

# SYN axioms

**SYN000+0.ax** A simple include file for FOF

```
ia1   fof(ia1, axiom)
ia2   fof(ia2, axiom)
ia3   fof(ia3, axiom)
```

**SYN000-0.ax** A simple include file for CNF

```
ia1   cnf(ia1, axiom)
ia2   cnf(ia2, axiom)
ia3   cnf(ia3, axiom)
```

**SYN000^0.ax** A simple include file for THF

```
ia1: $o   thf(ia1_type, type)
ia2: $o   thf(ia2_type, type)
ia3: $o   thf(ia3_type, type)
ia1   thf(ia1, axiom)
ia2   thf(ia2, axiom)
ia3   thf(ia3, axiom)
```

**SYN000\_0.ax** A simple include file for TFF

```
ia1: $o   tff(ia1_type, type)
ia2: $o   tff(ia2_type, type)
ia3: $o   tff(ia3_type, type)
ia1   tff(ia1, axiom)
ia2   tff(ia2, axiom)
ia3   tff(ia3, axiom)
```

**SYN002+0.ax** Orevkov formula

```
r(x,y,z)=y+2^x=z
∀y: r(y, 0, succ(y))   fof(hyp1, axiom)
∀y, x, z, z1: (r(y, x, z) ⇒ (r(z, x, z1) ⇒ r(y, succ(x), z1)))   fof(hyp2, axiom)
```

# SYN problems

**SYN000+1.p** Basic TPTP FOF syntax

Basic TPTP FOF syntax that you can't survive without parsing.

```
(p0 and ¬q0) ⇒ (r0 or ¬s0)   fof(propositional, axiom)
∀x: ((p(x) or ¬q(x, a)) ⇒ ∃y, z: (r(x, f(y), g(x, f(y), z)) and ¬s(f(f(f(b))))))   fof(first_order, axiom)
∃y: ∀x, z: (f(y) = g(x, f(y), z) or f(f(f(b))) ≠ a or x = f(y))   fof(equality, axiom)
$true or $false   fof(true_false, axiom)
'A proposition' or 'A predicate'(a) or p('A constant') or p('A function'(a)) or p('A quotedescape')   fof(single_quoted, axiom)
∀x: ((p(x) ⇐ ¬q(x, a)) ⇐⇒ ∃y, z: r(x, f(y), g(x, f(y), z)) < > ¬s(f(f(f(b))))))   fof(useful_connectives, axiom)
∀x: ((p(x) or ¬q(x, a)) ⇒ ∃y, z: (r(x, f(y), g(x, f(y), z)) and ¬s(f(f(f(b))))))   fof(123, axiom)
p(h)   fof(role_hypothesis, hypothesis)
∃x: p(x)   fof(role_conjecture, conjecture)
include('Axioms/SYN000+0.ax')
```

**SYN000+2.p** Advanced TPTP FOF syntax

Advanced TPTP FOF syntax that you will encounter some time.

```
"An Apple" ≠ "A Microsoftescape"   fof(distinct_object, axiom)
p(12) or p(-12)   fof(integers, axiom)
p(123/456) or p(-123/456) or p(+123/456)   fof(rationals, axiom)
p(123.456) or p(-123.456) or p(123.456E78) or p(123.456e78) or p(-123.456E78) or p(123.456E-78) or p(-123.456E-78)   fof(floats, axiom)
∀x: (p(x) nor ¬q(x, a)) nand p(x)   fof(never_used_connectives, axiom)
∀x: f(d) = f(x)   fof(role_definition, definition)
p(a)   fof(role_assumption, assumption)
p(l)   fof(role_lemma, lemma)
p(t)   fof(role_theorem, theorem)
p(u)   fof(role_unknown, unknown)
include('Axioms/SYN000+0.ax', [ia1, ia3])
∀x: p(x)   fof(source_unknown, axiom)
```

$\forall x: p(x)$     fof(source, axiom)  
 $\forall x: p(x)$     fof(source\_name, axiom)  
 $\forall x: p(x)$     fof(source\_copy, axiom)  
 $\forall x: p(x)$     fof(source\_introduced\_assumption, axiom)  
 $p(a)$     fof(source\_inference, axiom)  
 $p(a)$     fof(source\_inference\_with\_bind, axiom)  
 $\forall x: p(x)$     fof(useful\_info, axiom)

### SYN000-1.p Basic TPTP CNF syntax

Basic TPTP CNF syntax that you can't survive without parsing.

$(q_0 \text{ and } s_0) \Rightarrow (p_0 \text{ or } r_0)$     cnf(propositional, axiom)  
 $(g(x, a) \text{ and } s(f(f(f(b)))))) \Rightarrow (p(x) \text{ or } r(x, f(y), g(x, f(y), z)))$     cnf(first\_order, axiom)  
 $f(f(f(b))) = a \Rightarrow (f(y) = g(x, f(y), z) \text{ or } x = f(y))$     cnf(equality, axiom)  
 $\$true \text{ or } \$false$     cnf(true\_false, axiom)  
 'A proposition' or 'A predicate'(y) or p('A constant') or p('A function'(a)) or p('A quotedescape')    cnf(single\_quoted, axiom)  
 $(g(x, a) \text{ and } s(f(f(f(b)))))) \Rightarrow (p(x) \text{ or } r(x, f(y), g(x, f(y), z)))$     cnf(123, axiom)  
 $p(h)$     cnf(role\_hypothesis, hypothesis)  
 $\neg p(x)$     cnf(role\_negated\_conjecture, negated\_conjecture)  
 include('Axioms/SYN000-0.ax')

### SYN000-2.p Advanced TPTP CNF syntax

Advanced TPTP CNF syntax that you will encounter some time.

"An Apple"  $\neq$  "A Microsoftescape"    cnf(distinct\_object, axiom)  
 $p(12) \text{ or } p(-12)$     cnf(integers, axiom)  
 $p(123/456) \text{ or } p(-123/456) \text{ or } p(+123/456)$     cnf(rationals, axiom)  
 $p(123.456) \text{ or } p(-123.456) \text{ or } p(123.456E78) \text{ or } p(123.456e78) \text{ or } p(-123.456E78) \text{ or } p(123.456E-78) \text{ or } p(-123.456E-78)$     cnf(floats, axiom)  
 $f(d) = f(x)$     cnf(role\_definition, definition)  
 $p(a)$     cnf(role\_assumption, assumption)  
 $p(l)$     cnf(role\_lemma, lemma)  
 $p(t)$     cnf(role\_theorem, theorem)  
 $p(u)$     cnf(role\_unknown, unknown)  
 include('Axioms/SYN000-0.ax', [ia<sub>1</sub>, ia<sub>3</sub>])  
 $p(x)$     cnf(source\_unknown, axiom)  
 $p(x)$     cnf(source, axiom)  
 $p(x)$     cnf(source\_name, axiom)  
 $p(x)$     cnf(source\_copy, axiom)  
 $p(x)$     cnf(source\_introduced\_assumption, axiom)  
 $p(a)$     cnf(source\_inference, axiom)  
 $p(a)$     cnf(source\_inference\_with\_bind, axiom)  
 $p(x)$     cnf(useful\_info, axiom)

### SYN000^1.p Basic TPTP

Basic TPTP that you can't survive without parsing.

$p_0: \$o$     thf(p0\_type, type)  
 $q_0: \$o$     thf(q0\_type, type)  
 $r_0: \$o$     thf(r0\_type, type)  
 $s_0: \$o$     thf(s0\_type, type)  
 $(p_0 \text{ and } \neg q_0) \Rightarrow (r_0 \text{ or } \neg s_0)$     thf(propositional, axiom)  
 $a: \$i$     thf(a\_type, type)  
 $b: \$i$     thf(b\_type, type)  
 $h: \$i$     thf(h\_type, type)  
 $f: \$i \rightarrow \$i$     thf(f\_type, type)  
 $g: \$i \rightarrow \$i \rightarrow \$i \rightarrow \$i$     thf(g\_type, type)  
 $p: \$i \rightarrow \$o$     thf(p\_type, type)  
 $q: \$i \rightarrow \$i \rightarrow \$o$     thf(q\_type, type)  
 $r: \$i \rightarrow \$i \rightarrow \$i \rightarrow \$o$     thf(r\_type, type)  
 $s: \$i \rightarrow \$o$     thf(s\_type, type)  
 $\forall x: \$i: ((p@x \text{ or } \neg q@x@a) \Rightarrow \exists y: \$i, z: \$i: (r@x@(f@y)@(g@x@(f@y)@z) \text{ and } \neg s@(f@(f@(f@b))))))$     thf(first\_order, axiom)  
 $\exists y: \$i: \forall x: \$i, z: \$i: ((f@y) = (g@x@(f@y)@z) \text{ or } (f@(f@(f@b))) \neq a \text{ or } x = (f@y))$     thf(equality, axiom)  
 $\$true \text{ or } \$false$     thf(true\_false, axiom)  
 'A proposition': \$o    thf(quoted\_proposition\_type, type)

```

'A predicate': $i → $o    thf(quoted_predicate_type, type)
'A constant': $i    thf(quoted_constant_type, type)
'A function': $i → $i    thf(quoted_function_type, type)
'A quotedescape': $i    thf(quoted_escape_type, type)
'A proposition' or 'A predicate'@a or p@'A constant' or p@('A function'@a) or p@'A quotedescape'    thf(single_quoted, axiom)
∀x: $i: ((p@x) ← ¬q@x@a) ⇔ ∃y: $i, z: $i: (r@x@(f@y)@(g@x@(f@y)@z)) < > ¬s@(f@(f@(f@b))))    thf(useful_connectives, axiom)
l1: $i → ($i → $o) → $o    thf(l1_type, type)
l2: ($i → ($i → $i) → $i) → $o    thf(l2_type, type)
l1 = (λc: $i, p: $i → $o: (p@c))    thf(lambda_defn, axiom)
l2@λc: $i, f: $i → $i: (f@c)    thf(lambda_use, axiom)
new: $tType    thf(new_type, type)
newc: new    thf(newc_type, type)
newf: new → $i → new    thf(newf_type, type)
newp: new → $i → $o    thf(newp_type, type)
∀x: new: (newp@(newf@newc@a)@a)    thf(new_axiom, axiom)
∀x: $i: ((p@x or ¬q@x@a) ⇒ ∃y: $i, z: $i: (r@x@(f@y)@(g@x@(f@y)@z) and ¬s@(f@(f@(f@b))))))    thf(123, axiom)
p@h    thf(role_hypothesis, hypothesis)
∃x: $i: (p@x)    thf(role_conjecture, conjecture)
include('Axioms/SYN000^0.ax')

```

### SYN000\_1.p Basic TPTP TF0 syntax without arithmetic

Basic TPTP TF0 syntax that you can't survive without parsing.

```

p0: $o    tff(p0_type, type)
q0: $o    tff(q0_type, type)
r0: $o    tff(r0_type, type)
s0: $o    tff(s0_type, type)
(p0 and ¬q0) ⇒ (r0 or ¬s0)    tff(propositional, axiom)
a: $i    tff(a_type, type)
b: $i    tff(b_type, type)
h: $i    tff(h_type, type)
f: $i → $i    tff(f_type, type)
g: ($i × $i × $i) → $i    tff(g_type, type)
p: $i → $o    tff(p_type, type)
q: ($i × $i) → $o    tff(q_type, type)
r: ($i × $i × $i) → $o    tff(r_type, type)
s: $i → $o    tff(s_type, type)
∀x: $i: ((p(x) or ¬q(x, a)) ⇒ ∃y: $i, z: $i: (r(x, f(y), g(x, f(y), z)) and ¬s(f(f(f(b))))))    tff(first_order, axiom)
∃y: $i: ∀x: $i, z: $i: (f(y) = g(x, f(y), z) or f(f(f(b))) ≠ a or x = f(y))    tff(equality, axiom)
$true or $false    tff(true_false, axiom)
'A proposition': $o    tff(quoted_proposition_type, type)
'A predicate': $i → $o    tff(quoted_predicate_type, type)
'A constant': $i    tff(quoted_constant_type, type)
'A function': $i → $i    tff(quoted_function_type, type)
'A quotedescape': $i    tff(quoted_escape_type, type)
'A proposition' or 'A predicate'(a) or p('A constant') or p('A function'(a)) or p('A quotedescape')    tff(single_quoted, axiom)
∀x: $i: ((p(x) ← ¬q(x, a)) ⇔ ∃y: $i, z: $i: r(x, f(y), g(x, f(y), z)) < > ¬s(f(f(f(b))))))    tff(useful_connectives, axiom)
new: $tType    tff(new_type, type)
newc: new    tff(newc_type, type)
newf: (new × $i) → new    tff(newf_type, type)
newp: (new × $i) → $o    tff(newp_type, type)
∀x: new: newp(newf(newc, a), a)    tff(new_axiom, axiom)
∀x: $i: ((p(x) or ¬q(x, a)) ⇒ ∃y: $i, z: $i: (r(x, f(y), g(x, f(y), z)) and ¬s(f(f(f(b))))))    tff(123, axiom)
p(h)    tff(role_hypothesis, hypothesis)
∃x: $i: p(x)    tff(role_conjecture, conjecture)
include('Axioms/SYN000.0.ax')

```

### SYN000\_2.p Advanced TPTP TF0 syntax without arithmetic

Advanced TPTP TF0 syntax that you will encounter some time.

```

"An Apple" ≠ "A Microsoftescape"    tff(distinct_object, axiom)
a: $i    tff(a_type, type)

```

$b: \text{\$i} \quad \text{tff}(b\_type, type)$   
 $f: \text{\$i} \rightarrow \text{\$i} \quad \text{tff}(f\_type, type)$   
 $g: (\text{\$i} \times \text{\$i}) \rightarrow \text{\$i} \quad \text{tff}(g\_type, type)$   
 $h: (\text{\$i} \times \text{\$i} \times \text{\$i}) \rightarrow \text{\$i} \quad \text{tff}(h\_type, type)$   
 $p: \text{\$i} \rightarrow \text{\$o} \quad \text{tff}(p\_type, type)$   
 $q: (\text{\$i} \times \text{\$i}) \rightarrow \text{\$o} \quad \text{tff}(q\_type, type)$   
 $\forall z: \text{\$i}: \text{Site\_f}(\exists x: \text{\$i}: p(x), \forall x: \text{\$i}: q(x, x), q(z, \text{Site\_t}(\forall x: \text{\$i}: p(x), f(a), f(z)))) \quad \text{tff}(\text{conditionals}, \text{axiom})$   
 $\forall x: \text{\$i}: \text{\$let\_ff}(\forall y_1: \text{\$i}, y_2: \text{\$i}: (q(y_1, y_2) \iff p(y_1)), q(\text{\$let\_tt}(\forall z_1: \text{\$i}: f(z_1) = g(z_1, b), f(a)), x) \text{ and } p(\text{\$let\_ft}(\forall y_3: \text{\$i}, y_4: \text{\$i}: (q(y_3 = y_4, q(a, a), q(y_3, y_4))), \text{Site\_t}(q(b, b), f(a), f(x)))))) \quad \text{tff}(\text{let\_binders}, \text{axiom})$   
 $\forall x: \text{\$i}: (p(x) \text{ nor } \neg q(x, a)) \text{ nand } p(x) \quad \text{tff}(\text{never\_used\_connectives}, \text{axiom})$   
 $\forall x: \text{\$i}: f(a) = f(x) \quad \text{tff}(\text{role\_definition}, \text{definition})$   
 $p(a) \quad \text{tff}(\text{role\_assumption}, \text{assumption})$   
 $p(a) \quad \text{tff}(\text{role\_lemma}, \text{lemma})$   
 $p(a) \quad \text{tff}(\text{role\_theorem}, \text{theorem})$   
 $p(a) \quad \text{tff}(\text{role\_unknown}, \text{unknown})$   
 $\text{include}(\text{'Axioms/SYN000.0.ax'}, [ia_1, ia_3])$   
 $\forall x: \text{\$i}: p(x) \quad \text{tff}(\text{source\_unknown}, \text{axiom})$   
 $\forall x: \text{\$i}: p(x) \quad \text{tff}(\text{source}, \text{axiom})$   
 $\forall x: \text{\$i}: p(x) \quad \text{tff}(\text{source\_name}, \text{axiom})$   
 $\forall x: \text{\$i}: p(x) \quad \text{tff}(\text{source\_copy}, \text{axiom})$   
 $\forall x: \text{\$i}: p(x) \quad \text{tff}(\text{source\_introduced\_assumption}, \text{axiom})$   
 $p(a) \quad \text{tff}(\text{source\_inference}, \text{axiom})$   
 $p(a) \quad \text{tff}(\text{source\_inference\_with\_bind}, \text{axiom})$   
 $\forall x: \text{\$i}: p(x) \quad \text{tff}(\text{useful\_info}, \text{axiom})$

### SYN001+1.p Pelletier 2

2: A biconditional version of the 'most difficult' theorem proved by the new logic theorist.

$\neg \neg p \iff p \quad \text{fof}(\text{pel}_2, \text{conjecture})$

### SYN001^4.001.p Pelletier 2

$\text{include}(\text{'Axioms/LCL010^0.ax'})$

$p: \text{\$i} \rightarrow \text{\$o} \quad \text{thf}(p\_type, type)$

$\text{invalid}@\text{(iequiv}@\text{(inot}@\text{(inot}@\text{(iatom}@\text{p})))}@\text{(iatom}@\text{p}))} \quad \text{thf}(\text{pel}_2, \text{conjecture})$

### SYN001^4.002.p ILTP Problem SYJ212+1.002

$\text{include}(\text{'Axioms/LCL010^0.ax'})$

$a_1: \text{\$i} \rightarrow \text{\$o} \quad \text{thf}(a1\_type, type)$

$a_2: \text{\$i} \rightarrow \text{\$o} \quad \text{thf}(a2\_type, type)$

$\text{invalid}@\text{(iequiv}@\text{(iequiv}@\text{(inot}@\text{(inot}@\text{(iatom}@\text{a}_1)))}@\text{(iatom}@\text{a}_2))}@\text{(iequiv}@\text{(iatom}@\text{a}_2)}@\text{(iatom}@\text{a}_1)))} \quad \text{thf}(\text{con}, \text{conjecture})$

### SYN001^4.003.p ILTP Problem SYJ212+1.003

$\text{include}(\text{'Axioms/LCL010^0.ax'})$

$a_1: \text{\$i} \rightarrow \text{\$o} \quad \text{thf}(a1\_type, type)$

$a_2: \text{\$i} \rightarrow \text{\$o} \quad \text{thf}(a2\_type, type)$

$a_3: \text{\$i} \rightarrow \text{\$o} \quad \text{thf}(a3\_type, type)$

$\text{invalid}@\text{(iequiv}@\text{(iequiv}@\text{(iequiv}@\text{(inot}@\text{(inot}@\text{(iatom}@\text{a}_1)))}@\text{(iatom}@\text{a}_2))}@\text{(iatom}@\text{a}_3))}@\text{(iequiv}@\text{(iatom}@\text{a}_3)}@\text{(iequiv}@\text{(iatom}@\text{a}_2)}@\text{(iatom}@\text{a}_1)))} \quad \text{thf}(\text{con}, \text{conjecture})$

### SYN001^4.004.p ILTP Problem SYJ212+1.004

$\text{include}(\text{'Axioms/LCL010^0.ax'})$

$a_1: \text{\$i} \rightarrow \text{\$o} \quad \text{thf}(a1\_type, type)$

$a_2: \text{\$i} \rightarrow \text{\$o} \quad \text{thf}(a2\_type, type)$

$a_3: \text{\$i} \rightarrow \text{\$o} \quad \text{thf}(a3\_type, type)$

$a_4: \text{\$i} \rightarrow \text{\$o} \quad \text{thf}(a4\_type, type)$

$\text{invalid}@\text{(iequiv}@\text{(iequiv}@\text{(iequiv}@\text{(iequiv}@\text{(inot}@\text{(inot}@\text{(iatom}@\text{a}_1)))}@\text{(iatom}@\text{a}_2))}@\text{(iatom}@\text{a}_3))}@\text{(iatom}@\text{a}_4))}@\text{(iequiv}@\text{(iatom}@\text{a}_3)}@\text{(iequiv}@\text{(iatom}@\text{a}_2)}@\text{(iequiv}@\text{(iatom}@\text{a}_1)}@\text{(iatom}@\text{a}_4)))} \quad \text{thf}(\text{con}, \text{conjecture})$

### SYN002-1.007.008.p Odd and Even Problem

Given by the clauses C1:  $p(X) \vee p(f \wedge M(X))$  and C2:  $p(X) \vee p(f \wedge N(X))$ , where if M is odd N is even and vice versa,  $N > M$ . The sizes are used for N and M.

$p(x) \text{ or } p(f(f(f(f(f(f(f(x)))))))) \quad \text{cnf}(\text{positive}, \text{negated\_conjecture})$

$p(x) \Rightarrow \neg p(f(f(f(f(f(f(f(x)))))))) \quad \text{cnf}(\text{negative}, \text{negated\_conjecture})$

### SYN003-1.006.p Implications that form a contradiction

$P1 \ \& \ Q1 \rightarrow P2 \ P1 \ \& \ R1 \rightarrow P2 \ Q \rightarrow Q1 \ R \rightarrow R1 : P2 \ \& \ Q2 \rightarrow P3 \ P2 \ \& \ R2 \rightarrow P3 \ Q \rightarrow Q2 \ R \rightarrow R2 : \dots \dots \dots$   
 $\dots : P_{k-1} \ \& \ Q_{k-1} \rightarrow P_k \ P_{k-1} \ \& \ R_{k-1} \rightarrow P_k \ Q \rightarrow Q_{k-1} \ R \rightarrow R_{k-1} : P1 \ P_k \ Q \ R : :$  The size is k, in the above.

$(p_1 \ \text{and} \ q_1) \Rightarrow p_2 \quad \text{cnf}(\text{pqp}_1, \text{negated\_conjecture})$   
 $(p_2 \ \text{and} \ q_2) \Rightarrow p_3 \quad \text{cnf}(\text{pqp}_2, \text{negated\_conjecture})$   
 $(p_3 \ \text{and} \ q_3) \Rightarrow p_4 \quad \text{cnf}(\text{pqp}_3, \text{negated\_conjecture})$   
 $(p_4 \ \text{and} \ q_4) \Rightarrow p_5 \quad \text{cnf}(\text{pqp}_4, \text{negated\_conjecture})$   
 $(p_5 \ \text{and} \ q_5) \Rightarrow p_6 \quad \text{cnf}(\text{pqp}_5, \text{negated\_conjecture})$   
 $(p_1 \ \text{and} \ r_1) \Rightarrow p_2 \quad \text{cnf}(\text{prp}_1, \text{negated\_conjecture})$   
 $(p_2 \ \text{and} \ r_2) \Rightarrow p_3 \quad \text{cnf}(\text{prp}_2, \text{negated\_conjecture})$   
 $(p_3 \ \text{and} \ r_3) \Rightarrow p_4 \quad \text{cnf}(\text{prp}_3, \text{negated\_conjecture})$   
 $(p_4 \ \text{and} \ r_4) \Rightarrow p_5 \quad \text{cnf}(\text{prp}_4, \text{negated\_conjecture})$   
 $(p_5 \ \text{and} \ r_5) \Rightarrow p_6 \quad \text{cnf}(\text{prp}_5, \text{negated\_conjecture})$   
 $q \Rightarrow q_1 \quad \text{cnf}(\text{qq}_1, \text{negated\_conjecture})$   
 $q \Rightarrow q_2 \quad \text{cnf}(\text{qq}_2, \text{negated\_conjecture})$   
 $q \Rightarrow q_3 \quad \text{cnf}(\text{qq}_3, \text{negated\_conjecture})$   
 $q \Rightarrow q_4 \quad \text{cnf}(\text{qq}_4, \text{negated\_conjecture})$   
 $q \Rightarrow q_5 \quad \text{cnf}(\text{qq}_5, \text{negated\_conjecture})$   
 $r \Rightarrow r_1 \quad \text{cnf}(\text{rr}_1, \text{negated\_conjecture})$   
 $r \Rightarrow r_2 \quad \text{cnf}(\text{rr}_2, \text{negated\_conjecture})$   
 $r \Rightarrow r_3 \quad \text{cnf}(\text{rr}_3, \text{negated\_conjecture})$   
 $r \Rightarrow r_4 \quad \text{cnf}(\text{rr}_4, \text{negated\_conjecture})$   
 $r \Rightarrow r_5 \quad \text{cnf}(\text{rr}_5, \text{negated\_conjecture})$   
 $p_1 \quad \text{cnf}(\text{base}_1, \text{negated\_conjecture})$   
 $\neg p_6 \quad \text{cnf}(\text{base}_2, \text{negated\_conjecture})$   
 $q \quad \text{cnf}(\text{base}_3, \text{negated\_conjecture})$   
 $r \quad \text{cnf}(\text{base}_4, \text{negated\_conjecture})$

**SYN004-1.007.p** Implications that form a contradiction

$P1 \ \& \ Q1 \rightarrow P2 \ P1 \ \& \ Q1 \rightarrow Q2 : P2 \ \& \ Q2 \rightarrow P3 \ P2 \ \& \ Q2 \rightarrow Q3 : \dots \dots \dots : P_{k-1} \ \& \ Q_{k-1} \rightarrow P_k \ P_{k-1} \ \& \ Q_{k-1} \rightarrow$   
 $Q_k : P1 \ Q1 \ P_k \vee \ Q_k : :$  The size is k, in the above.

$(p_1 \ \text{and} \ q_1) \Rightarrow p_2 \quad \text{cnf}(\text{pqp}_1, \text{negated\_conjecture})$   
 $(p_2 \ \text{and} \ q_2) \Rightarrow p_3 \quad \text{cnf}(\text{pqp}_2, \text{negated\_conjecture})$   
 $(p_3 \ \text{and} \ q_3) \Rightarrow p_4 \quad \text{cnf}(\text{pqp}_3, \text{negated\_conjecture})$   
 $(p_4 \ \text{and} \ q_4) \Rightarrow p_5 \quad \text{cnf}(\text{pqp}_4, \text{negated\_conjecture})$   
 $(p_5 \ \text{and} \ q_5) \Rightarrow p_6 \quad \text{cnf}(\text{pqp}_5, \text{negated\_conjecture})$   
 $(p_6 \ \text{and} \ q_6) \Rightarrow p_7 \quad \text{cnf}(\text{pqp}_6, \text{negated\_conjecture})$   
 $(p_1 \ \text{and} \ q_1) \Rightarrow q_2 \quad \text{cnf}(\text{pqq}_1, \text{negated\_conjecture})$   
 $(p_2 \ \text{and} \ q_2) \Rightarrow q_3 \quad \text{cnf}(\text{pqq}_2, \text{negated\_conjecture})$   
 $(p_3 \ \text{and} \ q_3) \Rightarrow q_4 \quad \text{cnf}(\text{pqq}_3, \text{negated\_conjecture})$   
 $(p_4 \ \text{and} \ q_4) \Rightarrow q_5 \quad \text{cnf}(\text{pqq}_4, \text{negated\_conjecture})$   
 $(p_5 \ \text{and} \ q_5) \Rightarrow q_6 \quad \text{cnf}(\text{pqq}_5, \text{negated\_conjecture})$   
 $(p_6 \ \text{and} \ q_6) \Rightarrow q_7 \quad \text{cnf}(\text{pqq}_6, \text{negated\_conjecture})$   
 $p_1 \quad \text{cnf}(\text{base}_1, \text{negated\_conjecture})$   
 $q_1 \quad \text{cnf}(\text{base}_2, \text{negated\_conjecture})$   
 $p_7 \Rightarrow \neg q_7 \quad \text{cnf}(\text{base}_3, \text{negated\_conjecture})$

**SYN005-1.010.p** Disjunctions that form a contradiction

$p1(X1,X2) \vee p2(X2,X3) \vee \dots \vee p10(X10,X1). \ p1(a,a) \ p2(a,a) \dots \ p10(a,a)$

$(p_1(x_1, x_2) \ \text{and} \ p_2(x_2, x_3) \ \text{and} \ p_3(x_3, x_4) \ \text{and} \ p_4(x_4, x_5) \ \text{and} \ p_5(x_5, x_6) \ \text{and} \ p_6(x_6, x_7) \ \text{and} \ p_7(x_7, x_8) \ \text{and} \ p_8(x_8, x_9) \ \text{and} \ p_9(x_9, x_{10}) \ \text{and} \ p_{10}(x_{10}, x_1))$   
 $\neg p_{10}(x_{10}, x_1) \quad \text{cnf}(\text{disjunction, negated\_conjecture})$

$p_1(a, a) \quad \text{cnf}(p_1, \text{negated\_conjecture})$   
 $p_2(a, a) \quad \text{cnf}(p_2, \text{negated\_conjecture})$   
 $p_3(a, a) \quad \text{cnf}(p_3, \text{negated\_conjecture})$   
 $p_4(a, a) \quad \text{cnf}(p_4, \text{negated\_conjecture})$   
 $p_5(a, a) \quad \text{cnf}(p_5, \text{negated\_conjecture})$   
 $p_6(a, a) \quad \text{cnf}(p_6, \text{negated\_conjecture})$   
 $p_7(a, a) \quad \text{cnf}(p_7, \text{negated\_conjecture})$   
 $p_8(a, a) \quad \text{cnf}(p_8, \text{negated\_conjecture})$   
 $p_9(a, a) \quad \text{cnf}(p_9, \text{negated\_conjecture})$   
 $p_{10}(a, a) \quad \text{cnf}(p_{10}, \text{negated\_conjecture})$

**SYN006-1.p** A problem to demonstrate controlling splits

```

p1(x, f(y)) => (q1(f(x), y) or q2(x, f(y)))    cnf(clause1, negated_conjecture)
p1(a, y)    cnf(clause2, negated_conjecture)
¬ q2(x, f(y))    cnf(clause3, negated_conjecture)
p2(x, f(y)) => (q3(f(x), y) or q4(x, f(y)))    cnf(clause4, negated_conjecture)
¬ q3(x, g(y))    cnf(clause5, negated_conjecture)
¬ q4(f(f(x)), f(g(f(y))))    cnf(clause6, negated_conjecture)
q1(x, f(y)) => p2(f(x), y)    cnf(clause7, negated_conjecture)

```

**SYN007+1.014.p** Pelletier Problem 71

Clausal forms of statements of the form : (p1 <=> (p2 <=>... (pN <=> (p1 <=> (p2 <=>...<=> pN)...))

```

p1 <=> (p2 <=> (p3 <=> (p4 <=> (p5 <=> (p6 <=> (p7 <=> (p8 <=> (p9 <=> (p10 <=> (p11 <=>
(p12 <=> (p13 <=> (p14 <=> (p1 <=> (p2 <=> (p3 <=> (p4 <=> (p5 <=> (p6 <=> (p7 <=> (p8 <=>
(p9 <=> (p10 <=> (p11 <=> (p12 <=> (p13 <=> p14))))))))))))))))) fof(prove_this, conjecture)

```

**SYN007^4.014.p** Pelletier Problem 71

include('Axioms/LCL010^0.ax')

```

p1: $i -> $o    thf(p_1_type, type)
p10: $i -> $o   thf(p_10_type, type)
p11: $i -> $o   thf(p_11_type, type)
p12: $i -> $o   thf(p_12_type, type)
p13: $i -> $o   thf(p_13_type, type)
p14: $i -> $o   thf(p_14_type, type)
p2: $i -> $o    thf(p_2_type, type)
p3: $i -> $o    thf(p_3_type, type)
p4: $i -> $o    thf(p_4_type, type)
p5: $i -> $o    thf(p_5_type, type)
p6: $i -> $o    thf(p_6_type, type)
p7: $i -> $o    thf(p_7_type, type)
p8: $i -> $o    thf(p_8_type, type)
p9: $i -> $o    thf(p_9_type, type)
ivalid@(iequiv@(iatom@p1)@(iequiv@(iatom@p2)@(iequiv@(iatom@p3)@(iequiv@(iatom@p4)@(iequiv@(iatom@p5)@(iequiv@

```

**SYN008-1.p** A problem to demonstrate the usefulness of relevancy testing

```

¬ p    cnf(clause1, negated_conjecture)
¬ q    cnf(clause2, negated_conjecture)
r      cnf(clause3, negated_conjecture)
r => (a or b)    cnf(clause4, negated_conjecture)
r => (p or c or d)    cnf(clause5, negated_conjecture)
r => (p or q)    cnf(clause6, negated_conjecture)

```

**SYN009-1.p** A problem to demonstrate the usefulness of relevancy testing

```

¬ p(c, x, y)    cnf(clause1, negated_conjecture)
¬ q(x, c, y)    cnf(clause2, negated_conjecture)
¬ r(x, y, c)    cnf(clause3, negated_conjecture)
s(a)           cnf(clause4, negated_conjecture)
s(b)           cnf(clause5, negated_conjecture)
s(c)           cnf(clause6, negated_conjecture)
(s(x) and s(y) and s(z)) => (p(x, y, z) or q(x, y, z) or r(x, y, z))    cnf(clause7, negated_conjecture)

```

**SYN009-2.p** A problem to demonstrate the usefulness of relevancy testing

```

p(x, y, z) => ¬ t(x, y, z)    cnf(clause1, negated_conjecture)
q(x, y, z) => ¬ t(y, z, x)    cnf(clause2, negated_conjecture)
r(x, y, z) => ¬ t(z, x, y)    cnf(clause3, negated_conjecture)
s(a)       cnf(clause4, negated_conjecture)
s(b)       cnf(clause5, negated_conjecture)
s(c)       cnf(clause6, negated_conjecture)
t(c, c, c) cnf(clause7, negated_conjecture)
(s(x) and s(y) and s(z)) => (p(x, y, z) or q(y, z, x) or r(z, x, y))    cnf(clause8, negated_conjecture)

```

**SYN009-3.p** A problem to demonstrate the usefulness of relevancy testing

```

p(x, y, z) => ¬ t(x, y, z)    cnf(clause1, negated_conjecture)
q(x, y, z) => ¬ t(x, y, z)    cnf(clause2, negated_conjecture)

```

$r(x, y, z) \Rightarrow \neg t(x, y, z) \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $s(a) \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $s(b) \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $s(c) \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $\neg v(x, y, z) \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $u(c, c, c) \quad \text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $(s(x) \text{ and } s(y) \text{ and } s(z)) \Rightarrow (p(x, y, z) \text{ or } q(x, y, z) \text{ or } r(x, y, z)) \quad \text{cnf}(\text{clause}_9, \text{negated\_conjecture})$   
 $u(x, y, z) \Rightarrow (t(x, y, z) \text{ or } v(x, y, z)) \quad \text{cnf}(\text{clause}_{10}, \text{negated\_conjecture})$

**SYN009-4.p** A problem to demonstrate the usefulness of relevancy testing

$p(x, y, z) \Rightarrow \neg m(x, y, z) \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $q(x, y, z) \Rightarrow \neg m(x, y, z) \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture})$   
 $r(x, y, z) \Rightarrow \neg m(x, y, z) \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $s(a) \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $s(b) \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $s(c) \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $\neg n(c, c, c) \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $(s(x) \text{ and } s(y) \text{ and } s(z)) \Rightarrow (p(x, y, z) \text{ or } q(x, y, z) \text{ or } r(x, y, z)) \quad \text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $(s(x) \text{ and } s(y) \text{ and } s(z)) \Rightarrow (m(x, y, z) \text{ or } n(x, y, z)) \quad \text{cnf}(\text{clause}_9, \text{negated\_conjecture})$

**SYN010-1.005.005.p** Example for Proposition 5.2 in [LMG94]

Example to show that connection tableaux with factorization cannot polynomially simulate connection tableaux with folding up.

$\neg p_0 \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $(p_{.1_1} \text{ and } p_{.1_2} \text{ and } p_{.1_3} \text{ and } p_{.1_4} \text{ and } p_{.1_5}) \Rightarrow p_0 \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture})$   
 $(p_{.2_1} \text{ and } p_{.2_2} \text{ and } p_{.2_3} \text{ and } p_{.2_4} \text{ and } p_{.2_5}) \Rightarrow p_{.1_1} \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $(p_{.2_1} \text{ and } p_{.2_2} \text{ and } p_{.2_3} \text{ and } p_{.2_4} \text{ and } p_{.2_5}) \Rightarrow p_{.1_2} \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $(p_{.2_1} \text{ and } p_{.2_2} \text{ and } p_{.2_3} \text{ and } p_{.2_4} \text{ and } p_{.2_5}) \Rightarrow p_{.1_3} \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $(p_{.2_1} \text{ and } p_{.2_2} \text{ and } p_{.2_3} \text{ and } p_{.2_4} \text{ and } p_{.2_5}) \Rightarrow p_{.1_4} \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $(p_{.2_1} \text{ and } p_{.2_2} \text{ and } p_{.2_3} \text{ and } p_{.2_4} \text{ and } p_{.2_5}) \Rightarrow p_{.1_5} \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $(p_{.3_1} \text{ and } p_{.3_2} \text{ and } p_{.3_3} \text{ and } p_{.3_4} \text{ and } p_{.3_5}) \Rightarrow p_{.2_1} \quad \text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $(p_{.3_1} \text{ and } p_{.3_2} \text{ and } p_{.3_3} \text{ and } p_{.3_4} \text{ and } p_{.3_5}) \Rightarrow p_{.2_2} \quad \text{cnf}(\text{clause}_9, \text{negated\_conjecture})$   
 $(p_{.3_1} \text{ and } p_{.3_2} \text{ and } p_{.3_3} \text{ and } p_{.3_4} \text{ and } p_{.3_5}) \Rightarrow p_{.2_3} \quad \text{cnf}(\text{clause}_{10}, \text{negated\_conjecture})$   
 $(p_{.3_1} \text{ and } p_{.3_2} \text{ and } p_{.3_3} \text{ and } p_{.3_4} \text{ and } p_{.3_5}) \Rightarrow p_{.2_4} \quad \text{cnf}(\text{clause}_{11}, \text{negated\_conjecture})$   
 $(p_{.3_1} \text{ and } p_{.3_2} \text{ and } p_{.3_3} \text{ and } p_{.3_4} \text{ and } p_{.3_5}) \Rightarrow p_{.2_5} \quad \text{cnf}(\text{clause}_{12}, \text{negated\_conjecture})$   
 $(p_{.4_1} \text{ and } p_{.4_2} \text{ and } p_{.4_3} \text{ and } p_{.4_4} \text{ and } p_{.4_5}) \Rightarrow p_{.3_1} \quad \text{cnf}(\text{clause}_{13}, \text{negated\_conjecture})$   
 $(p_{.4_1} \text{ and } p_{.4_2} \text{ and } p_{.4_3} \text{ and } p_{.4_4} \text{ and } p_{.4_5}) \Rightarrow p_{.3_2} \quad \text{cnf}(\text{clause}_{14}, \text{negated\_conjecture})$   
 $(p_{.4_1} \text{ and } p_{.4_2} \text{ and } p_{.4_3} \text{ and } p_{.4_4} \text{ and } p_{.4_5}) \Rightarrow p_{.3_3} \quad \text{cnf}(\text{clause}_{15}, \text{negated\_conjecture})$   
 $(p_{.4_1} \text{ and } p_{.4_2} \text{ and } p_{.4_3} \text{ and } p_{.4_4} \text{ and } p_{.4_5}) \Rightarrow p_{.3_4} \quad \text{cnf}(\text{clause}_{16}, \text{negated\_conjecture})$   
 $(p_{.4_1} \text{ and } p_{.4_2} \text{ and } p_{.4_3} \text{ and } p_{.4_4} \text{ and } p_{.4_5}) \Rightarrow p_{.3_5} \quad \text{cnf}(\text{clause}_{17}, \text{negated\_conjecture})$   
 $(p_{.5_1} \text{ and } p_{.5_2} \text{ and } p_{.5_3} \text{ and } p_{.5_4} \text{ and } p_{.5_5}) \Rightarrow p_{.4_1} \quad \text{cnf}(\text{clause}_{18}, \text{negated\_conjecture})$   
 $(p_{.5_1} \text{ and } p_{.5_2} \text{ and } p_{.5_3} \text{ and } p_{.5_4} \text{ and } p_{.5_5}) \Rightarrow p_{.4_2} \quad \text{cnf}(\text{clause}_{19}, \text{negated\_conjecture})$   
 $(p_{.5_1} \text{ and } p_{.5_2} \text{ and } p_{.5_3} \text{ and } p_{.5_4} \text{ and } p_{.5_5}) \Rightarrow p_{.4_3} \quad \text{cnf}(\text{clause}_{20}, \text{negated\_conjecture})$   
 $(p_{.5_1} \text{ and } p_{.5_2} \text{ and } p_{.5_3} \text{ and } p_{.5_4} \text{ and } p_{.5_5}) \Rightarrow p_{.4_4} \quad \text{cnf}(\text{clause}_{21}, \text{negated\_conjecture})$   
 $(p_{.5_1} \text{ and } p_{.5_2} \text{ and } p_{.5_3} \text{ and } p_{.5_4} \text{ and } p_{.5_5}) \Rightarrow p_{.4_5} \quad \text{cnf}(\text{clause}_{22}, \text{negated\_conjecture})$   
 $p_{.5_1} \quad \text{cnf}(\text{clause}_{23}, \text{negated\_conjecture})$   
 $p_{.5_2} \quad \text{cnf}(\text{clause}_{24}, \text{negated\_conjecture})$   
 $p_{.5_3} \quad \text{cnf}(\text{clause}_{25}, \text{negated\_conjecture})$   
 $p_{.5_4} \quad \text{cnf}(\text{clause}_{26}, \text{negated\_conjecture})$   
 $p_{.5_5} \quad \text{cnf}(\text{clause}_{27}, \text{negated\_conjecture})$

**SYN011-1.p** A problem to demonstrate C-reduction

$n \Rightarrow \neg t \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $m \text{ or } q \text{ or } n \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture})$   
 $m \Rightarrow l \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $q \Rightarrow l \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $l \Rightarrow \neg p \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $r \text{ or } p \text{ or } n \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $r \Rightarrow \neg l \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $t \quad \text{cnf}(\text{clause}_8, \text{negated\_conjecture})$

