \text{sk}(a_1, a_2)$        $\text{cnf}(\text{hyp}_{42}, \text{hypothesis})$   
 $a_{80} = a_{82}$        $\text{cnf}(\text{hyp}_{43}, \text{hypothesis})$   
 $e_{84} \neq e_{85}$        $\text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV566-1.004.p** Store inverse (t3\_pp\_sf\_ai.00004)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e$        $\text{cnf}(a_1, \text{axiom})$   
 $i = j$  or  $\text{select}(\text{store}(a, i, e), j) = \text{select}(a, j)$        $\text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j))$        $\text{cnf}(a_3, \text{axiom})$   
 $a_{20} = \text{store}(a_1, i_1, e_{19})$        $\text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{22} = \text{store}(a_2, i_1, e_{21})$        $\text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{24} = \text{store}(a_{20}, i_2, e_{23})$        $\text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{26} = \text{store}(a_{22}, i_2, e_{25})$        $\text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{28} = \text{store}(a_{24}, i_3, e_{27})$        $\text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{30} = \text{store}(a_{26}, i_3, e_{29})$        $\text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{32} = \text{store}(a_{28}, i_1, e_{31})$        $\text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{34} = \text{store}(a_{30}, i_4, e_{33})$        $\text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $e_{19} = \text{select}(a_2, i_1)$        $\text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $e_{21} = \text{select}(a_1, i_1)$        $\text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $e_{23} = \text{select}(a_{22}, i_2)$        $\text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $e_{25} = \text{select}(a_{20}, i_2)$        $\text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $e_{27} = \text{select}(a_{26}, i_3)$        $\text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $e_{29} = \text{select}(a_{24}, i_3)$        $\text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{31} = \text{select}(a_{30}, i_4)$        $\text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{33} = \text{select}(a_{28}, i_4)$        $\text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{36} = \text{select}(a_1, i_{35})$        $\text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{37} = \text{select}(a_2, i_{35})$        $\text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $i_{35} = \text{sk}(a_1, a_2)$        $\text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{32} = a_{34}$        $\text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{36} \neq e_{37}$        $\text{cnf}(\text{goal}, \text{negated\_conjecture})$

**SWV566-1.007.p** Store inverse (t3\_pp\_sf\_ai.00007)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e$        $\text{cnf}(a_1, \text{axiom})$   
 $i = j$  or  $\text{select}(\text{store}(a, i, e), j) = \text{select}(a, j)$        $\text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j))$        $\text{cnf}(a_3, \text{axiom})$   
 $a_{32} = \text{store}(a_1, i_1, e_{31})$        $\text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{34} = \text{store}(a_2, i_1, e_{33})$        $\text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{36} = \text{store}(a_{32}, i_2, e_{35})$        $\text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{38} = \text{store}(a_{34}, i_2, e_{37})$        $\text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{40} = \text{store}(a_{36}, i_3, e_{39})$        $\text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{42} = \text{store}(a_{38}, i_3, e_{41})$        $\text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{44} = \text{store}(a_{40}, i_4, e_{43})$        $\text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{46} = \text{store}(a_{42}, i_4, e_{45})$        $\text{cnf}(\text{hyp}_7, \text{hypothesis})$

$a_{48} = \text{store}(a_{44}, i_5, e_{47}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{50} = \text{store}(a_{46}, i_5, e_{49}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{52} = \text{store}(a_{48}, i_6, e_{51}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{54} = \text{store}(a_{50}, i_6, e_{53}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{56} = \text{store}(a_{52}, i_1, e_{55}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{58} = \text{store}(a_{54}, i_7, e_{57}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $e_{31} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $e_{33} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $e_{35} = \text{select}(a_{34}, i_2) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $e_{37} = \text{select}(a_{32}, i_2) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $e_{39} = \text{select}(a_{38}, i_3) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $e_{41} = \text{select}(a_{36}, i_3) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{43} = \text{select}(a_{42}, i_4) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{45} = \text{select}(a_{40}, i_4) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{47} = \text{select}(a_{46}, i_5) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{49} = \text{select}(a_{44}, i_5) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{51} = \text{select}(a_{50}, i_6) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{53} = \text{select}(a_{48}, i_6) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{55} = \text{select}(a_{54}, i_7) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{57} = \text{select}(a_{52}, i_7) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$   
 $e_{60} = \text{select}(a_1, i_{59}) \quad \text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{61} = \text{select}(a_2, i_{59}) \quad \text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $i_{59} = \text{sk}(a_1, a_2) \quad \text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $a_{56} = a_{58} \quad \text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{60} \neq e_{61} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

### SWV566-1.010.p Store inverse (t3\_pp\_sf\_ai\_00010)

If the arrays resulting from swapping elements of array a with the elements of array b occurring in the same positions are equal, then a and b must have been equal to begin with.