**SYN012-1.p** A problem to demonstrate Model Elimination

$(\text{big\_f}(x, y) \text{ and } \text{big\_f}(x, g(x, y))) \Rightarrow \text{big\_g}(y, g(x, y)) \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $(\text{big\_f}(x, y) \text{ and } \text{big\_g}(y, g(x, y))) \Rightarrow \text{big\_f}(x, g(x, y)) \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture})$   
 $(\text{big\_f}(x, y) \text{ and } \text{big\_f}(g(x, y), g(x, y))) \Rightarrow \text{big\_g}(g(x, y), g(x, y)) \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $\text{big\_f}(x, y) \text{ or } \text{big\_f}(g(x, y), g(x, y)) \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $\text{big\_g}(g(x, y), g(x, y)) \Rightarrow \text{big\_f}(x, y) \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $\text{big\_g}(x, y) \text{ or } \text{big\_g}(g(x, y), g(x, y)) \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $\text{big\_g}(x, y) \Rightarrow \neg \text{big\_g}(g(x, y), g(x, y)) \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$

**SYN013-1.p** A problem in quantification theory

$m \neq n \quad \text{cnf}(c_1, \text{negated\_conjecture})$   
 $n \neq k \quad \text{cnf}(c_2, \text{negated\_conjecture})$   
 $k \neq m \quad \text{cnf}(c_3, \text{negated\_conjecture})$   
 $(\text{element}(y, m) \text{ and } f(y) = m) \Rightarrow y = m \quad \text{cnf}(c_4, \text{negated\_conjecture})$   
 $(\text{element}(y, m) \text{ and } f(y) = y) \Rightarrow y = m \quad \text{cnf}(c_5, \text{negated\_conjecture})$   
 $\text{element}(y, m) \Rightarrow (y = m \text{ or } \text{element}(y, f(y))) \quad \text{cnf}(c_6, \text{negated\_conjecture})$   
 $\text{element}(y, m) \Rightarrow (y = m \text{ or } \text{element}(f(y), y)) \quad \text{cnf}(c_7, \text{negated\_conjecture})$   
 $(\text{element}(y, v) \text{ and } \text{element}(v, y)) \Rightarrow (y = m \text{ or } \text{element}(y, m) \text{ or } v = m \text{ or } v = y) \quad \text{cnf}(c_8, \text{negated\_conjecture})$   
 $g(y) = n \Rightarrow (y = n \text{ or } \text{element}(y, n)) \quad \text{cnf}(c_9, \text{negated\_conjecture})$   
 $g(y) = y \Rightarrow (y = n \text{ or } \text{element}(y, n)) \quad \text{cnf}(c_{10}, \text{negated\_conjecture})$   
 $y = n \text{ or } \text{element}(y, n) \text{ or } \text{element}(y, g(y)) \quad \text{cnf}(c_{11}, \text{negated\_conjecture})$   
 $y = n \text{ or } \text{element}(y, n) \text{ or } \text{element}(g(y), y) \quad \text{cnf}(c_{12}, \text{negated\_conjecture})$   
 $(\text{element}(y, n) \text{ and } \text{element}(y, v) \text{ and } \text{element}(v, y)) \Rightarrow (y = n \text{ or } v = n \text{ or } v = y) \quad \text{cnf}(c_{13}, \text{negated\_conjecture})$   
 $y = m \Rightarrow (y = k \text{ or } \text{element}(y, k)) \quad \text{cnf}(c_{14}, \text{negated\_conjecture})$   
 $y = n \Rightarrow (y = k \text{ or } \text{element}(y, k)) \quad \text{cnf}(c_{15}, \text{negated\_conjecture})$   
 $\text{element}(y, k) \Rightarrow (y = k \text{ or } y = m \text{ or } y = n) \quad \text{cnf}(c_{16}, \text{negated\_conjecture})$

**SYN014-1.p** A problem in quantification theory

$m \neq n \quad \text{cnf}(c_1, \text{negated\_conjecture})$   
 $n = k \text{ or } m = k \quad \text{cnf}(c_2, \text{negated\_conjecture})$   
 $y = k \Rightarrow (y = j \text{ or } \text{element}(y, j)) \quad \text{cnf}(c_3, \text{negated\_conjecture})$   
 $\text{element}(y, j) \Rightarrow (y = j \text{ or } y = k) \quad \text{cnf}(c_4, \text{negated\_conjecture})$   
 $(\text{element}(y, m) \text{ and } f(y) = m) \Rightarrow y = m \quad \text{cnf}(c_5, \text{negated\_conjecture})$   
 $(\text{element}(y, m) \text{ and } f(y) = y) \Rightarrow y = m \quad \text{cnf}(c_6, \text{negated\_conjecture})$   
 $\text{element}(y, m) \Rightarrow (y = m \text{ or } \text{element}(y, f(y))) \quad \text{cnf}(c_7, \text{negated\_conjecture})$   
 $\text{element}(y, m) \Rightarrow (y = m \text{ or } \text{element}(f(y), y)) \quad \text{cnf}(c_8, \text{negated\_conjecture})$   
 $(\text{element}(y, v_1) \text{ and } \text{element}(v_1, y)) \Rightarrow (y = m \text{ or } \text{element}(y, m) \text{ or } v_1 = m \text{ or } v_1 = y) \quad \text{cnf}(c_9, \text{negated\_conjecture})$   
 $g(y) = n \Rightarrow (y = n \text{ or } \text{element}(y, n)) \quad \text{cnf}(c_{10}, \text{negated\_conjecture})$   
 $g(y) = y \Rightarrow (y = n \text{ or } \text{element}(y, n)) \quad \text{cnf}(c_{11}, \text{negated\_conjecture})$   
 $y = n \text{ or } \text{element}(y, n) \text{ or } \text{element}(y, g(y)) \quad \text{cnf}(c_{12}, \text{negated\_conjecture})$   
 $y = n \text{ or } \text{element}(y, n) \text{ or } \text{element}(g(y), y) \quad \text{cnf}(c_{13}, \text{negated\_conjecture})$   
 $(\text{element}(y, n) \text{ and } \text{element}(y, v) \text{ and } \text{element}(v, y)) \Rightarrow (y = n \text{ or } v = n \text{ or } v = y) \quad \text{cnf}(c_{14}, \text{negated\_conjecture})$   
 $y = m \Rightarrow (y = k \text{ or } \text{element}(y, k)) \quad \text{cnf}(c_{15}, \text{negated\_conjecture})$   
 $y = n \Rightarrow (y = k \text{ or } \text{element}(y, k)) \quad \text{cnf}(c_{16}, \text{negated\_conjecture})$   
 $\text{element}(y, k) \Rightarrow (y = k \text{ or } y = m \text{ or } y = n) \quad \text{cnf}(c_{17}, \text{negated\_conjecture})$

**SYN014-2.p** A problem in quantification theory

$x=x \quad \text{cnf}(\text{reflexivityish}, \text{axiom})$   
 $x=y \Rightarrow y=x \quad \text{cnf}(\text{symmetryish}, \text{axiom})$   
 $(x=y \text{ and } y=z) \Rightarrow x=z \quad \text{cnf}(\text{transitivityish}, \text{axiom})$   
 $(a=b \text{ and } \text{element}(c, a)) \Rightarrow \text{element}(c, b) \quad \text{cnf}(\text{element\_substitutionish}_1, \text{axiom})$   
 $(\text{element}(a, b) \text{ and } a=c) \Rightarrow \text{element}(c, b) \quad \text{cnf}(\text{element\_substitutionish}_2, \text{axiom})$   
 $\text{element}(a, a) \Rightarrow (a=k \text{ or } a=a) \quad \text{cnf}(c_3, \text{negated\_conjecture})$   
 $a=k \Rightarrow (\text{element}(a, a) \text{ or } a=a) \quad \text{cnf}(c_4, \text{negated\_conjecture})$   
 $(f(a)=m \text{ and } \text{element}(a, m)) \Rightarrow a=m \quad \text{cnf}(c_5, \text{negated\_conjecture})$   
 $(f(a)=a \text{ and } \text{element}(a, m)) \Rightarrow a=m \quad \text{cnf}(c_6, \text{negated\_conjecture})$   
 $\text{element}(a, m) \Rightarrow (\text{element}(a, f(a)) \text{ or } a=m) \quad \text{cnf}(c_7, \text{negated\_conjecture})$   
 $\text{element}(a, m) \Rightarrow (\text{element}(f(a), a) \text{ or } a=m) \quad \text{cnf}(c_8, \text{negated\_conjecture})$   
 $(\text{element}(a, b) \text{ and } \text{element}(b, a)) \Rightarrow (a=b \text{ or } a=m \text{ or } \text{element}(b, m) \text{ or } b=m) \quad \text{cnf}(c_9, \text{negated\_conjecture})$   
 $g(a)=n \Rightarrow (\text{element}(a, n) \text{ or } a=n) \quad \text{cnf}(c_{10}, \text{negated\_conjecture})$   
 $g(a)=a \Rightarrow (\text{element}(a, n) \text{ or } a=n) \quad \text{cnf}(c_{11}, \text{negated\_conjecture})$



$\text{element}(a, g(a))$  or  $\text{element}(a, n)$  or  $a=n$      $\text{cnf}(c_{12}, \text{negated\_conjecture})$   
 $\text{element}(g(a), a)$  or  $\text{element}(a, n)$  or  $a=n$      $\text{cnf}(c_{13}, \text{negated\_conjecture})$   
 $(\text{element}(a, b) \text{ and } \text{element}(b, a) \text{ and } \text{element}(b, n)) \Rightarrow (a=b \text{ or } a=n \text{ or } b=n)$      $\text{cnf}(c_{14}, \text{negated\_conjecture})$   
 $a=m \Rightarrow (\text{element}(a, k) \text{ or } a=k)$      $\text{cnf}(c_{15}, \text{negated\_conjecture})$   
 $a=n \Rightarrow (\text{element}(a, k) \text{ or } a=k)$      $\text{cnf}(c_{16}, \text{negated\_conjecture})$   
 $\text{element}(a, k) \Rightarrow (a=n \text{ or } a=m \text{ or } a=k)$      $\text{cnf}(c_{17}, \text{negated\_conjecture})$   
 $\neg n=a$      $\text{cnf}(c_{18}, \text{negated\_conjecture})$   
 $\neg m=n$      $\text{cnf}(c_{19}, \text{negated\_conjecture})$   
 $n=k$      $\text{cnf}(c_{20}, \text{negated\_conjecture})$   
 $\neg m=a$      $\text{cnf}(c_{21}, \text{negated\_conjecture})$   
 $\neg k=a$      $\text{cnf}(c_{22}, \text{negated\_conjecture})$   
 $m=k$      $\text{cnf}(c_{23}, \text{negated\_conjecture})$

**SYN015-1.p** A problem in quantification theory

$m \neq n$      $\text{cnf}(c_1, \text{negated\_conjecture})$   
 $y = k \Rightarrow (y = j \text{ or } \text{element}(y, j))$      $\text{cnf}(c_2, \text{negated\_conjecture})$   
 $\text{element}(y, j) \Rightarrow (y = j \text{ or } y = k)$      $\text{cnf}(c_3, \text{negated\_conjecture})$   
 $(\text{element}(y, m) \text{ and } f(y) = m) \Rightarrow y = m$      $\text{cnf}(c_4, \text{negated\_conjecture})$   
 $(\text{element}(y, m) \text{ and } f(y) = y) \Rightarrow y = m$      $\text{cnf}(c_5, \text{negated\_conjecture})$   
 $\text{element}(y, m) \Rightarrow (y = m \text{ or } \text{element}(y, f(y)))$      $\text{cnf}(c_6, \text{negated\_conjecture})$   
 $\text{element}(y, m) \Rightarrow (y = m \text{ or } \text{element}(f(y), y))$      $\text{cnf}(c_7, \text{negated\_conjecture})$   
 $(\text{element}(y, v_1) \text{ and } \text{element}(v_1, y)) \Rightarrow (y = m \text{ or } \text{element}(y, m) \text{ or } v_1 = m \text{ or } v_1 = y)$      $\text{cnf}(c_8, \text{negated\_conjecture})$   
 $g(y) = n \Rightarrow (y = n \text{ or } \text{element}(y, n))$      $\text{cnf}(c_9, \text{negated\_conjecture})$   
 $g(y) = y \Rightarrow (y = n \text{ or } \text{element}(y, n))$      $\text{cnf}(c_{10}, \text{negated\_conjecture})$   
 $y = n \text{ or } \text{element}(y, n) \text{ or } \text{element}(y, g(y))$      $\text{cnf}(c_{11}, \text{negated\_conjecture})$   
 $y = n \text{ or } \text{element}(y, n) \text{ or } \text{element}(g(y), y)$      $\text{cnf}(c_{12}, \text{negated\_conjecture})$   
 $(\text{element}(y, n) \text{ and } \text{element}(y, v) \text{ and } \text{element}(v, y)) \Rightarrow (y = n \text{ or } v = n \text{ or } v = y)$      $\text{cnf}(c_{13}, \text{negated\_conjecture})$   
 $y = m \Rightarrow (y = k \text{ or } \text{element}(y, k))$      $\text{cnf}(c_{14}, \text{negated\_conjecture})$   
 $y = n \Rightarrow (y = k \text{ or } \text{element}(y, k))$      $\text{cnf}(c_{15}, \text{negated\_conjecture})$   
 $\text{element}(y, k) \Rightarrow (y = k \text{ or } y = m \text{ or } y = n)$      $\text{cnf}(c_{16}, \text{negated\_conjecture})$

**SYN015-2.p** A problem in quantification theory

$x=x$      $\text{cnf}(\text{reflexivityish}, \text{axiom})$   
 $x=y \Rightarrow y=x$      $\text{cnf}(\text{symmetryish}, \text{axiom})$   
 $(x=y \text{ and } y=z) \Rightarrow x=z$      $\text{cnf}(\text{transitivityish}, \text{axiom})$   
 $(a=b \text{ and } \text{element}(c, a)) \Rightarrow \text{element}(c, b)$      $\text{cnf}(\text{element\_substitutionish}_1, \text{axiom})$   
 $(\text{element}(a, b) \text{ and } a=c) \Rightarrow \text{element}(c, b)$      $\text{cnf}(\text{element\_substitutionish}_2, \text{axiom})$   
 $\text{element}(a, a) \Rightarrow (a=k \text{ or } a=a)$      $\text{cnf}(c_3, \text{negated\_conjecture})$   
 $a=k \Rightarrow (\text{element}(a, a) \text{ or } a=a)$      $\text{cnf}(c_4, \text{negated\_conjecture})$   
 $(f(a)=m \text{ and } \text{element}(a, m)) \Rightarrow a=m$      $\text{cnf}(c_5, \text{negated\_conjecture})$   
 $(f(a)=a \text{ and } \text{element}(a, m)) \Rightarrow a=m$      $\text{cnf}(c_6, \text{negated\_conjecture})$   
 $\text{element}(a, m) \Rightarrow (\text{element}(a, f(a)) \text{ or } a=m)$      $\text{cnf}(c_7, \text{negated\_conjecture})$   
 $\text{element}(a, m) \Rightarrow (\text{element}(f(a), a) \text{ or } a=m)$      $\text{cnf}(c_8, \text{negated\_conjecture})$   
 $(\text{element}(a, b) \text{ and } \text{element}(b, a)) \Rightarrow (a=b \text{ or } a=m \text{ or } \text{element}(b, m) \text{ or } b=m)$      $\text{cnf}(c_9, \text{negated\_conjecture})$   
 $g(a)=n \Rightarrow (\text{element}(a, n) \text{ or } a=n)$      $\text{cnf}(c_{10}, \text{negated\_conjecture})$   
 $g(a)=a \Rightarrow (\text{element}(a, n) \text{ or } a=n)$      $\text{cnf}(c_{11}, \text{negated\_conjecture})$   
 $\text{element}(a, g(a))$  or  $\text{element}(a, n)$  or  $a=n$      $\text{cnf}(c_{12}, \text{negated\_conjecture})$   
 $\text{element}(g(a), a)$  or  $\text{element}(a, n)$  or  $a=n$      $\text{cnf}(c_{13}, \text{negated\_conjecture})$   
 $(\text{element}(a, b) \text{ and } \text{element}(b, a) \text{ and } \text{element}(b, n)) \Rightarrow (a=b \text{ or } a=n \text{ or } b=n)$      $\text{cnf}(c_{14}, \text{negated\_conjecture})$   
 $a=m \Rightarrow (\text{element}(a, k) \text{ or } a=k)$      $\text{cnf}(c_{15}, \text{negated\_conjecture})$   
 $a=n \Rightarrow (\text{element}(a, k) \text{ or } a=k)$      $\text{cnf}(c_{16}, \text{negated\_conjecture})$   
 $\text{element}(a, k) \Rightarrow (a=n \text{ or } a=m \text{ or } a=k)$      $\text{cnf}(c_{17}, \text{negated\_conjecture})$   
 $\neg n=a$      $\text{cnf}(c_{18}, \text{negated\_conjecture})$   
 $\neg m=n$      $\text{cnf}(c_{19}, \text{negated\_conjecture})$   
 $\neg n=k$      $\text{cnf}(c_{20}, \text{negated\_conjecture})$   
 $\neg m=a$      $\text{cnf}(c_{21}, \text{negated\_conjecture})$   
 $\neg k=a$      $\text{cnf}(c_{22}, \text{negated\_conjecture})$   
 $m=k$      $\text{cnf}(c_{23}, \text{negated\_conjecture})$

**SYN028-1.p** EW1

$q$  or  $p$      $\text{cnf}(\text{clause}_1, \text{axiom})$

$q \Rightarrow r$     cnf(*clause*<sub>2</sub>, axiom)  
 $r \Rightarrow s$     cnf(*clause*<sub>3</sub>, axiom)  
 $(s \text{ and } r) \Rightarrow t$     cnf(*clause*<sub>4</sub>, axiom)  
 $t \Rightarrow p$     cnf(*clause*<sub>5</sub>, axiom)  
 $\neg p$     cnf(*prove\_something*, *negated\_conjecture*)

**SYN029-1.p EW2**

$q \text{ or } p$     cnf(*clause*<sub>1</sub>, axiom)  
 $p \Rightarrow q$     cnf(*clause*<sub>2</sub>, axiom)  
 $(r \text{ and } q) \Rightarrow p$     cnf(*clause*<sub>3</sub>, axiom)  
 $r$     cnf(*clause*<sub>4</sub>, axiom)  
 $p \Rightarrow \neg q$     cnf(*prove\_something*, *negated\_conjecture*)

**SYN030-1.p EW3**

$(t \text{ and } s) \Rightarrow p$     cnf(*clause*<sub>1</sub>, axiom)  
 $r \Rightarrow s$     cnf(*clause*<sub>2</sub>, axiom)  
 $t \Rightarrow r$     cnf(*clause*<sub>3</sub>, axiom)  
 $(r \text{ and } q) \Rightarrow t$     cnf(*clause*<sub>4</sub>, axiom)  
 $q \Rightarrow r$     cnf(*clause*<sub>5</sub>, axiom)  
 $q \text{ or } r$     cnf(*clause*<sub>6</sub>, axiom)  
 $r \Rightarrow q$     cnf(*clause*<sub>7</sub>, axiom)  
 $(s \text{ and } p) \Rightarrow q$     cnf(*clause*<sub>8</sub>, axiom)  
 $(p \text{ and } q) \Rightarrow \neg r$     cnf(*theorem*, *negated\_conjecture*)

**SYN031-1.p MQW**

$g(a, a) \text{ or } g(f(a), a)$     cnf(*clause*<sub>1</sub>, axiom)  
 $g(a, a) \text{ or } g(a, f(a))$     cnf(*clause*<sub>2</sub>, axiom)  
 $g(a, b) \Rightarrow g(f(b), b)$     cnf(*clause*<sub>3</sub>, axiom)  
 $g(a, b) \Rightarrow g(b, f(b))$     cnf(*clause*<sub>4</sub>, axiom)  
 $g(a, b) \Rightarrow \neg g(b, a)$     cnf(*theorem*, *negated\_conjecture*)

**SYN032-1.p Ances**

$j \Rightarrow (h \text{ or } a)$     cnf(*three*, *hypothesis*)  
 $h \text{ or } k \text{ or } j$     cnf(*four*, *hypothesis*)  
 $k \Rightarrow (h \text{ or } j)$     cnf(*five*, *hypothesis*)  
 $a \Rightarrow b$     cnf(*six*, *hypothesis*)  
 $h \Rightarrow c$     cnf(*seven*, *hypothesis*)  
 $h \Rightarrow \neg c$     cnf(*one*, *hypothesis*)  
 $a \Rightarrow \neg b$     cnf(*prove\_something*, *negated\_conjecture*)

**SYN033-1.p DM**

$p(g(a, b), a, b)$     cnf(*clause*<sub>1</sub>, axiom)  
 $p(a, h(a, b), b)$     cnf(*clause*<sub>2</sub>, axiom)  
 $(p(a, b, c) \text{ and } p(d, e, b) \text{ and } p(a, d, f)) \Rightarrow p(f, e, c)$     cnf(*clause*<sub>3</sub>, axiom)  
 $\neg p(k(a), a, k(a))$     cnf(*prove\_something*, *negated\_conjecture*)

**SYN034-1.p QW**

$p(a, a) \text{ or } p(a, f(a))$     cnf(*clause*<sub>1</sub>, axiom)  
 $p(a, a) \text{ or } p(f(a), a)$     cnf(*clause*<sub>2</sub>, axiom)  
 $(p(a, b) \text{ and } p(b, a)) \Rightarrow \neg p(b, a)$     cnf(*theorem*, *negated\_conjecture*)

**SYN035-1.p ROB1**

$p(a, b)$     cnf(*clause*<sub>1</sub>, axiom)  
 $(p(f(a, b), f(a, b)) \text{ and } p(b, f(a, b))) \Rightarrow q(a, b)$     cnf(*clause*<sub>2</sub>, axiom)  
 $(q(f(a, b), f(a, b)) \text{ and } q(a, f(a, b)) \text{ and } p(f(a, b), f(a, b))) \Rightarrow \neg p(b, f(a, b))$     cnf(*theorem*, *negated\_conjecture*)

**SYN036+1.p Andrews Challenge Problem**

$(\exists x: \forall y: (\text{big\_p}(x) \iff \text{big\_p}(y)) \iff (\exists u: \text{big\_q}(u) \iff \forall w: \text{big\_q}(w))) \iff (\exists x_1: \forall y_1: (\text{big\_q}(x_1) \iff \text{big\_q}(y_1)) \iff (\exists u_1: \text{big\_p}(u_1) \iff \forall w_1: \text{big\_p}(w_1)))$     fof(*pel*<sub>34</sub>, *conjecture*)

**SYN036+2.p Andrews Challenge Problem**

$(\exists x: \forall y: (\text{big\_p}(x) \iff \text{big\_p}(y)) \iff (\exists u: \text{big\_q}(u) \iff \forall w: \text{big\_p}(w))) \iff (\exists x_1: \forall y_1: (\text{big\_q}(x_1) \iff \text{big\_q}(y_1)) \iff (\exists u_1: \text{big\_p}(u_1) \iff \forall w_1: \text{big\_q}(w_1)))$     fof(*pel*<sub>34</sub>, *conjecture*)

**SYN036-3.p Andrews Challenge Problem**

$(n_2 \text{ and } n_9 \text{ and } n_6) \Rightarrow \neg n_{10}$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $(n_2 \text{ and } n_9) \Rightarrow (n_6 \text{ or } n_{10})$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $(n_6 \text{ and } n_{10}) \Rightarrow (n_2 \text{ or } n_9)$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $n_2 \text{ or } n_9 \text{ or } n_6 \text{ or } n_{10}$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $(n_2 \text{ and } n_6) \Rightarrow (n_9 \text{ or } n_{10})$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $(n_2 \text{ and } n_{10}) \Rightarrow (n_9 \text{ or } n_6)$     cnf(clause<sub>6</sub>, negated\_conjecture)  
 $(n_9 \text{ and } n_6) \Rightarrow (n_2 \text{ or } n_{10})$     cnf(clause<sub>7</sub>, negated\_conjecture)  
 $(n_9 \text{ and } n_{10}) \Rightarrow (n_2 \text{ or } n_6)$     cnf(clause<sub>8</sub>, negated\_conjecture)  
 $p(s_8) \Rightarrow n_8$     cnf(clause<sub>9</sub>, negated\_conjecture)  
 $n_8 \Rightarrow p(x_8)$     cnf(clause<sub>10</sub>, negated\_conjecture)  
 $p(x_7) \Rightarrow n_7$     cnf(clause<sub>11</sub>, negated\_conjecture)  
 $n_7 \Rightarrow p(s_7)$     cnf(clause<sub>12</sub>, negated\_conjecture)  
 $n_5(x_6) \Rightarrow n_6$     cnf(clause<sub>13</sub>, negated\_conjecture)  
 $n_6 \Rightarrow n_5(s_6)$     cnf(clause<sub>14</sub>, negated\_conjecture)  
 $(q(x) \text{ and } q(s_5(x))) \Rightarrow n_5(x)$     cnf(clause<sub>15</sub>, negated\_conjecture)  
 $q(x) \text{ or } q(s_5(x)) \text{ or } n_5(x)$     cnf(clause<sub>16</sub>, negated\_conjecture)  
 $(n_5(x) \text{ and } q(x)) \Rightarrow q(x_5)$     cnf(clause<sub>17</sub>, negated\_conjecture)  
 $(n_5(x) \text{ and } q(x_5)) \Rightarrow q(x)$     cnf(clause<sub>18</sub>, negated\_conjecture)  
 $q(s_4) \Rightarrow n_4$     cnf(clause<sub>19</sub>, negated\_conjecture)  
 $n_4 \Rightarrow q(x_4)$     cnf(clause<sub>20</sub>, negated\_conjecture)  
 $q(x_3) \Rightarrow n_3$     cnf(clause<sub>21</sub>, negated\_conjecture)  
 $n_3 \Rightarrow q(s_3)$     cnf(clause<sub>22</sub>, negated\_conjecture)  
 $n_1(x_2) \Rightarrow n_2$     cnf(clause<sub>23</sub>, negated\_conjecture)  
 $n_2 \Rightarrow n_1(s_2)$     cnf(clause<sub>24</sub>, negated\_conjecture)  
 $(p(x) \text{ and } p(s_1(x))) \Rightarrow n_1(x)$     cnf(clause<sub>25</sub>, negated\_conjecture)  
 $p(x) \text{ or } p(s_1(x)) \text{ or } n_1(x)$     cnf(clause<sub>26</sub>, negated\_conjecture)  
 $(n_1(x) \text{ and } p(x)) \Rightarrow p(x_1)$     cnf(clause<sub>27</sub>, negated\_conjecture)  
 $(n_1(x) \text{ and } p(x_1)) \Rightarrow p(x)$     cnf(clause<sub>28</sub>, negated\_conjecture)  
 $(n_3 \text{ and } n_4) \Rightarrow n_9$     cnf(clause<sub>29</sub>, negated\_conjecture)  
 $n_3 \text{ or } n_4 \text{ or } n_9$     cnf(clause<sub>30</sub>, negated\_conjecture)  
 $(n_3 \text{ and } n_9) \Rightarrow n_4$     cnf(clause<sub>31</sub>, negated\_conjecture)  
 $(n_4 \text{ and } n_9) \Rightarrow n_3$     cnf(clause<sub>32</sub>, negated\_conjecture)  
 $(n_7 \text{ and } n_8) \Rightarrow n_{10}$     cnf(clause<sub>33</sub>, negated\_conjecture)  
 $n_7 \text{ or } n_8 \text{ or } n_{10}$     cnf(clause<sub>34</sub>, negated\_conjecture)  
 $(n_7 \text{ and } n_{10}) \Rightarrow n_8$     cnf(clause<sub>35</sub>, negated\_conjecture)  
 $(n_8 \text{ and } n_{10}) \Rightarrow n_7$     cnf(clause<sub>36</sub>, negated\_conjecture)

**SYN036^5.p** TPS problem X2129

cQ:  $\$i \rightarrow \$o$     thf(cQ, type)

cP:  $\$i \rightarrow \$o$     thf(cP, type)

$(\exists xx: \$i: \forall xy: \$i: ((cP@xx) \iff (cP@xy)) \iff (\exists xx: \$i: (cQ@xx) \iff \forall xy: \$i: (cP@xy))) \iff (\exists xx: \$i: \forall xy: \$i: ((cQ@xx) \iff (cQ@xy)) \iff (\exists xx: \$i: (cP@xx) \iff \forall xy: \$i: (cQ@xy)))$     thf(cX<sub>2129</sub>, conjecture)

**SYN037-1.p** Andrews Challenge Problem Variant

$(n_2 \text{ and } n_9 \text{ and } n_6) \Rightarrow \neg n_{10}$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $(n_2 \text{ and } n_9) \Rightarrow (n_6 \text{ or } n_{10})$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $(n_6 \text{ and } n_{10}) \Rightarrow (n_2 \text{ or } n_9)$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $n_2 \text{ or } n_9 \text{ or } n_6 \text{ or } n_{10}$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $(n_2 \text{ and } n_6) \Rightarrow (n_9 \text{ or } n_{10})$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $(n_2 \text{ and } n_{10}) \Rightarrow (n_9 \text{ or } n_6)$     cnf(clause<sub>6</sub>, negated\_conjecture)  
 $(n_9 \text{ and } n_6) \Rightarrow (n_2 \text{ or } n_{10})$     cnf(clause<sub>7</sub>, negated\_conjecture)  
 $(n_9 \text{ and } n_{10}) \Rightarrow (n_2 \text{ or } n_6)$     cnf(clause<sub>8</sub>, negated\_conjecture)  
 $q(s_8) \Rightarrow n_8$     cnf(clause<sub>9</sub>, negated\_conjecture)  
 $n_8 \Rightarrow q(x_{10})$     cnf(clause<sub>10</sub>, negated\_conjecture)  
 $p(x_9) \Rightarrow n_7$     cnf(clause<sub>11</sub>, negated\_conjecture)  
 $n_7 \Rightarrow p(s_7)$     cnf(clause<sub>12</sub>, negated\_conjecture)  
 $n_5(x_8) \Rightarrow n_6$     cnf(clause<sub>13</sub>, negated\_conjecture)  
 $n_6 \Rightarrow n_5(s_6)$     cnf(clause<sub>14</sub>, negated\_conjecture)  
 $(q(s_5(w)) \text{ and } q(w)) \Rightarrow n_5(w)$     cnf(clause<sub>15</sub>, negated\_conjecture)  
 $q(s_5(w)) \text{ or } q(w) \text{ or } n_5(w)$     cnf(clause<sub>16</sub>, negated\_conjecture)

$(n_5(w) \text{ and } q(x_7)) \Rightarrow q(w)$     cnf(clause<sub>17</sub>, negated\_conjecture)  
 $(n_5(w) \text{ and } q(w)) \Rightarrow q(x_7)$     cnf(clause<sub>18</sub>, negated\_conjecture)  
 $p(s_4) \Rightarrow n_4$     cnf(clause<sub>19</sub>, negated\_conjecture)  
 $n_4 \Rightarrow p(x_6)$     cnf(clause<sub>20</sub>, negated\_conjecture)  
 $q(x_5) \Rightarrow n_3$     cnf(clause<sub>21</sub>, negated\_conjecture)  
 $n_3 \Rightarrow q(s_3)$     cnf(clause<sub>22</sub>, negated\_conjecture)  
 $n_1(x_4) \Rightarrow n_2$     cnf(clause<sub>23</sub>, negated\_conjecture)  
 $n_2 \Rightarrow n_1(s_2)$     cnf(clause<sub>24</sub>, negated\_conjecture)  
 $(p(x) \text{ and } p(s_1(x))) \Rightarrow n_1(x)$     cnf(clause<sub>25</sub>, negated\_conjecture)  
 $p(x) \text{ or } p(s_1(x)) \text{ or } n_1(x)$     cnf(clause<sub>26</sub>, negated\_conjecture)  
 $(n_1(x) \text{ and } p(x)) \Rightarrow p(x_3)$     cnf(clause<sub>27</sub>, negated\_conjecture)  
 $(n_1(x) \text{ and } p(x_3)) \Rightarrow p(x)$     cnf(clause<sub>28</sub>, negated\_conjecture)  
 $(n_3 \text{ and } n_4) \Rightarrow n_9$     cnf(clause<sub>29</sub>, negated\_conjecture)  
 $n_3 \text{ or } n_4 \text{ or } n_9$     cnf(clause<sub>30</sub>, negated\_conjecture)  
 $(n_3 \text{ and } n_9) \Rightarrow n_4$     cnf(clause<sub>31</sub>, negated\_conjecture)  
 $(n_4 \text{ and } n_9) \Rightarrow n_3$     cnf(clause<sub>32</sub>, negated\_conjecture)  
 $(n_7 \text{ and } n_8) \Rightarrow n_{10}$     cnf(clause<sub>33</sub>, negated\_conjecture)  
 $n_7 \text{ or } n_8 \text{ or } n_{10}$     cnf(clause<sub>34</sub>, negated\_conjecture)  
 $(n_7 \text{ and } n_{10}) \Rightarrow n_8$     cnf(clause<sub>35</sub>, negated\_conjecture)  
 $(n_8 \text{ and } n_{10}) \Rightarrow n_7$     cnf(clause<sub>36</sub>, negated\_conjecture)

### SYN037-2.p Andrews Challenge Problem Variant

$(m_1 \text{ and } m_3 \text{ and } p(x_1)) \Rightarrow \neg p(\text{fy}(x_1))$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $(m_1 \text{ and } m_3) \Rightarrow (p(x_1) \text{ or } p(\text{fy}(x_1)))$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $(m_1 \text{ and } p(\text{cx})) \Rightarrow (m_3 \text{ or } p(y_4))$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $(m_1 \text{ and } p(y_5)) \Rightarrow (m_3 \text{ or } p(\text{cx}))$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $(m_2 \text{ and } m_3 \text{ and } q(\text{cw})) \Rightarrow q(z_1)$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $(m_2 \text{ and } m_3 \text{ and } q(z)) \Rightarrow q(\text{cw})$     cnf(clause<sub>6</sub>, negated\_conjecture)  
 $(m_2 \text{ and } q(w_2) \text{ and } q(\text{fz}_5(w_2))) \Rightarrow m_3$     cnf(clause<sub>7</sub>, negated\_conjecture)  
 $m_2 \Rightarrow (m_3 \text{ or } q(w_2) \text{ or } q(\text{fz}_5(w_2)))$     cnf(clause<sub>8</sub>, negated\_conjecture)  
 $(m_3 \text{ and } p(\text{cx})) \Rightarrow (m_1 \text{ or } p(y_1))$     cnf(clause<sub>9</sub>, negated\_conjecture)  
 $(m_3 \text{ and } p(y_2)) \Rightarrow (m_1 \text{ or } p(\text{cx}))$     cnf(clause<sub>10</sub>, negated\_conjecture)  
 $(m_3 \text{ and } q(w_1) \text{ and } q(\text{fz}_2(w_1))) \Rightarrow m_2$     cnf(clause<sub>11</sub>, negated\_conjecture)  
 $m_3 \Rightarrow (m_2 \text{ or } q(w_1) \text{ or } q(\text{fz}_2(w_1)))$     cnf(clause<sub>12</sub>, negated\_conjecture)  
 $(p(x_2) \text{ and } p(\text{fy}_3(x_2))) \Rightarrow (m_1 \text{ or } m_3)$     cnf(clause<sub>13</sub>, negated\_conjecture)  
 $q(\text{cw}) \Rightarrow (m_2 \text{ or } m_3 \text{ or } q(z_4))$     cnf(clause<sub>14</sub>, negated\_conjecture)  
 $q(z_3) \Rightarrow (m_2 \text{ or } m_3 \text{ or } q(\text{cw}))$     cnf(clause<sub>15</sub>, negated\_conjecture)  
 $m_1 \text{ or } m_3 \text{ or } p(x_2) \text{ or } p(\text{fy}_3(x_2))$     cnf(clause<sub>16</sub>, negated\_conjecture)  
 $(m_1 \text{ and } q(u_1)) \Rightarrow q(\text{uu}_1)$     cnf(clause<sub>17</sub>, negated\_conjecture)  
 $(m_2 \text{ and } p(v_1)) \Rightarrow p(\text{vv}_1)$     cnf(clause<sub>18</sub>, negated\_conjecture)  
 $p(\text{cvv}) \Rightarrow m_2$     cnf(clause<sub>19</sub>, negated\_conjecture)  
 $q(\text{cuu}) \Rightarrow m_1$     cnf(clause<sub>20</sub>, negated\_conjecture)  
 $m_2 \text{ or } p(\text{cv})$     cnf(clause<sub>21</sub>, negated\_conjecture)  
 $m_1 \text{ or } q(\text{cu})$     cnf(clause<sub>22</sub>, negated\_conjecture)

### SYN038-1.p Syntactic formula

Exists X, Exists Y, All Z (((p(X,Y)  $\rightarrow$  (p(X,Z)  $\leftrightarrow$  q(Y,Z))) & (p(X,Y)  $\leftrightarrow$  (p(Z,Z)  $\rightarrow$  q(Z,Z))))  $\rightarrow$  (q(Z,Y)  $\leftrightarrow$  q(Z,Z)))  
 $(p(x, f(x, y)) \text{ and } p(x, y)) \Rightarrow q(y, f(x, y))$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $(p(x, y) \text{ and } q(y, f(x, y))) \Rightarrow p(x, f(x, y))$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $(p(x, y) \text{ and } p(f(x, y), f(x, y))) \Rightarrow q(f(x, y), f(x, y))$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $p(x, y) \text{ or } p(f(x, y), f(x, y))$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $q(f(x, y), f(x, y)) \Rightarrow p(x, y)$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $q(x, y) \text{ or } q(f(x, y), f(x, y))$     cnf(clause<sub>6</sub>, negated\_conjecture)  
 $q(x, y) \Rightarrow \neg q(f(x, y), f(x, y))$     cnf(clause<sub>7</sub>, negated\_conjecture)

### SYN039-1.p A challenge to resolution programs

$(s(x, f_1(x, x_1)) \text{ and } q(x_1, f_1(x, x_1))) \Rightarrow p(f_1(x, x_1), f_1(x, x_1))$     cnf(c<sub>1</sub>, negated\_conjecture)  
 $s(x, f_1(x, x_1)) \Rightarrow (p(f_1(x, x_1), f_1(x, x_1)) \text{ or } q(f_1(x, x_1), z_1))$     cnf(c<sub>2</sub>, negated\_conjecture)  
 $(s(x, f_1(x, x_1)) \text{ and } s(x_1, x_1)) \Rightarrow p(f_1(x, x_1), f_1(x, x_1))$     cnf(c<sub>3</sub>, negated\_conjecture)  
 $q(x_1, f_1(x, x_1)) \Rightarrow (p(f_1(x, x_1), f_1(x, x_1)) \text{ or } s(f_1(x, x_1), z))$     cnf(c<sub>4</sub>, negated\_conjecture)

$p(f_1(x, x_1), f_1(x, x_1))$  or  $s(f_1(x, x_1), z)$  or  $q(f_1(x, x_1), z_1)$     cnf( $c_5$ , negated\_conjecture)  
 $s(x_1, x_1) \Rightarrow (p(f_1(x, x_1), f_1(x, x_1))$  or  $s(f_1(x, x_1), z))$     cnf( $c_6$ , negated\_conjecture)  
 $(q(z_1, z_1)$  and  $q(x_1, f_1(x, x_1))) \Rightarrow p(f_1(x, x_1), f_1(x, x_1))$     cnf( $c_7$ , negated\_conjecture)  
 $q(z_1, z_1) \Rightarrow (p(f_1(x, x_1), f_1(x, x_1))$  or  $q(f_1(x, x_1), z_1))$     cnf( $c_8$ , negated\_conjecture)  
 $(q(z_1, z_1)$  and  $s(x_1, x_1)) \Rightarrow p(f_1(x, x_1), f_1(x, x_1))$     cnf( $c_9$ , negated\_conjecture)  
 $(p(x, x)$  and  $s(x, f_1(x, x_1))) \Rightarrow \neg q(x_1, f_1(x, x_1))$     cnf( $c_{10}$ , negated\_conjecture)  
 $(p(x, x)$  and  $s(x, f_1(x, x_1))) \Rightarrow q(f_1(x, x_1), z_1)$     cnf( $c_{11}$ , negated\_conjecture)  
 $(p(x, x)$  and  $s(x, f_1(x, x_1))) \Rightarrow \neg s(x_1, x_1)$     cnf( $c_{12}$ , negated\_conjecture)  
 $(p(x, x)$  and  $q(x_1, f_1(x, x_1))) \Rightarrow s(f_1(x, x_1), z)$     cnf( $c_{13}$ , negated\_conjecture)  
 $p(x, x) \Rightarrow (s(f_1(x, x_1), z)$  or  $q(f_1(x, x_1), z_1))$     cnf( $c_{14}$ , negated\_conjecture)  
 $(p(x, x)$  and  $s(x_1, x_1)) \Rightarrow s(f_1(x, x_1), z)$     cnf( $c_{15}$ , negated\_conjecture)  
 $(p(x, x)$  and  $q(z_1, z_1)) \Rightarrow \neg q(x_1, f_1(x, x_1))$     cnf( $c_{16}$ , negated\_conjecture)  
 $(p(x, x)$  and  $q(z_1, z_1)) \Rightarrow q(f_1(x, x_1), z_1)$     cnf( $c_{17}$ , negated\_conjecture)  
 $(p(x, x)$  and  $q(z_1, z_1)) \Rightarrow \neg s(x_1, x_1)$     cnf( $c_{18}$ , negated\_conjecture)  
 $(s(x, f_1(x, x_1))$  and  $q(x_1, f_1(x, x_1))) \Rightarrow s(z, x)$     cnf( $c_{19}$ , negated\_conjecture)  
 $s(x, f_1(x, x_1)) \Rightarrow (s(z, x)$  or  $q(f_1(x, x_1), z_1))$     cnf( $c_{20}$ , negated\_conjecture)  
 $(s(x, f_1(x, x_1))$  and  $s(x_1, x_1)) \Rightarrow s(z, x)$     cnf( $c_{21}$ , negated\_conjecture)  
 $q(x_1, f_1(x, x_1)) \Rightarrow (s(z, x)$  or  $s(f_1(x, x_1), z))$     cnf( $c_{22}$ , negated\_conjecture)  
 $s(z, x)$  or  $s(f_1(x, x_1), z)$  or  $q(f_1(x, x_1), z_1)$     cnf( $c_{23}$ , negated\_conjecture)  
 $s(x_1, x_1) \Rightarrow (s(z, x)$  or  $s(f_1(x, x_1), z))$     cnf( $c_{24}$ , negated\_conjecture)  
 $(q(z_1, z_1)$  and  $q(x_1, f_1(x, x_1))) \Rightarrow s(z, x)$     cnf( $c_{25}$ , negated\_conjecture)  
 $q(z_1, z_1) \Rightarrow (s(z, x)$  or  $q(f_1(x, x_1), z_1))$     cnf( $c_{26}$ , negated\_conjecture)  
 $(q(z_1, z_1)$  and  $s(x_1, x_1)) \Rightarrow s(z, x)$     cnf( $c_{27}$ , negated\_conjecture)

#### SYN040+1.p Pelletier Problem 1

A biconditional version of the 'most difficult' theorem proved by the original Logic Theorist.

$(p \Rightarrow q) \iff (\neg q \Rightarrow \neg p)$     fof(pel<sub>1</sub>, conjecture)

#### SYN040-1.p Pelletier Problem 1

A biconditional version of the 'most difficult' theorem proved by the original Logic Theorist.

$p \Rightarrow q$     cnf(clause<sub>1</sub>, negated\_conjecture)

$q \Rightarrow p$     cnf(clause<sub>2</sub>, negated\_conjecture)

$\neg q$     cnf(clause<sub>3</sub>, negated\_conjecture)

$p$     cnf(clause<sub>4</sub>, negated\_conjecture)

#### SYN040^4.p Pelletier Problem 1

include('Axioms/LCL010^0.ax')

$p: \$i \rightarrow \$o$     thf(p\_type, type)

$q: \$i \rightarrow \$o$     thf(q\_type, type)

ivalid@(iequiv@(iimplies@(iatom@p)@(iatom@q))@(iimplies@(inot@(iatom@q))@(inot@(iatom@p))))    thf(pel<sub>1</sub>, conjecture)

#### SYN041+1.p Pelletier Problem 3

3: The hardest theorem proved by a breadth-first logic theorist.

$\neg p \Rightarrow q \Rightarrow (q \Rightarrow p)$     fof(pel<sub>3</sub>, conjecture)

#### SYN041-1.p Pelletier Problem 3, 16

3: The hardest theorem proved by a breadth-first logic theorist. 16:A surprising theorem of propositional logic.

$p$     cnf(clause<sub>1</sub>, negated\_conjecture)

$\neg q$     cnf(clause<sub>2</sub>, negated\_conjecture)

$q$     cnf(clause<sub>3</sub>, negated\_conjecture)

$\neg p$     cnf(clause<sub>4</sub>, negated\_conjecture)

#### SYN041^4.p Pelletier Problem 3

include('Axioms/LCL010^0.ax')

$p: \$i \rightarrow \$o$     thf(p\_type, type)

$q: \$i \rightarrow \$o$     thf(q\_type, type)

ivalid@(iimplies@(inot@(iimplies@(iatom@p)@(iatom@q))@(iimplies@(iatom@q)@(iatom@p))))    thf(pel<sub>3</sub>, conjecture)

#### SYN044+1.p Pelletier Problem 10

A reasonably simple problem designed to see whether 'natural' systems correctly manipulate premises.

$q \Rightarrow r$     fof(pel10<sub>1</sub>, axiom)

$r \Rightarrow (p$  and  $q)$     fof(pel10<sub>2</sub>, axiom)

$p \Rightarrow (q$  or  $r)$     fof(pel10<sub>3</sub>, axiom)

$p \iff q$     fof(pel<sub>10</sub>, conjecture)

**SYN044-1.p** Pelletier Problem 10

A reasonably simple problem designed to see whether 'natural' systems correctly manipulate premises.

$q \Rightarrow r$     cnf(clause<sub>1</sub>, axiom)  
 $r \Rightarrow p$     cnf(clause<sub>2</sub>, axiom)  
 $r \Rightarrow q$     cnf(clause<sub>3</sub>, axiom)  
 $p \Rightarrow (q \text{ or } r)$     cnf(clause<sub>4</sub>, axiom)  
 $p \Rightarrow \neg q$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $p \text{ or } q$     cnf(clause<sub>6</sub>, negated\_conjecture)

**SYN044^4.p** Pelletier Problem 10

include('Axioms/LCL010^0.ax')  
 $p: \$i \rightarrow \$o$     thf(p\_type, type)  
 $q: \$i \rightarrow \$o$     thf(q\_type, type)  
 $r: \$i \rightarrow \$o$     thf(r\_type, type)  
 invalid@(iimplies@(iatom@q)@(iatom@r))    thf(pel10<sub>1</sub>, axiom)  
 invalid@(iimplies@(iatom@r)@(iand@(iatom@p)@(iatom@q)))    thf(pel10<sub>2</sub>, axiom)  
 invalid@(iimplies@(iatom@p)@(ior@(iatom@q)@(iatom@r)))    thf(pel10<sub>3</sub>, axiom)  
 invalid@(iequiv@(iatom@p)@(iatom@q))    thf(pel<sub>10</sub>, conjecture)

**SYN045+1.p** Pelletier Problem 13

$(p \text{ or } (q \text{ and } r)) \iff ((p \text{ or } q) \text{ and } (p \text{ or } r))$     fof(pel<sub>13</sub>, conjecture)

**SYN045-1.p** Pelletier Problem 13

$p \text{ or } q$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $p \text{ or } r$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $\neg p$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $q \Rightarrow \neg r$     cnf(clause<sub>4</sub>, negated\_conjecture)

**SYN045^4.p** Pelletier Problem 13

include('Axioms/LCL010^0.ax')  
 $p: \$i \rightarrow \$o$     thf(p\_type, type)  
 $q: \$i \rightarrow \$o$     thf(q\_type, type)  
 $r: \$i \rightarrow \$o$     thf(r\_type, type)  
 invalid@(iequiv@(ior@(iatom@p)@(iand@(iatom@q)@(iatom@r)))@(iand@(ior@(iatom@p)@(iatom@q))@(ior@(iatom@p)@(iatom@q)))

**SYN045^7.p** Pelletier Problem 13

include('Axioms/LCL015^0.ax')  
 include('Axioms/LCL013^5.ax')  
 include('Axioms/LCL015^1.ax')  
 $r: \$i \rightarrow \$o$     thf(r\_type, type)  
 $q: \$i \rightarrow \$o$     thf(q\_type, type)  
 $p: \$i \rightarrow \$o$     thf(p\_type, type)  
 mvalid@(mand@(mbox\_s4@(mimplies@(mor@(mbox\_s4@p)@(mand@(mbox\_s4@q)@(mbox\_s4@r)))@(mand@(mor@(mbox\_s4@p)@(mbox\_s4@q)))))

**SYN046+1.p** Pelletier Problem 15

$(p \Rightarrow q) \iff (\neg p \text{ or } q)$     fof(pel<sub>15</sub>, conjecture)

**SYN046-1.p** Pelletier Problem 15

$p \Rightarrow q$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $p$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $\neg q$     cnf(clause<sub>3</sub>, negated\_conjecture)

**SYN046^4.p** Pelletier Problem 15

include('Axioms/LCL010^0.ax')  
 $p: \$i \rightarrow \$o$     thf(p\_type, type)  
 $q: \$i \rightarrow \$o$     thf(q\_type, type)  
 invalid@(iequiv@(iimplies@(iatom@p)@(iatom@q))@(ior@(inot@(iatom@p))@(iatom@q)))    thf(pel<sub>15</sub>, conjecture)

**SYN047+1.p** Pelletier Problem 17

A problem which appears to not be provable by [BBH72]. For details of why not, see [Pel82] p.135f.

$((p \text{ and } (q \Rightarrow r)) \Rightarrow s) \iff ((\neg p \text{ or } q \text{ or } s) \text{ and } (\neg p \text{ or } \neg r \text{ or } s))$     fof(pel<sub>17</sub>, conjecture)

**SYN047-1.p** Pelletier Problem 17

A problem which appears to not be provable by [BBH72]. For details of why not, see [Pel82] p.135f.

$p$      $\text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $p \Rightarrow (q \text{ or } s)$      $\text{cnf}(\text{clause}_2, \text{negated\_conjecture})$   
 $(p \text{ and } r) \Rightarrow s$      $\text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $\neg s$      $\text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $q \Rightarrow r$      $\text{cnf}(\text{clause}_5, \text{negated\_conjecture})$

**SYN047^4.p** Pelletier Problem 17

`include('Axioms/LCL010^0.ax')`

$p: \$i \rightarrow \$o$      $\text{thf}(p\_type, \text{type})$

$q: \$i \rightarrow \$o$      $\text{thf}(q\_type, \text{type})$

$r: \$i \rightarrow \$o$      $\text{thf}(r\_type, \text{type})$

$s: \$i \rightarrow \$o$      $\text{thf}(s\_type, \text{type})$

`invalid@(iequiv@(iimplies@(iand@(iatom@p)@(iimplies@(iatom@q)@(iatom@r))@(iatom@s))@(iand@(ior@(inot@(iatom@p)`

**SYN048+1.p** Pelletier Problem 18

$\exists y: \forall x: (\text{big\_f}(y) \Rightarrow \text{big\_f}(x))$      $\text{fof}(\text{pel}_{18}, \text{conjecture})$

**SYN048-1.p** Pelletier Problem 18

$\text{big\_f}(x)$      $\text{cnf}(\text{clause}_1, \text{negated\_conjecture})$

$\neg \text{big\_f}(f(x))$      $\text{cnf}(\text{clause}_2, \text{negated\_conjecture})$

**SYN049+1.p** Pelletier Problem 19

$\exists x: \forall y, z: ((\text{big\_p}(y) \Rightarrow \text{big\_q}(z)) \Rightarrow (\text{big\_p}(x) \Rightarrow \text{big\_q}(x)))$      $\text{fof}(\text{pel}_{19}, \text{conjecture})$

**SYN049-1.p** Pelletier Problem 19

$\text{big\_p}(f(x)) \Rightarrow \text{big\_q}(g(x))$      $\text{cnf}(\text{clause}_1, \text{negated\_conjecture})$

$\text{big\_p}(x)$      $\text{cnf}(\text{clause}_2, \text{negated\_conjecture})$

$\neg \text{big\_q}(x)$      $\text{cnf}(\text{clause}_3, \text{negated\_conjecture})$

**SYN049^5.p** TPS problem PELL19

$cQ: \$i \rightarrow \$o$      $\text{thf}(cQ, \text{type})$

$cP: \$i \rightarrow \$o$      $\text{thf}(cP, \text{type})$

$\exists xx: \$i: \forall xy: \$i, xz: \$i: (((cP@xy) \Rightarrow (cQ@xz)) \Rightarrow ((cP@xx) \Rightarrow (cQ@xx)))$      $\text{thf}(cPELL_{19}, \text{conjecture})$

**SYN050+1.p** Pelletier Problem 20

$\forall x, y: \exists z: \forall w: ((\text{big\_p}(x) \text{ and } \text{big\_q}(y)) \Rightarrow (\text{big\_r}(z) \text{ and } \text{big\_s}(w))) \Rightarrow \exists x_1, y_1: ((\text{big\_p}(x_1) \text{ and } \text{big\_q}(y_1)) \Rightarrow \exists z_1: \text{big\_r}(z_1))$      $\text{fof}(\text{pel}_{20}, \text{conjecture})$

**SYN050-1.p** Pelletier Problem 20

$(\text{big\_p}(y) \text{ and } \text{big\_q}(z)) \Rightarrow \text{big\_r}(f(y, z))$      $\text{cnf}(\text{clause}_1, \text{negated\_conjecture})$

$(\text{big\_p}(y) \text{ and } \text{big\_q}(z)) \Rightarrow \text{big\_s}(x)$      $\text{cnf}(\text{clause}_2, \text{negated\_conjecture})$

$\text{big\_p}(a)$      $\text{cnf}(\text{clause}_3, \text{negated\_conjecture})$

$\text{big\_q}(b)$      $\text{cnf}(\text{clause}_4, \text{negated\_conjecture})$

$\neg \text{big\_r}(w)$      $\text{cnf}(\text{clause}_5, \text{negated\_conjecture})$

**SYN051+1.p** Pelletier Problem 21

A moderately tricky problem, especially for 'natural' systems with 'strong' restrictions on variables generated from existential quantifiers.

$\exists x: (p \Rightarrow \text{big\_f}(x))$      $\text{fof}(\text{pel}_{21_1}, \text{axiom})$

$\exists x: (\text{big\_f}(x) \Rightarrow p)$      $\text{fof}(\text{pel}_{21_2}, \text{axiom})$

$\exists x: (p \iff \text{big\_f}(x))$      $\text{fof}(\text{pel}_{21}, \text{conjecture})$

**SYN051-1.p** Pelletier Problem 21

A moderately tricky problem, especially for 'natural' systems with 'strong' restrictions on variables generated from existential quantifiers.

$p \Rightarrow \text{big\_f}(a)$      $\text{cnf}(\text{clause}_1, \text{axiom})$

$\text{big\_f}(b) \Rightarrow p$      $\text{cnf}(\text{clause}_2, \text{axiom})$

$p \text{ or } \text{big\_f}(x)$      $\text{cnf}(\text{clause}_3, \text{negated\_conjecture})$

$\text{big\_f}(x) \Rightarrow \neg p$      $\text{cnf}(\text{clause}_4, \text{negated\_conjecture})$

**SYN051^5.p** TPS problem PELL21

$p: \$o$      $\text{thf}(p, \text{type})$

$cF: \$i \rightarrow \$o$      $\text{thf}(cF, \text{type})$

$(\exists xx: \$i: (p \Rightarrow (cF@xx)) \text{ and } \exists xx: \$i: ((cF@xx) \Rightarrow p)) \Rightarrow \exists xx: \$i: ((p \Rightarrow (cF@xx)) \text{ and } ((cF@xx) \Rightarrow p))$      $\text{thf}(cPELL_{21}, \text{conjecture})$

**SYN052+1.p** Pelletier Problem 22

$\forall x: (p \iff \text{big\_f}(x)) \Rightarrow (p \iff \forall x_1: \text{big\_f}(x_1))$     fof(pel<sub>22</sub>, conjecture)

**SYN052-1.p** Pelletier Problem 22

$\text{big\_f}(x) \Rightarrow p$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $p \Rightarrow \text{big\_f}(x)$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $\text{big\_f}(y) \text{ or } p$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $p \Rightarrow \neg \text{big\_f}(a)$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $\text{big\_f}(a) \Rightarrow \text{big\_f}(y)$     cnf(clause<sub>5</sub>, negated\_conjecture)

**SYN052^7.p** Pelletier Problem 22

include('Axioms/LCL015^0.ax')  
include('Axioms/LCL013^5.ax')  
include('Axioms/LCL015^1.ax')  
 $p: \$i \rightarrow \$o$     thf(p\_type, type)  
 $\text{big\_f}: \mu \rightarrow \$i \rightarrow \$o$     thf(big\_f\_type, type)  
mvalid@(mbox\_s4@(mimplies@(mbox\_s4@(mforall\_ind@ $\lambda x: \mu: (\text{mand}@(mbox_s4@(mimplies@(mbox_s4@p))@(mbox_s4@(big$

**SYN053+1.p** Pelletier Problem 23

$\forall x: (p \text{ or } \text{big\_f}(x)) \iff (p \text{ or } \forall x_1: \text{big\_f}(x_1))$     fof(pel<sub>23</sub>, conjecture)

**SYN053-1.p** Pelletier Problem 23

$p \text{ or } \text{big\_f}(x) \text{ or } \text{big\_f}(y)$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $p \text{ or } \text{big\_f}(x) \text{ or } \text{big\_f}(b)$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $\neg p$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $\text{big\_f}(a) \Rightarrow (p \text{ or } \text{big\_f}(y))$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $\text{big\_f}(a) \Rightarrow \neg \text{big\_f}(b)$     cnf(clause<sub>5</sub>, negated\_conjecture)

**SYN054+1.p** Pelletier Problem 24

$\neg \exists x: (\text{big\_s}(x) \text{ and } \text{big\_q}(x))$     fof(pel<sub>24</sub><sub>1</sub>, axiom)  
 $\forall x: (\text{big\_p}(x) \Rightarrow (\text{big\_q}(x) \text{ or } \text{big\_r}(x)))$     fof(pel<sub>24</sub><sub>2</sub>, axiom)  
 $\neg \exists x: \text{big\_p}(x) \Rightarrow \exists y: \text{big\_q}(y)$     fof(pel<sub>24</sub><sub>3</sub>, axiom)  
 $\forall x: ((\text{big\_q}(x) \text{ or } \text{big\_r}(x)) \Rightarrow \text{big\_s}(x))$     fof(pel<sub>24</sub><sub>4</sub>, axiom)  
 $\exists x: (\text{big\_p}(x) \text{ and } \text{big\_r}(x))$     fof(pel<sub>24</sub>, conjecture)

**SYN054-1.p** Pelletier Problem 24

$\text{big\_s}(x) \Rightarrow \neg \text{big\_q}(x)$     cnf(clause<sub>1</sub>, axiom)  
 $\text{big\_p}(x) \Rightarrow (\text{big\_q}(x) \text{ or } \text{big\_r}(x))$     cnf(clause<sub>2</sub>, axiom)  
 $\text{big\_p}(a) \text{ or } \text{big\_q}(b)$     cnf(clause<sub>3</sub>, axiom)  
 $\text{big\_q}(x) \Rightarrow \text{big\_s}(x)$     cnf(clause<sub>4</sub>, axiom)  
 $\text{big\_r}(x) \Rightarrow \text{big\_s}(x)$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $\text{big\_p}(x) \Rightarrow \neg \text{big\_r}(x)$     cnf(clause<sub>6</sub>, negated\_conjecture)

**SYN055+1.p** Pelletier Problem 25

$\exists x: \text{big\_p}(x)$     fof(pel<sub>25</sub><sub>1</sub>, axiom)  
 $\forall x: (\text{big\_f}(x) \Rightarrow (\neg \text{big\_g}(x) \text{ and } \text{big\_r}(x)))$     fof(pel<sub>25</sub><sub>2</sub>, axiom)  
 $\forall x: (\text{big\_p}(x) \Rightarrow (\text{big\_g}(x) \text{ and } \text{big\_f}(x)))$     fof(pel<sub>25</sub><sub>3</sub>, axiom)  
 $\forall x: (\text{big\_p}(x) \Rightarrow \text{big\_q}(x)) \text{ or } \exists z: (\text{big\_p}(z) \text{ and } \text{big\_r}(z))$     fof(pel<sub>25</sub><sub>4</sub>, axiom)  
 $\exists x: (\text{big\_q}(x) \text{ and } \text{big\_p}(x))$     fof(pel<sub>25</sub>, conjecture)

**SYN055-1.p** Pelletier Problem 25

$\text{big\_p}(a)$     cnf(clause<sub>1</sub>, axiom)  
 $(\text{big\_f}(x) \text{ and } \text{big\_g}(x)) \Rightarrow \neg \text{big\_r}(x)$     cnf(clause<sub>2</sub>, axiom)  
 $\text{big\_p}(x) \Rightarrow \text{big\_f}(x)$     cnf(clause<sub>3</sub>, axiom)  
 $\text{big\_p}(x) \Rightarrow \text{big\_g}(x)$     cnf(clause<sub>4</sub>, axiom)  
 $\text{big\_p}(x) \Rightarrow (\text{big\_q}(x) \text{ or } \text{big\_p}(b))$     cnf(clause<sub>5</sub>, axiom)  
 $\text{big\_p}(x) \Rightarrow (\text{big\_q}(x) \text{ or } \text{big\_r}(b))$     cnf(clause<sub>6</sub>, negated\_conjecture)  
 $\text{big\_q}(x) \Rightarrow \neg \text{big\_p}(x)$     cnf(clause<sub>7</sub>, negated\_conjecture)

**SYN055^5.p** TPS problem PELL25

cP:  $\$i \rightarrow \$o$     thf(cP, type)  
cQ:  $\$i \rightarrow \$o$     thf(cQ, type)  
cR:  $\$i \rightarrow \$o$     thf(cR, type)  
cF:  $\$i \rightarrow \$o$     thf(cF, type)  
cG:  $\$i \rightarrow \$o$     thf(cG, type)



$(\exists xx: \$i: (cP@xx) \text{ and } \forall xx: \$i: ((cF@xx) \Rightarrow (\neg cG@xx \text{ and } cR@xx)) \text{ and } \forall xx: \$i: ((cP@xx) \Rightarrow (cG@xx \text{ and } cF@xx)) \text{ and } (\forall (cQ@xx)) \text{ or } \exists xx: \$i: (cP@xx \text{ and } cR@xx))) \Rightarrow \exists xx: \$i: (cQ@xx \text{ and } cP@xx)$  thf(cPELL<sub>25</sub>, conjecture)

**SYN056+1.p** Pelletier Problem 26

$\exists x: \text{big\_p}(x) \iff \exists y: \text{big\_q}(y)$  fof(pel26<sub>1</sub>, axiom)  
 $\forall x, y: ((\text{big\_p}(x) \text{ and } \text{big\_q}(y)) \Rightarrow (\text{big\_r}(x) \iff \text{big\_s}(y)))$  fof(pel26<sub>2</sub>, axiom)  
 $\forall x: (\text{big\_p}(x) \Rightarrow \text{big\_r}(x)) \iff \forall y: (\text{big\_q}(y) \Rightarrow \text{big\_s}(y))$  fof(pel<sub>26</sub>, conjecture)

**SYN056-1.p** Pelletier Problem 26

$\text{big\_p}(x) \Rightarrow \text{big\_q}(a)$  cnf(clause<sub>1</sub>, axiom)  
 $\text{big\_q}(x) \Rightarrow \text{big\_p}(b)$  cnf(clause<sub>2</sub>, axiom)  
 $(\text{big\_p}(x) \text{ and } \text{big\_q}(y) \text{ and } \text{big\_r}(x)) \Rightarrow \text{big\_s}(y)$  cnf(clause<sub>3</sub>, axiom)  
 $(\text{big\_p}(x) \text{ and } \text{big\_q}(y) \text{ and } \text{big\_s}(y)) \Rightarrow \text{big\_r}(x)$  cnf(clause<sub>4</sub>, axiom)  
 $(\text{big\_p}(x) \text{ and } \text{big\_q}(x)) \Rightarrow (\text{big\_r}(x) \text{ or } \text{big\_s}(x))$  cnf(clause<sub>5</sub>, axiom)  
 $\text{big\_p}(x) \Rightarrow (\text{big\_p}(c) \text{ or } \text{big\_r}(x))$  cnf(clause<sub>6</sub>, negated\_conjecture)  
 $(\text{big\_p}(x) \text{ and } \text{big\_r}(c)) \Rightarrow \text{big\_r}(x)$  cnf(clause<sub>7</sub>, negated\_conjecture)  
 $\text{big\_q}(x) \Rightarrow (\text{big\_q}(d) \text{ or } \text{big\_s}(x))$  cnf(clause<sub>8</sub>, negated\_conjecture)  
 $(\text{big\_q}(x) \text{ and } \text{big\_s}(d)) \Rightarrow \text{big\_s}(x)$  cnf(clause<sub>9</sub>, negated\_conjecture)  
 $\text{big\_p}(c) \text{ or } \text{big\_q}(d)$  cnf(clause<sub>10</sub>, negated\_conjecture)  
 $\text{big\_r}(c) \Rightarrow \text{big\_q}(d)$  cnf(clause<sub>11</sub>, negated\_conjecture)  
 $\text{big\_s}(d) \Rightarrow \text{big\_p}(c)$  cnf(clause<sub>12</sub>, negated\_conjecture)  
 $\text{big\_r}(c) \Rightarrow \neg \text{big\_s}(d)$  cnf(clause<sub>13</sub>, negated\_conjecture)

**SYN056^5.p** TPS problem PELL26

$cR: \$i \rightarrow \$o$  thf(cR, type)  
 $cP: \$i \rightarrow \$o$  thf(cP, type)  
 $cS: \$i \rightarrow \$o$  thf(cS, type)  
 $cQ: \$i \rightarrow \$o$  thf(cQ, type)  
 $((\exists xx: \$i: (cP@xx) \Rightarrow \exists xx: \$i: (cQ@xx)) \text{ and } (\exists xx: \$i: (cQ@xx) \Rightarrow \exists xx: \$i: (cP@xx)) \text{ and } \forall xx: \$i, xy: \$i: ((cP@xx \text{ and } cQ@xx) \Rightarrow ((cR@xx) \Rightarrow (cS@xy)) \text{ and } ((cS@xy) \Rightarrow (cR@xx)))) \Rightarrow ((\forall xx: \$i: ((cP@xx) \Rightarrow (cR@xx)) \Rightarrow \forall xx: \$i: ((cQ@xx) \Rightarrow (cS@xx))) \text{ and } (\forall xx: \$i: ((cQ@xx) \Rightarrow (cS@xx)) \Rightarrow \forall xx: \$i: ((cP@xx) \Rightarrow (cR@xx))))$  thf(cPELL<sub>26</sub>, conjecture)

**SYN057+1.p** Pelletier Problem 27

$\exists x: (\text{big\_f}(x) \text{ and } \neg \text{big\_g}(x))$  fof(pel27<sub>1</sub>, axiom)  
 $\forall x: (\text{big\_f}(x) \Rightarrow \text{big\_h}(x))$  fof(pel27<sub>2</sub>, axiom)  
 $\forall x: ((\text{big\_j}(x) \text{ and } \text{big\_i}(x)) \Rightarrow \text{big\_f}(x))$  fof(pel27<sub>3</sub>, axiom)  
 $\exists x: (\text{big\_h}(x) \text{ and } \neg \text{big\_g}(x)) \Rightarrow \forall x_1: (\text{big\_i}(x_1) \Rightarrow \neg \text{big\_h}(x_1))$  fof(pel27<sub>4</sub>, axiom)  
 $\forall x: (\text{big\_j}(x) \Rightarrow \neg \text{big\_i}(x))$  fof(pel<sub>27</sub>, conjecture)

**SYN057-1.p** Pelletier Problem 27

$\text{big\_f}(a)$  cnf(clause<sub>1</sub>, axiom)  
 $\neg \text{big\_g}(a)$  cnf(clause<sub>2</sub>, axiom)  
 $\text{big\_f}(x) \Rightarrow \text{big\_h}(x)$  cnf(clause<sub>3</sub>, axiom)  
 $(\text{big\_j}(x) \text{ and } \text{big\_i}(x)) \Rightarrow \text{big\_f}(x)$  cnf(clause<sub>4</sub>, axiom)  
 $(\text{big\_h}(x) \text{ and } \text{big\_i}(y) \text{ and } \text{big\_h}(y)) \Rightarrow \text{big\_g}(x)$  cnf(clause<sub>5</sub>, axiom)  
 $\text{big\_j}(b)$  cnf(clause<sub>6</sub>, negated\_conjecture)  
 $\text{big\_i}(b)$  cnf(clause<sub>7</sub>, negated\_conjecture)

**SYN057^5.p** TPS problem PELL27

$cI: \$i \rightarrow \$o$  thf(cI, type)  
 $cJ: \$i \rightarrow \$o$  thf(cJ, type)  
 $cH: \$i \rightarrow \$o$  thf(cH, type)  
 $cG: \$i \rightarrow \$o$  thf(cG, type)  
 $cF: \$i \rightarrow \$o$  thf(cF, type)  
 $(\exists xx: \$i: (cF@xx \text{ and } \neg cG@xx) \text{ and } \forall xx: \$i: ((cF@xx) \Rightarrow (cH@xx)) \text{ and } \forall xx: \$i: ((cJ@xx \text{ and } cI@xx) \Rightarrow (cF@xx)) \text{ and } (\exists \forall xx: \$i: ((cI@xx) \Rightarrow \neg cH@xx))) \Rightarrow \forall xx: \$i: ((cJ@xx) \Rightarrow \neg cI@xx)$  thf(cPELL<sub>27</sub>, conjecture)

**SYN058+1.p** Pelletier Problem 28

$\forall x: (\text{big\_p}(x) \Rightarrow \forall z: \text{big\_q}(z))$  fof(pel28<sub>1</sub>, axiom)  
 $\forall x: (\text{big\_q}(x) \text{ or } \text{big\_r}(x)) \Rightarrow \exists x_1: (\text{big\_q}(x_1) \text{ and } \text{big\_s}(x_1))$  fof(pel28<sub>2</sub>, axiom)  
 $\exists x: \text{big\_s}(x) \Rightarrow \forall x_1: (\text{big\_f}(x_1) \Rightarrow \text{big\_g}(x_1))$  fof(pel28<sub>3</sub>, axiom)  
 $\forall x: ((\text{big\_p}(x) \text{ and } \text{big\_f}(x)) \Rightarrow \text{big\_g}(x))$  fof(pel<sub>28</sub>, conjecture)

**SYN058-1.p** Pelletier Problem 28

$\text{big\_p}(x) \Rightarrow \text{big\_q}(y) \quad \text{cnf}(\text{clause}_1, \text{axiom})$   
 $\text{big\_q}(b) \Rightarrow \text{big\_q}(c) \quad \text{cnf}(\text{clause}_2, \text{axiom})$   
 $\text{big\_q}(b) \Rightarrow \text{big\_s}(c) \quad \text{cnf}(\text{clause}_3, \text{axiom})$   
 $\text{big\_r}(b) \Rightarrow \text{big\_q}(c) \quad \text{cnf}(\text{clause}_4, \text{axiom})$   
 $\text{big\_r}(b) \Rightarrow \text{big\_s}(c) \quad \text{cnf}(\text{clause}_5, \text{axiom})$   
 $(\text{big\_s}(y) \text{ and } \text{big\_f}(x)) \Rightarrow \text{big\_g}(x) \quad \text{cnf}(\text{clause}_6, \text{axiom})$   
 $\text{big\_p}(d) \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $\text{big\_f}(d) \quad \text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $\neg \text{big\_g}(d) \quad \text{cnf}(\text{clause}_9, \text{negated\_conjecture})$

**SYN058^5.p** TPS problem PELL28

$\text{cG}: \$i \rightarrow \$o \quad \text{thf}(\text{cG}, \text{type})$   
 $\text{cF}: \$i \rightarrow \$o \quad \text{thf}(\text{cF}, \text{type})$   
 $\text{cP}: \$i \rightarrow \$o \quad \text{thf}(\text{cP}, \text{type})$   
 $\text{cS}: \$i \rightarrow \$o \quad \text{thf}(\text{cS}, \text{type})$   
 $\text{cQ}: \$i \rightarrow \$o \quad \text{thf}(\text{cQ}, \text{type})$   
 $\text{cR}: \$i \rightarrow \$o \quad \text{thf}(\text{cR}, \text{type})$   
 $(\forall \text{xx}: \$i: ((\text{cP}@xx) \Rightarrow \forall \text{xx}_0: \$i: (\text{cQ}@xx_0))) \text{ and } (\forall \text{xx}: \$i: (\text{cQ}@xx \text{ or } \text{cR}@xx) \Rightarrow \exists \text{xx}: \$i: (\text{cQ}@xx \text{ and } \text{cS}@xx)) \text{ and } (\exists \text{xx}: \$i: \forall \text{xx}: \$i: ((\text{cF}@xx) \Rightarrow (\text{cG}@xx)))) \Rightarrow \forall \text{xx}: \$i: ((\text{cP}@xx \text{ and } \text{cF}@xx) \Rightarrow (\text{cG}@xx)) \quad \text{thf}(\text{cPELL}_{28}, \text{conjecture})$

**SYN059+1.p** Pelletier Problem 29

$\exists x: \text{big\_f}(x) \quad \text{fof}(\text{pel}_{29_1}, \text{axiom})$   
 $\exists y: \text{big\_g}(y) \quad \text{fof}(\text{pel}_{29_2}, \text{axiom})$   
 $(\forall x: (\text{big\_f}(x) \Rightarrow \text{big\_h}(x))) \text{ and } \forall u: (\text{big\_g}(u) \Rightarrow \text{big\_j}(u)) \iff \forall w, y: ((\text{big\_f}(w) \text{ and } \text{big\_g}(y)) \Rightarrow (\text{big\_h}(w) \text{ and } \text{big\_j}(y)))$

**SYN059-1.p** Pelletier Problem 29

$\text{big\_f}(a) \quad \text{cnf}(\text{clause}_1, \text{axiom})$   
 $\text{big\_g}(b) \quad \text{cnf}(\text{clause}_2, \text{axiom})$   
 $(\text{big\_f}(x) \text{ and } \text{big\_f}(y) \text{ and } \text{big\_g}(z)) \Rightarrow (\text{big\_h}(x) \text{ or } \text{big\_h}(y)) \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $(\text{big\_f}(x) \text{ and } \text{big\_f}(y) \text{ and } \text{big\_g}(z)) \Rightarrow (\text{big\_h}(x) \text{ or } \text{big\_j}(z)) \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $\text{big\_f}(x) \Rightarrow (\text{big\_h}(x) \text{ or } \text{big\_f}(e) \text{ or } \text{big\_g}(f)) \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $(\text{big\_f}(x) \text{ and } \text{big\_j}(f)) \Rightarrow (\text{big\_h}(x) \text{ or } \text{big\_f}(e)) \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $(\text{big\_f}(x) \text{ and } \text{big\_h}(e)) \Rightarrow (\text{big\_h}(x) \text{ or } \text{big\_g}(f)) \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $(\text{big\_f}(x) \text{ and } \text{big\_h}(e) \text{ and } \text{big\_j}(f)) \Rightarrow \text{big\_h}(x) \quad \text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $(\text{big\_g}(x) \text{ and } \text{big\_f}(y) \text{ and } \text{big\_g}(z)) \Rightarrow (\text{big\_j}(x) \text{ or } \text{big\_h}(y)) \quad \text{cnf}(\text{clause}_9, \text{negated\_conjecture})$   
 $(\text{big\_g}(x) \text{ and } \text{big\_f}(y) \text{ and } \text{big\_g}(z)) \Rightarrow (\text{big\_j}(x) \text{ or } \text{big\_j}(z)) \quad \text{cnf}(\text{clause}_{10}, \text{negated\_conjecture})$   
 $\text{big\_g}(x) \Rightarrow (\text{big\_j}(x) \text{ or } \text{big\_f}(e) \text{ or } \text{big\_g}(j)) \quad \text{cnf}(\text{clause}_{11}, \text{negated\_conjecture})$   
 $(\text{big\_g}(x) \text{ and } \text{big\_j}(f)) \Rightarrow (\text{big\_j}(x) \text{ or } \text{big\_f}(e)) \quad \text{cnf}(\text{clause}_{12}, \text{negated\_conjecture})$   
 $(\text{big\_g}(x) \text{ and } \text{big\_h}(e)) \Rightarrow (\text{big\_j}(x) \text{ or } \text{big\_g}(f)) \quad \text{cnf}(\text{clause}_{13}, \text{negated\_conjecture})$   
 $(\text{big\_g}(x) \text{ and } \text{big\_h}(e) \text{ and } \text{big\_j}(f)) \Rightarrow \text{big\_j}(x) \quad \text{cnf}(\text{clause}_{14}, \text{negated\_conjecture})$   
 $(\text{big\_f}(x) \text{ and } \text{big\_g}(y)) \Rightarrow (\text{big\_f}(c) \text{ or } \text{big\_h}(x)) \quad \text{cnf}(\text{clause}_{15}, \text{negated\_conjecture})$   
 $(\text{big\_f}(x) \text{ and } \text{big\_g}(y)) \Rightarrow (\text{big\_f}(c) \text{ or } \text{big\_j}(y)) \quad \text{cnf}(\text{clause}_{16}, \text{negated\_conjecture})$   
 $\text{big\_f}(c) \text{ or } \text{big\_f}(e) \text{ or } \text{big\_g}(f) \quad \text{cnf}(\text{clause}_{17}, \text{negated\_conjecture})$   
 $\text{big\_j}(f) \Rightarrow (\text{big\_f}(c) \text{ or } \text{big\_f}(e)) \quad \text{cnf}(\text{clause}_{18}, \text{negated\_conjecture})$   
 $\text{big\_h}(e) \Rightarrow (\text{big\_f}(c) \text{ or } \text{big\_g}(f)) \quad \text{cnf}(\text{clause}_{19}, \text{negated\_conjecture})$   
 $(\text{big\_h}(e) \text{ and } \text{big\_j}(f)) \Rightarrow \text{big\_f}(c) \quad \text{cnf}(\text{clause}_{20}, \text{negated\_conjecture})$   
 $(\text{big\_f}(x) \text{ and } \text{big\_g}(y)) \Rightarrow (\text{big\_g}(d) \text{ or } \text{big\_h}(x)) \quad \text{cnf}(\text{clause}_{21}, \text{negated\_conjecture})$   
 $(\text{big\_f}(x) \text{ and } \text{big\_g}(y)) \Rightarrow (\text{big\_g}(d) \text{ or } \text{big\_j}(y)) \quad \text{cnf}(\text{clause}_{22}, \text{negated\_conjecture})$   
 $\text{big\_g}(d) \text{ or } \text{big\_f}(e) \text{ or } \text{big\_g}(f) \quad \text{cnf}(\text{clause}_{23}, \text{negated\_conjecture})$   
 $\text{big\_j}(f) \Rightarrow (\text{big\_g}(d) \text{ or } \text{big\_f}(e)) \quad \text{cnf}(\text{clause}_{24}, \text{negated\_conjecture})$   
 $\text{big\_h}(e) \Rightarrow (\text{big\_g}(d) \text{ or } \text{big\_g}(f)) \quad \text{cnf}(\text{clause}_{25}, \text{negated\_conjecture})$   
 $(\text{big\_h}(e) \text{ and } \text{big\_j}(f)) \Rightarrow \text{big\_g}(d) \quad \text{cnf}(\text{clause}_{26}, \text{negated\_conjecture})$   
 $(\text{big\_h}(c) \text{ and } \text{big\_j}(d) \text{ and } \text{big\_f}(x) \text{ and } \text{big\_g}(y)) \Rightarrow \text{big\_h}(x) \quad \text{cnf}(\text{clause}_{27}, \text{negated\_conjecture})$   
 $(\text{big\_h}(c) \text{ and } \text{big\_j}(d) \text{ and } \text{big\_f}(x) \text{ and } \text{big\_g}(y)) \Rightarrow \text{big\_j}(y) \quad \text{cnf}(\text{clause}_{28}, \text{negated\_conjecture})$   
 $(\text{big\_h}(c) \text{ and } \text{big\_j}(d)) \Rightarrow (\text{big\_f}(e) \text{ or } \text{big\_g}(f)) \quad \text{cnf}(\text{clause}_{29}, \text{negated\_conjecture})$   
 $(\text{big\_h}(c) \text{ and } \text{big\_j}(d) \text{ and } \text{big\_j}(f)) \Rightarrow \text{big\_f}(e) \quad \text{cnf}(\text{clause}_{30}, \text{negated\_conjecture})$   
 $(\text{big\_h}(c) \text{ and } \text{big\_h}(e)) \Rightarrow (\text{big\_j}(d) \text{ or } \text{big\_g}(f)) \quad \text{cnf}(\text{clause}_{31}, \text{negated\_conjecture})$   
 $(\text{big\_h}(c) \text{ and } \text{big\_j}(d) \text{ and } \text{big\_h}(e)) \Rightarrow \neg \text{big\_j}(f) \quad \text{cnf}(\text{clause}_{32}, \text{negated\_conjecture})$

**SYN059^5.p** TPS problem PELL29

$\text{cJ}: \$i \rightarrow \$o \quad \text{thf}(\text{cJ}, \text{type})$

$cG: \$i \rightarrow \$o$     thf(cG, type)

$cH: \$i \rightarrow \$o$     thf(cH, type)

$cF: \$i \rightarrow \$o$     thf(cF, type)

$(\exists xx: \$i: (cF@xx) \text{ and } \exists xx: \$i: (cG@xx)) \Rightarrow (((\forall xx: \$i: ((cF@xx) \Rightarrow (cH@xx)) \text{ and } \forall xx: \$i: ((cG@xx) \Rightarrow (cJ@xx))) \Rightarrow \forall xx: \$i, xy: \$i: ((cF@xx \text{ and } cG@xy) \Rightarrow (cH@xx \text{ and } cJ@xy))) \text{ and } (\forall xx: \$i, xy: \$i: ((cF@xx \text{ and } cG@xy) \Rightarrow (cH@xx \text{ and } cJ@xy)) \Rightarrow \forall xx: \$i: ((cG@xx) \Rightarrow (cJ@xx))))$     thf(cPELL<sub>29</sub>, conjecture)

**SYN060+1.p** Pelletier Problem 30

$\forall x: ((big\_f(x) \text{ or } big\_g(x)) \Rightarrow \neg big\_h(x))$     fof(pel30<sub>1</sub>, axiom)

$\forall x: ((big\_g(x) \Rightarrow \neg big\_i(x)) \Rightarrow (big\_f(x) \text{ and } big\_h(x)))$     fof(pel30<sub>2</sub>, axiom)

$\forall x: big\_i(x)$     fof(pel<sub>30</sub>, conjecture)

**SYN060-1.p** Pelletier Problem 30

$big\_f(x) \Rightarrow \neg big\_h(x)$     cnf(clause<sub>1</sub>, axiom)