$\text{select}(\text{store}(a, i, e), i) = e \quad \text{cnf}(a_1, \text{axiom})$   
 $i = j \text{ or } \text{select}(\text{store}(a, i, e), j) = \text{select}(a, j) \quad \text{cnf}(a_2, \text{axiom})$   
 $\text{store}(\text{store}(a, i, \text{select}(a, j)), j, \text{select}(a, i)) = \text{store}(\text{store}(a, j, \text{select}(a, i)), i, \text{select}(a, j)) \quad \text{cnf}(a_3, \text{axiom})$   
 $a_{44} = \text{store}(a_1, i_1, e_{43}) \quad \text{cnf}(\text{hyp}_0, \text{hypothesis})$   
 $a_{46} = \text{store}(a_2, i_1, e_{45}) \quad \text{cnf}(\text{hyp}_1, \text{hypothesis})$   
 $a_{48} = \text{store}(a_{44}, i_2, e_{47}) \quad \text{cnf}(\text{hyp}_2, \text{hypothesis})$   
 $a_{50} = \text{store}(a_{46}, i_2, e_{49}) \quad \text{cnf}(\text{hyp}_3, \text{hypothesis})$   
 $a_{52} = \text{store}(a_{48}, i_3, e_{51}) \quad \text{cnf}(\text{hyp}_4, \text{hypothesis})$   
 $a_{54} = \text{store}(a_{50}, i_3, e_{53}) \quad \text{cnf}(\text{hyp}_5, \text{hypothesis})$   
 $a_{56} = \text{store}(a_{52}, i_4, e_{55}) \quad \text{cnf}(\text{hyp}_6, \text{hypothesis})$   
 $a_{58} = \text{store}(a_{54}, i_4, e_{57}) \quad \text{cnf}(\text{hyp}_7, \text{hypothesis})$   
 $a_{60} = \text{store}(a_{56}, i_5, e_{59}) \quad \text{cnf}(\text{hyp}_8, \text{hypothesis})$   
 $a_{62} = \text{store}(a_{58}, i_5, e_{61}) \quad \text{cnf}(\text{hyp}_9, \text{hypothesis})$   
 $a_{64} = \text{store}(a_{60}, i_6, e_{63}) \quad \text{cnf}(\text{hyp}_{10}, \text{hypothesis})$   
 $a_{66} = \text{store}(a_{62}, i_6, e_{65}) \quad \text{cnf}(\text{hyp}_{11}, \text{hypothesis})$   
 $a_{68} = \text{store}(a_{64}, i_7, e_{67}) \quad \text{cnf}(\text{hyp}_{12}, \text{hypothesis})$   
 $a_{70} = \text{store}(a_{66}, i_7, e_{69}) \quad \text{cnf}(\text{hyp}_{13}, \text{hypothesis})$   
 $a_{72} = \text{store}(a_{68}, i_8, e_{71}) \quad \text{cnf}(\text{hyp}_{14}, \text{hypothesis})$   
 $a_{74} = \text{store}(a_{70}, i_8, e_{73}) \quad \text{cnf}(\text{hyp}_{15}, \text{hypothesis})$   
 $a_{76} = \text{store}(a_{72}, i_9, e_{75}) \quad \text{cnf}(\text{hyp}_{16}, \text{hypothesis})$   
 $a_{78} = \text{store}(a_{74}, i_9, e_{77}) \quad \text{cnf}(\text{hyp}_{17}, \text{hypothesis})$   
 $a_{80} = \text{store}(a_{76}, i_1, e_{79}) \quad \text{cnf}(\text{hyp}_{18}, \text{hypothesis})$   
 $a_{82} = \text{store}(a_{78}, i_{10}, e_{81}) \quad \text{cnf}(\text{hyp}_{19}, \text{hypothesis})$   
 $e_{43} = \text{select}(a_2, i_1) \quad \text{cnf}(\text{hyp}_{20}, \text{hypothesis})$   
 $e_{45} = \text{select}(a_1, i_1) \quad \text{cnf}(\text{hyp}_{21}, \text{hypothesis})$   
 $e_{47} = \text{select}(a_{46}, i_2) \quad \text{cnf}(\text{hyp}_{22}, \text{hypothesis})$   
 $e_{49} = \text{select}(a_{44}, i_2) \quad \text{cnf}(\text{hyp}_{23}, \text{hypothesis})$   
 $e_{51} = \text{select}(a_{50}, i_3) \quad \text{cnf}(\text{hyp}_{24}, \text{hypothesis})$   
 $e_{53} = \text{select}(a_{48}, i_3) \quad \text{cnf}(\text{hyp}_{25}, \text{hypothesis})$   
 $e_{55} = \text{select}(a_{54}, i_4) \quad \text{cnf}(\text{hyp}_{26}, \text{hypothesis})$   
 $e_{57} = \text{select}(a_{52}, i_4) \quad \text{cnf}(\text{hyp}_{27}, \text{hypothesis})$