$big\_g(x) \text{ or } big\_f(x)$     cnf(clause<sub>2</sub>, axiom)

$big\_g(x) \Rightarrow \neg big\_h(x)$     cnf(clause<sub>3</sub>, axiom)

$big\_g(x) \text{ or } big\_h(x)$     cnf(clause<sub>4</sub>, axiom)

$big\_i(x) \text{ or } big\_f(x)$     cnf(clause<sub>5</sub>, axiom)

$big\_i(x) \text{ or } big\_h(x)$     cnf(clause<sub>6</sub>, axiom)

$\neg big\_i(a)$     cnf(clause<sub>7</sub>, negated\_conjecture)

**SYN061+1.p** Pelletier Problem 31

$\neg \exists x: (big\_f(x) \text{ and } (big\_g(x) \text{ or } big\_h(x)))$     fof(pel31<sub>1</sub>, axiom)

$\exists x: (big\_i(x) \text{ and } big\_f(x))$     fof(pel31<sub>2</sub>, axiom)

$\forall x: (\neg big\_h(x) \Rightarrow big\_j(x))$     fof(pel31<sub>3</sub>, axiom)

$\exists x: (big\_i(x) \text{ and } big\_j(x))$     fof(pel<sub>31</sub>, conjecture)

**SYN061-1.p** Pelletier Problem 31

$big\_f(x) \Rightarrow \neg big\_g(x)$     cnf(clause<sub>1</sub>, axiom)

$big\_f(x) \Rightarrow \neg big\_h(x)$     cnf(clause<sub>2</sub>, axiom)

$big\_i(a)$     cnf(clause<sub>3</sub>, axiom)

$big\_f(a)$     cnf(clause<sub>4</sub>, axiom)

$big\_h(x) \text{ or } big\_j(x)$     cnf(clause<sub>5</sub>, axiom)

$big\_i(x) \Rightarrow \neg big\_j(x)$     cnf(clause<sub>6</sub>, negated\_conjecture)

**SYN062+1.p** Pelletier Problem 32

$\forall x: ((big\_f(x) \text{ and } (big\_g(x) \text{ or } big\_h(x))) \Rightarrow big\_i(x))$     fof(pel32<sub>1</sub>, axiom)

$\forall x: ((big\_i(x) \text{ and } big\_h(x)) \Rightarrow big\_j(x))$     fof(pel32<sub>2</sub>, axiom)

$\forall x: (big\_k(x) \Rightarrow big\_h(x))$     fof(pel32<sub>3</sub>, axiom)

$\forall x: ((big\_f(x) \text{ and } big\_k(x)) \Rightarrow big\_j(x))$     fof(pel<sub>32</sub>, conjecture)

**SYN062-1.p** Pelletier Problem 32

$(big\_f(x) \text{ and } big\_g(x)) \Rightarrow big\_i(x)$     cnf(clause<sub>1</sub>, axiom)

$(big\_f(x) \text{ and } big\_h(x)) \Rightarrow big\_i(x)$     cnf(clause<sub>2</sub>, axiom)

$(big\_i(x) \text{ and } big\_h(x)) \Rightarrow big\_j(x)$     cnf(clause<sub>3</sub>, axiom)

$big\_k(x) \Rightarrow big\_h(x)$     cnf(clause<sub>4</sub>, axiom)

$big\_f(a)$     cnf(clause<sub>5</sub>, negated\_conjecture)

$big\_k(a)$     cnf(clause<sub>6</sub>, negated\_conjecture)

$\neg big\_j(a)$     cnf(clause<sub>7</sub>, negated\_conjecture)

**SYN063+1.p** Pelletier Problem 33

$\forall x: ((big\_p(a) \text{ and } (big\_p(x) \Rightarrow big\_p(b))) \Rightarrow big\_p(c)) \iff \forall x_1: ((\neg big\_p(a) \text{ or } big\_p(x_1) \text{ or } big\_p(c)) \text{ and } (\neg big\_p(a) \text{ or } big\_p(b)))$

**SYN063-1.p** Pelletier Problem 33

$big\_p(a)$     cnf(clause<sub>1</sub>, negated\_conjecture)

$big\_p(a) \Rightarrow (big\_p(x) \text{ or } big\_p(c) \text{ or } big\_p(y))$     cnf(clause<sub>2</sub>, negated\_conjecture)

$(big\_p(a) \text{ and } big\_p(b)) \Rightarrow big\_p(c)$     cnf(clause<sub>3</sub>, negated\_conjecture)

$\neg big\_p(c)$     cnf(clause<sub>4</sub>, negated\_conjecture)

$(big\_p(e) \text{ and } big\_p(d)) \Rightarrow big\_p(b)$     cnf(clause<sub>5</sub>, negated\_conjecture)

$(big\_p(a) \text{ and } big\_p(d)) \Rightarrow (big\_p(x) \text{ or } big\_p(c) \text{ or } big\_p(b))$     cnf(clause<sub>6</sub>, negated\_conjecture)

$(big\_p(e) \text{ and } big\_p(a)) \Rightarrow (big\_p(b) \text{ or } big\_p(x) \text{ or } big\_p(c))$     cnf(clause<sub>7</sub>, negated\_conjecture)

**SYN063-2.p** Pelletier Problem 33

$big\_p(a) \Rightarrow big\_p(c)$     cnf(pel33<sub>1</sub>, negated\_conjecture)

$big\_p(a)$     cnf(pel33<sub>2</sub>, negated\_conjecture)

$\neg \text{big\_p}(c)$      $\text{cnf}(\text{pel33}_3, \text{negated\_conjecture})$

**SYN064+1.p** Pelletier Problem 35

$\exists x, y: (\text{big\_p}(x, y) \Rightarrow \forall z, w: \text{big\_p}(z, w))$      $\text{fof}(\text{pel35}, \text{conjecture})$

**SYN064-1.p** Pelletier Problem 35

$\text{big\_p}(x, y)$      $\text{cnf}(\text{clause}_1, \text{negated\_conjecture})$

$\neg \text{big\_p}(f(x, y), g(x, y))$      $\text{cnf}(\text{clause}_2, \text{negated\_conjecture})$

**SYN064 $\wedge$ 5.p** TPS problem PELL35

$\text{cP}: \$i \rightarrow \$i \rightarrow \$o$      $\text{thf}(\text{cP}, \text{type})$

$\exists \text{xx}: \$i, \text{xy}: \$i: ((\text{cP}@xx@xy) \Rightarrow \forall \text{xx}_0: \$i, \text{xy}_0: \$i: (\text{cP}@xx_0@xy_0))$      $\text{thf}(\text{cPELL35}, \text{conjecture})$

**SYN065+1.p** Pelletier Problem 36

$\forall x: \exists y: \text{big\_f}(x, y)$      $\text{fof}(\text{pel36}_1, \text{axiom})$

$\forall x: \exists y: \text{big\_g}(x, y)$      $\text{fof}(\text{pel36}_2, \text{axiom})$

$\forall x, y: ((\text{big\_f}(x, y) \text{ or } \text{big\_g}(x, y)) \Rightarrow \forall z: ((\text{big\_f}(y, z) \text{ or } \text{big\_g}(y, z)) \Rightarrow \text{big\_h}(x, z)))$      $\text{fof}(\text{pel36}_3, \text{axiom})$

$\forall x: \exists y: \text{big\_h}(x, y)$      $\text{fof}(\text{pel36}, \text{conjecture})$

**SYN065-1.p** Pelletier Problem 36

$\text{big\_f}(x, f(x))$      $\text{cnf}(\text{clause}_1, \text{axiom})$

$\text{big\_g}(x, g(x))$      $\text{cnf}(\text{clause}_2, \text{axiom})$

$(\text{big\_f}(x, y) \text{ and } \text{big\_f}(y, z)) \Rightarrow \text{big\_h}(x, z)$      $\text{cnf}(\text{clause}_3, \text{axiom})$

$(\text{big\_f}(x, y) \text{ and } \text{big\_g}(y, z)) \Rightarrow \text{big\_h}(x, z)$      $\text{cnf}(\text{clause}_4, \text{axiom})$

$(\text{big\_g}(x, y) \text{ and } \text{big\_f}(y, z)) \Rightarrow \text{big\_h}(x, z)$      $\text{cnf}(\text{clause}_5, \text{axiom})$

$(\text{big\_g}(x, y) \text{ and } \text{big\_g}(y, z)) \Rightarrow \text{big\_h}(x, z)$      $\text{cnf}(\text{clause}_6, \text{axiom})$

$\neg \text{big\_h}(a, x)$      $\text{cnf}(\text{clause}_7, \text{negated\_conjecture})$

**SYN066+1.p** Pelletier Problem 37

$\forall z: \exists w: \forall x: \exists y: ((\text{big\_p}(x, z) \Rightarrow \text{big\_p}(y, w)) \text{ and } \text{big\_p}(y, z) \text{ and } (\text{big\_p}(y, w) \Rightarrow \exists u: \text{big\_q}(u, w)))$      $\text{fof}(\text{pel37}_1, \text{axiom})$

$\forall x, z: (\neg \text{big\_p}(x, z) \Rightarrow \exists y: \text{big\_q}(y, z))$      $\text{fof}(\text{pel37}_2, \text{axiom})$

$\exists x, y: \text{big\_q}(x, y) \Rightarrow \forall z: \text{big\_r}(z, z)$      $\text{fof}(\text{pel37}_3, \text{axiom})$

$\forall x: \exists y: \text{big\_r}(x, y)$      $\text{fof}(\text{pel37}, \text{conjecture})$

**SYN066-1.p** Pelletier Problem 37

$\text{big\_p}(y, x) \Rightarrow \text{big\_p}(f(x, y), g(x))$      $\text{cnf}(\text{clause}_1, \text{axiom})$

$\text{big\_p}(f(x, y), x)$      $\text{cnf}(\text{clause}_2, \text{axiom})$

$\text{big\_p}(f(x, y), g(x)) \Rightarrow \text{big\_q}(h(x, y), g(x))$      $\text{cnf}(\text{clause}_3, \text{axiom})$

$\text{big\_p}(x, y) \text{ or } \text{big\_q}(i(x, y), x)$      $\text{cnf}(\text{clause}_4, \text{axiom})$

$\text{big\_q}(x, y) \Rightarrow \text{big\_r}(z, z)$      $\text{cnf}(\text{clause}_5, \text{axiom})$

$\neg \text{big\_r}(a, z)$      $\text{cnf}(\text{clause}_6, \text{negated\_conjecture})$

**SYN067+1.p** Pelletier Problem 38

$\forall x: ((\text{big\_p}(a) \text{ and } (\text{big\_p}(x) \Rightarrow \exists y: (\text{big\_p}(y) \text{ and } \text{big\_r}(x, y)))) \Rightarrow \exists z, w: (\text{big\_p}(z) \text{ and } \text{big\_r}(x, w) \text{ and } \text{big\_r}(w, z))) \iff$

$\forall x_1: ((\neg \text{big\_p}(a) \text{ or } \text{big\_p}(x_1) \text{ or } \exists z_1, w_1: (\text{big\_p}(z_1) \text{ and } \text{big\_r}(x_1, w_1) \text{ and } \text{big\_r}(w_1, z_1))) \text{ and } (\neg \text{big\_p}(a) \text{ or } \neg \exists y_1: (\text{big\_p}(y_1)$

**SYN068+1.p** Pelletier Problem 44

$\forall x: (\text{big\_f}(x) \Rightarrow (\exists y: (\text{big\_g}(y) \text{ and } \text{big\_h}(x, y)) \text{ and } \exists y_1: (\text{big\_g}(y_1) \text{ and } \neg \text{big\_h}(x, y_1))))$      $\text{fof}(\text{pel44}_1, \text{axiom})$

$\exists x: (\text{big\_j}(x) \text{ and } \forall y: (\text{big\_g}(y) \Rightarrow \text{big\_h}(x, y)))$      $\text{fof}(\text{pel44}_2, \text{axiom})$

$\exists x: (\text{big\_j}(x) \text{ and } \neg \text{big\_f}(x))$      $\text{fof}(\text{pel44}, \text{conjecture})$

**SYN068-1.p** Pelletier Problem 44

$\text{big\_f}(x) \Rightarrow \text{big\_g}(f(x))$      $\text{cnf}(\text{clause}_1, \text{axiom})$

$\text{big\_f}(x) \Rightarrow \text{big\_h}(x, f(x))$      $\text{cnf}(\text{clause}_2, \text{axiom})$

$\text{big\_f}(x) \Rightarrow \text{big\_g}(g(x))$      $\text{cnf}(\text{clause}_3, \text{axiom})$

$\text{big\_f}(x) \Rightarrow \neg \text{big\_h}(x, g(x))$      $\text{cnf}(\text{clause}_4, \text{axiom})$

$\text{big\_j}(a)$      $\text{cnf}(\text{clause}_5, \text{axiom})$

$\text{big\_g}(x) \Rightarrow \text{big\_h}(a, x)$      $\text{cnf}(\text{clause}_6, \text{axiom})$

$\text{big\_j}(x) \Rightarrow \text{big\_f}(x)$      $\text{cnf}(\text{clause}_7, \text{negated\_conjecture})$

**SYN069+1.p** Pelletier Problem 45

$\forall x: ((\text{big\_f}(x) \text{ and } \forall y: ((\text{big\_g}(y) \text{ and } \text{big\_h}(x, y)) \Rightarrow \text{big\_j}(x, y))) \Rightarrow \forall y_1: (\text{big\_g}(y_1) \text{ and } \text{big\_h}(x, y_1) \text{ and } \text{big\_k}(y_1)))$      $\text{fof}$

$\neg \exists y: (\text{big\_l}(y) \text{ and } \text{big\_k}(y))$      $\text{fof}(\text{pel45}_2, \text{axiom})$

$\exists x: (\text{big\_f}(x) \text{ and } \forall y: (\text{big\_h}(x, y) \Rightarrow \text{big\_l}(y)) \text{ and } \forall y_1: ((\text{big\_g}(y_1) \text{ and } \text{big\_h}(x, y_1)) \Rightarrow \text{big\_j}(x, y_1)))$      $\text{fof}(\text{pel45}_3, \text{axiom})$

$\exists x: (\text{big\_f}(x) \text{ and } \neg \exists y: (\text{big\_g}(y) \text{ and } \text{big\_h}(x, y)))$      $\text{fof}(\text{pel45}, \text{conjecture})$

**SYN069-1.p** Pelletier Problem 45

$(\text{big\_f}(x) \text{ and } \text{big\_g}(y) \text{ and } \text{big\_h}(x, y)) \Rightarrow (\text{big\_g}(f(x)) \text{ or } \text{big\_k}(y))$      $\text{cnf}(\text{clause}_1, \text{axiom})$   
 $(\text{big\_f}(x) \text{ and } \text{big\_g}(y) \text{ and } \text{big\_h}(x, y)) \Rightarrow (\text{big\_h}(x, f(x)) \text{ or } \text{big\_k}(y))$      $\text{cnf}(\text{clause}_2, \text{axiom})$   
 $(\text{big\_f}(x) \text{ and } \text{big\_j}(x, f(x)) \text{ and } \text{big\_g}(y) \text{ and } \text{big\_h}(x, y)) \Rightarrow \text{big\_k}(y)$      $\text{cnf}(\text{clause}_3, \text{axiom})$   
 $\text{big\_l}(x) \Rightarrow \neg \text{big\_k}(x)$      $\text{cnf}(\text{clause}_4, \text{axiom})$   
 $\text{big\_f}(a)$      $\text{cnf}(\text{clause}_5, \text{axiom})$   
 $\text{big\_h}(a, x) \Rightarrow \text{big\_l}(x)$      $\text{cnf}(\text{clause}_6, \text{axiom})$   
 $(\text{big\_g}(x) \text{ and } \text{big\_h}(a, x)) \Rightarrow \text{big\_j}(a, x)$      $\text{cnf}(\text{clause}_7, \text{axiom})$   
 $\text{big\_f}(x) \Rightarrow \text{big\_g}(g(x))$      $\text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $\text{big\_f}(x) \Rightarrow \text{big\_h}(x, g(x))$      $\text{cnf}(\text{clause}_9, \text{negated\_conjecture})$

**SYN070+1.p** Pelletier Problem 46

$\forall x, y: ((\text{big\_f}(x) \text{ and } ((\text{big\_f}(y) \text{ and } \text{big\_h}(y, x)) \Rightarrow \text{big\_g}(y))) \Rightarrow \text{big\_g}(x))$      $\text{fof}(\text{pel46}_1, \text{axiom})$   
 $\exists x: (\text{big\_f}(x) \text{ and } \neg \text{big\_g}(x)) \Rightarrow \exists x_1: (\text{big\_f}(x_1) \text{ and } \neg \text{big\_g}(x_1)) \text{ and } \forall y: ((\text{big\_f}(y) \text{ and } \neg \text{big\_g}(y)) \Rightarrow \text{big\_j}(x_1, y))$      $\text{fof}(\text{pel46}_2, \text{conjecture})$   
 $\forall x, y: ((\text{big\_f}(x) \text{ and } \text{big\_f}(y) \text{ and } \text{big\_h}(x, y)) \Rightarrow \neg \text{big\_j}(y, x))$      $\text{fof}(\text{pel46}_3, \text{axiom})$   
 $\forall x: (\text{big\_f}(x) \Rightarrow \text{big\_g}(x))$      $\text{fof}(\text{pel46}_4, \text{conjecture})$

**SYN070-1.p** Pelletier Problem 46

$\text{big\_f}(x) \Rightarrow (\text{big\_f}(f(x)) \text{ or } \text{big\_g}(x))$      $\text{cnf}(\text{clause}_1, \text{axiom})$   
 $\text{big\_f}(x) \Rightarrow (\text{big\_h}(f(x), x) \text{ or } \text{big\_g}(x))$      $\text{cnf}(\text{clause}_2, \text{axiom})$   
 $(\text{big\_f}(x) \text{ and } \text{big\_g}(f(x))) \Rightarrow \text{big\_g}(x)$      $\text{cnf}(\text{clause}_3, \text{axiom})$   
 $\text{big\_f}(x) \Rightarrow (\text{big\_g}(x) \text{ or } \text{big\_f}(a))$      $\text{cnf}(\text{clause}_4, \text{axiom})$   
 $(\text{big\_f}(x) \text{ and } \text{big\_g}(a)) \Rightarrow \text{big\_g}(x)$      $\text{cnf}(\text{clause}_5, \text{axiom})$   
 $(\text{big\_f}(x) \text{ and } \text{big\_f}(y)) \Rightarrow (\text{big\_g}(x) \text{ or } \text{big\_g}(y) \text{ or } \text{big\_j}(a, y))$      $\text{cnf}(\text{clause}_6, \text{axiom})$   
 $(\text{big\_f}(x) \text{ and } \text{big\_f}(y) \text{ and } \text{big\_h}(x, y)) \Rightarrow \neg \text{big\_j}(y, x)$      $\text{cnf}(\text{clause}_7, \text{axiom})$   
 $\text{big\_f}(b)$      $\text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $\neg \text{big\_g}(b)$      $\text{cnf}(\text{clause}_9, \text{negated\_conjecture})$

**SYN071+1.p** Pelletier Problem 48

$a = b \text{ or } c = d$      $\text{fof}(\text{pel48}_1, \text{axiom})$   
 $a = c \text{ or } b = d$      $\text{fof}(\text{pel48}_2, \text{axiom})$   
 $a = d \text{ or } b = c$      $\text{fof}(\text{pel48}_3, \text{conjecture})$

**SYN071-1.p** Pelletier Problem 48

$a = b \text{ or } c = d$      $\text{cnf}(\text{clause}_1, \text{axiom})$   
 $a = c \text{ or } b = d$      $\text{cnf}(\text{clause}_2, \text{axiom})$   
 $a \neq d$      $\text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $b \neq c$      $\text{cnf}(\text{clause}_4, \text{negated\_conjecture})$

**SYN072+1.p** Pelletier Problem 49

$\exists x, y: \forall z: (z = x \text{ or } z = y)$      $\text{fof}(\text{pel49}_1, \text{axiom})$   
 $\text{big\_p}(a)$      $\text{fof}(\text{pel49}_2, \text{axiom})$   
 $\text{big\_p}(b)$      $\text{fof}(\text{pel49}_3, \text{axiom})$   
 $a \neq b$      $\text{fof}(\text{pel49}_4, \text{axiom})$   
 $\forall x: \text{big\_p}(x)$      $\text{fof}(\text{pel49}_5, \text{conjecture})$

**SYN072-1.p** Pelletier Problem 49

$x = c \text{ or } x = d$      $\text{cnf}(\text{clause}_1, \text{axiom})$   
 $\text{big\_p}(a)$      $\text{cnf}(\text{clause}_2, \text{axiom})$   
 $\text{big\_p}(b)$      $\text{cnf}(\text{clause}_3, \text{axiom})$   
 $a \neq b$      $\text{cnf}(\text{clause}_4, \text{axiom})$   
 $\neg \text{big\_p}(e)$      $\text{cnf}(\text{prove\_this}, \text{negated\_conjecture})$

**SYN073+1.p** Pelletier Problem 50

$\forall x: (\text{big\_f}(a, x) \text{ or } \forall y: \text{big\_f}(x, y)) \Rightarrow \exists x_1: \forall y_1: \text{big\_f}(x_1, y_1)$      $\text{fof}(\text{pel50}, \text{conjecture})$

**SYN073-1.p** Pelletier Problem 50

$\text{big\_f}(a, x) \text{ or } \text{big\_f}(x, y)$      $\text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $\neg \text{big\_f}(x, f(x))$      $\text{cnf}(\text{prove\_this}, \text{negated\_conjecture})$

**SYN074+1.p** Pelletier Problem 51

$\exists z, w: \forall x, y: (\text{big\_f}(x, y) \iff (x = z \text{ and } y = w))$      $\text{fof}(\text{pel51}_1, \text{axiom})$   
 $\exists z: \forall x: (\exists w: \forall y: (\text{big\_f}(x, y) \iff y = w) \iff x = z)$      $\text{fof}(\text{pel51}_2, \text{conjecture})$

**SYN074-1.p** Pelletier Problem 51

$\text{big\_f}(x, y) \Rightarrow x = a$      $\text{cnf}(\text{clause}_1, \text{axiom})$

$\text{big\_f}(x, y) \Rightarrow y = b \quad \text{cnf}(\text{clause}_2, \text{axiom})$   
 $(x = a \text{ and } y = b) \Rightarrow \text{big\_f}(x, y) \quad \text{cnf}(\text{clause}_3, \text{axiom})$   
 $\text{big\_f}(f(x), y) \Rightarrow (y = g(x) \text{ or } f(x) = x) \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $\text{big\_f}(f(x), y) \Rightarrow (y = g(x) \text{ or } \text{big\_f}(f(x), h(x, z)) \text{ or } h(x, z) = z) \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $(\text{big\_f}(f(x), y) \text{ and } h(x, z) = z \text{ and } \text{big\_f}(f(x), h(x, z))) \Rightarrow y = g(x) \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $y = g(x) \Rightarrow (\text{big\_f}(f(x), y) \text{ or } \text{big\_f}(f(x), h(x, z)) \text{ or } h(x, z) = z) \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $y = g(x) \Rightarrow (\text{big\_f}(f(x), y) \text{ or } f(x) = x) \quad \text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $(y = g(x) \text{ and } h(x, z) = z \text{ and } \text{big\_f}(f(x), h(x, z))) \Rightarrow \text{big\_f}(f(x), y) \quad \text{cnf}(\text{clause}_9, \text{negated\_conjecture})$   
 $f(x) = x \Rightarrow (\text{big\_f}(f(x), h(x, z)) \text{ or } h(x, z) = z) \quad \text{cnf}(\text{clause}_{10}, \text{negated\_conjecture})$   
 $(f(x) = x \text{ and } h(x, z) = z) \Rightarrow \neg \text{big\_f}(f(x), h(x, z)) \quad \text{cnf}(\text{clause}_{11}, \text{negated\_conjecture})$

**SYN075+1.p** Pelletier Problem 52

$\exists z, w: \forall x, y: (\text{big\_f}(x, y) \iff (x = z \text{ and } y = w)) \quad \text{fof}(\text{pel52}_1, \text{axiom})$   
 $\exists w: \forall y: (\exists z: \forall x: (\text{big\_f}(x, y) \iff x = z) \iff y = w) \quad \text{fof}(\text{pel}_{52}, \text{conjecture})$

**SYN075-1.p** Pelletier Problem 52

$\text{big\_f}(x, y) \Rightarrow x = a \quad \text{cnf}(\text{clause}_1, \text{axiom})$   
 $\text{big\_f}(x, y) \Rightarrow y = b \quad \text{cnf}(\text{clause}_2, \text{axiom})$   
 $(x = a \text{ and } y = b) \Rightarrow \text{big\_f}(x, y) \quad \text{cnf}(\text{clause}_3, \text{axiom})$   
 $(\text{big\_f}(y, f(x)) \text{ and } y = g(x)) \Rightarrow f(x) = x \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $(\text{big\_f}(y, f(x)) \text{ and } \text{big\_f}(h(x, z), f(x))) \Rightarrow (y = g(x) \text{ or } \text{big\_f}(h(x, z), f(x))) \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $y = g(x) \Rightarrow (\text{big\_f}(y, f(x)) \text{ or } f(x) = x) \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $y = g(x) \Rightarrow (\text{big\_f}(y, f(x)) \text{ or } \text{big\_f}(h(x, z), f(x)) \text{ or } h(x, z) = z) \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $(y = g(x) \text{ and } h(x, z) = z \text{ and } \text{big\_f}(h(x, z), f(x))) \Rightarrow \text{big\_f}(y, f(x)) \quad \text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $f(x) = x \Rightarrow (\text{big\_f}(h(x, z), f(x)) \text{ or } h(x, z) = z) \quad \text{cnf}(\text{clause}_9, \text{negated\_conjecture})$   
 $(f(x) = x \text{ and } h(x, z) = z) \Rightarrow \neg \text{big\_f}(h(x, z), f(x)) \quad \text{cnf}(\text{clause}_{10}, \text{negated\_conjecture})$

**SYN076+1.p** Pelletier Problem 53

$\exists x, y: (x \neq y \text{ and } \forall z: (z = x \text{ or } z = y)) \quad \text{fof}(\text{pel53}_1, \text{axiom})$   
 $\exists z: \forall x: (\exists w: \forall y: (\text{big\_f}(x, y) \iff y = w) \iff x = z) \iff \exists w_1: \forall y_1: (\exists z_1: \forall x_1: (\text{big\_f}(x_1, y_1) \iff x_1 = z_1) \iff y_1 = w_1) \quad \text{fof}(\text{pel}_{53}, \text{conjecture})$

**SYN077+1.p** Pelletier Problem 54

Montegue's paradox of grounded classes

$\forall y: \exists z: \forall x: (\text{big\_f}(x, z) \iff x = y) \quad \text{fof}(\text{pel54}_1, \text{axiom})$   
 $\neg \exists w: \forall x: (\text{big\_f}(x, w) \iff \forall u: (\text{big\_f}(x, u) \Rightarrow \exists y: (\text{big\_f}(y, u) \text{ and } \neg \exists z: (\text{big\_f}(z, u) \text{ and } \text{big\_f}(z, y)))))) \quad \text{fof}(\text{pel}_{54}, \text{conjecture})$

**SYN077-1.p** Pelletier Problem 54

Montegue's paradox of grounded classes

$\text{big\_f}(x, f(y)) \Rightarrow x = y \quad \text{cnf}(\text{clause}_1, \text{axiom})$   
 $x = y \Rightarrow \text{big\_f}(x, f(y)) \quad \text{cnf}(\text{clause}_2, \text{axiom})$   
 $(\text{big\_f}(x, a) \text{ and } \text{big\_f}(x, y)) \Rightarrow \text{big\_f}(g(x, y), y) \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $(\text{big\_f}(x, a) \text{ and } \text{big\_f}(x, y) \text{ and } \text{big\_f}(z, g(x, y))) \Rightarrow \neg \text{big\_f}(z, y) \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $\text{big\_f}(x, h(x)) \text{ or } \text{big\_f}(x, a) \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $\text{big\_f}(x, h(y)) \Rightarrow (\text{big\_f}(i(y, x), x) \text{ or } \text{big\_f}(y, a)) \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $\text{big\_f}(y, h(x)) \Rightarrow (\text{big\_f}(x, a) \text{ or } \text{big\_f}(i(x, y), h(x))) \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$

**SYN078+1.p** Pelletier Problem 56

$\forall x: (\exists y: (\text{big\_p}(y) \text{ and } x = f(y)) \Rightarrow \text{big\_p}(x)) \iff \forall u: (\text{big\_p}(u) \Rightarrow \text{big\_p}(f(u))) \quad \text{fof}(\text{pel}_{56}, \text{conjecture})$

**SYN078-1.p** Pelletier Problem 56

$(\text{big\_f}(x) \text{ and } y = f(y) \text{ and } \text{big\_f}(z)) \Rightarrow (\text{big\_f}(y) \text{ or } \text{big\_f}(f(z))) \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $(\text{big\_f}(x) \text{ and } y = f(y)) \Rightarrow (\text{big\_f}(y) \text{ or } \text{big\_f}(a)) \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture})$   
 $(\text{big\_f}(x) \text{ and } y = f(y)) \Rightarrow (\text{big\_f}(y) \text{ or } b = f(b)) \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $(\text{big\_f}(x) \text{ and } y = f(y) \text{ and } \text{big\_f}(b)) \Rightarrow \text{big\_f}(y) \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $\text{big\_f}(x) \Rightarrow (\text{big\_f}(c) \text{ or } \text{big\_f}(f(x))) \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $\text{big\_f}(c) \text{ or } \text{big\_f}(a) \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $\text{big\_f}(c) \text{ or } b = f(b) \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $\text{big\_f}(b) \Rightarrow \text{big\_f}(c) \quad \text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $(\text{big\_f}(f(c)) \text{ and } \text{big\_f}(x)) \Rightarrow \text{big\_f}(f(x)) \quad \text{cnf}(\text{clause}_9, \text{negated\_conjecture})$   
 $\text{big\_f}(f(c)) \Rightarrow \text{big\_f}(a) \quad \text{cnf}(\text{clause}_{10}, \text{negated\_conjecture})$   
 $\text{big\_f}(f(c)) \Rightarrow b = f(b) \quad \text{cnf}(\text{clause}_{11}, \text{negated\_conjecture})$   
 $\text{big\_f}(f(c)) \Rightarrow \neg \text{big\_f}(b) \quad \text{cnf}(\text{clause}_{12}, \text{negated\_conjecture})$

**SYN079+1.p** Pelletier Problem 57

$\text{big\_f}(f(a, b), f(b, c)) \quad \text{fof}(\text{pel57}_1, \text{axiom})$   
 $\text{big\_f}(f(b, c), f(a, c)) \quad \text{fof}(\text{pel57}_2, \text{axiom})$   
 $\forall x, y, z: ((\text{big\_f}(x, y) \text{ and } \text{big\_f}(y, z)) \Rightarrow \text{big\_f}(x, z)) \quad \text{fof}(\text{pel57}_3, \text{axiom})$   
 $\text{big\_f}(f(a, b), f(a, c)) \quad \text{fof}(\text{pel57}, \text{conjecture})$

**SYN079-1.p** Pelletier Problem 57

$\text{big\_f}(f(a, b), f(b, c)) \quad \text{cnf}(\text{clause}_1, \text{axiom})$   
 $\text{big\_f}(f(b, c), f(a, c)) \quad \text{cnf}(\text{clause}_2, \text{axiom})$   
 $(\text{big\_f}(x, y) \text{ and } \text{big\_f}(y, z)) \Rightarrow \text{big\_f}(x, z) \quad \text{cnf}(\text{clause}_3, \text{axiom})$   
 $\neg \text{big\_f}(f(a, b), f(a, c)) \quad \text{cnf}(\text{prove\_this}, \text{negated\_conjecture})$

**SYN080+1.p** Pelletier Problem 58

$\forall x, y: f(x) = g(y) \quad \text{fof}(\text{pel58}_1, \text{axiom})$   
 $\forall x, y: f(f(x)) = f(g(y)) \quad \text{fof}(\text{pel58}, \text{conjecture})$

**SYN080-1.p** Pelletier Problem 58

$f(x) = g(y) \quad \text{cnf}(\text{clause}_1, \text{axiom})$   
 $f(f(a)) \neq f(g(b)) \quad \text{cnf}(\text{prove\_this}, \text{negated\_conjecture})$

**SYN081+1.p** Pelletier Problem 59

$\forall x: (\text{big\_f}(x) \iff \neg \text{big\_f}(f(x))) \quad \text{fof}(\text{pel59}_1, \text{axiom})$   
 $\exists x: (\text{big\_f}(x) \text{ and } \neg \text{big\_f}(f(x))) \quad \text{fof}(\text{pel59}, \text{conjecture})$

**SYN081-1.p** Pelletier Problem 59

$\text{big\_f}(x) \Rightarrow \neg \text{big\_f}(f(x)) \quad \text{cnf}(\text{clause}_1, \text{axiom})$   
 $\text{big\_f}(f(x)) \text{ or } \text{big\_f}(x) \quad \text{cnf}(\text{clause}_2, \text{axiom})$   
 $\text{big\_f}(x) \Rightarrow \text{big\_f}(f(x)) \quad \text{cnf}(\text{prove\_this}, \text{negated\_conjecture})$

**SYN082+1.p** Pelletier Problem 60

$\forall x: (\text{big\_f}(x, f(x)) \iff \exists y: (\forall z: (\text{big\_f}(z, y) \Rightarrow \text{big\_f}(z, f(x))) \text{ and } \text{big\_f}(x, y))) \quad \text{fof}(\text{pel60}, \text{conjecture})$

**SYN082-1.p** Pelletier Problem 60

$\text{big\_f}(y, b) \Rightarrow (\text{big\_f}(a, f(a)) \text{ or } \text{big\_f}(y, f(a))) \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $\text{big\_f}(a, f(a)) \text{ or } \text{big\_f}(a, b) \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture})$   
 $(\text{big\_f}(a, x) \text{ and } \text{big\_f}(y, b)) \Rightarrow (\text{big\_f}(g(x), x) \text{ or } \text{big\_f}(y, f(a))) \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $\text{big\_f}(a, x) \Rightarrow (\text{big\_f}(g(x), x) \text{ or } \text{big\_f}(a, b)) \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $(\text{big\_f}(a, x) \text{ and } \text{big\_f}(a, f(a))) \Rightarrow \text{big\_f}(g(x), x) \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $(\text{big\_f}(g(x), x) \text{ and } \text{big\_f}(a, x) \text{ and } \text{big\_f}(y, b)) \Rightarrow \text{big\_f}(y, f(a)) \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $(\text{big\_f}(g(x), x) \text{ and } \text{big\_f}(a, x)) \Rightarrow \text{big\_f}(a, b) \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $(\text{big\_f}(g(x), x) \text{ and } \text{big\_f}(a, x)) \Rightarrow \neg \text{big\_f}(a, f(a)) \quad \text{cnf}(\text{clause}_8, \text{negated\_conjecture})$

**SYN083+1.p** Pelletier Problem 61

$\forall x, y, z: f(x, f(y, z)) = f(f(x, y), z) \quad \text{fof}(\text{p61}_1, \text{axiom})$   
 $\forall x, y, z, w: f(x, f(y, f(z, w))) = f(f(f(x, y), z), w) \quad \text{fof}(\text{pel61}, \text{conjecture})$

**SYN083-1.p** Pelletier Problem 61

$f(x, f(y, z)) = f(f(x, y), z) \quad \text{cnf}(\text{f\_is\_associative}, \text{axiom})$   
 $f(a, f(b, f(c, d))) \neq f(f(f(a, b), c), d) \quad \text{cnf}(\text{prove\_this}, \text{negated\_conjecture})$

**SYN084+1.p** Pelletier Problem 62

$\forall x: ((\text{big\_p}(a) \text{ and } (\text{big\_p}(x) \Rightarrow \text{big\_p}(f(x)))) \Rightarrow \text{big\_p}(f(f(x)))) \iff \forall x_1: ((\neg \text{big\_p}(a) \text{ or } \text{big\_p}(x_1) \text{ or } \text{big\_p}(f(f(x_1)))) \text{ and } \text{big\_p}(f(f(x_1)))) \Rightarrow \text{big\_p}(x_1))$

**SYN084-1.p** Pelletier Problem 62

$\text{big\_p}(a) \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture})$   
 $(\text{big\_p}(f(y)) \text{ and } \text{big\_p}(a)) \Rightarrow (\text{big\_p}(f(f(x))) \text{ or } \text{big\_p}(x)) \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture})$   
 $\text{big\_p}(a) \Rightarrow (\text{big\_p}(y) \text{ or } \text{big\_p}(f(f(x))) \text{ or } \text{big\_p}(x)) \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture})$   
 $(\text{big\_p}(c) \text{ and } \text{big\_p}(a)) \Rightarrow (\text{big\_p}(f(c)) \text{ or } \text{big\_p}(f(f(x))) \text{ or } \text{big\_p}(x)) \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture})$   
 $(\text{big\_p}(f(f(c))) \text{ and } \text{big\_p}(a)) \Rightarrow (\text{big\_p}(f(f(x))) \text{ or } \text{big\_p}(x)) \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture})$   
 $(\text{big\_p}(f(f(c))) \text{ and } \text{big\_p}(f(x)) \text{ and } \text{big\_p}(a)) \Rightarrow \text{big\_p}(f(f(x))) \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture})$   
 $(\text{big\_p}(c) \text{ and } \text{big\_p}(f(x)) \text{ and } \text{big\_p}(a)) \Rightarrow (\text{big\_p}(f(c)) \text{ or } \text{big\_p}(f(f(x)))) \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture})$   
 $(\text{big\_p}(f(x)) \text{ and } \text{big\_p}(a)) \Rightarrow (\text{big\_p}(y) \text{ or } \text{big\_p}(f(f(x)))) \quad \text{cnf}(\text{clause}_8, \text{negated\_conjecture})$   
 $(\text{big\_p}(f(y)) \text{ and } \text{big\_p}(f(x)) \text{ and } \text{big\_p}(a)) \Rightarrow \text{big\_p}(f(f(x))) \quad \text{cnf}(\text{clause}_9, \text{negated\_conjecture})$   
 $(\text{big\_p}(f(f(c))) \text{ and } \text{big\_p}(b)) \Rightarrow \text{big\_p}(f(b)) \quad \text{cnf}(\text{clause}_{10}, \text{negated\_conjecture})$   
 $(\text{big\_p}(c) \text{ and } \text{big\_p}(b)) \Rightarrow (\text{big\_p}(f(c)) \text{ or } \text{big\_p}(f(b))) \quad \text{cnf}(\text{clause}_{11}, \text{negated\_conjecture})$   
 $(\text{big\_p}(a) \text{ and } \text{big\_p}(b)) \Rightarrow (\text{big\_p}(y) \text{ or } \text{big\_p}(f(b))) \quad \text{cnf}(\text{clause}_{12}, \text{negated\_conjecture})$

$(\text{big\_p}(a) \text{ and } \text{big\_p}(f(y)) \text{ and } \text{big\_p}(b)) \Rightarrow \text{big\_p}(f(b)) \quad \text{cnf}(\text{clause}_{13}, \text{negated\_conjecture})$

**SYN084-2.p** Pelletier Problem 62

$\text{big\_p}(a) \quad \text{cnf}(\text{pel62}_1, \text{negated\_conjecture})$   
 $\text{big\_p}(a) \Rightarrow (\text{big\_p}(f(f(a))) \text{ or } \text{big\_p}(a)) \quad \text{cnf}(\text{pel62}_2, \text{negated\_conjecture})$   
 $(\text{big\_p}(f(a)) \text{ and } \text{big\_p}(a)) \Rightarrow \text{big\_p}(f(f(a))) \quad \text{cnf}(\text{pel62}_3, \text{negated\_conjecture})$   
 $\text{big\_p}(f(f(\text{sk}_1))) \Rightarrow \neg \text{big\_p}(f(f(\text{sk}_2))) \quad \text{cnf}(\text{pel62}_4, \text{negated\_conjecture})$   
 $(\text{big\_p}(\text{sk}_1) \text{ and } \text{big\_p}(\text{sk}_2)) \Rightarrow (\text{big\_p}(f(\text{sk}_1)) \text{ or } \text{big\_p}(f(\text{sk}_2))) \quad \text{cnf}(\text{pel62}_5, \text{negated\_conjecture})$   
 $(\text{big\_p}(\text{sk}_1) \text{ and } \text{big\_p}(f(f(\text{sk}_2)))) \Rightarrow \text{big\_p}(f(\text{sk}_1)) \quad \text{cnf}(\text{pel62}_6, \text{negated\_conjecture})$   
 $(\text{big\_p}(\text{sk}_2) \text{ and } \text{big\_p}(f(f(\text{sk}_1)))) \Rightarrow \text{big\_p}(f(\text{sk}_2)) \quad \text{cnf}(\text{pel62}_7, \text{negated\_conjecture})$

**SYN085-1.010.p** Plaisted problem s(1,10)

$\neg p_0 \quad \text{cnf}(\text{s1\_goal}_1, \text{negated\_conjecture})$   
 $(p_1 \text{ and } p_2 \text{ and } p_3 \text{ and } p_4 \text{ and } p_5 \text{ and } p_6 \text{ and } p_7 \text{ and } p_8 \text{ and } p_9 \text{ and } p_{10}) \Rightarrow p_0 \quad \text{cnf}(\text{s1}_1, \text{axiom})$   
 $p_1 \quad \text{cnf}(\text{s1}_2, \text{axiom})$   
 $p_2 \quad \text{cnf}(\text{s1}_3, \text{axiom})$   
 $p_3 \quad \text{cnf}(\text{s1}_4, \text{axiom})$   
 $p_4 \quad \text{cnf}(\text{s1}_5, \text{axiom})$   
 $p_5 \quad \text{cnf}(\text{s1}_6, \text{axiom})$   
 $p_6 \quad \text{cnf}(\text{s1}_7, \text{axiom})$   
 $p_7 \quad \text{cnf}(\text{s1}_8, \text{axiom})$   
 $p_8 \quad \text{cnf}(\text{s1}_9, \text{axiom})$   
 $p_9 \quad \text{cnf}(\text{s1}_{10}, \text{axiom})$   
 $p_{10} \quad \text{cnf}(\text{s1}_{11}, \text{axiom})$