$e_{59} = \text{select}(a_{58}, i_5) \quad \text{cnf}(\text{hyp}_{28}, \text{hypothesis})$   
 $e_{61} = \text{select}(a_{56}, i_5) \quad \text{cnf}(\text{hyp}_{29}, \text{hypothesis})$   
 $e_{63} = \text{select}(a_{62}, i_6) \quad \text{cnf}(\text{hyp}_{30}, \text{hypothesis})$   
 $e_{65} = \text{select}(a_{60}, i_6) \quad \text{cnf}(\text{hyp}_{31}, \text{hypothesis})$   
 $e_{67} = \text{select}(a_{66}, i_7) \quad \text{cnf}(\text{hyp}_{32}, \text{hypothesis})$   
 $e_{69} = \text{select}(a_{64}, i_7) \quad \text{cnf}(\text{hyp}_{33}, \text{hypothesis})$   
 $e_{71} = \text{select}(a_{70}, i_8) \quad \text{cnf}(\text{hyp}_{34}, \text{hypothesis})$   
 $e_{73} = \text{select}(a_{68}, i_8) \quad \text{cnf}(\text{hyp}_{35}, \text{hypothesis})$   
 $e_{75} = \text{select}(a_{74}, i_9) \quad \text{cnf}(\text{hyp}_{36}, \text{hypothesis})$   
 $e_{77} = \text{select}(a_{72}, i_9) \quad \text{cnf}(\text{hyp}_{37}, \text{hypothesis})$   
 $e_{79} = \text{select}(a_{78}, i_{10}) \quad \text{cnf}(\text{hyp}_{38}, \text{hypothesis})$   
 $e_{81} = \text{select}(a_{76}, i_{10}) \quad \text{cnf}(\text{hyp}_{39}, \text{hypothesis})$   
 $e_{84} = \text{select}(a_1, i_{83}) \quad \text{cnf}(\text{hyp}_{40}, \text{hypothesis})$   
 $e_{85} = \text{select}(a_2, i_{83}) \quad \text{cnf}(\text{hyp}_{41}, \text{hypothesis})$   
 $i_{83} = \text{sk}(a_1, a_2) \quad \text{cnf}(\text{hyp}_{42}, \text{hypothesis})$   
 $a_{80} = a_{82} \quad \text{cnf}(\text{hyp}_{43}, \text{hypothesis})$   
 $e_{84} \neq e_{85} \quad \text{cnf}(\text{goal}, \text{negated\_conjecture})$

### SWV817-1.p Hoare logic with procedures 112.1

Completeness is taken relative to completeness of the underlying logic. Two versions of completeness proof: nested single recursion and simultaneous recursion in call rule.

$c\_Fun\_Oid(v\_x, t\_a) = v\_x \quad \text{cnf}(\text{cls\_id\_apply}_0, \text{axiom})$   
 $c\_Fun\_Oid(v\_x, t\_a) = v\_x \quad \text{cnf}(\text{cls\_id\_def}_0, \text{axiom})$   
 $v\_sko\_Hoare\_Mirabelle\_Xstate\_not\_singleton\_def\_raw\_1 = v\_sko\_Hoare\_Mirabelle\_Xstate\_not\_singleton\_def\_raw\_2 =$   
 $\neg c\_Hoare\_Mirabelle\_Ostate\_not\_singleton \quad \text{cnf}(\text{cls\_state\_not\_singleton\_def\_raw}_0, \text{axiom})$   
 $c\_Hoare\_Mirabelle\_Ostate\_not\_singleton \text{ or } v\_x = v\_xa \quad \text{cnf}(\text{cls\_state\_not\_singleton\_def}_1, \text{axiom})$   
 $v\_sko\_Hoare\_Mirabelle\_Xstate\_not\_singleton\_def\_1 = v\_sko\_Hoare\_Mirabelle\_Xstate\_not\_singleton\_def\_2 \Rightarrow$   
 $\neg c\_Hoare\_Mirabelle\_Ostate\_not\_singleton \quad \text{cnf}(\text{cls\_state\_not\_singleton\_def}_0, \text{axiom})$   
 $c\_Hoare\_Mirabelle\_Ostate\_not\_singleton \quad \text{cnf}(\text{cls\_conjecture}_0, \text{negated\_conjecture})$   
 $v\_s = v\_x \quad \text{cnf}(\text{cls\_conjecture}_1, \text{negated\_conjecture})$

### SWV818-1.p Hoare logic with procedures 114.1

Completeness is taken relative to completeness of the underlying logic. Two versions of completeness proof: nested single recursion and simultaneous recursion in call rule.

$c\_Code\_Evaluation\_Otracing(v\_s, v\_x, t\_a) = v\_x \quad \text{cnf}(\text{cls\_tracing\_def}_0, \text{axiom})$   
 $c\_Code\_Evaluation\_Otracing(v\_s, v\_x, t\_a) = v\_x \quad \text{cnf}(\text{cls\_tracing\_def\_raw}_0, \text{axiom})$   
 $v\_s \neq v\_t \quad \text{cnf}(\text{cls\_conjecture}_0, \text{negated\_conjecture})$   
 $v\_s = v\_ta \quad \text{cnf}(\text{cls\_conjecture}_1, \text{negated\_conjecture})$

### SWV819-1.p Hoare logic with procedures 116.1

Completeness is taken relative to completeness of the underlying logic. Two versions of completeness proof: nested single recursion and simultaneous recursion in call rule.

$c\_Code\_Evaluation\_Otracing(v\_s, v\_x, t\_a) = v\_x \quad \text{cnf}(\text{cls\_tracing\_def}_0, \text{axiom})$   
 $c\_Code\_Evaluation\_Otracing(v\_s, v\_x, t\_a) = v\_x \quad \text{cnf}(\text{cls\_tracing\_def\_raw}_0, \text{axiom})$   
 $v\_s \neq v\_t \quad \text{cnf}(\text{cls\_conjecture}_0, \text{negated\_conjecture})$   
 $v\_s = v\_ta \quad \text{cnf}(\text{cls\_conjecture}_1, \text{negated\_conjecture})$   
 $v\_ta \neq v\_t \quad \text{cnf}(\text{cls\_conjecture}_2, \text{negated\_conjecture})$

### SWV904-1.p Hoare logic with procedures 450.1

Completeness is taken relative to completeness of the underlying logic. Two versions of completeness proof: nested single recursion and simultaneous recursion in call rule.

$c\_Option\_Option\_ONone(t\_a) \neq c\_Option\_Option\_OSome(v\_a\_H, t\_a) \quad \text{cnf}(\text{cls\_option\_Osimps\_I2\_J}_0, \text{axiom})$   
 $c\_Option\_Option\_ONone(t\_a) \neq c\_Option\_Option\_OSome(v\_y, t\_a) \quad \text{cnf}(\text{cls\_not\_Some\_eq}_1, \text{axiom})$   
 $c\_Option\_Option\_OSome(v\_a\_H, t\_a) \neq c\_Option\_Option\_ONone(t\_a) \quad \text{cnf}(\text{cls\_option\_Osimps\_I3\_J}_0, \text{axiom})$   
 $c\_Option\_Option\_OSome(v\_xa, t\_a) \neq c\_Option\_Option\_ONone(t\_a) \quad \text{cnf}(\text{cls\_not\_None\_eq}_1, \text{axiom})$   
 $c\_Com\_OWT(c\_Com\_Ocom\_OBODY(v\_pn)) \text{ or } c\_Com\_Obody(v\_pn) = c\_Option\_Option\_ONone(tc\_Com\_Ocom) \quad \text{cnf}(\text{cls\_com\_Osimps\_I19\_J}_0, \text{axiom})$   
 $c\_Com\_Ocom\_OBODY(v\_pname\_H) \neq c\_Com\_Ocom\_OSKIP \quad \text{cnf}(\text{cls\_com\_Osimps\_I19\_J}_0, \text{axiom})$   
 $c\_Com\_Ocom\_OBODY(v\_pname\_H) \neq c\_Com\_Ocom\_OSemi(v\_com_1, v\_com_2) \quad \text{cnf}(\text{cls\_com\_Osimps\_I49\_J}_0, \text{axiom})$   
 $c\_Com\_Ocom\_OSemi(v\_com_1, v\_com_2) \neq c\_Com\_Ocom\_OBODY(v\_pname\_H) \quad \text{cnf}(\text{cls\_com\_Osimps\_I48\_J}_0, \text{axiom})$   
 $c\_Com\_Ocom\_OBODY(v\_pname) = c\_Com\_Ocom\_OBODY(v\_pname\_H) \Rightarrow v\_pname = v\_pname\_H \quad \text{cnf}(\text{cls\_com\_Osimps\_I18\_J}_0, \text{axiom})$   
 $c\_Com\_Ocom\_OSKIP \neq c\_Com\_Ocom\_OBODY(v\_pname\_H) \quad \text{cnf}(\text{cls\_com\_Osimps\_I18\_J}_0, \text{axiom})$