**SYN086-1.003.p** Plaisted problem s(2,3)

$\neg p_{13} \quad \text{cnf}(\text{s2\_goal}_1, \text{negated\_conjecture})$   
 $(p_{22} \text{ and } p_{11}) \Rightarrow p_{12} \quad \text{cnf}(\text{s2\_type11}_1, \text{axiom})$   
 $(q_{22} \text{ and } q_{11}) \Rightarrow p_{12} \quad \text{cnf}(\text{s2\_type11}_2, \text{axiom})$   
 $(p_{23} \text{ and } p_{12}) \Rightarrow p_{13} \quad \text{cnf}(\text{s2\_type11}_3, \text{axiom})$   
 $(q_{23} \text{ and } q_{12}) \Rightarrow p_{13} \quad \text{cnf}(\text{s2\_type11}_4, \text{axiom})$   
 $(p_{33} \text{ and } p_{22}) \Rightarrow p_{23} \quad \text{cnf}(\text{s2\_type11}_5, \text{axiom})$   
 $(q_{33} \text{ and } q_{22}) \Rightarrow p_{23} \quad \text{cnf}(\text{s2\_type11}_6, \text{axiom})$   
 $(p_{22} \text{ and } q_{11}) \Rightarrow q_{12} \quad \text{cnf}(\text{s2\_type12}_1, \text{axiom})$   
 $(q_{22} \text{ and } p_{11}) \Rightarrow q_{12} \quad \text{cnf}(\text{s2\_type12}_2, \text{axiom})$   
 $(p_{23} \text{ and } q_{12}) \Rightarrow q_{13} \quad \text{cnf}(\text{s2\_type12}_3, \text{axiom})$   
 $(q_{23} \text{ and } p_{12}) \Rightarrow q_{13} \quad \text{cnf}(\text{s2\_type12}_4, \text{axiom})$   
 $(p_{33} \text{ and } q_{22}) \Rightarrow q_{23} \quad \text{cnf}(\text{s2\_type12}_5, \text{axiom})$   
 $(q_{33} \text{ and } p_{22}) \Rightarrow q_{23} \quad \text{cnf}(\text{s2\_type12}_6, \text{axiom})$   
 $p_{12} \Rightarrow p_{11} \quad \text{cnf}(\text{s2\_type21}_1, \text{axiom})$   
 $q_{12} \Rightarrow q_{11} \quad \text{cnf}(\text{s2\_type21}_2, \text{axiom})$   
 $p_{12} \Rightarrow p_{22} \quad \text{cnf}(\text{s2\_type22}_1, \text{axiom})$   
 $p_{23} \Rightarrow p_{33} \quad \text{cnf}(\text{s2\_type22}_2, \text{axiom})$   
 $q_{12} \Rightarrow q_{22} \quad \text{cnf}(\text{s2\_type22}_3, \text{axiom})$   
 $q_{23} \Rightarrow q_{33} \quad \text{cnf}(\text{s2\_type22}_4, \text{axiom})$

**SYN087-1.003.p** Plaisted problem s(3,3)

$p_0 \Rightarrow \neg q_0 \quad \text{cnf}(\text{s3\_goal}_1, \text{negated\_conjecture})$   
 $(p_1 \text{ and } p_2) \Rightarrow p_0 \quad \text{cnf}(\text{s3\_type11}_1, \text{axiom})$   
 $(q_1 \text{ and } q_2) \Rightarrow p_0 \quad \text{cnf}(\text{s3\_type11}_2, \text{axiom})$   
 $(p_2 \text{ and } p_3) \Rightarrow p_1 \quad \text{cnf}(\text{s3\_type11}_3, \text{axiom})$   
 $(q_2 \text{ and } q_3) \Rightarrow p_1 \quad \text{cnf}(\text{s3\_type11}_4, \text{axiom})$   
 $(p_3 \text{ and } p_4) \Rightarrow p_2 \quad \text{cnf}(\text{s3\_type11}_5, \text{axiom})$   
 $(q_3 \text{ and } q_4) \Rightarrow p_2 \quad \text{cnf}(\text{s3\_type11}_6, \text{axiom})$   
 $(p_4 \text{ and } p_5) \Rightarrow p_3 \quad \text{cnf}(\text{s3\_type11}_7, \text{axiom})$   
 $(q_4 \text{ and } q_5) \Rightarrow p_3 \quad \text{cnf}(\text{s3\_type11}_8, \text{axiom})$   
 $(p_1 \text{ and } q_2) \Rightarrow q_0 \quad \text{cnf}(\text{s3\_type12}_1, \text{axiom})$   
 $(q_1 \text{ and } p_2) \Rightarrow q_0 \quad \text{cnf}(\text{s3\_type12}_2, \text{axiom})$   
 $(p_2 \text{ and } q_3) \Rightarrow q_1 \quad \text{cnf}(\text{s3\_type12}_3, \text{axiom})$   
 $(q_2 \text{ and } p_3) \Rightarrow q_1 \quad \text{cnf}(\text{s3\_type12}_4, \text{axiom})$   
 $(p_3 \text{ and } q_4) \Rightarrow q_2 \quad \text{cnf}(\text{s3\_type12}_5, \text{axiom})$



$(q_3 \text{ and } p_4) \Rightarrow q_2 \quad \text{cnf}(s3\_type12_6, \text{axiom})$   
 $(p_4 \text{ and } q_5) \Rightarrow q_3 \quad \text{cnf}(s3\_type12_7, \text{axiom})$   
 $(q_4 \text{ and } p_5) \Rightarrow q_3 \quad \text{cnf}(s3\_type12_8, \text{axiom})$   
 $p_2 \Rightarrow p_5 \quad \text{cnf}(s3\_type2_1, \text{axiom})$   
 $p_3 \Rightarrow p_6 \quad \text{cnf}(s3\_type2_2, \text{axiom})$   
 $q_2 \Rightarrow q_5 \quad \text{cnf}(s3\_type2_3, \text{axiom})$   
 $q_3 \Rightarrow q_6 \quad \text{cnf}(s3\_type2_4, \text{axiom})$

**SYN088-1.010.p** Plaisted problem s(4,10)

$\neg p(a, a, a, a, a, a, a, a, a, a) \quad \text{cnf}(s4\_goal_1, \text{negated\_conjecture})$   
 $(q_1(x_1) \text{ and } q_2(x_2) \text{ and } q_3(x_3) \text{ and } q_4(x_4) \text{ and } q_5(x_5) \text{ and } q_6(x_6) \text{ and } q_7(x_7) \text{ and } q_8(x_8) \text{ and } q_9(x_9) \text{ and } q_{10}(x_{10})) \Rightarrow$   
 $p(x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8, x_9, x_{10}) \quad \text{cnf}(s4_1, \text{axiom})$   
 $q_1(a) \quad \text{cnf}(s4_2, \text{axiom})$   
 $q_1(b) \quad \text{cnf}(s4_3, \text{axiom})$   
 $q_2(a) \quad \text{cnf}(s4_4, \text{axiom})$   
 $q_2(b) \quad \text{cnf}(s4_5, \text{axiom})$   
 $q_3(a) \quad \text{cnf}(s4_6, \text{axiom})$   
 $q_3(b) \quad \text{cnf}(s4_7, \text{axiom})$   
 $q_4(a) \quad \text{cnf}(s4_8, \text{axiom})$   
 $q_4(b) \quad \text{cnf}(s4_9, \text{axiom})$   
 $q_5(a) \quad \text{cnf}(s4_{10}, \text{axiom})$   
 $q_5(b) \quad \text{cnf}(s4_{11}, \text{axiom})$   
 $q_6(a) \quad \text{cnf}(s4_{12}, \text{axiom})$   
 $q_6(b) \quad \text{cnf}(s4_{13}, \text{axiom})$   
 $q_7(a) \quad \text{cnf}(s4_{14}, \text{axiom})$   
 $q_7(b) \quad \text{cnf}(s4_{15}, \text{axiom})$   
 $q_8(a) \quad \text{cnf}(s4_{16}, \text{axiom})$   
 $q_8(b) \quad \text{cnf}(s4_{17}, \text{axiom})$   
 $q_9(a) \quad \text{cnf}(s4_{18}, \text{axiom})$   
 $q_9(b) \quad \text{cnf}(s4_{19}, \text{axiom})$   
 $q_{10}(a) \quad \text{cnf}(s4_{20}, \text{axiom})$   
 $q_{10}(b) \quad \text{cnf}(s4_{21}, \text{axiom})$

**SYN089-1.002.p** Plaisted problem t(2,2)

$\neg p_{1_2} \quad \text{cnf}(s2\_goal_1, \text{negated\_conjecture})$   
 $(p_{2_2} \text{ and } p_{1_1}) \Rightarrow p_{1_2} \quad \text{cnf}(s2\_type11_1, \text{axiom})$   
 $(q_{2_2} \text{ and } q_{1_1}) \Rightarrow p_{1_2} \quad \text{cnf}(s2\_type11_2, \text{axiom})$   
 $(p_{2_2} \text{ and } q_{1_1}) \Rightarrow q_{1_2} \quad \text{cnf}(s2\_type12_1, \text{axiom})$   
 $(q_{2_2} \text{ and } p_{1_1}) \Rightarrow q_{1_2} \quad \text{cnf}(s2\_type12_2, \text{axiom})$   
 $p_{1_2} \Rightarrow p_{1_1} \quad \text{cnf}(s2\_type21_1, \text{axiom})$   
 $q_{1_2} \Rightarrow q_{1_1} \quad \text{cnf}(s2\_type21_2, \text{axiom})$   
 $p_{1_2} \Rightarrow p_{2_2} \quad \text{cnf}(s2\_type22_1, \text{axiom})$   
 $q_{1_2} \Rightarrow q_{2_2} \quad \text{cnf}(s2\_type22_2, \text{axiom})$   
 $p_{1_1} \quad \text{cnf}(t2_1, \text{axiom})$   
 $q_{1_1} \quad \text{cnf}(t2_2, \text{axiom})$   
 $p_{2_2} \quad \text{cnf}(t2_3, \text{axiom})$   
 $q_{2_2} \quad \text{cnf}(t2_4, \text{axiom})$

**SYN091-1.003.p** Plaisted problem sym(s(2,3))

$\neg p_{1_3} \quad \text{cnf}(s2\_goal_1, \text{negated\_conjecture})$   
 $(p_{2_2} \text{ and } p_{1_1}) \Rightarrow p_{1_2} \quad \text{cnf}(s2\_type11_1, \text{axiom})$   
 $(q_{2_2} \text{ and } q_{1_1}) \Rightarrow p_{1_2} \quad \text{cnf}(s2\_type11_2, \text{axiom})$   
 $(p_{2_3} \text{ and } p_{1_2}) \Rightarrow p_{1_3} \quad \text{cnf}(s2\_type11_3, \text{axiom})$   
 $(q_{2_3} \text{ and } q_{1_2}) \Rightarrow p_{1_3} \quad \text{cnf}(s2\_type11_4, \text{axiom})$   
 $(p_{3_3} \text{ and } p_{2_2}) \Rightarrow p_{2_3} \quad \text{cnf}(s2\_type11_5, \text{axiom})$   
 $(q_{3_3} \text{ and } q_{2_2}) \Rightarrow p_{2_3} \quad \text{cnf}(s2\_type11_6, \text{axiom})$   
 $(p_{2_2} \text{ and } q_{1_1}) \Rightarrow q_{1_2} \quad \text{cnf}(s2\_type12_1, \text{axiom})$   
 $(q_{2_2} \text{ and } p_{1_1}) \Rightarrow q_{1_2} \quad \text{cnf}(s2\_type12_2, \text{axiom})$   
 $(p_{2_3} \text{ and } q_{1_2}) \Rightarrow q_{1_3} \quad \text{cnf}(s2\_type12_3, \text{axiom})$   
 $(q_{2_3} \text{ and } p_{1_2}) \Rightarrow q_{1_3} \quad \text{cnf}(s2\_type12_4, \text{axiom})$   
 $(p_{3_3} \text{ and } q_{2_2}) \Rightarrow q_{2_3} \quad \text{cnf}(s2\_type12_5, \text{axiom})$

$(q_3 \text{ and } p_2) \Rightarrow q_2$      $\text{cnf}(s2\_type12_6, \text{axiom})$   
 $p_1 \Rightarrow p_1$      $\text{cnf}(s2\_type21_1, \text{axiom})$   
 $q_1 \Rightarrow q_1$      $\text{cnf}(s2\_type21_2, \text{axiom})$   
 $p_1 \Rightarrow p_2$      $\text{cnf}(s2\_type22_1, \text{axiom})$   
 $p_2 \Rightarrow p_3$      $\text{cnf}(s2\_type22_2, \text{axiom})$   
 $q_1 \Rightarrow q_2$      $\text{cnf}(s2\_type22_3, \text{axiom})$   
 $q_2 \Rightarrow q_3$      $\text{cnf}(s2\_type22_4, \text{axiom})$   
 $\text{sym\_p}_1 \Rightarrow \text{sym\_p}_1$      $\text{cnf}(\text{sym\_s2\_goal}_1, \text{axiom})$   
 $\text{sym\_p}_1 \Rightarrow (\text{sym\_p}_2 \text{ or } \text{sym\_p}_1)$      $\text{cnf}(\text{sym\_s2\_type11}_1, \text{axiom})$   
 $\text{sym\_p}_1 \Rightarrow (\text{sym\_q}_2 \text{ or } \text{sym\_q}_1)$      $\text{cnf}(\text{sym\_s2\_type11}_2, \text{axiom})$   
 $\text{sym\_p}_1 \Rightarrow (\text{sym\_p}_3 \text{ or } \text{sym\_p}_1)$      $\text{cnf}(\text{sym\_s2\_type11}_3, \text{axiom})$   
 $\text{sym\_p}_1 \Rightarrow (\text{sym\_q}_3 \text{ or } \text{sym\_q}_1)$      $\text{cnf}(\text{sym\_s2\_type11}_4, \text{axiom})$   
 $\text{sym\_p}_2 \Rightarrow (\text{sym\_p}_3 \text{ or } \text{sym\_p}_2)$      $\text{cnf}(\text{sym\_s2\_type11}_5, \text{axiom})$   
 $\text{sym\_p}_2 \Rightarrow (\text{sym\_q}_3 \text{ or } \text{sym\_q}_2)$      $\text{cnf}(\text{sym\_s2\_type11}_6, \text{axiom})$   
 $\text{sym\_q}_1 \Rightarrow (\text{sym\_p}_2 \text{ or } \text{sym\_q}_1)$      $\text{cnf}(\text{sym\_s2\_type12}_1, \text{axiom})$   
 $\text{sym\_q}_1 \Rightarrow (\text{sym\_q}_2 \text{ or } \text{sym\_p}_1)$      $\text{cnf}(\text{sym\_s2\_type12}_2, \text{axiom})$   
 $\text{sym\_q}_1 \Rightarrow (\text{sym\_p}_3 \text{ or } \text{sym\_q}_1)$      $\text{cnf}(\text{sym\_s2\_type12}_3, \text{axiom})$   
 $\text{sym\_q}_1 \Rightarrow (\text{sym\_q}_3 \text{ or } \text{sym\_p}_1)$      $\text{cnf}(\text{sym\_s2\_type12}_4, \text{axiom})$   
 $\text{sym\_q}_2 \Rightarrow (\text{sym\_p}_3 \text{ or } \text{sym\_q}_2)$      $\text{cnf}(\text{sym\_s2\_type12}_5, \text{axiom})$   
 $\text{sym\_q}_2 \Rightarrow (\text{sym\_q}_3 \text{ or } \text{sym\_p}_2)$      $\text{cnf}(\text{sym\_s2\_type12}_6, \text{axiom})$   
 $\text{sym\_p}_1 \Rightarrow \text{sym\_p}_1$      $\text{cnf}(\text{sym\_s2\_type21}_1, \text{axiom})$   
 $\text{sym\_q}_1 \Rightarrow \text{sym\_q}_1$      $\text{cnf}(\text{sym\_s2\_type21}_2, \text{axiom})$   
 $\text{sym\_p}_2 \Rightarrow \text{sym\_p}_1$      $\text{cnf}(\text{sym\_s2\_type22}_1, \text{axiom})$   
 $\text{sym\_p}_3 \Rightarrow \text{sym\_p}_2$      $\text{cnf}(\text{sym\_s2\_type22}_2, \text{axiom})$   
 $\text{sym\_q}_2 \Rightarrow \text{sym\_q}_1$      $\text{cnf}(\text{sym\_s2\_type22}_3, \text{axiom})$   
 $\text{sym\_q}_3 \Rightarrow \text{sym\_q}_2$      $\text{cnf}(\text{sym\_s2\_type22}_4, \text{axiom})$

**SYN092-1.003.p** Plaisted problem  $\text{sym}(s(3,3))$

$p_0 \Rightarrow \neg q_0$      $\text{cnf}(s3\_goal_1, \text{negated\_conjecture})$   
 $(p_1 \text{ and } p_2) \Rightarrow p_0$      $\text{cnf}(s3\_type11_1, \text{axiom})$   
 $(q_1 \text{ and } q_2) \Rightarrow p_0$      $\text{cnf}(s3\_type11_2, \text{axiom})$   
 $(p_2 \text{ and } p_3) \Rightarrow p_1$      $\text{cnf}(s3\_type11_3, \text{axiom})$   
 $(q_2 \text{ and } q_3) \Rightarrow p_1$      $\text{cnf}(s3\_type11_4, \text{axiom})$   
 $(p_3 \text{ and } p_4) \Rightarrow p_2$      $\text{cnf}(s3\_type11_5, \text{axiom})$   
 $(q_3 \text{ and } q_4) \Rightarrow p_2$      $\text{cnf}(s3\_type11_6, \text{axiom})$   
 $(p_4 \text{ and } p_5) \Rightarrow p_3$      $\text{cnf}(s3\_type11_7, \text{axiom})$   
 $(q_4 \text{ and } q_5) \Rightarrow p_3$      $\text{cnf}(s3\_type11_8, \text{axiom})$   
 $(p_1 \text{ and } q_2) \Rightarrow q_0$      $\text{cnf}(s3\_type12_1, \text{axiom})$   
 $(q_1 \text{ and } p_2) \Rightarrow q_0$      $\text{cnf}(s3\_type12_2, \text{axiom})$   
 $(p_2 \text{ and } q_3) \Rightarrow q_1$      $\text{cnf}(s3\_type12_3, \text{axiom})$   
 $(q_2 \text{ and } p_3) \Rightarrow q_1$      $\text{cnf}(s3\_type12_4, \text{axiom})$   
 $(p_3 \text{ and } q_4) \Rightarrow q_2$      $\text{cnf}(s3\_type12_5, \text{axiom})$   
 $(q_3 \text{ and } p_4) \Rightarrow q_2$      $\text{cnf}(s3\_type12_6, \text{axiom})$   
 $(p_4 \text{ and } q_5) \Rightarrow q_3$      $\text{cnf}(s3\_type12_7, \text{axiom})$   
 $(q_4 \text{ and } p_5) \Rightarrow q_3$      $\text{cnf}(s3\_type12_8, \text{axiom})$   
 $p_2 \Rightarrow p_5$      $\text{cnf}(s3\_type2_1, \text{axiom})$   
 $p_3 \Rightarrow p_6$      $\text{cnf}(s3\_type2_2, \text{axiom})$   
 $q_2 \Rightarrow q_5$      $\text{cnf}(s3\_type2_3, \text{axiom})$   
 $q_3 \Rightarrow q_6$      $\text{cnf}(s3\_type2_4, \text{axiom})$   
 $\text{sym\_p}_0 \text{ or } \text{sym\_q}_0$      $\text{cnf}(\text{sym\_s3\_goal}_1, \text{axiom})$   
 $\text{sym\_p}_0 \Rightarrow (\text{sym\_p}_1 \text{ or } \text{sym\_p}_2)$      $\text{cnf}(\text{sym\_s3\_type11}_1, \text{axiom})$   
 $\text{sym\_p}_0 \Rightarrow (\text{sym\_q}_1 \text{ or } \text{sym\_q}_2)$      $\text{cnf}(\text{sym\_s3\_type11}_2, \text{axiom})$   
 $\text{sym\_p}_1 \Rightarrow (\text{sym\_p}_2 \text{ or } \text{sym\_p}_3)$      $\text{cnf}(\text{sym\_s3\_type11}_3, \text{axiom})$   
 $\text{sym\_p}_1 \Rightarrow (\text{sym\_q}_2 \text{ or } \text{sym\_q}_3)$      $\text{cnf}(\text{sym\_s3\_type11}_4, \text{axiom})$   
 $\text{sym\_p}_2 \Rightarrow (\text{sym\_p}_3 \text{ or } \text{sym\_p}_4)$      $\text{cnf}(\text{sym\_s3\_type11}_5, \text{axiom})$   
 $\text{sym\_p}_2 \Rightarrow (\text{sym\_q}_3 \text{ or } \text{sym\_q}_4)$      $\text{cnf}(\text{sym\_s3\_type11}_6, \text{axiom})$   
 $\text{sym\_p}_3 \Rightarrow (\text{sym\_p}_4 \text{ or } \text{sym\_p}_5)$      $\text{cnf}(\text{sym\_s3\_type11}_7, \text{axiom})$   
 $\text{sym\_p}_3 \Rightarrow (\text{sym\_q}_4 \text{ or } \text{sym\_q}_5)$      $\text{cnf}(\text{sym\_s3\_type11}_8, \text{axiom})$   
 $\text{sym\_q}_0 \Rightarrow (\text{sym\_p}_1 \text{ or } \text{sym\_q}_2)$      $\text{cnf}(\text{sym\_s3\_type12}_1, \text{axiom})$   
 $\text{sym\_q}_0 \Rightarrow (\text{sym\_q}_1 \text{ or } \text{sym\_p}_2)$      $\text{cnf}(\text{sym\_s3\_type12}_2, \text{axiom})$

$\text{sym\_q}_1 \Rightarrow (\text{sym\_p}_2 \text{ or } \text{sym\_q}_3) \quad \text{cnf}(\text{sym\_s3\_type12}_3, \text{axiom})$   
 $\text{sym\_q}_1 \Rightarrow (\text{sym\_q}_2 \text{ or } \text{sym\_p}_3) \quad \text{cnf}(\text{sym\_s3\_type12}_4, \text{axiom})$   
 $\text{sym\_q}_2 \Rightarrow (\text{sym\_p}_3 \text{ or } \text{sym\_q}_4) \quad \text{cnf}(\text{sym\_s3\_type12}_5, \text{axiom})$   
 $\text{sym\_q}_2 \Rightarrow (\text{sym\_q}_3 \text{ or } \text{sym\_p}_4) \quad \text{cnf}(\text{sym\_s3\_type12}_6, \text{axiom})$   
 $\text{sym\_q}_3 \Rightarrow (\text{sym\_p}_4 \text{ or } \text{sym\_q}_5) \quad \text{cnf}(\text{sym\_s3\_type12}_7, \text{axiom})$   
 $\text{sym\_q}_3 \Rightarrow (\text{sym\_q}_4 \text{ or } \text{sym\_p}_5) \quad \text{cnf}(\text{sym\_s3\_type12}_8, \text{axiom})$   
 $\text{sym\_p}_5 \Rightarrow \text{sym\_p}_2 \quad \text{cnf}(\text{sym\_s3\_type2}_1, \text{axiom})$   
 $\text{sym\_p}_6 \Rightarrow \text{sym\_p}_3 \quad \text{cnf}(\text{sym\_s3\_type2}_2, \text{axiom})$   
 $\text{sym\_q}_5 \Rightarrow \text{sym\_q}_2 \quad \text{cnf}(\text{sym\_s3\_type2}_3, \text{axiom})$   
 $\text{sym\_q}_6 \Rightarrow \text{sym\_q}_3 \quad \text{cnf}(\text{sym\_s3\_type2}_4, \text{axiom})$

**SYN093-1.002.p** Plaisted problem  $u(t(2,2))$

$p_{-1_2} \Rightarrow u_1 \quad \text{cnf}(u_{s2\_goal}_1, \text{negated\_conjecture})$   
 $\neg u_1 \quad \text{cnf}(u_{1\_s2\_goal}_1, \text{axiom})$   
 $(p_{2_2} \text{ and } p_{1_1}) \Rightarrow (u_2 \text{ or } p_{-1_2}) \quad \text{cnf}(u_{s2\_type11}_1, \text{axiom})$   
 $u_2 \Rightarrow p_{-1_2} \quad \text{cnf}(u_{2\_s2\_type11}_1, \text{axiom})$   
 $(q_{2_2} \text{ and } q_{1_1}) \Rightarrow (u_3 \text{ or } p_{-1_2}) \quad \text{cnf}(u_{s2\_type11}_2, \text{axiom})$   
 $u_3 \Rightarrow p_{-1_2} \quad \text{cnf}(u_{3\_s2\_type11}_2, \text{axiom})$   
 $(p_{2_2} \text{ and } q_{1_1}) \Rightarrow (u_4 \text{ or } q_{-1_2}) \quad \text{cnf}(u_{s2\_type12}_1, \text{axiom})$   
 $u_4 \Rightarrow q_{-1_2} \quad \text{cnf}(u_{4\_s2\_type12}_1, \text{axiom})$   
 $(q_{2_2} \text{ and } p_{1_1}) \Rightarrow (u_5 \text{ or } q_{-1_2}) \quad \text{cnf}(u_{s2\_type12}_2, \text{axiom})$   
 $u_5 \Rightarrow q_{-1_2} \quad \text{cnf}(u_{5\_s2\_type12}_2, \text{axiom})$   
 $p_{-1_2} \Rightarrow (u_6 \text{ or } p_{-1_1}) \quad \text{cnf}(u_{s2\_type21}_1, \text{axiom})$   
 $u_6 \Rightarrow p_{-1_1} \quad \text{cnf}(u_{6\_s2\_type21}_1, \text{axiom})$   
 $q_{-1_2} \Rightarrow (u_7 \text{ or } q_{-1_1}) \quad \text{cnf}(u_{s2\_type21}_2, \text{axiom})$   
 $u_7 \Rightarrow q_{-1_1} \quad \text{cnf}(u_{7\_s2\_type21}_2, \text{axiom})$   
 $p_{-1_2} \Rightarrow (u_8 \text{ or } p_{-2_2}) \quad \text{cnf}(u_{s2\_type22}_1, \text{axiom})$   
 $u_8 \Rightarrow p_{-2_2} \quad \text{cnf}(u_{8\_s2\_type22}_1, \text{axiom})$   
 $q_{-1_2} \Rightarrow (u_9 \text{ or } q_{-2_2}) \quad \text{cnf}(u_{s2\_type22}_2, \text{axiom})$   
 $u_9 \Rightarrow q_{-2_2} \quad \text{cnf}(u_{9\_s2\_type22}_2, \text{axiom})$   
 $u_{10} \text{ or } p_{-1_1} \quad \text{cnf}(u_{t2}_1, \text{axiom})$   
 $u_{10} \Rightarrow p_{-1_1} \quad \text{cnf}(u_{10\_t2}_1, \text{axiom})$   
 $u_{11} \text{ or } q_{-1_1} \quad \text{cnf}(u_{t2}_2, \text{axiom})$   
 $u_{11} \Rightarrow q_{-1_1} \quad \text{cnf}(u_{11\_t2}_2, \text{axiom})$   
 $u_{12} \text{ or } p_{-2_2} \quad \text{cnf}(u_{t2}_3, \text{axiom})$   
 $u_{12} \Rightarrow p_{-2_2} \quad \text{cnf}(u_{12\_t2}_3, \text{axiom})$   
 $u_{13} \text{ or } q_{-2_2} \quad \text{cnf}(u_{t2}_4, \text{axiom})$   
 $u_{13} \Rightarrow q_{-2_2} \quad \text{cnf}(u_{13\_t2}_4, \text{axiom})$

**SYN095-1.002.p** Plaisted problem  $m(t(2,2))$

$\neg p_{-1_2}(x) \quad \text{cnf}(m_{s2\_goal}_1, \text{negated\_conjecture})$   
 $(p_{2_2}(x) \text{ and } p_{1_1}(x)) \Rightarrow p_{-1_2}(x) \quad \text{cnf}(m_{s2\_type11}_1, \text{axiom})$   
 $(q_{2_2}(x) \text{ and } q_{1_1}(x)) \Rightarrow p_{-1_2}(x) \quad \text{cnf}(m_{s2\_type11}_2, \text{axiom})$   
 $(p_{2_2}(x) \text{ and } q_{1_1}(x)) \Rightarrow q_{-1_2}(x) \quad \text{cnf}(m_{s2\_type12}_1, \text{axiom})$   
 $(q_{2_2}(x) \text{ and } p_{1_1}(x)) \Rightarrow q_{-1_2}(x) \quad \text{cnf}(m_{s2\_type12}_2, \text{axiom})$   
 $p_{-1_2}(x) \Rightarrow p_{-1_1}(x) \quad \text{cnf}(m_{s2\_type21}_1, \text{axiom})$   
 $q_{-1_2}(x) \Rightarrow q_{-1_1}(x) \quad \text{cnf}(m_{s2\_type21}_2, \text{axiom})$   
 $p_{-1_2}(x) \Rightarrow p_{-2_2}(x) \quad \text{cnf}(m_{s2\_type22}_1, \text{axiom})$   
 $q_{-1_2}(x) \Rightarrow q_{-2_2}(x) \quad \text{cnf}(m_{s2\_type22}_2, \text{axiom})$   
 $p_{-1_1}(a) \quad \text{cnf}(m_{t2}_1, \text{axiom})$   
 $q_{-1_1}(a) \quad \text{cnf}(m_{t2}_2, \text{axiom})$   
 $p_{-2_2}(a) \quad \text{cnf}(m_{t2}_3, \text{axiom})$   
 $q_{-2_2}(a) \quad \text{cnf}(m_{t2}_4, \text{axiom})$

**SYN097-1.002.p** Plaisted problem  $\text{sym}(u(t(2,2)))$

$p_{-1_2} \Rightarrow u_1 \quad \text{cnf}(u_{s2\_goal}_1, \text{negated\_conjecture})$   
 $\neg u_1 \quad \text{cnf}(u_{1\_s2\_goal}_1, \text{axiom})$   
 $(p_{2_2} \text{ and } p_{1_1}) \Rightarrow (u_2 \text{ or } p_{-1_2}) \quad \text{cnf}(u_{s2\_type11}_1, \text{axiom})$   
 $u_2 \Rightarrow p_{-1_2} \quad \text{cnf}(u_{2\_s2\_type11}_1, \text{axiom})$   
 $(q_{2_2} \text{ and } q_{1_1}) \Rightarrow (u_3 \text{ or } p_{-1_2}) \quad \text{cnf}(u_{s2\_type11}_2, \text{axiom})$   
 $u_3 \Rightarrow p_{-1_2} \quad \text{cnf}(u_{3\_s2\_type11}_2, \text{axiom})$

$(p.2_2 \text{ and } q.1_1) \Rightarrow (u_4 \text{ or } q.1_2) \quad \text{cnf}(u.s2\_type12_1, \text{axiom})$   
 $u_4 \Rightarrow q.1_2 \quad \text{cnf}(u.4.s2\_type12_1, \text{axiom})$   
 $(q.2_2 \text{ and } p.1_1) \Rightarrow (u_5 \text{ or } q.1_2) \quad \text{cnf}(u.s2\_type12_2, \text{axiom})$   
 $u_5 \Rightarrow q.1_2 \quad \text{cnf}(u.5.s2\_type12_2, \text{axiom})$   
 $p.1_2 \Rightarrow (u_6 \text{ or } p.1_1) \quad \text{cnf}(u.s2\_type21_1, \text{axiom})$   
 $u_6 \Rightarrow p.1_1 \quad \text{cnf}(u.6.s2\_type21_1, \text{axiom})$   
 $q.1_2 \Rightarrow (u_7 \text{ or } q.1_1) \quad \text{cnf}(u.s2\_type21_2, \text{axiom})$   
 $u_7 \Rightarrow q.1_1 \quad \text{cnf}(u.7.s2\_type21_2, \text{axiom})$   
 $p.1_2 \Rightarrow (u_8 \text{ or } p.2_2) \quad \text{cnf}(u.s2\_type22_1, \text{axiom})$   
 $u_8 \Rightarrow p.2_2 \quad \text{cnf}(u.8.s2\_type22_1, \text{axiom})$   
 $q.1_2 \Rightarrow (u_9 \text{ or } q.2_2) \quad \text{cnf}(u.s2\_type22_2, \text{axiom})$   
 $u_9 \Rightarrow q.2_2 \quad \text{cnf}(u.9.s2\_type22_2, \text{axiom})$   
 $u_{10} \text{ or } p.1_1 \quad \text{cnf}(u.t2_1, \text{axiom})$   
 $u_{10} \Rightarrow p.1_1 \quad \text{cnf}(u.10.t2_1, \text{axiom})$   
 $u_{11} \text{ or } q.1_1 \quad \text{cnf}(u.t2_2, \text{axiom})$   
 $u_{11} \Rightarrow q.1_1 \quad \text{cnf}(u.11.t2_2, \text{axiom})$   
 $u_{12} \text{ or } p.2_2 \quad \text{cnf}(u.t2_3, \text{axiom})$   
 $u_{12} \Rightarrow p.2_2 \quad \text{cnf}(u.12.t2_3, \text{axiom})$   
 $u_{13} \text{ or } q.2_2 \quad \text{cnf}(u.t2_4, \text{axiom})$   
 $u_{13} \Rightarrow q.2_2 \quad \text{cnf}(u.13.t2_4, \text{axiom})$   
 $\text{sym}.u_1 \Rightarrow \text{sym}.p.1_2 \quad \text{cnf}(\text{sym}.u.s2\_goal_1, \text{axiom})$   
 $\text{sym}.u_1 \quad \text{cnf}(\text{sym}.u.1.s2\_goal_1, \text{axiom})$   
 $(\text{sym}.u_2 \text{ and } \text{sym}.p.1_2) \Rightarrow (\text{sym}.p.2_2 \text{ or } \text{sym}.p.1_1) \quad \text{cnf}(\text{sym}.u.s2\_type11_1, \text{axiom})$   
 $\text{sym}.p.1_2 \Rightarrow \text{sym}.u_2 \quad \text{cnf}(\text{sym}.u.2.s2\_type11_1, \text{axiom})$   
 $(\text{sym}.u_3 \text{ and } \text{sym}.p.1_2) \Rightarrow (\text{sym}.q.2_2 \text{ or } \text{sym}.q.1_1) \quad \text{cnf}(\text{sym}.u.s2\_type11_2, \text{axiom})$   
 $\text{sym}.p.1_2 \Rightarrow \text{sym}.u_3 \quad \text{cnf}(\text{sym}.u.3.s2\_type11_2, \text{axiom})$   
 $(\text{sym}.u_4 \text{ and } \text{sym}.q.1_2) \Rightarrow (\text{sym}.p.2_2 \text{ or } \text{sym}.q.1_1) \quad \text{cnf}(\text{sym}.u.s2\_type12_1, \text{axiom})$   
 $\text{sym}.q.1_2 \Rightarrow \text{sym}.u_4 \quad \text{cnf}(\text{sym}.u.4.s2\_type12_1, \text{axiom})$   
 $(\text{sym}.u_5 \text{ and } \text{sym}.q.1_2) \Rightarrow (\text{sym}.q.2_2 \text{ or } \text{sym}.p.1_1) \quad \text{cnf}(\text{sym}.u.s2\_type12_2, \text{axiom})$   
 $\text{sym}.q.1_2 \Rightarrow \text{sym}.u_5 \quad \text{cnf}(\text{sym}.u.5.s2\_type12_2, \text{axiom})$   
 $(\text{sym}.u_6 \text{ and } \text{sym}.p.1_1) \Rightarrow \text{sym}.p.1_2 \quad \text{cnf}(\text{sym}.u.s2\_type21_1, \text{axiom})$   
 $\text{sym}.p.1_1 \Rightarrow \text{sym}.u_6 \quad \text{cnf}(\text{sym}.u.6.s2\_type21_1, \text{axiom})$   
 $(\text{sym}.u_7 \text{ and } \text{sym}.q.1_1) \Rightarrow \text{sym}.q.1_2 \quad \text{cnf}(\text{sym}.u.s2\_type21_2, \text{axiom})$   
 $\text{sym}.q.1_1 \Rightarrow \text{sym}.u_7 \quad \text{cnf}(\text{sym}.u.7.s2\_type21_2, \text{axiom})$   
 $(\text{sym}.u_8 \text{ and } \text{sym}.p.2_2) \Rightarrow \text{sym}.p.1_2 \quad \text{cnf}(\text{sym}.u.s2\_type22_1, \text{axiom})$   
 $\text{sym}.p.2_2 \Rightarrow \text{sym}.u_8 \quad \text{cnf}(\text{sym}.u.8.s2\_type22_1, \text{axiom})$   
 $(\text{sym}.u_9 \text{ and } \text{sym}.q.2_2) \Rightarrow \text{sym}.q.1_2 \quad \text{cnf}(\text{sym}.u.s2\_type22_2, \text{axiom})$   
 $\text{sym}.q.2_2 \Rightarrow \text{sym}.u_9 \quad \text{cnf}(\text{sym}.u.9.s2\_type22_2, \text{axiom})$   
 $\text{sym}.u_{10} \Rightarrow \neg \text{sym}.p.1_1 \quad \text{cnf}(\text{sym}.u.t2_1, \text{axiom})$   
 $\text{sym}.p.1_1 \Rightarrow \text{sym}.u_{10} \quad \text{cnf}(\text{sym}.u.10.t2_1, \text{axiom})$   
 $\text{sym}.u_{11} \Rightarrow \neg \text{sym}.q.1_1 \quad \text{cnf}(\text{sym}.u.t2_2, \text{axiom})$   
 $\text{sym}.q.1_1 \Rightarrow \text{sym}.u_{11} \quad \text{cnf}(\text{sym}.u.11.t2_2, \text{axiom})$   
 $\text{sym}.u_{12} \Rightarrow \neg \text{sym}.p.2_2 \quad \text{cnf}(\text{sym}.u.t2_3, \text{axiom})$   
 $\text{sym}.p.2_2 \Rightarrow \text{sym}.u_{12} \quad \text{cnf}(\text{sym}.u.12.t2_3, \text{axiom})$   
 $\text{sym}.u_{13} \Rightarrow \neg \text{sym}.q.2_2 \quad \text{cnf}(\text{sym}.u.t2_4, \text{axiom})$   
 $\text{sym}.q.2_2 \Rightarrow \text{sym}.u_{13} \quad \text{cnf}(\text{sym}.u.13.t2_4, \text{axiom})$

**SYN099-1.003.p** Plaisted problem  $\text{sym}(m(t(2,3)))$

$\neg p.1_3(x) \quad \text{cnf}(m.s2\_goal_1, \text{negated\_conjecture})$   
 $(p.2_2(x) \text{ and } p.1_1(x)) \Rightarrow p.1_2(x) \quad \text{cnf}(m.s2\_type11_1, \text{axiom})$   
 $(q.2_2(x) \text{ and } q.1_1(x)) \Rightarrow p.1_2(x) \quad \text{cnf}(m.s2\_type11_2, \text{axiom})$   
 $(p.2_3(x) \text{ and } p.1_2(x)) \Rightarrow p.1_3(x) \quad \text{cnf}(m.s2\_type11_3, \text{axiom})$   
 $(q.2_3(x) \text{ and } q.1_2(x)) \Rightarrow p.1_3(x) \quad \text{cnf}(m.s2\_type11_4, \text{axiom})$   
 $(p.3_3(x) \text{ and } p.2_2(x)) \Rightarrow p.2_3(x) \quad \text{cnf}(m.s2\_type11_5, \text{axiom})$   
 $(q.3_3(x) \text{ and } q.2_2(x)) \Rightarrow p.2_3(x) \quad \text{cnf}(m.s2\_type11_6, \text{axiom})$   
 $(p.2_2(x) \text{ and } q.1_1(x)) \Rightarrow q.1_2(x) \quad \text{cnf}(m.s2\_type12_1, \text{axiom})$   
 $(q.2_2(x) \text{ and } p.1_1(x)) \Rightarrow q.1_2(x) \quad \text{cnf}(m.s2\_type12_2, \text{axiom})$   
 $(p.2_3(x) \text{ and } q.1_2(x)) \Rightarrow q.1_3(x) \quad \text{cnf}(m.s2\_type12_3, \text{axiom})$   
 $(q.2_3(x) \text{ and } p.1_2(x)) \Rightarrow q.1_3(x) \quad \text{cnf}(m.s2\_type12_4, \text{axiom})$   
 $(p.3_3(x) \text{ and } q.2_2(x)) \Rightarrow q.2_3(x) \quad \text{cnf}(m.s2\_type12_5, \text{axiom})$

$(q_3(x) \text{ and } p_2(x)) \Rightarrow q_2(x)$      $\text{cnf}(\text{m\_s2\_type12}_6, \text{axiom})$   
 $p_1(x) \Rightarrow p_2(x)$      $\text{cnf}(\text{m\_s2\_type21}_1, \text{axiom})$   
 $q_1(x) \Rightarrow q_2(x)$      $\text{cnf}(\text{m\_s2\_type21}_2, \text{axiom})$   
 $p_2(x) \Rightarrow p_3(x)$      $\text{cnf}(\text{m\_s2\_type22}_1, \text{axiom})$   
 $p_3(x) \Rightarrow p_4(x)$      $\text{cnf}(\text{m\_s2\_type22}_2, \text{axiom})$   
 $q_2(x) \Rightarrow q_3(x)$      $\text{cnf}(\text{m\_s2\_type22}_3, \text{axiom})$   
 $q_3(x) \Rightarrow q_4(x)$      $\text{cnf}(\text{m\_s2\_type22}_4, \text{axiom})$   
 $p_1(a)$      $\text{cnf}(\text{m\_t2}_1, \text{axiom})$   
 $q_1(a)$      $\text{cnf}(\text{m\_t2}_2, \text{axiom})$   
 $p_2(a)$      $\text{cnf}(\text{m\_t2}_3, \text{axiom})$   
 $q_2(a)$      $\text{cnf}(\text{m\_t2}_4, \text{axiom})$   
 $p_3(a)$      $\text{cnf}(\text{m\_t2}_5, \text{axiom})$   
 $q_3(a)$      $\text{cnf}(\text{m\_t2}_6, \text{axiom})$   
 $\text{sym\_p\_1}_3(x)$      $\text{cnf}(\text{sym\_m\_s2\_goal}_1, \text{axiom})$   
 $\text{sym\_p\_1}_2(x) \Rightarrow (\text{sym\_p\_2}_2(x) \text{ or } \text{sym\_p\_1}_1(x))$      $\text{cnf}(\text{sym\_m\_s2\_type11}_1, \text{axiom})$   
 $\text{sym\_p\_1}_2(x) \Rightarrow (\text{sym\_q\_2}_2(x) \text{ or } \text{sym\_q\_1}_1(x))$      $\text{cnf}(\text{sym\_m\_s2\_type11}_2, \text{axiom})$   
 $\text{sym\_p\_1}_3(x) \Rightarrow (\text{sym\_p\_2}_3(x) \text{ or } \text{sym\_p\_1}_2(x))$      $\text{cnf}(\text{sym\_m\_s2\_type11}_3, \text{axiom})$   
 $\text{sym\_p\_1}_3(x) \Rightarrow (\text{sym\_q\_2}_3(x) \text{ or } \text{sym\_q\_1}_2(x))$      $\text{cnf}(\text{sym\_m\_s2\_type11}_4, \text{axiom})$   
 $\text{sym\_p\_2}_3(x) \Rightarrow (\text{sym\_p\_3}_3(x) \text{ or } \text{sym\_p\_2}_2(x))$      $\text{cnf}(\text{sym\_m\_s2\_type11}_5, \text{axiom})$   
 $\text{sym\_p\_2}_3(x) \Rightarrow (\text{sym\_q\_3}_3(x) \text{ or } \text{sym\_q\_2}_2(x))$      $\text{cnf}(\text{sym\_m\_s2\_type11}_6, \text{axiom})$   
 $\text{sym\_q\_1}_2(x) \Rightarrow (\text{sym\_p\_2}_2(x) \text{ or } \text{sym\_q\_1}_1(x))$      $\text{cnf}(\text{sym\_m\_s2\_type12}_1, \text{axiom})$   
 $\text{sym\_q\_1}_2(x) \Rightarrow (\text{sym\_q\_2}_2(x) \text{ or } \text{sym\_p\_1}_1(x))$      $\text{cnf}(\text{sym\_m\_s2\_type12}_2, \text{axiom})$   
 $\text{sym\_q\_1}_3(x) \Rightarrow (\text{sym\_p\_2}_3(x) \text{ or } \text{sym\_q\_1}_2(x))$      $\text{cnf}(\text{sym\_m\_s2\_type12}_3, \text{axiom})$   
 $\text{sym\_q\_1}_3(x) \Rightarrow (\text{sym\_q\_2}_3(x) \text{ or } \text{sym\_p\_1}_2(x))$      $\text{cnf}(\text{sym\_m\_s2\_type12}_4, \text{axiom})$   
 $\text{sym\_q\_2}_3(x) \Rightarrow (\text{sym\_p\_3}_3(x) \text{ or } \text{sym\_q\_2}_2(x))$      $\text{cnf}(\text{sym\_m\_s2\_type12}_5, \text{axiom})$   
 $\text{sym\_q\_2}_3(x) \Rightarrow (\text{sym\_q\_3}_3(x) \text{ or } \text{sym\_p\_2}_2(x))$      $\text{cnf}(\text{sym\_m\_s2\_type12}_6, \text{axiom})$   
 $\text{sym\_p\_1}_1(x) \Rightarrow \text{sym\_p\_1}_2(x)$      $\text{cnf}(\text{sym\_m\_s2\_type21}_1, \text{axiom})$   
 $\text{sym\_q\_1}_1(x) \Rightarrow \text{sym\_q\_1}_2(x)$      $\text{cnf}(\text{sym\_m\_s2\_type21}_2, \text{axiom})$   
 $\text{sym\_p\_2}_2(x) \Rightarrow \text{sym\_p\_1}_2(x)$      $\text{cnf}(\text{sym\_m\_s2\_type22}_1, \text{axiom})$   
 $\text{sym\_p\_3}_3(x) \Rightarrow \text{sym\_p\_2}_3(x)$      $\text{cnf}(\text{sym\_m\_s2\_type22}_2, \text{axiom})$   
 $\text{sym\_q\_2}_2(x) \Rightarrow \text{sym\_q\_1}_2(x)$      $\text{cnf}(\text{sym\_m\_s2\_type22}_3, \text{axiom})$   
 $\text{sym\_q\_3}_3(x) \Rightarrow \text{sym\_q\_2}_3(x)$      $\text{cnf}(\text{sym\_m\_s2\_type22}_4, \text{axiom})$   
 $\neg \text{sym\_p\_1}_1(a)$      $\text{cnf}(\text{sym\_m\_t2}_1, \text{axiom})$   
 $\neg \text{sym\_q\_1}_1(a)$      $\text{cnf}(\text{sym\_m\_t2}_2, \text{axiom})$   
 $\neg \text{sym\_p\_2}_2(a)$      $\text{cnf}(\text{sym\_m\_t2}_3, \text{axiom})$   
 $\neg \text{sym\_q\_2}_2(a)$      $\text{cnf}(\text{sym\_m\_t2}_4, \text{axiom})$   
 $\neg \text{sym\_p\_3}_3(a)$      $\text{cnf}(\text{sym\_m\_t2}_5, \text{axiom})$   
 $\neg \text{sym\_q\_3}_3(a)$      $\text{cnf}(\text{sym\_m\_t2}_6, \text{axiom})$

**SYN101-1.002.002.p** Plaisted problem  $n(t(2,2),2)$

$\neg p_1(a, a)$      $\text{cnf}(\text{n\_s2\_goal}_1, \text{negated\_conjecture})$   
 $(p_2(x_1, x_2) \text{ and } p_1(x_1, x_2)) \Rightarrow p_2(x_1, x_2)$      $\text{cnf}(\text{n\_s2\_type11}_1, \text{axiom})$   
 $(q_2(x_1, x_2) \text{ and } q_1(x_1, x_2)) \Rightarrow p_2(x_1, x_2)$      $\text{cnf}(\text{n\_s2\_type11}_2, \text{axiom})$   
 $(p_2(x_1, x_2) \text{ and } q_1(x_1, x_2)) \Rightarrow q_2(x_1, x_2)$      $\text{cnf}(\text{n\_s2\_type12}_1, \text{axiom})$   
 $(q_2(x_1, x_2) \text{ and } p_1(x_1, x_2)) \Rightarrow q_2(x_1, x_2)$      $\text{cnf}(\text{n\_s2\_type12}_2, \text{axiom})$   
 $p_1(x_1, x_2) \Rightarrow p_2(x_1, x_2)$      $\text{cnf}(\text{n\_s2\_type21}_1, \text{axiom})$   
 $q_1(x_1, x_2) \Rightarrow q_2(x_1, x_2)$      $\text{cnf}(\text{n\_s2\_type21}_2, \text{axiom})$   
 $p_2(x_1, x_2) \Rightarrow p_3(x_1, x_2)$      $\text{cnf}(\text{n\_s2\_type22}_1, \text{axiom})$   
 $q_2(x_1, x_2) \Rightarrow q_3(x_1, x_2)$      $\text{cnf}(\text{n\_s2\_type22}_2, \text{axiom})$   
 $(nq_1(x_1) \text{ and } nq_2(x_2)) \Rightarrow p_1(x_1, x_2)$      $\text{cnf}(\text{n\_t2}_1, \text{axiom})$   
 $(nq_1(x_1) \text{ and } nq_2(x_2)) \Rightarrow q_1(x_1, x_2)$      $\text{cnf}(\text{n\_t2}_2, \text{axiom})$   
 $(nq_1(x_1) \text{ and } nq_2(x_2)) \Rightarrow p_2(x_1, x_2)$      $\text{cnf}(\text{n\_t2}_3, \text{axiom})$   
 $(nq_1(x_1) \text{ and } nq_2(x_2)) \Rightarrow q_2(x_1, x_2)$      $\text{cnf}(\text{n\_t2}_4, \text{axiom})$   
 $nq_1(a)$      $\text{cnf}(n_1, \text{axiom})$   
 $nq_1(b)$      $\text{cnf}(n_2, \text{axiom})$   
 $nq_2(a)$      $\text{cnf}(n_3, \text{axiom})$   
 $nq_2(b)$      $\text{cnf}(n_4, \text{axiom})$

**SYN103-1.p** RPT63 synthetic problem 1 (quasi-uniform distribution)

include('Axioms/SYN001-0.ax')

$\neg k_0(b)$     `cnf(prove_this, negated_conjecture)`  
**SYN104-1.p** RPT63 synthetic problem 2 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg k_0(e)$     `cnf(prove_this, negated_conjecture)`  
**SYN105-1.p** RPT63 synthetic problem 3 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg k_1(b)$     `cnf(prove_this, negated_conjecture)`  
**SYN106-1.p** RPT63 synthetic problem 4 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg k_1(e)$     `cnf(prove_this, negated_conjecture)`  
**SYN107-1.p** RPT63 synthetic problem 5 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg k_2(x, d)$     `cnf(prove_this, negated_conjecture)`  
**SYN108-1.p** RPT63 synthetic problem 6 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg k_2(a, x)$     `cnf(prove_this, negated_conjecture)`  
**SYN109-1.p** RPT63 synthetic problem 7 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg k_2(b, c)$     `cnf(prove_this, negated_conjecture)`  
**SYN110-1.p** RPT63 synthetic problem 8 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg k_2(c, a)$     `cnf(prove_this, negated_conjecture)`  
**SYN111-1.p** RPT63 synthetic problem 9 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg k_2(c, b)$     `cnf(prove_this, negated_conjecture)`  
**SYN112-1.p** RPT63 synthetic problem 10 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg k_2(e, x)$     `cnf(prove_this, negated_conjecture)`  
**SYN113-1.p** RPT63 synthetic problem 11 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg k_2(e, d)$     `cnf(prove_this, negated_conjecture)`  
**SYN114-1.p** RPT63 synthetic problem 12 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg k_3(x, x, b)$     `cnf(prove_this, negated_conjecture)`  
**SYN115-1.p** RPT63 synthetic problem 13 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg k_4(c)$     `cnf(prove_this, negated_conjecture)`  
**SYN116-1.p** RPT63 synthetic problem 14 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg k_5(b)$     `cnf(prove_this, negated_conjecture)`  
**SYN117-1.p** RPT63 synthetic problem 15 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg k_5(e)$     `cnf(prove_this, negated_conjecture)`  
**SYN118-1.p** RPT63 synthetic problem 16 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg l_0(a)$     `cnf(prove_this, negated_conjecture)`  
**SYN119-1.p** RPT63 synthetic problem 17 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg l_0(c)$     `cnf(prove_this, negated_conjecture)`  
**SYN120-1.p** RPT63 synthetic problem 18 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg l_1(e, e)$     `cnf(prove_this, negated_conjecture)`  
**SYN121-1.p** RPT63 synthetic problem 19 (quasi-uniform distribution)

include('Axioms/SYN001-0.ax')  
 $\neg l_2(a, b)$     cnf(prove\_this, negated\_conjecture)

**SYN122-1.p** RPT63 synthetic problem 20 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg l_2(b, e)$     cnf(prove\_this, negated\_conjecture)

**SYN123-1.p** RPT63 synthetic problem 21 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg l_2(d, d)$     cnf(prove\_this, negated\_conjecture)

**SYN124-1.p** RPT63 synthetic problem 22 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg l_3(a, a)$     cnf(prove\_this, negated\_conjecture)

**SYN125-1.p** RPT63 synthetic problem 23 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg l_3(e, c)$     cnf(prove\_this, negated\_conjecture)

**SYN126-1.p** RPT63 synthetic problem 24 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg l_4(b)$     cnf(prove\_this, negated\_conjecture)

**SYN127-1.p** RPT63 synthetic problem 25 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg l_4(e)$     cnf(prove\_this, negated\_conjecture)

**SYN128-1.p** RPT63 synthetic problem 26 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg l_5(c)$     cnf(prove\_this, negated\_conjecture)

**SYN129-1.p** RPT63 synthetic problem 27 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg l_5(e)$     cnf(prove\_this, negated\_conjecture)

**SYN130-1.p** RPT63 synthetic problem 28 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg m_0(x, y, b)$     cnf(prove\_this, negated\_conjecture)

**SYN131-1.p** RPT63 synthetic problem 29 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg m_0(x, y, e)$     cnf(prove\_this, negated\_conjecture)

**SYN132-1.p** RPT63 synthetic problem 30 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg m_0(x, e, a)$     cnf(prove\_this, negated\_conjecture)

**SYN133-1.p** RPT63 synthetic problem 31 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg m_0(d, x, d)$     cnf(prove\_this, negated\_conjecture)

**SYN134-1.p** RPT63 synthetic problem 32 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg m_2(d)$     cnf(prove\_this, negated\_conjecture)

**SYN135-1.p** RPT63 synthetic problem 33 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg m_3(x, y, a)$     cnf(prove\_this, negated\_conjecture)

**SYN136-1.p** RPT63 synthetic problem 34 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg m_3(x, a, a)$     cnf(prove\_this, negated\_conjecture)

**SYN137-1.p** RPT63 synthetic problem 35 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg m_3(b, c, b)$     cnf(prove\_this, negated\_conjecture)

**SYN138-1.p** RPT63 synthetic problem 36 (quasi-uniform distribution)  
 include('Axioms/SYN001-0.ax')  
 $\neg m_3(c, e, c)$     cnf(prove\_this, negated\_conjecture)

**SYN139-1.p** RPT63 synthetic problem 37 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_4(a, a)$      cnf(prove\_this, negated\_conjecture)

**SYN140-1.p** RPT63 synthetic problem 38 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_4(b, x)$      cnf(prove\_this, negated\_conjecture)

**SYN141-1.p** RPT63 synthetic problem 39 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_5(c, x)$      cnf(prove\_this, negated\_conjecture)

**SYN142-1.p** RPT63 synthetic problem 40 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_5(d, x)$      cnf(prove\_this, negated\_conjecture)

**SYN143-1.p** RPT63 synthetic problem 41 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_5(d, d)$      cnf(prove\_this, negated\_conjecture)

**SYN144-1.p** RPT63 synthetic problem 42 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_5(e, a)$      cnf(prove\_this, negated\_conjecture)

**SYN145-1.p** RPT63 synthetic problem 43 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg n_0(d, x)$      cnf(prove\_this, negated\_conjecture)

**SYN146-1.p** RPT63 synthetic problem 44 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg n_1(x, c, y)$     cnf(prove\_this, negated\_conjecture)

**SYN147-1.p** RPT63 synthetic problem 45 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg n_1(x, d, x)$     cnf(prove\_this, negated\_conjecture)

**SYN148-1.p** RPT63 synthetic problem 46 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg n_1(c, d, d)$     cnf(prove\_this, negated\_conjecture)

**SYN149-1.p** RPT63 synthetic problem 47 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg n_1(e, e, x)$     cnf(prove\_this, negated\_conjecture)

**SYN150-1.p** RPT63 synthetic problem 48 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg n_2(b)$      cnf(prove\_this, negated\_conjecture)

**SYN151-1.p** RPT63 synthetic problem 49 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg n_2(d)$      cnf(prove\_this, negated\_conjecture)

**SYN152-1.p** RPT63 synthetic problem 50 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg n_2(e)$      cnf(prove\_this, negated\_conjecture)

**SYN153-1.p** RPT63 synthetic problem 51 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg n_3(a)$      cnf(prove\_this, negated\_conjecture)

**SYN154-1.p** RPT63 synthetic problem 52 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg n_3(e)$      cnf(prove\_this, negated\_conjecture)

**SYN155-1.p** RPT63 synthetic problem 53 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg n_4(x, a)$      cnf(prove\_this, negated\_conjecture)

**SYN156-1.p** RPT63 synthetic problem 54 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')



$\neg n_4(a, e)$     `cnf(prove_this, negated_conjecture)`  
**SYN157-1.p** RPT63 synthetic problem 55 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg n_5(x, d)$     `cnf(prove_this, negated_conjecture)`  
**SYN158-1.p** RPT63 synthetic problem 56 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg n_5(a, a)$     `cnf(prove_this, negated_conjecture)`  
**SYN159-1.p** RPT63 synthetic problem 57 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg n_5(a, e)$     `cnf(prove_this, negated_conjecture)`  
**SYN160-1.p** RPT63 synthetic problem 58 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg n_5(b, b)$     `cnf(prove_this, negated_conjecture)`  
**SYN161-1.p** RPT63 synthetic problem 59 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg n_5(c, x)$     `cnf(prove_this, negated_conjecture)`  
**SYN162-1.p** RPT63 synthetic problem 60 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg n_5(c, c)$     `cnf(prove_this, negated_conjecture)`  
**SYN163-1.p** RPT63 synthetic problem 61 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg n_5(e, a)$     `cnf(prove_this, negated_conjecture)`  
**SYN164-1.p** RPT63 synthetic problem 62 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg p_0(b, c)$     `cnf(prove_this, negated_conjecture)`  
**SYN165-1.p** RPT63 synthetic problem 63 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg p_1(x, a, x)$     `cnf(prove_this, negated_conjecture)`  
**SYN166-1.p** RPT63 synthetic problem 64 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg p_1(a, b, b)$     `cnf(prove_this, negated_conjecture)`  
**SYN167-1.p** RPT63 synthetic problem 65 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg p_1(d, x, d)$     `cnf(prove_this, negated_conjecture)`  
**SYN168-1.p** RPT63 synthetic problem 66 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg p_3(x, y, b)$     `cnf(prove_this, negated_conjecture)`  
**SYN169-1.p** RPT63 synthetic problem 67 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg p_3(x, d, y)$     `cnf(prove_this, negated_conjecture)`  
**SYN170-1.p** RPT63 synthetic problem 68 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg p_4(x, c, y)$     `cnf(prove_this, negated_conjecture)`  
**SYN171-1.p** RPT63 synthetic problem 69 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg p_4(d, a, a)$     `cnf(prove_this, negated_conjecture)`  
**SYN172-1.p** RPT63 synthetic problem 70 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg q_0(c, d)$     `cnf(prove_this, negated_conjecture)`  
**SYN173-1.p** RPT63 synthetic problem 71 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg q_1(e, a, e)$     `cnf(prove_this, negated_conjecture)`  
**SYN174-1.p** RPT63 synthetic problem 72 (quasi-uniform distribution)

include('Axioms/SYN001-0.ax')  
 $\neg q_1(e, c, e)$      cnf(prove\_this, negated\_conjecture)

**SYN175-1.p** RPT63 synthetic problem 73 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg q_2(x, d, y)$      cnf(prove\_this, negated\_conjecture)

**SYN176-1.p** RPT63 synthetic problem 74 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg q_2(e, c, x)$      cnf(prove\_this, negated\_conjecture)

**SYN177-1.p** RPT63 synthetic problem 75 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg q_3(x, b)$      cnf(prove\_this, negated\_conjecture)

**SYN178-1.p** RPT63 synthetic problem 76 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg q_3(b, d)$      cnf(prove\_this, negated\_conjecture)

**SYN179-1.p** RPT63 synthetic problem 77 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg q_3(d, x)$      cnf(prove\_this, negated\_conjecture)

**SYN180-1.p** RPT63 synthetic problem 78 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg q_4(a, e)$      cnf(prove\_this, negated\_conjecture)

**SYN181-1.p** RPT63 synthetic problem 79 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg q_4(d, b)$      cnf(prove\_this, negated\_conjecture)

**SYN182-1.p** RPT63 synthetic problem 80 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg q_5(x, c)$      cnf(prove\_this, negated\_conjecture)

**SYN183-1.p** RPT63 synthetic problem 81 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg q_5(e, e)$      cnf(prove\_this, negated\_conjecture)

**SYN184-1.p** RPT63 synthetic problem 82 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg r_0(b)$      cnf(prove\_this, negated\_conjecture)

**SYN185-1.p** RPT63 synthetic problem 83 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg r_0(e)$      cnf(prove\_this, negated\_conjecture)

**SYN186-1.p** RPT63 synthetic problem 84 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg r_1(a)$      cnf(prove\_this, negated\_conjecture)

**SYN187-1.p** RPT63 synthetic problem 85 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg r_1(d)$      cnf(prove\_this, negated\_conjecture)

**SYN188-1.p** RPT63 synthetic problem 86 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg r_1(e)$      cnf(prove\_this, negated\_conjecture)

**SYN189-1.p** RPT63 synthetic problem 87 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg r_2(c)$      cnf(prove\_this, negated\_conjecture)

**SYN190-1.p** RPT63 synthetic problem 88 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg r_3(a, x, d)$      cnf(prove\_this, negated\_conjecture)

**SYN191-1.p** RPT63 synthetic problem 89 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg r_3(c, b, c)$      cnf(prove\_this, negated\_conjecture)

**SYN192-1.p** RPT63 synthetic problem 90 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg r_4(a)$      cnf(prove\_this, negated\_conjecture)

**SYN193-1.p** RPT63 synthetic problem 91 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg r_4(b)$      cnf(prove\_this, negated\_conjecture)

**SYN194-1.p** RPT63 synthetic problem 92 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg r_5(c, c)$      cnf(prove\_this, negated\_conjecture)

**SYN195-1.p** RPT63 synthetic problem 93 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg r_5(d, d)$      cnf(prove\_this, negated\_conjecture)

**SYN196-1.p** RPT63 synthetic problem 94 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg s_1(a)$      cnf(prove\_this, negated\_conjecture)

**SYN197-1.p** RPT63 synthetic problem 95 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg s_1(b)$      cnf(prove\_this, negated\_conjecture)

**SYN198-1.p** RPT63 synthetic problem 96 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg s_1(c)$      cnf(prove\_this, negated\_conjecture)

**SYN199-1.p** RPT63 synthetic problem 97 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg s_1(d)$      cnf(prove\_this, negated\_conjecture)

**SYN200-1.p** RPT63 synthetic problem 98 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg s_1(e)$      cnf(prove\_this, negated\_conjecture)

**SYN201-1.p** RPT63 synthetic problem 99 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg s_2(b)$      cnf(prove\_this, negated\_conjecture)

**SYN202-1.p** RPT63 synthetic problem 100 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg s_2(e)$      cnf(prove\_this, negated\_conjecture)

**SYN203-1.p** RPT63 synthetic problem 101 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg s_3(x, b)$      cnf(prove\_this, negated\_conjecture)

**SYN204-1.p** RPT63 synthetic problem 102 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg s_3(a, c)$      cnf(prove\_this, negated\_conjecture)

**SYN205-1.p** RPT63 synthetic problem 103 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg s_3(a, d)$      cnf(prove\_this, negated\_conjecture)

**SYN206-1.p** RPT63 synthetic problem 104 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg s_3(b, b)$      cnf(prove\_this, negated\_conjecture)

**SYN207-1.p** RPT63 synthetic problem 105 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg s_3(c, c)$      cnf(prove\_this, negated\_conjecture)

**SYN208-1.p** RPT63 synthetic problem 106 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg s_3(d, b)$      cnf(prove\_this, negated\_conjecture)

**SYN209-1.p** RPT63 synthetic problem 107 (quasi-uniform distribution)  
include('Axioms/SYN001-0.ax')

$\neg s_4(b)$     `cnf(prove_this, negated_conjecture)`  
**SYN210-1.p** RPT63 synthetic problem 108 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg s_4(c)$     `cnf(prove_this, negated_conjecture)`  
**SYN211-1.p** RPT63 synthetic problem 109 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg s_4(d)$     `cnf(prove_this, negated_conjecture)`  
**SYN212-1.p** RPT63 synthetic problem 110 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg s_4(e)$     `cnf(prove_this, negated_conjecture)`  
**SYN213-1.p** RPT63 synthetic problem 111 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg s_5(b)$     `cnf(prove_this, negated_conjecture)`  
**SYN214-1.p** RPT63 synthetic problem 112 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg s_5(c)$     `cnf(prove_this, negated_conjecture)`  
**SYN215-1.p** RPT63 synthetic problem 113 (quasi-uniform distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg s_5(d)$     `cnf(prove_this, negated_conjecture)`  
**SYN216-1.p** RPT63 synthetic problem 1 (skewed distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg l_2(a, a)$     `cnf(prove_this, negated_conjecture)`  
**SYN217-1.p** RPT63 synthetic problem 2 (skewed distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg l_2(b, b)$     `cnf(prove_this, negated_conjecture)`  
**SYN218-1.p** RPT63 synthetic problem 3 (skewed distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg l_2(c, x)$     `cnf(prove_this, negated_conjecture)`  
**SYN219-1.p** RPT63 synthetic problem 4 (skewed distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg l_2(e, b)$     `cnf(prove_this, negated_conjecture)`  
**SYN220-1.p** RPT63 synthetic problem 5 (skewed distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg l_3(x, b)$     `cnf(prove_this, negated_conjecture)`  
**SYN221-1.p** RPT63 synthetic problem 6 (skewed distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg l_3(x, c)$     `cnf(prove_this, negated_conjecture)`  
**SYN222-1.p** RPT63 synthetic problem 7 (skewed distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg l_3(x, d)$     `cnf(prove_this, negated_conjecture)`  
**SYN223-1.p** RPT63 synthetic problem 8 (skewed distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg l_3(x, e)$     `cnf(prove_this, negated_conjecture)`  
**SYN224-1.p** RPT63 synthetic problem 9 (skewed distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg l_3(a, x)$     `cnf(prove_this, negated_conjecture)`  
**SYN225-1.p** RPT63 synthetic problem 10 (skewed distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg l_3(b, a)$     `cnf(prove_this, negated_conjecture)`  
**SYN226-1.p** RPT63 synthetic problem 11 (skewed distribution)  
`include('Axioms/SYN001-0.ax')`  
 $\neg l_3(b, b)$     `cnf(prove_this, negated_conjecture)`  
**SYN227-1.p** RPT63 synthetic problem 12 (skewed distribution)

include('Axioms/SYN001-0.ax')  
 $\neg l_3(b, c)$     cnf(prove\_this, negated\_conjecture)

**SYN228-1.p** RPT63 synthetic problem 13 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg l_3(b, e)$     cnf(prove\_this, negated\_conjecture)

**SYN229-1.p** RPT63 synthetic problem 14 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg l_3(c, x)$     cnf(prove\_this, negated\_conjecture)

**SYN230-1.p** RPT63 synthetic problem 15 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg l_3(c, c)$     cnf(prove\_this, negated\_conjecture)

**SYN231-1.p** RPT63 synthetic problem 16 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg l_3(d, x)$     cnf(prove\_this, negated\_conjecture)

**SYN232-1.p** RPT63 synthetic problem 17 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg l_3(d, d)$     cnf(prove\_this, negated\_conjecture)

**SYN233-1.p** RPT63 synthetic problem 18 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg l_3(e, x)$     cnf(prove\_this, negated\_conjecture)

**SYN234-1.p** RPT63 synthetic problem 19 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg l_3(e, a)$     cnf(prove\_this, negated\_conjecture)

**SYN235-1.p** RPT63 synthetic problem 20 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg l_3(e, b)$     cnf(prove\_this, negated\_conjecture)

**SYN236-1.p** RPT63 synthetic problem 21 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg l_3(e, e)$     cnf(prove\_this, negated\_conjecture)

**SYN237-1.p** RPT63 synthetic problem 22 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_1(x, x, e)$     cnf(prove\_this, negated\_conjecture)

**SYN238-1.p** RPT63 synthetic problem 23 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_1(x, b, y)$     cnf(prove\_this, negated\_conjecture)

**SYN239-1.p** RPT63 synthetic problem 24 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_1(x, c, x)$     cnf(prove\_this, negated\_conjecture)

**SYN240-1.p** RPT63 synthetic problem 25 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_1(x, e, e)$     cnf(prove\_this, negated\_conjecture)

**SYN241-1.p** RPT63 synthetic problem 26 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_1(a, a, x)$     cnf(prove\_this, negated\_conjecture)

**SYN242-1.p** RPT63 synthetic problem 27 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_1(a, a, a)$     cnf(prove\_this, negated\_conjecture)

**SYN243-1.p** RPT63 synthetic problem 28 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_1(a, d, d)$     cnf(prove\_this, negated\_conjecture)

**SYN244-1.p** RPT63 synthetic problem 29 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_1(c, x, x)$     cnf(prove\_this, negated\_conjecture)

**SYN245-1.p** RPT63 synthetic problem 30 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_1(c, x, c)$     cnf(prove\_this, negated\_conjecture)

**SYN246-1.p** RPT63 synthetic problem 31 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_1(c, b, c)$     cnf(prove\_this, negated\_conjecture)

**SYN247-1.p** RPT63 synthetic problem 32 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_1(d, x, y)$     cnf(prove\_this, negated\_conjecture)

**SYN248-1.p** RPT63 synthetic problem 33 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_1(d, c, c)$     cnf(prove\_this, negated\_conjecture)

**SYN249-1.p** RPT63 synthetic problem 34 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_1(d, e, e)$     cnf(prove\_this, negated\_conjecture)

**SYN250-1.p** RPT63 synthetic problem 35 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_1(e, a, a)$     cnf(prove\_this, negated\_conjecture)

**SYN251-1.p** RPT63 synthetic problem 36 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_1(e, b, b)$     cnf(prove\_this, negated\_conjecture)

**SYN252-1.p** RPT63 synthetic problem 37 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_4(x, d)$     cnf(prove\_this, negated\_conjecture)

**SYN253-1.p** RPT63 synthetic problem 38 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_4(e, x)$     cnf(prove\_this, negated\_conjecture)

**SYN254-1.p** RPT63 synthetic problem 39 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg m_4(e, b)$     cnf(prove\_this, negated\_conjecture)

**SYN255-1.p** RPT63 synthetic problem 40 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg n_2(a)$     cnf(prove\_this, negated\_conjecture)

**SYN256-1.p** RPT63 synthetic problem 41 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg n_2(c)$     cnf(prove\_this, negated\_conjecture)

**SYN257-1.p** RPT63 synthetic problem 42 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_0(c, b)$     cnf(prove\_this, negated\_conjecture)

**SYN258-1.p** RPT63 synthetic problem 43 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_1(x, y, d)$     cnf(prove\_this, negated\_conjecture)

**SYN259-1.p** RPT63 synthetic problem 44 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_1(x, d, x)$     cnf(prove\_this, negated\_conjecture)

**SYN260-1.p** RPT63 synthetic problem 45 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_1(x, d, d)$     cnf(prove\_this, negated\_conjecture)

**SYN261-1.p** RPT63 synthetic problem 46 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_1(b, x, b)$     cnf(prove\_this, negated\_conjecture)

**SYN262-1.p** RPT63 synthetic problem 47 (skewed distribution)  
include('Axioms/SYN001-0.ax')

$\neg p_1(b, c, b)$     cnf(prove\_this, negated\_conjecture)  
**SYN263-1.p** RPT63 synthetic problem 48 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_1(d, d, a)$     cnf(prove\_this, negated\_conjecture)  
**SYN264-1.p** RPT63 synthetic problem 49 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_1(e, c, e)$     cnf(prove\_this, negated\_conjecture)  
**SYN265-1.p** RPT63 synthetic problem 50 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_3(x, x, a)$     cnf(prove\_this, negated\_conjecture)  
**SYN266-1.p** RPT63 synthetic problem 51 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_3(b, e, e)$     cnf(prove\_this, negated\_conjecture)  
**SYN267-1.p** RPT63 synthetic problem 52 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_4(x, y, c)$     cnf(prove\_this, negated\_conjecture)  
**SYN268-1.p** RPT63 synthetic problem 53 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_4(a, x, y)$     cnf(prove\_this, negated\_conjecture)  
**SYN269-1.p** RPT63 synthetic problem 54 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_4(b, a, a)$     cnf(prove\_this, negated\_conjecture)  
**SYN270-1.p** RPT63 synthetic problem 55 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_4(b, b, c)$     cnf(prove\_this, negated\_conjecture)  
**SYN271-1.p** RPT63 synthetic problem 56 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_4(d, x, a)$     cnf(prove\_this, negated\_conjecture)  
**SYN272-1.p** RPT63 synthetic problem 57 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_4(d, e, x)$     cnf(prove\_this, negated\_conjecture)  
**SYN273-1.p** RPT63 synthetic problem 58 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg p_4(e, c, e)$     cnf(prove\_this, negated\_conjecture)  
**SYN274-1.p** RPT63 synthetic problem 59 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg q_0(x, d)$     cnf(prove\_this, negated\_conjecture)  
**SYN275-1.p** RPT63 synthetic problem 60 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg q_0(d, x)$     cnf(prove\_this, negated\_conjecture)  
**SYN276-1.p** RPT63 synthetic problem 61 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg q_0(d, b)$     cnf(prove\_this, negated\_conjecture)  
**SYN277-1.p** RPT63 synthetic problem 62 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg q_1(x, x, d)$     cnf(prove\_this, negated\_conjecture)  
**SYN278-1.p** RPT63 synthetic problem 63 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg q_1(x, y, e)$     cnf(prove\_this, negated\_conjecture)  
**SYN279-1.p** RPT63 synthetic problem 64 (skewed distribution)  
include('Axioms/SYN001-0.ax')  
 $\neg q_1(x, a, c)$     cnf(prove\_this, negated\_conjecture)  
**SYN280-1.p** RPT63 synthetic problem 65 (skewed distribution)

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include('Axioms/SYN001-0.ax')
¬ q1(x, b, y)    cnf(prove_this, negated_conjecture)
SYN281-1.p RPT63 synthetic problem 66 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(x, c, c)    cnf(prove_this, negated_conjecture)
SYN282-1.p RPT63 synthetic problem 67 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(x, d, y)    cnf(prove_this, negated_conjecture)
SYN283-1.p RPT63 synthetic problem 68 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(a, b, a)    cnf(prove_this, negated_conjecture)
SYN284-1.p RPT63 synthetic problem 69 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(a, c, a)    cnf(prove_this, negated_conjecture)
SYN285-1.p RPT63 synthetic problem 70 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(a, d, d)    cnf(prove_this, negated_conjecture)
SYN286-1.p RPT63 synthetic problem 71 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(a, e, x)    cnf(prove_this, negated_conjecture)
SYN287-1.p RPT63 synthetic problem 72 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(b, x, y)    cnf(prove_this, negated_conjecture)
SYN288-1.p RPT63 synthetic problem 73 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(b, b, b)    cnf(prove_this, negated_conjecture)
SYN289-1.p RPT63 synthetic problem 74 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(b, d, b)    cnf(prove_this, negated_conjecture)
SYN290-1.p RPT63 synthetic problem 75 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(c, x, y)    cnf(prove_this, negated_conjecture)
SYN291-1.p RPT63 synthetic problem 76 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(d, x, y)    cnf(prove_this, negated_conjecture)
SYN292-1.p RPT63 synthetic problem 77 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(d, b, b)    cnf(prove_this, negated_conjecture)
SYN293-1.p RPT63 synthetic problem 78 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(d, d, a)    cnf(prove_this, negated_conjecture)
SYN294-1.p RPT63 synthetic problem 79 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(d, d, c)    cnf(prove_this, negated_conjecture)
SYN295-1.p RPT63 synthetic problem 80 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(d, d, d)    cnf(prove_this, negated_conjecture)
SYN296-1.p RPT63 synthetic problem 81 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(e, b, e)    cnf(prove_this, negated_conjecture)
SYN297-1.p RPT63 synthetic problem 82 (skewed distribution)
include('Axioms/SYN001-0.ax')
¬ q1(e, e, e)    cnf(prove_this, negated_conjecture)

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**SYN298-1.p** RPT63 synthetic problem 83 (skewed distribution)

include('Axioms/SYN001-0.ax')

$\neg s_3(b, x)$     cnf(prove\_this, negated\_conjecture)

**SYN299-1.p** RPT63 synthetic problem 84 (skewed distribution)

include('Axioms/SYN001-0.ax')

$\neg s_3(b, a)$     cnf(prove\_this, negated\_conjecture)

**SYN300-1.p** RPT63 synthetic problem 85 (skewed distribution)

include('Axioms/SYN001-0.ax')

$\neg s_3(b, d)$     cnf(prove\_this, negated\_conjecture)

**SYN301-1.p** RPT63 synthetic problem 86 (skewed distribution)

include('Axioms/SYN001-0.ax')

$\neg s_4(a)$     cnf(prove\_this, negated\_conjecture)

**SYN303-1.p** Problem for testing satisfiability

$p(x, x)$     cnf(clause<sub>1</sub>, negated\_conjecture)

$p(x, y) \Rightarrow p(y, x)$     cnf(clause<sub>2</sub>, negated\_conjecture)

$p(f(x), f(y)) \Rightarrow p(x, y)$     cnf(clause<sub>3</sub>, negated\_conjecture)

$p(x, y) \Rightarrow p(f(x), f(y))$     cnf(clause<sub>4</sub>, negated\_conjecture)

$\neg p(a, f(x))$     cnf(clause<sub>5</sub>, negated\_conjecture)

**SYN304-1.p** Problem for testing satisfiability

$p(x, f(x)) \Rightarrow r(f(x), g(x), x)$     cnf(clause<sub>1</sub>, negated\_conjecture)

$p(a, x)$     cnf(clause<sub>2</sub>, negated\_conjecture)

$r(f(a), g(a), a)$     cnf(clause<sub>3</sub>, negated\_conjecture)

$s(f(x), x, x)$  or  $l(x)$     cnf(clause<sub>4</sub>, negated\_conjecture)

$\neg s(f(x), x, a)$     cnf(clause<sub>5</sub>, negated\_conjecture)

$\neg s(f(x), x, b)$     cnf(clause<sub>6</sub>, negated\_conjecture)

$l(a)$     cnf(clause<sub>7</sub>, negated\_conjecture)

$l(b)$     cnf(clause<sub>8</sub>, negated\_conjecture)

**SYN305-1.p** Problem for testing satisfiability

$f(g_1(x)) = x$     cnf(clause<sub>1</sub>, negated\_conjecture)

$f(g_2(x)) = x$     cnf(clause<sub>2</sub>, negated\_conjecture)

$g_1(x) \neq g_2(x)$     cnf(clause<sub>3</sub>, negated\_conjecture)

**SYN306-1.p** Problem for testing satisfiability

$p(x)$  or  $q(g(x), x)$     cnf(clause<sub>1</sub>, negated\_conjecture)

$q(y) \Rightarrow r(x, y)$     cnf(clause<sub>2</sub>, negated\_conjecture)

$r(a, a) \Rightarrow \neg r(f(b), a)$     cnf(clause<sub>3</sub>, negated\_conjecture)

$r(f(x), y)$     cnf(clause<sub>4</sub>, negated\_conjecture)

$p(f(x)) \Rightarrow p(x)$     cnf(clause<sub>5</sub>, negated\_conjecture)

$\neg p(a)$     cnf(clause<sub>6</sub>, negated\_conjecture)

**SYN307-1.p** Problem for testing satisfiability

$(p(x, y, u)$  and  $p(y, z, u)) \Rightarrow p(x, z, u)$     cnf(clause<sub>1</sub>, negated\_conjecture)

$p(x, x, a)$     cnf(clause<sub>2</sub>, negated\_conjecture)

$p(x, z, u) \Rightarrow (p(x, y, u)$  or  $p(y, z, u))$     cnf(clause<sub>3</sub>, negated\_conjecture)

$\neg p(x, x, b)$     cnf(clause<sub>4</sub>, negated\_conjecture)

**SYN308-1.p** Problem for testing satisfiability

$p(f(f(a)), \text{gf}(c, \text{gf}(y, x)))$  or  $p(u, f(u))$     cnf(clause<sub>1</sub>, negated\_conjecture)

$(p(f(h(x, y, z)), z)$  and  $g(u)) \Rightarrow (g(b)$  or  $g(v))$     cnf(clause<sub>2</sub>, negated\_conjecture)

$e(\text{gf}(h(z, x, y), f(b)))$     cnf(clause<sub>3</sub>, negated\_conjecture)

$r(\text{gf}(v, \text{gf}(v, u)), \text{gf}(u, v))$  or  $r(f(b), \text{gf}(f(f(a)), \text{gf}(u, v)))$     cnf(clause<sub>4</sub>, negated\_conjecture)

**SYN309-1.p** Problem for testing satisfiability

$s(h(x, y, z), a, h(x, y, z)) \Rightarrow p(f(x), a, g(x))$     cnf(clause<sub>1</sub>, negated\_conjecture)

$r(f(a), a, b)$  or  $s(h(a, y, z), b, h(a, y, z))$     cnf(clause<sub>2</sub>, negated\_conjecture)

$p(k(x, y), k(x, y), b) \Rightarrow (s(f(x), x, x)$  or  $p(f(x), g(x), g(x)))$     cnf(clause<sub>3</sub>, negated\_conjecture)

$s(f(x), x, x)$  or  $p(f(y), y, f(y))$     cnf(clause<sub>4</sub>, negated\_conjecture)

$p(x, x, x)$     cnf(clause<sub>5</sub>, negated\_conjecture)

$p(a, b, c)$     cnf(clause<sub>6</sub>, negated\_conjecture)