$c\_Com\_OWT(c\_Com\_Ocom\_OBODY(v\_P)) \Rightarrow c\_Com\_Obody(v\_P) = c\_Option\_Ooption\_OSome(c\_Com\_Osco\_Com\_XWTs$   
 $c\_Com\_Ocom\_OSemi(v\_com_1, v\_com_2) = c\_Com\_Ocom\_OSemi(v\_com1\_H, v\_com2\_H) \Rightarrow v\_com_2 = v\_com2\_H \quad \text{cnf}(cls\_com$   
 $c\_Com\_Ocom\_OSemi(v\_com_1, v\_com_2) = c\_Com\_Ocom\_OSemi(v\_com1\_H, v\_com2\_H) \Rightarrow v\_com_1 = v\_com1\_H \quad \text{cnf}(cls\_com$   
 $c\_Option\_Ooption\_OSome(v\_a, t\_a) = c\_Option\_Ooption\_OSome(v\_a\_H, t\_a) \Rightarrow v\_a = v\_a\_H \quad \text{cnf}(cls\_option\_Oinject_0, axiom)$   
 $c\_Com\_Ocom\_OSemi(v\_com1\_H, v\_com2\_H) \neq c\_Com\_Ocom\_OSkip \quad \text{cnf}(cls\_com\_Osimps\_I13\_J_0, axiom)$   
 $c\_Com\_Ocom\_OSkip \neq c\_Com\_Ocom\_OSemi(v\_com1\_H, v\_com2\_H) \quad \text{cnf}(cls\_com\_Osimps\_I12\_J_0, axiom)$   
 $(c\_Com\_Obody(v\_pn) = c\_Option\_Ooption\_OSome(v\_b, tc\_Com\_Ocom) \text{ and } c\_Com\_OWT\_bodies) \Rightarrow c\_Com\_OWT(v\_b)$   
 $(c\_Com\_OWT(v\_c_1) \text{ and } c\_Com\_OWT(v\_c_0)) \Rightarrow c\_Com\_OWT(c\_Com\_Ocom\_OSemi(v\_c_0, v\_c_1)) \quad \text{cnf}(cls\_WT\_OSemi_0, axiom)$   
 $c\_Com\_OWT(c\_Com\_Ocom\_OSemi(v\_c_1, v\_c_2)) \Rightarrow c\_Com\_OWT(v\_c_1) \quad \text{cnf}(cls\_WTs\_elim\_cases\_I4\_J_0, axiom)$   
 $c\_Com\_OWT(c\_Com\_Ocom\_OSemi(v\_c_1, v\_c_2)) \Rightarrow c\_Com\_OWT(v\_c_2) \quad \text{cnf}(cls\_WTs\_elim\_cases\_I4\_J_1, axiom)$   
 $v\_sko\_Hoare\_Mirabelle\_Xstate\_not\_singleton\_def\_raw_1 = v\_sko\_Hoare\_Mirabelle\_Xstate\_not\_singleton\_def\_raw_2 =$   
 $\neg c\_Hoare\_Mirabelle\_Ostate\_not\_singleton \quad \text{cnf}(cls\_state\_not\_singleton\_def\_raw_0, axiom)$   
 $c\_Hoare\_Mirabelle\_Ostate\_not\_singleton \text{ or } v\_x = v\_xa \quad \text{cnf}(cls\_state\_not\_singleton\_def_1, axiom)$   
 $v\_sko\_Hoare\_Mirabelle\_Xsingle\_stateE_1(v\_t) = v\_t \Rightarrow \neg c\_Hoare\_Mirabelle\_Ostate\_not\_singleton \quad \text{cnf}(cls\_single\_stat$   
 $c\_Com\_OWT(c\_Com\_Ocom\_OSkip) \quad \text{cnf}(cls\_WT\_OSkip_0, axiom)$   
 $v\_sko\_Hoare\_Mirabelle\_Xstate\_not\_singleton\_def_1 = v\_sko\_Hoare\_Mirabelle\_Xstate\_not\_singleton\_def_2 \Rightarrow$   
 $\neg c\_Hoare\_Mirabelle\_Ostate\_not\_singleton \quad \text{cnf}(cls\_state\_not\_singleton\_def_0, axiom)$   
 $c\_Hoare\_Mirabelle\_Ostate\_not\_singleton \quad \text{cnf}(cls\_conjecture_0, negated\_conjecture)$   
 $c\_Com\_OWT\_bodies \quad \text{cnf}(cls\_conjecture_1, negated\_conjecture)$   
 $c\_Com\_OWT(v\_c) \quad \text{cnf}(cls\_conjecture_2, negated\_conjecture)$   
 $\neg c\_Hoare\_Mirabelle\_Ostate\_not\_singleton \quad \text{cnf}(cls\_conjecture_3, negated\_conjecture)$

### SWV917-1.p Java type soundness 027\_36

$v\_v = c\_Option\_Ooption\_OSome(c\_ATP\_Linkup\_Osco\_Option\_Xoption\_Xnchotomy\_1_1(v\_v, t\_a), t\_a) \text{ or } v\_v = c\_Option\_O$   
 $v\_x = c\_Option\_Ooption\_OSome(c\_ATP\_Linkup\_Osco\_Option\_Xnot\_None\_eq\_1_1(v\_x, t\_a), t\_a) \text{ or } v\_x = c\_Option\_Ooption$   
 $c\_Option\_Ooption\_OSome(v\_a, t\_a) = c\_Option\_Ooption\_OSome(v\_a\_H, t\_a) \Rightarrow v\_a = v\_a\_H \quad \text{cnf}(cls\_option\_Oinject_0, axiom)$   
 $\neg c\_Option\_Ois\_none(c\_Option\_Ooption\_OSome(v\_x, t\_a), t\_a) \quad \text{cnf}(cls\_is\_none\_code\_I2\_J_0, axiom)$   
 $v\_x = c\_Option\_Ooption\_ONone(t\_a) \text{ or } v\_x = c\_Option\_Ooption\_OSome(c\_ATP\_Linkup\_Osco\_Option\_Xnot\_Some\_eq\_1_1$   
 $v\_y = c\_Option\_Ooption\_OSome(c\_ATP\_Linkup\_Osco\_Option\_Xoption\_Xexhaust\_1_1(v\_y, t\_a), t\_a) \text{ or } v\_y = c\_Option\_O$   
 $c\_Option\_Ois\_none(c\_Option\_Ooption\_ONone(t\_a), t\_a) \quad \text{cnf}(cls\_is\_none\_def_1, axiom)$   
 $c\_Option\_Ooption\_OSome(v\_xa, t\_a) \neq c\_Option\_Ooption\_ONone(t\_a) \quad \text{cnf}(cls\_not\_None\_eq_1, axiom)$   
 $c\_Option\_Ooption\_OSome(v\_a\_H, t\_a) \neq c\_Option\_Ooption\_ONone(t\_a) \quad \text{cnf}(cls\_option\_Osimps\_I3\_J_0, axiom)$   
 $c\_Option\_Ooption\_ONone(t\_a) \neq c\_Option\_Ooption\_OSome(v\_y, t\_a) \quad \text{cnf}(cls\_not\_Some\_eq_1, axiom)$   
 $c\_Option\_Ooption\_ONone(t\_a) \neq c\_Option\_Ooption\_OSome(v\_a\_H, t\_a) \quad \text{cnf}(cls\_option\_Osimps\_I2\_J_0, axiom)$   
 $c\_Option\_Ois\_none(v\_x, t\_a) \Rightarrow v\_x = c\_Option\_Ooption\_ONone(t\_a) \quad \text{cnf}(cls\_is\_none\_def_0, axiom)$   
 $c\_Objects\_Onew\_Addr(v\_ha\_----) = c\_Option\_Ooption\_OSome(v\_a\_----, tc\_nat) \quad \text{cnf}(cls\_CHAINED_0, axiom)$   
 $hAPP(v\_ha\_----, v\_a\_----) \neq c\_Option\_Ooption\_ONone(tc\_prod(tc\_List\_Olist(tc\_String\_Ochar), tc\_fun(tc\_prod(tc\_List\_Olist(tc\_S$

### SWV918-1.p Java type soundness 030\_39

$c\_COMBI(v\_P, t\_a) = v\_P \quad \text{cnf}(cls\_COMBI\_def_0, axiom)$   
 $c\_Conform\_Ohconf(v\_P, v\_h, t\_a) \Rightarrow c\_Exceptions\_Opreallocated(v\_h) \quad \text{cnf}(cls\_hconf\_def_1, axiom)$   
 $c\_Conform\_Ohconf(v\_P, v\_ha\_----, tc\_prod(tc\_List\_Olist(tc\_List\_Olist(tc\_String\_Ochar)), tc\_Expr\_Oexp(tc\_List\_Olist(tc\_String\_C$   
 $c\_COMBI(v\_P, t\_a) = v\_P \quad \text{cnf}(cls\_COMBI\_def\_raw_0, axiom)$   
 $v\_h\_Ha\_---- = c\_Fun\_Ofun\_upd(v\_ha\_----, v\_a\_----, c\_Option\_Ooption\_OSome(c\_Pair(v\_C\_----, c\_Objects\_Oinit\_fields(v\_FDTs\_----))$   
 $c\_Conform\_Ooconf(v\_P, v\_ha\_----, c\_Pair(v\_C\_----, c\_Objects\_Oinit\_fields(v\_FDTs\_----)), tc\_List\_Olist(tc\_String\_Ochar), tc\_fun(tc$   
 $hAPP(v\_ha\_----, v\_a\_----) = c\_Option\_Ooption\_ONone(tc\_prod(tc\_List\_Olist(tc\_String\_Ochar), tc\_fun(tc\_prod(tc\_List\_Olist(tc\_S$   
 $\neg c\_Conform\_Ohconf(v\_P, v\_h\_Ha\_----, tc\_prod(tc\_List\_Olist(tc\_List\_Olist(tc\_String\_Ochar)), tc\_Expr\_Oexp(tc\_List\_Olist(tc\_S$   
 $c\_fequal(v\_x, v\_x, t\_a) \quad \text{cnf}(cls\_ATP\_Linkup\_Oequal\_imp\_fequal_0, axiom)$   
 $c\_fequal(v\_X, v\_Y, t\_a) \Rightarrow v\_X = v\_Y \quad \text{cnf}(cls\_ATP\_Linkup\_Ofequal\_imp\_equal_0, axiom)$

### SWV920-1.p Java type soundness 058\_5

$c\_Objects\_Ohext(v\_h, v\_h) \quad \text{cnf}(cls\_hext\_refl_0, axiom)$   
 $(c\_Objects\_Ohext(v\_h\_H, v\_h\_H\_H) \text{ and } c\_Objects\_Ohext(v\_h, v\_h\_H\_H)) \Rightarrow c\_Objects\_Ohext(v\_h, v\_h\_H\_H) \quad \text{cnf}(cls\_hext\_tr$   
 $c\_COMBI(v\_P, t\_a) = v\_P \quad \text{cnf}(cls\_COMBI\_def_0, axiom)$   
 $c\_Conform\_Olconf(v\_P, v\_ha\_----, v\_la\_----, v\_E\_----, tc\_prod(tc\_List\_Olist(tc\_List\_Olist(tc\_String\_Ochar)), tc\_Expr\_Oexp(tc\_L$   
 $(c\_Objects\_Ohext(v\_h, v\_h\_H) \text{ and } c\_Conform\_Olconf(v\_P, v\_h, v\_l, v\_E, t\_a)) \Rightarrow c\_Conform\_Olconf(v\_P, v\_h\_H, v\_l, v\_E, t\_a)$   
 $c\_COMBI(v\_P, t\_a) = v\_P \quad \text{cnf}(cls\_COMBI\_def\_raw_0, axiom)$   
 $c\_Conform\_Olconf(v\_P, v\_ha\_----, v\_la\_----, v\_E\_----, tc\_prod(tc\_List\_Olist(tc\_List\_Olist(tc\_String\_Ochar)), tc\_Expr\_Oexp(tc\_L$   
 $c\_WellTypeRT\_OWTrt(v\_P, v\_ha\_----, v\_E\_----, c\_Expr\_Oexp\_Onew(v\_C\_----, tc\_List\_Olist(tc\_String\_Ochar)), v\_T\_----) \quad \text{cnf}($   
 $v\_h\_Ha\_---- = c\_Fun\_Ofun\_upd(v\_ha\_----, v\_a\_----, c\_Option\_Ooption\_OSome(c\_Pair(v\_C\_----, c\_Objects\_Oinit\_fields(v\_FD$   
 $c\_TypeRel\_OFields(v\_P, v\_C\_----, v\_FDTs\_----, tc\_prod(tc\_List\_Olist(tc\_List\_Olist(tc\_String\_Ochar)), tc\_Expr\_Oexp(tc\_List\_C$