**SYN310-1.p** Problem for testing satisfiability

$p(x_2, x_1, x) \Rightarrow p(x, x_1, x_2)$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $p(x_1, x, x_2) \Rightarrow p(x, x_1, x_2)$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $p(x, x_1, g(x_2)) \Rightarrow p(x, x_1, x_2)$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $p(f(x), x_1, x_2) \Rightarrow p(x, x_1, x_2)$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $\neg p(a, b, c)$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $p(f(g(a)), f(g(b)), f(g(c)))$     cnf(clause<sub>6</sub>, negated\_conjecture)

**SYN311-1.p** Problem for testing satisfiability

$p(x, x_1, x_2, x_3) \Rightarrow p(x_3, x, x_1, x_2)$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $p(x, x_1, x_2, x_3) \Rightarrow p(x_3, x_2, x_1, x)$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $p(x, x_1, x_2, x_3) \Rightarrow p(x, x_1, x_2, g(x_3))$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $p(x, x_1, x_2, x_3) \Rightarrow p(f(x), x_1, x_2, x_3)$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $p(a, b, c, d)$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $\neg p(f(g(d)), f(g(c)), f(g(b)), f(g(a)))$     cnf(clause<sub>6</sub>, negated\_conjecture)

**SYN312-1.p** Problem for testing satisfiability

$(p(x, x_1, x_2) \text{ and } p(x_1, x_3, x_2)) \Rightarrow p(x, x_3, x_2)$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $p(x, x_1, x_2) \Rightarrow p(x_2, x_1, x)$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $p(x, x_1, x_2) \Rightarrow p(x_1, x, x_2)$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $p(x, x_1, x_2) \Rightarrow p(x, x_1, f(x_2))$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $p(x, x_1, x_2) \Rightarrow p(g(x), x_1, x_2)$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $p(a, f(b), c)$     cnf(clause<sub>6</sub>, negated\_conjecture)  
 $p(f(b), d, c)$     cnf(clause<sub>7</sub>, negated\_conjecture)  
 $\neg p(f(g(a)), f(g(d)), f(g(c)))$     cnf(clause<sub>8</sub>, negated\_conjecture)

**SYN313-1.001.002.p** Problem for testing satisfiability

$p(x_0, f_0(x_0), x_1) \Rightarrow \neg p(x_0, f_1(x_1), x_2)$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $p(h_0, y_0, j_0(y_2)) \text{ or } p(h_1(y_0), y_1, j_1(y_2)) \text{ or } p(h_2(y_1), y_2, j_2(y_2))$     cnf(clause<sub>2</sub>, negated\_conjecture)

**SYN314-1.002.001.p** Problem for testing satisfiability

$p(x_0, f_0(x_0), x_1, g_0(x_3)) \text{ or } p(x_0, f_1(x_1), x_2, g_1(x_3)) \text{ or } p(x_0, f_2(x_2), x_3, g_2(x_3))$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $p(h_0, y_0, j_0(y_1), y_2) \Rightarrow \neg p(h_1(y_0), y_1, j_1(y_2), y_3)$     cnf(clause<sub>2</sub>, negated\_conjecture)

**SYN315+1.p** Church problem 46.2 (1)

$\exists x: \forall y: ((\text{big\_f}(x) \iff p) \Rightarrow (\text{big\_f}(y) \iff p))$     fof(church\_46\_2<sub>1</sub>, conjecture)

**SYN315-1.p** Church problem 46.2 (1)

$f(x) \Rightarrow p(a)$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $p(a) \Rightarrow f(x)$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $f(y(x)) \Rightarrow \neg p(a)$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $p(a) \text{ or } f(y(x))$     cnf(clause<sub>4</sub>, negated\_conjecture)

**SYN316+1.p** Church problem 46.2 (2)

$\exists x: \forall y: (\text{big\_f}(x) \iff \text{big\_f}(y))$     fof(church\_46\_2<sub>2</sub>, conjecture)

**SYN316-1.p** Church problem 46.2 (2)

$f(x) \Rightarrow \neg f(y(x))$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $f(x) \text{ or } f(y(x))$     cnf(clause<sub>2</sub>, negated\_conjecture)

**SYN317+1.p** Church problem 46.2 (3)

$\exists x: (\text{big\_f}(x) \Rightarrow \text{big\_g}(x)) \iff \exists x, y: (\text{big\_f}(x) \Rightarrow \text{big\_g}(y))$     fof(church\_46\_2<sub>3</sub>, conjecture)

**SYN317-1.p** Church problem 46.2 (3)

$f(z)$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $\neg g(z)$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $f(c) \Rightarrow (g(c) \text{ or } f(a) \text{ or } g(b))$     cnf(clause<sub>3</sub>, negated\_conjecture)

**SYN318+1.p** Church problem 46.2 (4)

$\exists y: (\forall x: (\text{big\_f}(x) \Rightarrow (\text{big\_f}(y) \Rightarrow \text{big\_g}(x)))) \Rightarrow (p \Rightarrow \forall x: (\text{big\_f}(x) \Rightarrow \text{big\_g}(y)))$     fof(church\_46\_2<sub>4</sub>, conjecture)

**SYN318-1.p** Church problem 46.2 (4)

$(f(x) \text{ and } f(b)) \Rightarrow g(x)$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $p(a)$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $f(x)$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $\neg g(b)$     cnf(clause<sub>4</sub>, negated\_conjecture)

**SYN319+1.p** Church problem 46.2 (5)
$$\exists x, y: \forall z_1, z_2: (((\text{big\_f}(y) \Rightarrow \text{big\_g}(z_1)) \Rightarrow (\text{big\_g}(x) \text{ and } \neg \text{big\_f}(z_1))) \Rightarrow (((\text{big\_f}(x) \text{ or } \text{big\_g}(x)) \Rightarrow \text{big\_h}(x)) \Rightarrow (\text{big\_h}(z_2) \text{ and } (\text{big\_h}(y) \Rightarrow ((\text{big\_f}(z_2) \text{ or } \text{big\_g}(z_2)) \Rightarrow \text{big\_h}(z_2)))))) \Rightarrow \text{fof}(\text{church\_46\_2}_5, \text{conjecture})$$
**SYN319-1.p** Church problem 46.2 (5)
$$\begin{aligned} f(y) \text{ or } g(x) & \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture}) \\ f(z_1(x, y)) \Rightarrow f(y) & \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture}) \\ g(z_1(x, y)) \Rightarrow g(x) & \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture}) \\ g(z_1(x, y)) \Rightarrow \neg f(z_1(x, y)) & \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture}) \\ f(x) \Rightarrow h(x) & \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture}) \\ g(x) \Rightarrow h(x) & \quad \text{cnf}(\text{clause}_6, \text{negated\_conjecture}) \\ \neg h(z_2(x, y)) & \quad \text{cnf}(\text{clause}_7, \text{negated\_conjecture}) \end{aligned}$$
**SYN320+1.p** Church problem 46.3 (1)
$$\exists z, x: \forall y_1, y_2: ((\neg \text{big\_f}(x, z) \Rightarrow \text{big\_f}(z, y_1)) \Rightarrow (\text{big\_f}(y_2, z) \Rightarrow \text{big\_f}(z, y_2))) \quad \text{fof}(\text{church\_46\_3}_1, \text{conjecture})$$
**SYN320-1.p** Church problem 46.3 (1)
$$\begin{aligned} f(x, a) \text{ or } f(a, y_1(x)) & \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture}) \\ f(y_2(x), a) & \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture}) \\ \neg f(a, y_2(x)) & \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture}) \end{aligned}$$
**SYN321+1.p** Church problem 46.3 (2)
$$\exists x, y: ((\exists z: \text{big\_f}(x, z) \Rightarrow \forall z: \text{big\_g}(x, z)) \Rightarrow (\forall z: (\text{big\_g}(z, z) \Rightarrow \text{big\_f}(z, y)) \Rightarrow (\text{big\_f}(x, y) \iff \forall z: \text{big\_g}(x, z)))) \quad \text{fof}(\text{church\_46\_3}_2, \text{conjecture})$$
**SYN321-1.p** Church problem 46.3 (2)
$$\begin{aligned} f(a, z) \Rightarrow g(a, u) & \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture}) \\ g(u, u) \Rightarrow f(u, b) & \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture}) \\ f(a, b) \text{ or } g(a, u) & \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture}) \\ f(a, b) \Rightarrow \neg g(a, d) & \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture}) \end{aligned}$$
**SYN322+1.p** Church problem 46.4 (1)
$$\exists y: (\forall x: (\text{big\_f}(x, y) \Rightarrow \text{big\_f}(y, x)) \Rightarrow \neg \forall x: (\text{big\_f}(x, y) \Rightarrow \neg \text{big\_f}(y, x))) \quad \text{fof}(\text{church\_46\_4}_1, \text{conjecture})$$
**SYN322-1.p** Church problem 46.4 (1)
$$\begin{aligned} f(x, a) \Rightarrow f(a, x) & \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture}) \\ f(x, a) \Rightarrow \neg f(a, x) & \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture}) \end{aligned}$$
**SYN323+1.p** Church problem 46.4 (2)
$$\exists y: (\forall x: ((\text{big\_f}(x, y) \Rightarrow \text{big\_f}(y, x)) \Rightarrow \text{big\_g}(x, y)) \Rightarrow \neg \forall x: ((\text{big\_f}(x, y) \Rightarrow \text{big\_f}(y, x)) \Rightarrow \neg \text{big\_g}(x, y))) \quad \text{fof}(\text{church\_46\_4}_2, \text{conjecture})$$
**SYN323-1.p** Church problem 46.4 (2)
$$\begin{aligned} f(x, a) \text{ or } g(x, a) & \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture}) \\ f(a, x) \Rightarrow g(x, a) & \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture}) \\ g(x, a) \Rightarrow f(x, a) & \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture}) \\ f(a, x) \Rightarrow \neg g(x, a) & \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture}) \end{aligned}$$
**SYN324+1.p** Church problem 46.9 (1)
$$\exists x: \forall y: ((\text{big\_f}(x, y) \iff \text{big\_f}(x, x)) \Rightarrow (\text{big\_f}(x, y) \iff \text{big\_f}(y, y))) \quad \text{fof}(\text{church\_46\_9}_1, \text{conjecture})$$
**SYN324-1.p** Church problem 46.9 (1)
$$\begin{aligned} f(x, x) \Rightarrow f(x, y(x)) & \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture}) \\ f(x, y(x)) \Rightarrow f(x, x) & \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture}) \\ f(x, y(x)) \text{ or } f(y(x), y(x)) & \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture}) \\ f(x, y(x)) \Rightarrow \neg f(y(x), y(x)) & \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture}) \end{aligned}$$
**SYN325+1.p** Church problem 46.9 (2)
$$\exists x: \forall y: (((\text{big\_f}(x, x) \Rightarrow \text{big\_f}(y, y)) \Rightarrow (\text{big\_f}(x, y) \text{ and } \text{big\_g}(x))) \Rightarrow \text{big\_g}(y)) \quad \text{fof}(\text{church\_46\_9}_2, \text{conjecture})$$
**SYN325-1.p** Church problem 46.9 (2)
$$\begin{aligned} f(x, x) \text{ or } f(x, y(x)) & \quad \text{cnf}(\text{clause}_1, \text{negated\_conjecture}) \\ f(x, x) \text{ or } g(x) & \quad \text{cnf}(\text{clause}_2, \text{negated\_conjecture}) \\ f(y(x), y(x)) \Rightarrow f(x, y(x)) & \quad \text{cnf}(\text{clause}_3, \text{negated\_conjecture}) \\ f(y(x), y(x)) \Rightarrow g(x) & \quad \text{cnf}(\text{clause}_4, \text{negated\_conjecture}) \\ \neg g(y(x)) & \quad \text{cnf}(\text{clause}_5, \text{negated\_conjecture}) \end{aligned}$$
**SYN326+1.p** Church problem 46.12 (1)
$$\exists x: \forall y, z: (((\text{big\_f}(y, z) \Rightarrow (\text{big\_g}(y) \Rightarrow \text{big\_h}(x))) \Rightarrow \text{big\_f}(x, x)) \Rightarrow (((\text{big\_f}(z, x) \Rightarrow \text{big\_g}(x)) \Rightarrow \text{big\_h}(z)) \Rightarrow (\text{big\_f}(x, y) \Rightarrow \text{big\_f}(z, z)))) \quad \text{fof}(\text{church\_46\_12}_1, \text{conjecture})$$

**SYN326-1.p** Church problem 46.12 (1)

$f(y(x), z(x))$  or  $f(x, x)$     cnf(`clause1`, `negated_conjecture`)  
 $g(y(x))$  or  $f(x, x)$     cnf(`clause2`, `negated_conjecture`)  
 $h(x) \Rightarrow f(x, x)$     cnf(`clause3`, `negated_conjecture`)  
 $f(z(x), x)$  or  $h(z(x))$     cnf(`clause4`, `negated_conjecture`)  
 $g(x) \Rightarrow h(z(x))$     cnf(`clause5`, `negated_conjecture`)  
 $f(x, y(x))$     cnf(`clause6`, `negated_conjecture`)  
 $\neg f(z(x), z(x))$     cnf(`clause7`, `negated_conjecture`)

**SYN327+1.p** Church problem 46.12 (2)

$\forall x: \exists y: \forall z: ((\text{big\_f}(y, x) \Rightarrow ((\text{big\_f}(x, z) \Rightarrow \text{big\_f}(x, y)) \text{ and } (\text{big\_f}(x, y) \Rightarrow (\neg \text{big\_f}(x, z) \Rightarrow (\text{big\_f}(y, x) \text{ and } \text{big\_f}(z, y)))))))$

**SYN327-1.p** Church problem 46.12 (2)

$f(y, a)$  or  $f(a, y)$     cnf(`clause1`, `negated_conjecture`)  
 $f(a, z(y)) \Rightarrow f(y, a)$     cnf(`clause2`, `negated_conjecture`)  
 $f(a, z(y))$  or  $f(a, y)$     cnf(`clause3`, `negated_conjecture`)  
 $(f(y, a) \text{ and } f(z(y), y)) \Rightarrow f(a, z(y))$     cnf(`clause4`, `negated_conjecture`)  
 $f(a, y) \Rightarrow \neg f(a, z(y))$     cnf(`clause5`, `negated_conjecture`)  
 $(f(a, y) \text{ and } f(y, a)) \Rightarrow \neg f(z(y), y)$     cnf(`clause6`, `negated_conjecture`)

**SYN328+1.p** Church problem 46.12 (3)

$\exists x: \forall y, z: (((\text{big\_f}(y) \Rightarrow \text{big\_g}(y)) \iff \text{big\_f}(x)) \Rightarrow (((\text{big\_f}(y) \Rightarrow \text{big\_h}(y)) \iff \text{big\_g}(x)) \Rightarrow (((\text{big\_f}(y) \Rightarrow \text{big\_g}(y)) \Rightarrow \text{big\_h}(y)) \iff \text{big\_h}(x)) \Rightarrow (\text{big\_f}(z) \text{ and } \text{big\_g}(z) \text{ and } \text{big\_h}(z))))))$     fof(`church_46_123`, `conjecture`)

**SYN328-1.p** Church problem 46.12 (3)

$(f(y(x)) \text{ and } f(x)) \Rightarrow g(y(x))$     cnf(`clause1`, `negated_conjecture`)  
 $f(y(x))$  or  $f(x)$     cnf(`clause2`, `negated_conjecture`)  
 $g(y(x)) \Rightarrow f(x)$     cnf(`clause3`, `negated_conjecture`)  
 $(f(y(x)) \text{ and } g(x)) \Rightarrow h(y(x))$     cnf(`clause4`, `negated_conjecture`)  
 $f(y(x))$  or  $g(x)$     cnf(`clause5`, `negated_conjecture`)  
 $h(y(x)) \Rightarrow g(x)$     cnf(`clause6`, `negated_conjecture`)  
 $h(x) \Rightarrow (f(y(x)) \text{ or } h(y(x)))$     cnf(`clause7`, `negated_conjecture`)  
 $(g(y(x)) \text{ and } h(x)) \Rightarrow h(y(x))$     cnf(`clause8`, `negated_conjecture`)  
 $f(y(x)) \Rightarrow (g(y(x)) \text{ or } h(x))$     cnf(`clause9`, `negated_conjecture`)  
 $h(y(x)) \Rightarrow h(x)$     cnf(`clause10`, `negated_conjecture`)  
 $(f(z(x)) \text{ and } g(z(x))) \Rightarrow \neg h(z(x))$     cnf(`clause11`, `negated_conjecture`)

**SYN329+1.p** Church problem 46.14 (1)

$\exists x, y: \forall z: (\text{big\_f}(x, x) \Rightarrow (\text{big\_f}(y, y) \Rightarrow (\text{big\_f}(x, z) \Rightarrow \text{big\_f}(z, y))))$     fof(`church_46_141`, `conjecture`)

**SYN329-1.p** Church problem 46.14 (1)

$f(x, x)$     cnf(`clause1`, `negated_conjecture`)  
 $f(y, y)$     cnf(`clause2`, `negated_conjecture`)  
 $f(x, z(x, y))$     cnf(`clause3`, `negated_conjecture`)  
 $\neg f(z(x, y), y)$     cnf(`clause4`, `negated_conjecture`)

**SYN330+1.p** Church problem 46.14 (2)

$\exists x, y: \forall z: ((\text{big\_f}(x, z) \iff \text{big\_f}(z, y)) \Rightarrow ((\text{big\_f}(z, y) \iff \text{big\_f}(z, z)) \Rightarrow ((\text{big\_f}(x, y) \iff \text{big\_f}(y, x)) \Rightarrow (\text{big\_f}(x, y) \iff \text{big\_f}(x, z))))))$     fof(`church_46_142`, `conjecture`)

**SYN330-1.p** Church problem 46.14 (2)

$f(z(x, y), y) \Rightarrow f(x, z(x, y))$     cnf(`clause1`, `negated_conjecture`)  
 $f(x, z(x, y)) \Rightarrow f(z(x, y), y)$     cnf(`clause2`, `negated_conjecture`)  
 $f(z(x, y), z(x, y)) \Rightarrow f(z(x, y), y)$     cnf(`clause3`, `negated_conjecture`)  
 $f(z(x, y), y) \Rightarrow f(z(x, y), z(x, y))$     cnf(`clause4`, `negated_conjecture`)  
 $f(y, x) \Rightarrow f(x, y)$     cnf(`clause5`, `negated_conjecture`)  
 $f(y, x) \Rightarrow f(x, y)$     cnf(`clause6`, `negated_conjecture`)  
 $f(x, y)$  or  $f(x, z(x, y))$     cnf(`clause7`, `negated_conjecture`)  
 $f(x, y) \Rightarrow \neg f(x, z(x, y))$     cnf(`clause8`, `negated_conjecture`)

**SYN331+1.p** Church problem 46.14 (3)

$\exists x, y: \forall z: (\text{big\_f}(x, z) \Rightarrow (\text{big\_f}(y, z) \Rightarrow ((\text{big\_f}(x, y) \iff \text{big\_f}(z, z)) \Rightarrow ((\text{big\_f}(y, x) \text{ or } \text{big\_f}(z, z)) \Rightarrow (\text{big\_f}(z, x) \text{ or } \text{big\_f}(z, y))))))$     fof(`church_46_143`, `conjecture`)

**SYN331-1.p** Church problem 46.14 (3)

$f(x, z(x, y))$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $f(y, z(x, y))$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $f(z(x, y), z(x, y)) \Rightarrow f(x, y)$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $f(x, y) \Rightarrow f(z(x, y), z(x, y))$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $f(y, x)$  or  $f(z(x, y), z(x, y))$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $\neg f(z(x, y), x)$     cnf(clause<sub>6</sub>, negated\_conjecture)  
 $\neg f(z(x, y), y)$     cnf(clause<sub>7</sub>, negated\_conjecture)

**SYN332+1.p** Church problem 46.14 (4)

$\exists x, y: \forall z: ((\text{big\_f}(x, y) \text{ and } \text{big\_f}(y, x)) < > \text{big\_f}(x, z) \Rightarrow ((\text{big\_f}(x, z) \iff \text{big\_f}(z, x)) \Rightarrow ((\text{big\_f}(x, z) \iff \text{big\_f}(y, z)) \Rightarrow (((\text{big\_f}(y, x) \Rightarrow \text{big\_f}(x, y)) \iff \text{big\_f}(z, z)) \Rightarrow ((\text{big\_f}(x, y) \iff \text{big\_f}(y, x)) \iff \text{big\_f}(z, y))))))$     fof(church\_46\_14<sub>4</sub>, conjecture)

**SYN332-1.p** Church problem 46.14 (4)

$f(x, y)$  or  $f(x, z(x, y))$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $f(y, x)$  or  $f(x, z(x, y))$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $(f(x, y) \text{ and } f(y, x)) \Rightarrow \neg f(x, z(x, y))$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $f(z(x, y), x) \Rightarrow f(x, z(x, y))$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $f(x, z(x, y)) \Rightarrow f(z(x, y), x)$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $f(y, z(x, y)) \Rightarrow f(x, z(x, y))$     cnf(clause<sub>6</sub>, negated\_conjecture)  
 $f(x, z(x, y)) \Rightarrow f(y, z(x, y))$     cnf(clause<sub>7</sub>, negated\_conjecture)  
 $(f(y, x) \text{ and } f(z(x, y), z(x, y))) \Rightarrow f(x, y)$     cnf(clause<sub>8</sub>, negated\_conjecture)  
 $f(y, x)$  or  $f(z(x, y), z(x, y))$     cnf(clause<sub>9</sub>, negated\_conjecture)  
 $f(x, y) \Rightarrow f(z(x, y), z(x, y))$     cnf(clause<sub>10</sub>, negated\_conjecture)  
 $f(y, x) \Rightarrow (f(x, y) \text{ or } f(z(x, y), y))$     cnf(clause<sub>11</sub>, negated\_conjecture)  
 $f(x, y) \Rightarrow (f(y, x) \text{ or } f(z(x, y), y))$     cnf(clause<sub>12</sub>, negated\_conjecture)  
 $f(z(x, y), y) \Rightarrow (f(x, y) \text{ or } f(y, x))$     cnf(clause<sub>13</sub>, negated\_conjecture)  
 $(f(x, y) \text{ and } f(y, x)) \Rightarrow \neg f(z(x, y), y)$     cnf(clause<sub>14</sub>, negated\_conjecture)

**SYN333+1.p** Church problem 46.14 (5)

$\exists x, y: \forall z: (\text{big\_f}(x, y) \Rightarrow (\text{big\_f}(y, z) \text{ and } \text{big\_f}(z, z) \text{ and } ((\text{big\_f}(x, y) \text{ and } \text{big\_g}(x, y)) \Rightarrow (\text{big\_g}(x, z) \text{ and } \text{big\_g}(z, z))))))$     f

**SYN333-1.p** Church problem 46.14 (5)

$f(x, y)$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $(f(y, z(x, y)) \text{ and } f(z(x, y), z(x, y))) \Rightarrow g(x, y)$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $(f(y, z(x, y)) \text{ and } f(z(x, y), z(x, y)) \text{ and } g(x, z(x, y))) \Rightarrow \neg g(z(x, y), z(x, y))$     cnf(clause<sub>3</sub>, negated\_conjecture)

**SYN334+1.p** Church problem 46.14 (6)

$\exists x, y: \forall z: ((\text{big\_f}(x, y) \Rightarrow (\text{big\_f}(x, z) \iff \text{big\_g}(y, z))) \Rightarrow ((\text{big\_f}(x, y) \iff (\text{big\_f}(z, z) \Rightarrow \text{big\_g}(z, z))) \Rightarrow (\text{big\_g}(x, y) \iff \text{big\_g}(z, z))))$     fof(church\_46\_14<sub>6</sub>, conjecture)

**SYN334-1.p** Church problem 46.14 (6)

$(f(x, y) \text{ and } g(y, z(x, y))) \Rightarrow f(x, z(x, y))$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $(f(x, y) \text{ and } f(x, z(x, y))) \Rightarrow g(y, z(x, y))$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $(f(z(x, y), z(x, y)) \text{ and } f(x, y)) \Rightarrow g(z(x, y), z(x, y))$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $f(z(x, y), z(x, y))$  or  $f(x, y)$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $g(z(x, y), z(x, y)) \Rightarrow f(x, y)$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $g(x, y)$  or  $g(z(x, y), z(x, y))$     cnf(clause<sub>6</sub>, negated\_conjecture)  
 $g(x, y) \Rightarrow \neg g(z(x, y), z(x, y))$     cnf(clause<sub>7</sub>, negated\_conjecture)

**SYN335+1.p** Church problem 46.14 (7)

$\exists x, y: \forall z: (\text{big\_f}(x, z) \Rightarrow (((\text{big\_f}(z, z) \Rightarrow \text{big\_g}(z, z)) \iff \text{big\_f}(x, y)) \Rightarrow (((\text{big\_g}(z, z) \Rightarrow \text{big\_f}(z, z)) \iff \text{big\_g}(x, y)) \Rightarrow (((\text{big\_g}(x, y) \Rightarrow \text{big\_f}(y, x)) \iff \text{big\_g}(y, z)) \Rightarrow (\text{big\_f}(z, y) \iff \text{big\_f}(y, x))))))$     fof(church\_46\_14<sub>7</sub>, conjecture)

**SYN335-1.p** Church problem 46.14 (7)

$f(x, z(x, y))$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $(f(z(x, y), z(x, y)) \text{ and } f(x, y)) \Rightarrow g(z(x, y), z(x, y))$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $f(z(x, y), z(x, y))$  or  $f(x, y)$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $g(z(x, y), z(x, y)) \Rightarrow f(x, y)$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $(g(z(x, y), z(x, y)) \text{ and } g(x, y)) \Rightarrow f(z(x, y), z(x, y))$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $g(z(x, y), z(x, y))$  or  $g(x, y)$     cnf(clause<sub>6</sub>, negated\_conjecture)  
 $f(z(x, y), z(x, y)) \Rightarrow g(x, y)$     cnf(clause<sub>7</sub>, negated\_conjecture)  
 $(g(x, y) \text{ and } g(y, z(x, y))) \Rightarrow f(y, x)$     cnf(clause<sub>8</sub>, negated\_conjecture)  
 $g(x, y)$  or  $g(y, z(x, y))$     cnf(clause<sub>9</sub>, negated\_conjecture)

$f(y, x) \Rightarrow g(y, z(x, y))$     cnf(*clause*<sub>10</sub>, *negated\_conjecture*)  
 $f(z(x, y), y) \text{ or } f(y, x)$     cnf(*clause*<sub>11</sub>, *negated\_conjecture*)  
 $f(z(x, y), y) \Rightarrow \neg f(y, x)$     cnf(*clause*<sub>12</sub>, *negated\_conjecture*)

**SYN336+1.p** Church problem 46.15 (1)

$\forall x: \exists y_1, y_2: \forall z: (\text{big\_f}(x, z) \Rightarrow (\text{big\_f}(y_1, z) \Rightarrow (\text{big\_f}(y_2, z) \Rightarrow (\text{big\_f}(y_1, x) \Rightarrow \text{big\_f}(z, y_2))))))$     fof(*church\_46\_15\_1*, *conjecture*)

**SYN336-1.p** Church problem 46.15 (1)

$f(a, z(y_1, y_2))$     cnf(*clause*<sub>1</sub>, *negated\_conjecture*)  
 $f(y_1, z(y_1, y_2))$     cnf(*clause*<sub>2</sub>, *negated\_conjecture*)  
 $f(y_2, z(y_1, y_2))$     cnf(*clause*<sub>3</sub>, *negated\_conjecture*)  
 $f(y_1, a)$     cnf(*clause*<sub>4</sub>, *negated\_conjecture*)  
 $\neg f(z(y_1, y_2), y_2)$     cnf(*clause*<sub>5</sub>, *negated\_conjecture*)

**SYN337+1.p** Church problem 46.15 (2)

$\forall x_1, x_2: \exists y: \forall z: (\text{big\_f}(x_1, y) \Rightarrow (\text{big\_f}(z, x_1) \Rightarrow (\text{big\_f}(z, y) \Rightarrow (\text{big\_f}(x_2, y) \text{ or } \text{big\_f}(x_2, z))))))$     fof(*church\_46\_15\_2*, *conjecture*)

**SYN337-1.p** Church problem 46.15 (2)

$f(a, y)$     cnf(*clause*<sub>1</sub>, *negated\_conjecture*)  
 $f(z(y), a)$     cnf(*clause*<sub>2</sub>, *negated\_conjecture*)  
 $f(z(y), y)$     cnf(*clause*<sub>3</sub>, *negated\_conjecture*)  
 $\neg f(b, y)$     cnf(*clause*<sub>4</sub>, *negated\_conjecture*)  
 $\neg f(b, z(y))$     cnf(*clause*<sub>5</sub>, *negated\_conjecture*)

**SYN338+1.p** Church problem 46.15 (3)

$\exists x: \forall y: \exists z: (\text{big\_f}(x, y) \Rightarrow (\text{big\_f}(z, x) \Rightarrow \text{big\_f}(y, y)))$     fof(*church\_46\_15\_3*, *conjecture*)

**SYN338-1.p** Church problem 46.15 (3)

$f(x, y(x))$     cnf(*clause*<sub>1</sub>, *negated\_conjecture*)  
 $f(z, x)$     cnf(*clause*<sub>2</sub>, *negated\_conjecture*)  
 $\neg f(y(x), y(x))$     cnf(*clause*<sub>3</sub>, *negated\_conjecture*)

**SYN339+1.p** Church problem 46.15 (4)

$\exists x: \forall y: \exists z: (\text{big\_f}(x, y, z) \Rightarrow \text{big\_f}(y, z, z))$     fof(*church\_46\_15\_4*, *conjecture*)

**SYN339-1.p** Church problem 46.15 (4)

$f(x, y(x), z)$     cnf(*clause*<sub>1</sub>, *negated\_conjecture*)  
 $\neg f(y(x), z, z)$     cnf(*clause*<sub>2</sub>, *negated\_conjecture*)

**SYN340+1.p** Church problem 46.15 (5)

$\exists x: \forall y: \exists z_1, z_2: (\text{big\_f}(x, y, z_1, z_2, z_1) \Rightarrow \text{big\_f}(z_1, x, y, z_1, z_2))$     fof(*church\_46\_15\_5*, *conjecture*)

**SYN340-1.p** Church problem 46.15 (5)

$f(x, y(x), z_1, z_2, z_1)$     cnf(*clause*<sub>1</sub>, *negated\_conjecture*)  
 $\neg f(z_1, x, y(x), z_1, z_2)$     cnf(*clause*<sub>2</sub>, *negated\_conjecture*)

**SYN341+1.p** Church problem 46.15 (6)

$\exists x_1: \forall x_2: \exists x_3: \forall x_4: (\text{big\_f}(x_1, x_2, x_3) \Rightarrow \text{big\_f}(x_2, x_3, x_4))$     fof(*church\_46\_15\_6*, *conjecture*)

**SYN341-1.p** Church problem 46.15 (6)

$f(y_1, y_2(y_1), y_3)$     cnf(*clause*<sub>1</sub>, *negated\_conjecture*)  
 $\neg f(y_2(y_1), y_3, y_4(y_1, y_3))$     cnf(*clause*<sub>2</sub>, *negated\_conjecture*)

**SYN342+1.p** Church problem 46.15 (7)

$\forall x_1: \exists x_2: \forall x_3: \exists x_4: (\text{big\_f}(x_1, x_2, x_3) \Rightarrow \text{big\_f}(x_4, x_4, x_1))$     fof(*church\_46\_15\_7*, *conjecture*)

**SYN342-1.p** Church problem 46.15 (7)

$f(a, y_2, y_3(y_2))$     cnf(*clause*<sub>1</sub>, *negated\_conjecture*)  
 $\neg f(y_4, y_4, a)$     cnf(*clause*<sub>2</sub>, *negated\_conjecture*)

**SYN343+1.p** Church problem 46.16 (2)

$\exists x, y_1, y_2: \forall z: (((\text{big\_f}(x, y_1) \Rightarrow \text{big\_f}(z, x)) \Rightarrow \text{big\_f}(x, x)) \Rightarrow (\text{big\_f}(x, x) \text{ and } \text{big\_f}(y_1, y_2)))$     fof(*church\_46\_16\_2*, *conjecture*)

**SYN343-1.p** Church problem 46.16 (2)

$f(a, y_1) \text{ or } f(a, a)$     cnf(*clause*<sub>1</sub>, *negated\_conjecture*)  
 $f(z(y_1, y_2), a) \Rightarrow f(a, a)$     cnf(*clause*<sub>2</sub>, *negated\_conjecture*)  
 $f(a, a) \Rightarrow \neg f(y_1, y_2)$     cnf(*clause*<sub>3</sub>, *negated\_conjecture*)

**SYN344+1.p** Church problem 46.16 (3)

$\forall x: \exists y_1, y_2: \forall z: (((\text{big\_f}(x, z) \Rightarrow (\text{big\_f}(y_1, z) \Rightarrow \text{big\_f}(y_2, x))) \Rightarrow \text{big\_f}(x, x)) \Rightarrow (\text{big\_f}(x, x) \text{ and } (\text{big\_f}(y_1, y_2) \Rightarrow \text{big\_f}(z, z))))))$  fof(church\_46\_16<sub>3</sub>, conjecture)

**SYN344-1.p** Church problem 46.16 (3)

$f(a, z(y_1, y_2))$  or  $f(a, a)$  cnf(clause<sub>1</sub>, negated\_conjecture)  
 $f(y_1, z(y_1, y_2))$  or  $f(a, a)$  cnf(clause<sub>2</sub>, negated\_conjecture)  
 $f(y_2, a) \Rightarrow f(a, a)$  cnf(clause<sub>3</sub>, negated\_conjecture)  
 $f(a, a) \Rightarrow f(y_1, y_2)$  cnf(clause<sub>4</sub>, negated\_conjecture)  
 $f(a, a) \Rightarrow \neg f(z(y_1, y_2), z(y_1, y_2))$  cnf(clause<sub>5</sub>, negated\_conjecture)

**SYN345+1.p** Church problem 46.16 (4)

$\forall x_1, x_2: \exists y_1, y_2: \forall z: (((\text{big\_f}(x_1, x_2, y_1) \Rightarrow \text{big\_f}(y_2, y_1, z)) \Rightarrow (\text{big\_f}(x_1, x_1, x_2) \Rightarrow \text{big\_f}(x_1, x_2, x_2))) \Rightarrow (((\text{big\_f}(x_2, y_1, y_2) \Rightarrow \text{big\_f}(y_1, z, z)) \Rightarrow (\text{big\_f}(x_1, x_2, x_2) \Rightarrow \text{big\_f}(x_1, x_1, x_2))) \Rightarrow (\text{big\_f}(y_1, y_2, z) \Rightarrow (\text{big\_f}(x_2, x_2, y_1) \text{ and } \text{big\_f}(x_1, x_2, x_2))))))$  fof(church\_46\_16<sub>4</sub>, conjecture)

**SYN345-1.p** Church problem 46.16 (4)

$f(a, a, b) \Rightarrow (f(a, b, y_1) \text{ or } f(a, b, b))$  cnf(clause<sub>1</sub>, negated\_conjecture)  
 $(f(y_2, y_1, z(y_1, y_2)) \text{ and } f(a, a, b)) \Rightarrow f(a, b, b)$  cnf(clause<sub>2</sub>, negated\_conjecture)  
 $f(a, b, b) \Rightarrow (f(b, y_1, y_2) \text{ or } f(a, a, b))$  cnf(clause<sub>3</sub>, negated\_conjecture)  
 $(f(y_1, z(y_1, y_2), z(y_1, y_2)) \text{ and } f(a, b, b)) \Rightarrow f(a, a, b)$  cnf(clause<sub>4</sub>, negated\_conjecture)  
 $f(y_1, y_2, z(y_1, y_2))$  or  $f(a, a, b)$  or  $f(a, b, b)$  cnf(clause<sub>5</sub>, negated\_conjecture)  
 $(f(a, a, b) \text{ and } f(a, b, b)) \Rightarrow f(y_1, y_2, z(y_1, y_2))$  cnf(clause<sub>6</sub>, negated\_conjecture)  
 $f(b, b, y_1) \Rightarrow (f(a, a, b) \text{ or } f(a, b, b))$  cnf(clause<sub>7</sub>, negated\_conjecture)  
 $(f(b, b, y_1) \text{ and } f(a, a, b)) \Rightarrow \neg f(a, b, b)$  cnf(clause<sub>8</sub>, negated\_conjecture)

**SYN346+1.p** Church problem 46.17 (2)

$\forall x_1, x_2: \exists y_1, y_2: \forall z_1, z_2: (\text{big\_f}(x_2, z_1) \Rightarrow (\text{big\_f}(y_1, z_2) \Rightarrow ((\text{big\_f}(y_1, z_1) \text{ and } \text{big\_f}(y_2, z_1)) \text{ or } (\text{big\_f}(x_2, z_2) \text{ and } \text{big\_f}(y_2, z_2))))$

**SYN346-1.p** Church problem 46.17 (2)

$f(b, z_1(y_1, y_2))$  cnf(clause<sub>1</sub>, negated\_conjecture)  
 $f(y_1, z_2(y_1, y_2))$  cnf(clause<sub>2</sub>, negated\_conjecture)  
 $f(y_1, z_1(y_1, y_2)) \Rightarrow \neg f(y_2, z_1(y_1, y_2))$  cnf(clause<sub>3</sub>, negated\_conjecture)  
 $f(b, z_2(y_1, y_2)) \Rightarrow \neg f(y_2, z_2(y_1, y_2))$  cnf(clause<sub>4</sub>, negated\_conjecture)

**SYN347+1.p** Church problem 46.17 (3)

$\forall z_1, z_2: \exists x_1, x_2: \forall y: (((\text{big\_f}(x_1, y) \iff \text{big\_f}(x_2, y)) \iff \text{big\_f}(z_1, z_2)) \text{ or } (\text{big\_f}(z_1, y) \iff \text{big\_f}(z_2, y)))$  fof(church\_46\_17\_3, conjecture)

**SYN347-1.p** Church problem 46.17 (3)

$f(x_2, y(x_1, x_2)) \Rightarrow (f(x_1, y(x_1, x_2)) \text{ or } f(a, b))$  cnf(clause<sub>1</sub>, negated\_conjecture)  
 $f(x_1, y(x_1, x_2)) \Rightarrow (f(x_2, y(x_1, x_2)) \text{ or } f(a, b))$  cnf(clause<sub>2</sub>, negated\_conjecture)  
 $(f(x_1, y(x_1, x_2)) \text{ and } f(x_2, y(x_1, x_2))) \Rightarrow \neg f(a, b)$  cnf(clause<sub>3</sub>, negated\_conjecture)  
 $f(a, b) \Rightarrow (f(x_1, y(x_1, x_2)) \text{ or } f(x_2, y(x_1, x_2)))$  cnf(clause<sub>4</sub>, negated\_conjecture)  
 $f(a, y(x_1, x_2))$  or  $f(b, y(x_1, x_2))$  cnf(clause<sub>5</sub>, negated\_conjecture)  
 $f(a, y(x_1, x_2)) \Rightarrow \neg f(b, y(x_1, x_2))$  cnf(clause<sub>6</sub>, negated\_conjecture)

**SYN348+1.p** Church problem 46.17 (4)

$\exists x_1: \forall x_2: \exists x_3: \forall x_4: (((\text{big\_f}(x_1, x_4) \iff \text{big\_f}(x_4, x_3)) \iff \text{big\_f}(x_3, x_4)) \iff \text{big\_f}(x_4, x_1)) \text{ and } (((\text{big\_f}(x_2, x_4) \iff \text{big\_f}(x_4, x_3)) \iff \text{big\_f}(x_3, x_4)) \iff \text{big\_f}(x_4, x_2)))$  fof(church\_46\_17\_4, conjecture)