$c\_Objects\_Onew\_Addr(v\_ha\_-----) = c\_Option\_Ooption\_OSome(v\_a\_-----, tc\_nat)$      $cnf(cls\_CHAINED\_004, axiom)$   
 $\neg c\_Conform\_Oconf(v\_P, v\_h\_Ha\_-----, v\_la\_-----, v\_E\_-----, tc\_prod(tc\_List\_Olist(tc\_List\_Olist(tc\_String\_Ochar)), tc\_Expr\_Oexp(tc\_fequal(v\_x, v\_x, t\_a)))$      $cnf(cls\_ATP\_Linkup\_Oequal\_imp\_fequal_0, axiom)$   
 $c\_fequal(v\_X, v\_Y, t\_a) \Rightarrow v\_X = v\_Y$      $cnf(cls\_ATP\_Linkup\_Ofequal\_imp\_equal_0, axiom)$

**SWV973-1.p** Java type soundness 464\_31

$c\_Value\_Oval\_OUnit \neq c\_Value\_Oval\_OAddr(v\_nat\_H)$      $cnf(cls\_val\_Osimps\_I10\_J_0, axiom)$   
 $c\_Value\_Oval\_OIntg(v\_int) \neq c\_Value\_Oval\_OAddr(v\_nat\_H)$      $cnf(cls\_val\_Osimps\_I22\_J_0, axiom)$   
 $c\_Value\_Oval\_OAddr(v\_nat\_H) \neq c\_Value\_Oval\_OIntg(v\_int)$      $cnf(cls\_val\_Osimps\_I23\_J_0, axiom)$   
 $c\_Value\_Oval\_OAddr(v\_nat\_H) \neq c\_Value\_Oval\_OUnit$      $cnf(cls\_val\_Osimps\_I11\_J_0, axiom)$   
 $c\_Value\_Oval\_OUnit \neq c\_Value\_Oval\_OIntg(v\_int\_H)$      $cnf(cls\_val\_Osimps\_I8\_J_0, axiom)$   
 $c\_Value\_Oval\_OAddr(v\_nat) = c\_Value\_Oval\_OAddr(v\_nat\_H) \Rightarrow v\_nat = v\_nat\_H$      $cnf(cls\_val\_Osimps\_I3\_J_0, axiom)$   
 $c\_Value\_Oval\_OIntg(v\_int\_H) \neq c\_Value\_Oval\_OUnit$      $cnf(cls\_val\_Osimps\_I9\_J_0, axiom)$   
 $c\_Value\_Oval\_OIntg(v\_int) = c\_Value\_Oval\_OIntg(v\_int\_H) \Rightarrow v\_int = v\_int\_H$      $cnf(cls\_val\_Osimps\_I2\_J_0, axiom)$   
 $c\_Value\_Oval\_ONull \neq c\_Value\_Oval\_OUnit$      $cnf(cls\_val\_Osimps\_I5\_J_0, axiom)$   
 $c\_Value\_Oval\_OIntg(v\_int\_H) \neq c\_Value\_Oval\_ONull$      $cnf(cls\_val\_Osimps\_I15\_J_0, axiom)$   
 $c\_Value\_Oval\_OUnit \neq c\_Value\_Oval\_ONull$      $cnf(cls\_val\_Osimps\_I4\_J_0, axiom)$   
 $c\_Value\_Oval\_ONull \neq c\_Value\_Oval\_OIntg(v\_int\_H)$      $cnf(cls\_val\_Osimps\_I14\_J_0, axiom)$   
 $c\_Value\_Oval\_OAddr(v\_nat\_H) \neq c\_Value\_Oval\_ONull$      $cnf(cls\_val\_Osimps\_I17\_J_0, axiom)$   
 $c\_Value\_Oval\_ONull \neq c\_Value\_Oval\_OAddr(v\_nat\_H)$      $cnf(cls\_val\_Osimps\_I16\_J_0, axiom)$   
 $c\_WellTypeRT\_OWTrt(v\_P, v\_ha\_-----, v\_E\_-----, c\_Expr\_Oexp\_OVal(v\_v\_-----, tc\_List\_Olist(tc\_String\_Ochar)), c\_Type\_Oty\_ONT)$   
 $v\_v\_----- \neq c\_Value\_Oval\_ONull$      $cnf(cls\_conjecture_0, negated\_conjecture)$

**SWV985-1.p** Java type soundness 555\_24

$c\_COMBI(v\_P, t\_a) = v\_P$      $cnf(cls\_COMBI\_def_0, axiom)$   
 $c\_TypeSafe\_Mirabelle\_Oconf(v\_P, v\_E, v\_s\_H)$      $cnf(cls\_refl\_I2\_J_0, axiom)$   
 $c\_WellTypeRT\_OWTrt(v\_P, c\_State\_Ohp(v\_s\_H), v\_E, v\_e\_H, v\_T\_-----)$      $cnf(cls\_refl\_I1\_J_0, axiom)$   
 $c\_COMBI(v\_P, t\_a) = v\_P$      $cnf(cls\_COMBI\_def\_raw_0, axiom)$   
 $\neg c\_TypeSafe\_Mirabelle\_Oconf(v\_P, v\_E, v\_s\_H)$      $cnf(cls\_conjecture_0, negated\_conjecture)$   
 $c\_fequal(v\_x, v\_x, t\_a)$      $cnf(cls\_ATP\_Linkup\_Oequal\_imp\_fequal_0, axiom)$   
 $c\_fequal(v\_X, v\_Y, t\_a) \Rightarrow v\_X = v\_Y$      $cnf(cls\_ATP\_Linkup\_Ofequal\_imp\_equal_0, axiom)$

**SWV996=1.p** Backward simplification: node deletion 2

A problem extracted from model checking a safety problem (no violation of mutual exclusion) for a parameterized system (a variant of the protocol due to Szymanski).

$z_1: \$int$      $tff(z1\_type, type)$   
 $z_2: \$int$      $tff(z2\_type, type)$   
 $z_3: \$int$      $tff(z3\_type, type)$   
 $a: \$int \rightarrow \$int$      $tff(a\_type, type)$   
 $b: \$int \rightarrow \$int$      $tff(b\_type, type)$   
 $(\forall z_1: \$int: (\$lesseq(1, a(z_1)) \text{ and } \$lesseq(a(z_1), 12)) \text{ and } \forall z_1: \$int: (\$lesseq(1, b(z_1)) \text{ and } \$lesseq(b(z_1), 5)) \text{ and } \$true \text{ and } z_1 \neq z_2 \text{ and } z_1 \neq z_3 \text{ and } z_2 \neq z_3 \text{ and } \forall z_1: \$int, z_2: \$int: \neg z_1 \neq z_2 \text{ and } a(z_1) = 10 \text{ and } a(z_2) = 10) \Rightarrow \neg a(z_1) = 9 \text{ and } a(z_2) = 10 \text{ and } \$less(b(z_2), 3) \text{ and } \$less(z_2, z_1))$      $tff(0, conjecture)$

**SWV997=1.p** Fix-point check 20

A problem extracted from model checking a safety problem (no violation of mutual exclusion) for a parameterized system (a variant of the protocol due to Szymanski).

$z_1: \$int$      $tff(z1\_type, type)$   
 $z_2: \$int$      $tff(z2\_type, type)$   
 $z_3: \$int$      $tff(z3\_type, type)$   
 $z_4: \$int$      $tff(z4\_type, type)$   
 $a: \$int \rightarrow \$int$      $tff(a\_type, type)$   
 $b: \$int \rightarrow \$int$      $tff(b\_type, type)$   
 $(\forall z_1: \$int: (\$lesseq(1, a(z_1)) \text{ and } \$lesseq(a(z_1), 12)) \text{ and } \forall z_1: \$int: (\$lesseq(1, b(z_1)) \text{ and } \$lesseq(b(z_1), 5)) \text{ and } \$true \text{ and } z_1 \neq z_2 \text{ and } z_1 \neq z_3 \text{ and } z_1 \neq z_4 \text{ and } z_2 \neq z_3 \text{ and } z_2 \neq z_4 \text{ and } z_3 \neq z_4 \text{ and } \forall z_1: \$int, z_2: \$int: \neg z_1 \neq z_2 \text{ and } a(z_1) = 10 \text{ and } a(z_2) = 10 \text{ and } \forall z_1: \$int, z_2: \$int: \neg z_1 \neq z_2 \text{ and } a(z_1) = 9 \text{ and } a(z_2) = 10 \text{ and } \$less(b(z_2), 3) \text{ and } \$less(z_2, z_1) \text{ and } \forall z_1: z_2 \text{ and } a(z_1) = 8 \text{ and } a(z_2) = 10 \text{ and } \$less(b(z_2), 3) \text{ and } \$less(z_2, z_1) \text{ and } \forall z_1: \$int, z_2: \$int, z_3: \$int: \neg z_1 \neq z_2 \text{ and } z_1 \neq z_3 \text{ and } z_2 \neq z_3 \text{ and } a(z_1) = 7 \text{ and } a(z_2) = 10 \text{ and } \$less(b(z_2), 3) \text{ and } b(z_3) = 5 \text{ and } \$less(z_2, z_1) \text{ and } \forall z_1: \$int, z_2: \$int, z_3: \$int: \neg z_1 \neq z_2 \text{ and } z_1 \neq z_3 \text{ and } z_2 \neq z_3 \text{ and } a(z_1) = 6 \text{ and } a(z_2) = 10 \text{ and } \$less(b(z_2), 3) \text{ and } b(z_3) = 5 \text{ and } \$less(z_2, z_1) \text{ and } \forall z_1: \$int, z_2: \$int, z_3: \$int: \neg z_1 \neq z_2 \text{ and } z_1 \neq z_3 \text{ and } z_2 \neq z_3 \text{ and } a(z_1) = 7 \text{ and } a(z_2) = 10 \text{ and } a(z_3) = 8 \text{ and } \$less(b(z_2), 3) \text{ and } \$less(z_2, z_1)) \Rightarrow \neg a(z_1) = 6 \text{ and } a(z_2) = 10 \text{ and } a(z_3) = 1 \text{ and } \$less(b(z_2), 3) \text{ and } b(z_3) = 5 \text{ and } \$less(z_2, z_1))$      $tff(0, conjecture)$