**SYN348-1.p** Church problem 46.17 (4)

$(f(x, g(x, y)) \text{ and } f(y, g(x, y)) \text{ and } f(w(x), g(x, y))) \Rightarrow (f(g(x, y), y) \text{ or } f(g(x, y), x) \text{ or } f(g(x, y), w(x)))$  cnf(clause<sub>1</sub>, negated\_conjecture)  
 $(f(x, g(x, y)) \text{ and } f(y, g(x, y)) \text{ and } f(g(x, y), w(x))) \Rightarrow (f(g(x, y), y) \text{ or } f(g(x, y), x) \text{ or } f(w(x), g(x, y)))$  cnf(clause<sub>2</sub>, negated\_conjecture)  
 $(f(g(x, y), y) \text{ and } f(y, g(x, y))) \Rightarrow (f(x, g(x, y)) \text{ or } f(g(x, y), x) \text{ or } f(w(x), g(x, y)) \text{ or } f(g(x, y), w(x)))$  cnf(clause<sub>3</sub>, negated\_conjecture)  
 $(f(g(x, y), y) \text{ and } f(y, g(x, y)) \text{ and } f(w(x), g(x, y)) \text{ and } f(g(x, y), w(x))) \Rightarrow (f(x, g(x, y)) \text{ or } f(g(x, y), x))$  cnf(clause<sub>4</sub>, negated\_conjecture)  
 $f(x, g(x, y))$  or  $f(g(x, y), y)$  or  $f(y, g(x, y))$  or  $f(g(x, y), x)$  or  $f(w(x), g(x, y))$  or  $f(g(x, y), w(x))$  cnf(clause<sub>5</sub>, negated\_conjecture)  
 $(f(w(x), g(x, y)) \text{ and } f(g(x, y), w(x))) \Rightarrow (f(x, g(x, y)) \text{ or } f(g(x, y), y) \text{ or } f(y, g(x, y)) \text{ or } f(g(x, y), x))$  cnf(clause<sub>6</sub>, negated\_conjecture)  
 $(f(x, g(x, y)) \text{ and } f(g(x, y), y) \text{ and } f(w(x), g(x, y))) \Rightarrow (f(y, g(x, y)) \text{ or } f(g(x, y), x) \text{ or } f(g(x, y), w(x)))$  cnf(clause<sub>7</sub>, negated\_conjecture)  
 $(f(x, g(x, y)) \text{ and } f(g(x, y), y) \text{ and } f(g(x, y), w(x))) \Rightarrow (f(y, g(x, y)) \text{ or } f(g(x, y), x) \text{ or } f(w(x), g(x, y)))$  cnf(clause<sub>8</sub>, negated\_conjecture)  
 $(f(x, g(x, y)) \text{ and } f(g(x, y), x)) \Rightarrow (f(g(x, y), y) \text{ or } f(y, g(x, y)) \text{ or } f(w(x), g(x, y)) \text{ or } f(g(x, y), w(x)))$  cnf(clause<sub>9</sub>, negated\_conjecture)  
 $(f(x, g(x, y)) \text{ and } f(g(x, y), x) \text{ and } f(w(x), g(x, y)) \text{ and } f(g(x, y), w(x))) \Rightarrow (f(g(x, y), y) \text{ or } f(y, g(x, y)))$  cnf(clause<sub>10</sub>, negated\_conjecture)  
 $(f(g(x, y), y) \text{ and } f(g(x, y), x) \text{ and } f(w(x), g(x, y))) \Rightarrow (f(x, g(x, y)) \text{ or } f(y, g(x, y)) \text{ or } f(g(x, y), w(x)))$  cnf(clause<sub>11</sub>, negated\_conjecture)  
 $(f(g(x, y), y) \text{ and } f(g(x, y), x) \text{ and } f(g(x, y), w(x))) \Rightarrow (f(x, g(x, y)) \text{ or } f(y, g(x, y)) \text{ or } f(w(x), g(x, y)))$  cnf(clause<sub>12</sub>, negated\_conjecture)  
 $(f(y, g(x, y)) \text{ and } f(g(x, y), x) \text{ and } f(w(x), g(x, y))) \Rightarrow (f(x, g(x, y)) \text{ or } f(g(x, y), y) \text{ or } f(g(x, y), w(x)))$  cnf(clause<sub>13</sub>, negated\_conjecture)  
 $(f(y, g(x, y)) \text{ and } f(g(x, y), x) \text{ and } f(g(x, y), w(x))) \Rightarrow (f(x, g(x, y)) \text{ or } f(g(x, y), y) \text{ or } f(w(x), g(x, y)))$  cnf(clause<sub>14</sub>, negated\_conjecture)  
 $(f(x, g(x, y)) \text{ and } f(g(x, y), y) \text{ and } f(y, g(x, y)) \text{ and } f(g(x, y), x)) \Rightarrow (f(w(x), g(x, y)) \text{ or } f(g(x, y), w(x)))$  cnf(clause<sub>15</sub>, negated\_conjecture)

$(f(x, g(x, y)) \text{ and } f(g(x, y), y) \text{ and } f(y, g(x, y)) \text{ and } f(g(x, y), x) \text{ and } f(w(x), g(x, y))) \Rightarrow \neg f(g(x, y), w(x))$     cnf(clause<sub>16</sub>)

**SYN349+1.p** Church problem 46.17 (5)

$\exists x_1: \forall x_2: \exists x_3: \forall x_4: ((\text{big\_f}(x_1, x_4) \iff \text{big\_f}(x_2, x_4)) \Rightarrow (((\text{big\_f}(x_1, x_4) \iff \text{big\_f}(x_4, x_3)) \iff \text{big\_f}(x_3, x_4)) \iff \text{big\_f}(x_4, x_2)))$     fof(church\_46\_17<sub>5</sub>, conjecture)

**SYN349-1.p** Church problem 46.17 (5)

$f(w(x), g(x, y)) \Rightarrow f(x, g(x, y))$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $f(x, g(x, y)) \Rightarrow f(w(x), g(x, y))$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $(f(x, g(x, y)) \text{ and } f(y, g(x, y))) \Rightarrow (f(g(x, y), y) \text{ or } f(g(x, y), w(x)))$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $(f(g(x, y), y) \text{ and } f(y, g(x, y))) \Rightarrow (f(x, g(x, y)) \text{ or } f(g(x, y), w(x)))$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $f(x, g(x, y)) \text{ or } f(g(x, y), y) \text{ or } f(y, g(x, y)) \text{ or } f(g(x, y), w(x))$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $(f(x, g(x, y)) \text{ and } f(g(x, y), y)) \Rightarrow (f(y, g(x, y)) \text{ or } f(g(x, y), w(x)))$     cnf(clause<sub>6</sub>, negated\_conjecture)  
 $(f(x, g(x, y)) \text{ and } f(g(x, y), w(x))) \Rightarrow (f(g(x, y), y) \text{ or } f(y, g(x, y)))$     cnf(clause<sub>7</sub>, negated\_conjecture)  
 $(f(g(x, y), y) \text{ and } f(g(x, y), w(x))) \Rightarrow (f(x, g(x, y)) \text{ or } f(y, g(x, y)))$     cnf(clause<sub>8</sub>, negated\_conjecture)  
 $(f(y, g(x, y)) \text{ and } f(g(x, y), w(x))) \Rightarrow (f(x, g(x, y)) \text{ or } f(g(x, y), y))$     cnf(clause<sub>9</sub>, negated\_conjecture)  
 $(f(x, g(x, y)) \text{ and } f(g(x, y), y) \text{ and } f(y, g(x, y))) \Rightarrow \neg f(g(x, y), w(x))$     cnf(clause<sub>10</sub>, negated\_conjecture)

**SYN350+1.p** Church problem 46.18 (2)

$\forall x: \exists y_1, y_2: \forall z: ((\text{big\_f}(x, z) \iff \text{big\_f}(z, x)) \Rightarrow (\text{big\_f}(x, z) \iff (\text{big\_f}(y_2, z) \text{ and } (\text{big\_f}(y_1, z) \Rightarrow \text{big\_f}(y_1, y_2))))))$     fof(ch

**SYN350-1.p** Church problem 46.18 (2)

$f(a, z(x, y)) \Rightarrow f(z(x, y), a)$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $f(z(x, y), a) \Rightarrow f(a, z(x, y))$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $f(a, z(x, y)) \text{ or } f(y, z(x, y)) \text{ or } f(x, z(x, y))$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $(f(a, z(x, y)) \text{ and } f(y, z(x, y))) \Rightarrow f(x, z(x, y))$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $f(x, y) \Rightarrow (f(a, z(x, y)) \text{ or } f(y, z(x, y)))$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $(f(a, z(x, y)) \text{ and } f(y, z(x, y))) \Rightarrow \neg f(x, y)$     cnf(clause<sub>6</sub>, negated\_conjecture)

**SYN351+1.p** Church problem 46.18 (3)

$\forall x_1, x_2: \exists y_1, y_2: \forall z: (\text{big\_f}(x_1, y_2, x_1, z) \Rightarrow ((\text{big\_f}(x_1, y_1, x_1, y_2) \iff \text{big\_f}(y_1, x_2, y_1, y_2)) \Rightarrow (\text{big\_f}(x_1, y_1, x_1, y_2) \Rightarrow (\text{big\_f}(x_1, y_2, y_1, y_2) \Rightarrow \text{big\_f}(x_1, z, y_1, z)) \text{ and } (\text{big\_f}(x_1, z, y_1, z) \Rightarrow (\text{big\_f}(x_1, y_1, x_1, y_2) \iff \text{big\_f}(x_1, y_2, y_1, y_2))))))$     fo

**SYN351-1.p** Church problem 46.18 (3)

$f(a, y, a, z(x, y))$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $f(x, b, x, y) \Rightarrow f(a, x, a, y)$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $f(a, x, a, y) \Rightarrow f(x, b, x, y)$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $f(a, x, a, y) \text{ or } f(a, z(x, y), x, z(x, y))$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $f(a, x, a, y) \text{ or } f(a, y, x, y)$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $f(a, y, x, y) \text{ or } f(a, z(x, y), x, z(x, y))$     cnf(clause<sub>6</sub>, negated\_conjecture)  
 $(f(a, z(x, y), x, z(x, y)) \text{ and } f(a, x, a, y)) \Rightarrow \neg f(a, y, x, y)$     cnf(clause<sub>7</sub>, negated\_conjecture)

**SYN352+1.p** Church problem 46.18 (4)

$\forall x_1, x_2: \exists y_1, y_2: \forall z: (\text{big\_f}(x_1, x_2) \Rightarrow ((\text{big\_f}(y_1, y_2) \Rightarrow (\text{big\_f}(x_2, z) \text{ or } \text{big\_f}(y_2, z))) \Rightarrow (((\text{big\_f}(y_1, y_2) \Rightarrow (\text{big\_f}(x_2, z) \iff \text{big\_f}(y_1, z))) \Rightarrow \text{big\_f}(z, z)) \Rightarrow (\text{big\_f}(y_1, y_2) \text{ and } (\text{big\_f}(y_1, z) \iff \text{big\_f}(y_2, z))))))$     fof(church\_46\_18<sub>4</sub>,

**SYN352-1.p** Church problem 46.18 (4)

$f(a, b)$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $f(x, y) \Rightarrow (f(b, z(x, y)) \text{ or } f(y, z(x, y)))$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $f(x, y) \text{ or } f(z(x, y), z(x, y))$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $f(b, z(x, y)) \text{ or } f(x, z(x, y)) \text{ or } f(z(x, y), z(x, y))$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $(f(b, z(x, y)) \text{ and } f(x, z(x, y))) \Rightarrow f(z(x, y), z(x, y))$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $(f(x, y) \text{ and } f(x, z(x, y))) \Rightarrow \neg f(y, z(x, y))$     cnf(clause<sub>6</sub>, negated\_conjecture)  
 $f(x, y) \Rightarrow (f(x, z(x, y)) \text{ or } f(y, z(x, y)))$     cnf(clause<sub>7</sub>, negated\_conjecture)

**SYN353+1.p** Church problem 46.18 (5)

$\forall x: \exists y_1, y_2, y_3: \forall z: ((\text{big\_f}(y_1, y_2, y_3) \Rightarrow \text{big\_f}(x, x, z) \Rightarrow (\text{big\_f}(y_2, y_3, y_1) \text{ or } \text{big\_f}(y_3, y_1, y_2)))) \Rightarrow (((\text{big\_f}(y_3, y_1, y_2) \Rightarrow (\text{big\_f}(y_1, y_2, y_3) \text{ and } \text{big\_f}(y_2, y_3, y_1))) \iff \text{big\_f}(y_2, y_1, z)) \Rightarrow (((\text{big\_f}(y_2, y_3, y_1) \Rightarrow (\text{big\_f}(y_1, y_2, y_3) \text{ and } \text{big\_f}(y_3, y_1, y_2))) \text{ big\_f}(y_1, z, y_2)) \Rightarrow (((\text{big\_f}(y_3, y_1, y_2) \Rightarrow \neg \text{big\_f}(y_2, y_3, y_1)) \Rightarrow \text{big\_f}(y_1, y_2, y_3)) \iff \text{big\_f}(z, y_2, y_1)) \Rightarrow ((\text{big\_f}(y_1, y_2, y_3) \text{ and } \text{big\_f}(y_2, y_3, y_1) \text{ and } \text{big\_f}(y_3, y_1, y_2)) \iff \text{big\_f}(z, z, z))))))$     fof(church\_46\_18<sub>5</sub>, conjecture)

**SYN353-1.p** Church problem 46.18 (5)

$(f(y_1, y_2, y_3) \text{ and } f(a, a, z(y_1, y_2, y_3))) \Rightarrow (f(y_2, y_3, y_1) \text{ or } f(y_3, y_1, y_2))$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $(f(y_3, y_1, y_2) \text{ and } f(y_2, y_1, z(y_1, y_2, y_3))) \Rightarrow f(y_1, y_2, y_3)$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $(f(y_3, y_1, y_2) \text{ and } f(y_2, y_1, z(y_1, y_2, y_3))) \Rightarrow f(y_2, y_3, y_1)$     cnf(clause<sub>3</sub>, negated\_conjecture)



$f(y_3, y_1, y_2)$  or  $f(y_2, y_1, z(y_1, y_2, y_3))$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $(f(y_1, y_2, y_3) \text{ and } f(y_2, y_3, y_1)) \Rightarrow f(y_2, y_1, z(y_1, y_2, y_3))$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $(f(y_2, y_3, y_1) \text{ and } f(y_1, z(y_1, y_2, y_3), y_2)) \Rightarrow f(y_1, y_2, y_3)$     cnf(clause<sub>6</sub>, negated\_conjecture)  
 $(f(y_2, y_3, y_1) \text{ and } f(y_1, z(y_1, y_2, y_3), y_2)) \Rightarrow f(y_3, y_1, y_2)$     cnf(clause<sub>7</sub>, negated\_conjecture)  
 $f(y_2, y_3, y_1)$  or  $f(y_1, z(y_1, y_2, y_3), y_2)$     cnf(clause<sub>8</sub>, negated\_conjecture)  
 $(f(y_1, y_2, y_3) \text{ and } f(y_3, y_1, y_2)) \Rightarrow f(y_1, z(y_1, y_2, y_3), y_2)$     cnf(clause<sub>9</sub>, negated\_conjecture)  
 $f(z(y_1, y_2, y_3), y_2, y_1) \Rightarrow (f(y_3, y_1, y_2) \text{ or } f(y_1, y_2, y_3))$     cnf(clause<sub>10</sub>, negated\_conjecture)  
 $f(z(y_1, y_2, y_3), y_2, y_1) \Rightarrow (f(y_2, y_3, y_1) \text{ or } f(y_1, y_2, y_3))$     cnf(clause<sub>11</sub>, negated\_conjecture)  
 $(f(y_3, y_1, y_2) \text{ and } f(y_2, y_3, y_1)) \Rightarrow f(z(y_1, y_2, y_3), y_2, y_1)$     cnf(clause<sub>12</sub>, negated\_conjecture)  
 $f(y_1, y_2, y_3) \Rightarrow f(z(y_1, y_2, y_3), y_2, y_1)$     cnf(clause<sub>13</sub>, negated\_conjecture)  
 $f(y_1, y_2, y_3)$  or  $f(z(y_1, y_2, y_3), z(y_1, y_2, y_3), z(y_1, y_2, y_3))$     cnf(clause<sub>14</sub>, negated\_conjecture)  
 $f(y_2, y_3, y_1)$  or  $f(z(y_1, y_2, y_3), z(y_1, y_2, y_3), z(y_1, y_2, y_3))$     cnf(clause<sub>15</sub>, negated\_conjecture)  
 $f(y_3, y_1, y_2)$  or  $f(z(y_1, y_2, y_3), z(y_1, y_2, y_3), z(y_1, y_2, y_3))$     cnf(clause<sub>16</sub>, negated\_conjecture)  
 $(f(y_1, y_2, y_3) \text{ and } f(y_2, y_3, y_1) \text{ and } f(y_3, y_1, y_2)) \Rightarrow \neg f(z(y_1, y_2, y_3), z(y_1, y_2, y_3), z(y_1, y_2, y_3))$     cnf(clause<sub>17</sub>, negated\_conjecture)

**SYN354+1.p** Church problem 46.20 (1)

$\forall x_1, x_2: \exists y_1, y_2: \forall z: (\text{big\_f}(x_1, x_2) \Rightarrow (\text{big\_g}(x_1, x_2) \Rightarrow (((\text{big\_g}(x_2, z) \iff \text{big\_g}(y_2, z)) \Rightarrow (\text{big\_f}(y_1, y_2) \Rightarrow \text{big\_f}(x_2, y_2)))) \Rightarrow ((\text{big\_g}(x_2, z) \iff \text{big\_g}(y_1, z)) \Rightarrow (\text{big\_f}(x_1, y_1) \text{ and } \text{big\_f}(x_2, y_1) \text{ and } \text{big\_f}(y_1, y_2))))))$     fof(church\_46)

**SYN354-1.p** Church problem 46.20 (1)

$f(a, b)$     cnf(clause<sub>1</sub>, negated\_conjecture)  
 $g(a, b)$     cnf(clause<sub>2</sub>, negated\_conjecture)  
 $f(y_1, y_2) \Rightarrow (g(b, z(y_1, y_2)) \text{ or } g(y_2, z(y_1, y_2)) \text{ or } f(b, y_2))$     cnf(clause<sub>3</sub>, negated\_conjecture)  
 $(g(b, z(y_1, y_2)) \text{ and } g(y_2, z(y_1, y_2)) \text{ and } f(y_1, y_2)) \Rightarrow f(b, y_2)$     cnf(clause<sub>4</sub>, negated\_conjecture)  
 $g(y_1, z(y_1, y_2)) \Rightarrow g(b, z(y_1, y_2))$     cnf(clause<sub>5</sub>, negated\_conjecture)  
 $g(b, z(y_1, y_2)) \Rightarrow g(y_1, z(y_1, y_2))$     cnf(clause<sub>6</sub>, negated\_conjecture)  
 $(f(a, y_1) \text{ and } f(b, y_1)) \Rightarrow \neg f(y_1, y_2)$     cnf(clause<sub>7</sub>, negated\_conjecture)

**SYN355+1.p** Peter Andrews Problem X2106

$(\forall x: (\text{big\_r}(x) \Rightarrow \text{big\_p}(x)) \text{ and } \forall x: (\neg \text{big\_q}(x) \Rightarrow \text{big\_r}(x))) \Rightarrow \forall x: (\text{big\_p}(x) \text{ or } \text{big\_q}(x))$     fof(x<sub>2106</sub>, conjecture)

**SYN355^5.p** TPS problem X2106

$cQ: \$i \rightarrow \$o$     thf(cQ, type)  
 $cP: \$i \rightarrow \$o$     thf(cP, type)  
 $cR: \$i \rightarrow \$o$     thf(cR, type)  
 $(\forall xx: \$i: ((cR@xx) \Rightarrow (cP@xx)) \text{ and } \forall xx: \$i: (\neg cQ@xx \Rightarrow (cR@xx))) \Rightarrow \forall xx: \$i: (cP@xx \text{ or } cQ@xx)$     thf(cX<sub>2106</sub>, conjecture)

**SYN356+1.p** Peter Andrews Problem X2107

$(\text{big\_r}(a, b) \text{ and } \forall x, y: (\text{big\_r}(x, y) \Rightarrow (\text{big\_r}(y, x) \text{ and } \text{big\_q}(x, y))) \text{ and } \forall u, v: (\text{big\_q}(u, v) \Rightarrow \text{big\_q}(u, u))) \Rightarrow (\text{big\_q}(a, a) \text{ and } \text{big\_q}(b, b))$     fof(x<sub>2107</sub>, conjecture)

**SYN356^5.p** TPS problem from BASIC-FO-THMS

$cB: \$i$     thf(cB, type)  
 $cQ: \$i \rightarrow \$i \rightarrow \$o$     thf(cQ, type)  
 $cA: \$i$     thf(cA, type)  
 $cR: \$i \rightarrow \$i \rightarrow \$o$     thf(cR, type)  
 $(cR@cA@cB \text{ and } \forall x: \$i, y: \$i: ((cR@x@y) \Rightarrow (cR@y@x \text{ and } cQ@x@y)) \text{ and } \forall u: \$i, v: \$i: ((cQ@u@v) \Rightarrow (cQ@u@u))) \Rightarrow (cQ@cA@cA \text{ and } cQ@cB@cB)$     thf(cLX<sub>2107</sub>, conjecture)

**SYN357+1.p** Peter Andrews Problem X2108

$\forall x: \exists y: (\text{big\_p}(x) \Rightarrow \text{big\_p}(y))$     fof(x<sub>2108</sub>, conjecture)

**SYN357^5.p** TPS problem from BASIC-FO-THMS

$cP: \$i \rightarrow \$o$     thf(cP, type)  
 $\forall x: \$i: \exists y: \$i: ((cP@x) \Rightarrow (cP@y))$     thf(cLX<sub>2108</sub>, conjecture)

**SYN357^7.p** Peter Andrews Problem X2108

include('Axioms/LCL015^0.ax')  
include('Axioms/LCL013^5.ax')  
include('Axioms/LCL015^1.ax')  
 $\text{big\_p}: \text{mu} \rightarrow \$i \rightarrow \$o$     thf(big\_p.type, type)  
 $\text{mvalid}@(\text{mbox\_s}_4@(\text{mforall\_ind}@ \lambda x: \text{mu}: (\text{mexists\_ind}@ \lambda y: \text{mu}: (\text{mbox\_s}_4@(\text{mimplies}@(\text{mbox\_s}_4@(\text{big\_p}@x))@(\text{mbox\_s}_4@(\text{big\_p}@y))$

**SYN358+1.p** Peter Andrews Problem X2109

$\exists x: (p \text{ and } \text{big\_q}(x)) \iff (p \text{ and } \exists x: \text{big\_q}(x))$     fof(x<sub>2109</sub>, conjecture)

**SYN358**<sup>5.p</sup> TPS problem X2109

cQ: \$i → \$o thf(cQ, type)

p: \$o thf(p, type)

∃xx: \$i: (p and cQ@xx) ⇔ (p and ∃xx: \$i: (cQ@xx)) thf(cX<sub>2109</sub>, conjecture)**SYN359**+1.p Peter Andrews Problem X2110

(∃x: big\_r(x) and ∀y: (big\_r(y) ⇒ ∃z: big\_q(y, z)) and ∀x, y: (big\_q(x, y) ⇒ big\_q(x, x))) ⇒ ∃x, y: (big\_q(x, y) and big\_r(y))

**SYN360**+1.p Peter Andrews Problem X2111(∀x: (∃y: big\_p(x, y) ⇒ ∀y: big\_q(x, y)) and ∀z: ∃y: big\_p(z, y) ⇒ ∀y, x: big\_q(x, y) fof(x<sub>2111</sub>, conjecture)**SYN360**<sup>5.p</sup> TPS problem X2111A

Variant of X2111 for testing infix mechanism.

cQ: \$i → \$i → \$o thf(cQ, type)

c\_less.: \$i → \$i → \$o thf(c\_less., type)

(∀xx: \$i: (∃xy: \$i: (c\_less.@xx@xy) ⇒ ∀xy: \$i: (cQ@xx@xy)) and ∀xz: \$i: ∃xy: \$i: (c\_less.@xz@xy)) ⇒ ∀xy: \$i, xx: \$i: (cQ@xx@xy)

**SYN361**+1.p Peter Andrews Problem X2112(∃v: ∀x: big\_p(x, v) and ∀x: (big\_s(x) ⇒ ∃y: big\_q(y, x)) and ∀x, y: (big\_p(x, y) ⇒ ¬big\_q(x, y))) ⇒ ∃u: ¬big\_s(u) fof(x<sub>2112</sub>, conjecture)**SYN361**<sup>5.p</sup> TPS problem X2112

cS: \$i → \$o thf(cS, type)

cQ: \$i → \$i → \$o thf(cQ, type)

cP: \$i → \$i → \$o thf(cP, type)

(∃xv: \$i: ∀xx: \$i: (cP@xx@xv) and ∀xx: \$i: ((cS@xx) ⇒ ∃xy: \$i: (cQ@xy@xx)) and ∀xx: \$i, xy: \$i: ((cP@xx@xy) ⇒ ¬cQ@xx@xy)) ⇒ ∃xu: \$i: ¬cS@xu thf(cX<sub>2112</sub>, conjecture)**SYN362**+1.p Peter Andrews Problem X2113(∀y: ∃w: big\_r(y, w) and ∃z: ∀x: (big\_p(x) ⇒ ¬big\_r(z, x))) ⇒ ∃x: ¬big\_p(x) fof(x<sub>2113</sub>, conjecture)**SYN363**+1.p Peter Andrews Problem X2114(∀x: big\_r(x, b) and ∀y: (∃z: big\_r(y, z) ⇒ big\_r(a, y))) ⇒ ∃u: ∀v: big\_r(u, v) fof(x<sub>2114</sub>, conjecture)**SYN364**+1.p Peter Andrews Problem X2115(∀x: (∃y: big\_p(x, y) ⇒ ∀z: big\_p(z, z)) and ∀u: ∃v: (big\_p(u, v) or (big\_m(u) and big\_q(f(u, v)))) and ∀w: (big\_q(w) ⇒ ¬big\_m(g(w)))) ⇒ ∃u: ∃v: (big\_p(g(u), v) and big\_p(u, u)) fof(x<sub>2115</sub>, conjecture)**SYN364**<sup>5.p</sup> TPS problem X2115

cP: \$i → \$i → \$o thf(cP, type)

g: \$i → \$i thf(g, type)

cM: \$i → \$o thf(cM, type)

cQ: \$i → \$o thf(cQ, type)

f: \$i → \$i → \$i thf(f, type)

(∀xx: \$i: (∃xy: \$i: (cP@xx@xy) ⇒ ∀xz: \$i: (cP@xz@xz)) and ∀xu: \$i: ∃xv: \$i: (cP@xu@xv or (cM@xu and cQ@(f@xu@xv))) ⇒ ¬cM@(g@xw))) ⇒ ∃xu: \$i: ∃xv: \$i: (cP@(g@xu)@xv and cP@xu@xu) thf(cX<sub>2115</sub>, conjecture)**SYN365**+1.p Peter Andrews Problem X2116(∀x: ∃y: (big\_p(x) ⇒ (big\_r(x, g(h(y))) and big\_p(y))) and ∀w: (big\_p(w) ⇒ (big\_p(g(w)) and big\_p(h(w))))) ⇒ ∃x: (big\_p(x) ⇒ ∃y: (big\_r(x, y) and big\_p(y))) fof(x<sub>2116</sub>, conjecture)**SYN365**<sup>5.p</sup> TPS problem X2116

cP: \$i → \$o thf(cP, type)

cR: \$i → \$i → \$o thf(cR, type)

h: \$i → \$i thf(h, type)

g: \$i → \$i thf(g, type)

(∀xx: \$i: ∃xy: \$i: ((cP@xx) ⇒ (cR@xx@(g@(h@xy)) and cP@xy)) and ∀xw: \$i: ((cP@xw) ⇒ (cP@(g@xw) and cP@(h@xw))) ⇒ ∃xy: \$i: (cR@xx@xy and cP@xy)) thf(cX<sub>2116</sub>, conjecture)**SYN366**+1.p Peter Andrews Problem X2117(∀u, v: (big\_r(u, u) ⇔ big\_r(u, v)) and ∀w, z: (big\_r(w, w) ⇔ big\_r(z, w))) ⇒ (∃x: big\_r(x, x) ⇒ ∀y: big\_r(y, y)) fof(x<sub>2117</sub>, conjecture)**SYN367**+1.p Peter Andrews Problem X2118∀x: ((p and big\_q(x)) or (¬p and big\_r(x))) ⇒ (∀x: big\_q(x) or ∀x: big\_r(x)) fof(x<sub>2118</sub>, conjecture)**SYN367**<sup>7.p</sup> Peter Andrews Problem X2118

include('Axioms/LCL015^0.ax')

include('Axioms/LCL013^5.ax')

include('Axioms/LCL015^1.ax')

$p: \$i \rightarrow \$o \quad \text{thf}(p\_type, \text{type})$   
 $\text{big\_r}: \mu u \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{big\_r\_type}, \text{type})$   
 $\text{big\_q}: \mu u \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{big\_q\_type}, \text{type})$   
 $\text{mvalid}@(\text{mbox\_s}_4@(\text{mimplies}@(\text{mbox\_s}_4@(\text{mforall\_ind}@ \lambda x: \mu u: (\text{mor}@(\text{mand}@(\text{mbox\_s}_4@p))@(\text{mbox\_s}_4@(\text{big\_q}@x))))@(\text{mand}$

**SYN368+1.p** Peter Andrews Problem X2119  
 $\exists y: \forall x: (\text{big\_p}(y) \Rightarrow \text{big\_p}(x)) \quad \text{fof}(x_{2119}, \text{conjecture})$

**SYN369+1.p** Peter Andrews Problem X2120  
 $\forall u, v, w: (\text{big\_p}(u, v) \text{ or } \text{big\_p}(v, w)) \Rightarrow \exists x: \forall y: \text{big\_p}(x, y) \quad \text{fof}(x_{2120}, \text{conjecture})$

**SYN370+1.p** Peter Andrews Problem X2121  
 $\exists v: \forall y: \exists z: ((\text{big\_p}(a, y, h(y)) \text{ or } \text{big\_p}(v, y, f(y))) \Rightarrow \text{big\_p}(v, y, z)) \quad \text{fof}(x_{2121}, \text{conjecture})$

**SYN371+1.p** Peter Andrews Problem X2122  
 $(\exists x: \text{big\_r}(x, x) \Rightarrow \forall y: \text{big\_r}(y, y)) \Rightarrow \exists u: \forall v: (\text{big\_r}(u, u) \Rightarrow \text{big\_r}(v, v)) \quad \text{fof}(x_{2122}, \text{conjecture})$

**SYN372+1.p** Peter Andrews Problem X2123  
 $\forall x: (\exists y: (\text{big\_p}(y) \Rightarrow \text{big\_q}(x)) \Rightarrow \exists y: (\text{big\_p}(y) \Rightarrow \text{big\_q}(y))) \quad \text{fof}(x_{2123}, \text{conjecture})$

**SYN373+1.p** Peter Andrews Problem X2124  
 $\exists x: (\text{big\_p}(x) \Rightarrow \text{big\_q}(x)) \iff (\forall x: \text{big\_p}(x) \Rightarrow \exists x: \text{big\_q}(x)) \quad \text{fof}(x_{2124}, \text{conjecture})$

**SYN374+1.p** Peter Andrews Problem X2125  
 $\exists x: \forall y: (\text{big\_p}(x) \iff \text{big\_p}(y)) \iff (\exists x: \text{big\_p}(x) \iff \forall y: \text{big\_p}(y)) \quad \text{fof}(x_{2125}, \text{conjecture})$

**SYN374^5.p** TPS problem X2125  
 $\text{cP}: \$i \rightarrow \$o \quad \text{thf}(\text{cP}, \text{type})$   
 $\exists xx: \$i: \forall xy: \$i: ((\text{cP}@xx) \iff (\text{cP}@xy)) \iff (\exists xx: \$i: (\text{cP}@xx) \iff \forall xy: \$i: (\text{cP}@xy)) \quad \text{thf}(\text{cX}_{2125}, \text{conjecture})$

**SYN375+1.p** Peter Andrews Problem X2126  
 $\forall x: (\text{big\_p}(x) \iff \exists y: \text{big\_p}(y)) \iff (\forall x: \text{big\_p}(x) \iff \exists y: \text{big\_p}(y)) \quad \text{fof}(x_{2126}, \text{conjecture})$

**SYN375^5.p** TPS problem from BASIC-FO-THMS  
 $\text{cP}: \$i \rightarrow \$o \quad \text{thf}(\text{cP}, \text{type})$   
 $((\forall xx: \$i: (\text{cP}@xx) \Rightarrow \exists xy: \$i: (\text{cP}@xy)) \text{ and } (\exists xy: \$i: (\text{cP}@xy) \Rightarrow \forall xx: \$i: (\text{cP}@xx))) \Rightarrow (\exists xy: \$i: (\text{cP}@xy) \iff \forall xx: \$i: (\text{cP}@xx)) \quad \text{thf}(\text{cX}_{2126\_BUG}, \text{conjecture})$

**SYN376+1.p** Peter Andrews Problem X2127  
 $\exists x: \forall y: (\text{big\_p}(y) \iff \text{big\_p}(x)) \Rightarrow (\forall x: \text{big\_p}(x) \text{ or } \forall x: \neg \text{big\_p}(x)) \quad \text{fof}(x_{2127}, \text{conjecture})$

**SYN377+1.p** Peter Andrews Problem X2128  
 $\forall x: (\text{big\_p}(x) \iff \forall y: \text{big\_p}(y)) \iff (\exists x: \text{big\_p}(x) \iff \forall y: \text{big\_p}(y)) \quad \text{fof}(x_{2128}, \text{conjecture})$

**SYN377^5.p** TPS problem X2128  
 $\text{cP}: \$i \rightarrow \$o \quad \text{thf}(\text{cP}, \text{type})$   
 $\forall xx: \$i: ((\text{cP}@xx) \iff \forall xy: \$i: (\text{cP}@xy)) \iff (\exists xx: \$i: (\text{cP}@xx) \iff \forall xy: \$i: (\text{cP}@xy)) \quad \text{thf}(\text{cX}_{2128}, \text{conjecture})$

**SYN377^7.p** Peter Andrews Problem X2128  
 $\text{include}('Axioms/LCL015^0.ax')$   
 $\text{include}('Axioms/LCL013^5.ax')$   
 $\text{include}('Axioms/LCL015^1.ax')$   
 $\text{big\_p}: \mu u \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{big\_p\_type}, \text{type})$   
 $\text{mvalid}@(\text{mand}@(\text{mbox\_s}_4@(\text{mimplies}@(\text{mbox\_s}_4@(\text{mforall\_ind}@ \lambda x: \mu u: (\text{mand}@(\text{mbox\_s}_4@(\text{mimplies}@(\text{mbox\_s}_4@(\text{big\_p}@x))))@(\text{mand}$

**SYN378+1.p** Peter Andrews Problem X2130  
 $\forall x: \text{big\_p}(x) \Rightarrow (\neg \exists y: \text{big\_q}(y) \text{ or } \exists z: (\text{big\_p}(z) \Rightarrow \text{big\_q}(z))) \quad \text{fof}(x_{2130}, \text{conjecture})$

**SYN379+1.p** Peter Andrews Problem X2131  
 $\forall x: \text{big\_p}(x) \Rightarrow \exists y: (\forall x, z: \text{big\_q}(x, y, z) \Rightarrow \neg \forall z: (\text{big\_p}(z) \text{ and } \neg \text{big\_q}(y, y, z))) \quad \text{fof}(x_{2131}, \text{conjecture})$

**SYN380+1.p** Peter Andrews Problem X2132  
 $\forall w: \neg \text{big\_r}(w, w) \Rightarrow \exists x, y: (\neg \text{big\_r}(x, y) \text{ and } (\text{big\_q}(y, x) \Rightarrow \forall z: \text{big\_q}(z, z))) \quad \text{fof}(x_{2132}, \text{conjecture})$

**SYN381+1.p** Peter Andrews Problem X2133  
 $(\forall x: (\exists y: \text{big\_q}(x, y) \Rightarrow \text{big\_p}(x)) \text{ and } \forall v: \exists u: \text{big\_q}(u, v) \text{ and } \forall w, z: (\text{big\_q}(w, z) \Rightarrow (\text{big\_q}(z, w) \text{ or } \text{big\_q}(z, z)))) \Rightarrow \forall z: \text{big\_p}(z) \quad \text{fof}(x_{2133}, \text{conjecture})$

**SYN381^5.p** TPS problem X2133  
 $\text{cP}: \$i \rightarrow \$o \quad \text{thf}(\text{cP}, \text{type})$   
 $\text{cQ}: \$i \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{cQ}, \text{type})$

$(\forall xx: \$i: (\exists xy: \$i: (cQ@xx@xy) \Rightarrow (cP@xx)))$  and  $\forall xv: \$i: \exists xu: \$i: (cQ@xu@xv)$  and  $\forall xw: \$i, xz: \$i: ((cQ@xw@xz) \Rightarrow (cQ@xz@xw \text{ or } cQ@xz@xz))) \Rightarrow \forall xz: \$i: (cP@xz)$     thf(cX<sub>2133</sub>, conjecture)

**SYN382+1.p** Peter Andrews Problem X2134

$\forall z: \exists x: (\forall y: \text{big\_p}(x, y) \text{ or } \text{big\_q}(x, z)) \Rightarrow \forall y: \exists x: (\text{big\_p}(x, y) \text{ or } \text{big\_q}(x, y))$     fof(x<sub>2134</sub>, conjecture)

**SYN382^5.p** TPS problem X2134

cQ:  $\$i \rightarrow \$i \rightarrow \$o$     thf(cQ, type)

cP:  $\$i \rightarrow \$i \rightarrow \$o$     thf(cP, type)

$\forall xz: \$i: \exists xx: \$i: (\forall xy: \$i: (cP@xx@xy) \text{ or } cQ@xx@xz) \Rightarrow \forall xy: \$i: \exists xx: \$i: (cP@xx@xy \text{ or } cQ@xx@xy)$     thf(cX<sub>2134</sub>, conjecture)

**SYN383+1.p** Peter Andrews Problem X2135

$\exists x: \forall y: ((\text{big\_p}(x) \text{ and } \text{big\_q}(y)) \Rightarrow (\text{big\_q}(x) \text{ or } \text{big\_p}(y)))$     fof(x<sub>2135</sub>, conjecture)

**SYN384+1.p** Peter Andrews Problem X2136

$\forall z: \exists x, y: \forall u: (\text{big\_p}(x, y, z) \Rightarrow \text{big\_p}(u, x, x))$     fof(x<sub>2136</sub>, conjecture)

**SYN385+1.p** Peter Andrews Problem X2137

$\exists x: \forall y: (\text{big\_p}(x) \Rightarrow (\text{big\_q}(x) \text{ or } \text{big\_p}(y)))$     fof(x<sub>2137</sub>, conjecture)

**SYN386+1.p** Peter Andrews Problem X2138

$(\forall x: \exists y: \text{big\_f}(x, y) \text{ and } \exists x: \forall e: \exists n: \forall w: (\text{big\_s}(n, w) \Rightarrow \text{big\_d}(w, x, e)) \text{ and } \forall e: \exists d: \forall a, b: (\text{big\_d}(a, b, d) \Rightarrow \forall y, z: ((\text{big\_f}(a, y) \text{ and } \text{big\_f}(b, z)) \Rightarrow \text{big\_d}(y, z, e)))) \Rightarrow \exists y: \forall e: \exists m: \forall w: (\text{big\_s}(m, w) \Rightarrow \forall z: (\text{big\_f}(w, z) \Rightarrow \text{big\_d}(z, y, e)))$     fof(x<sub>2138</sub>, conjecture)

**SYN386^5.p** TPS problem X2138

cD:  $\$i \rightarrow \$i \rightarrow \$i \rightarrow \$o$     thf(cD, type)

cF:  $\$i \rightarrow \$i \rightarrow \$o$     thf(cF, type)

cS:  $\$i \rightarrow \$i \rightarrow \$o$     thf(cS, type)

$(\forall xx: \$i: \exists xy: \$i: (cF@xx@xy) \text{ and } \exists xx: \$i: \forall xe: \$i: \exists xn: \$i: \forall xw: \$i: ((cS@xn@xw) \Rightarrow (cD@xw@xx@xe)) \text{ and } \forall xe: \$i: \exists xd: \$i: \forall xy: \$i, xz: \$i: ((cF@xa@xy \text{ and } cF@xb@xz) \Rightarrow (cD@xy@xz@xe)))) \Rightarrow \exists xy: \$i: \forall xe: \$i: \exists xm: \$i: \forall xw: \$i: ((cS@xm@xw) \Rightarrow \forall xz: \$i: ((cF@xw@xz) \Rightarrow (cD@xz@xy@xe)))$     thf(cX<sub>2138</sub>, conjecture)

**SYN387+1.p** The Law of Excluded Middle

The Law of Excluded Middle: can be quite difficult for 'natural' systems.

$p \text{ or } \neg p$     fof(pel<sub>6</sub>, conjecture)

**SYN387^4.p** The Law of Excluded Middle

include('Axioms/LCL010^0.ax')

$p: \$i \rightarrow \$o$     thf(p.type, type)

ivalid@(ior@(iatom@p))(inot@(iatom@p)))    thf(pel<sub>6</sub>, conjecture)

**SYN387^7.p** The Law of Excluded Middle

include('Axioms/LCL015^0.ax')

include('Axioms/LCL013^5.ax')

include('Axioms/LCL015^1.ax')

$p: \$i \rightarrow \$o$     thf(p.type, type)

mvalid@(mor@(mbox\_s4@p))(mbox\_s4@(mnot@(mbox\_s4@p))))    thf(pel<sub>6</sub>, conjecture)

**SYN388+1.p** Expanded Law of Excluded Middle

Expanded Law of Excluded Middle. The strategies of the original Logic Theorist cannot prove this.

$p \text{ or } \neg \neg \neg p$     fof(pel<sub>7</sub>, conjecture)

**SYN388^4.p** Expanded Law of Excluded Middle

include('Axioms/LCL010^0.ax')

$p: \$i \rightarrow \$o$     thf(p.type, type)

ivalid@(ior@(iatom@p))(inot@(inot@(inot@(iatom@p))))    thf(pel<sub>7</sub>, conjecture)

**SYN389+1.p** Pierce's Law

Pierce's Law. Unprovable by Logic Theorist, and tricky for 'natural' systems.

$((p \Rightarrow q) \Rightarrow p) \Rightarrow p$     fof(pel<sub>8</sub>, conjecture)

**SYN389^4.p** Pierce's Law

include('Axioms/LCL010^0.ax')

$p: \$i \rightarrow \$o$     thf(p.type, type)

$q: \$i \rightarrow \$o$     thf(q.type, type)

ivalid@(iimplies@(iimplies@(iimplies@(iatom@p))(iatom@q))(iatom@p))(iatom@p))    thf(pel<sub>8</sub>, conjecture)

**SYN390+1.p** Pelletier 11

A simple problem designed to see whether 'natural' systems can do it efficiently (or whether they incorrectly try to prove the  $\rightarrow$  each way).

$p \iff p$  fof(pel<sub>11</sub>, conjecture)

**SYN390^4.p** Pelletier 11

include('Axioms/LCL010^0.ax')

$p: \$i \rightarrow \$o$  thf(p\_type, type)

ivalid@(iequiv@(iatom@p))(iatom@p)) thf(pel<sub>11</sub>, conjecture)

**SYN391+1.p** Pelletier 9

$((p_1 \text{ or } p_2) \text{ and } (\neg p_1 \text{ or } p_2) \text{ and } (p_1 \text{ or } \neg p_2)) \Rightarrow \neg \neg p_1 \text{ or } \neg p_2$  fof(pel<sub>9</sub>, conjecture)

**SYN391^4.p** Pelletier 9

include('Axioms/LCL010^0.ax')

$p_1: \$i \rightarrow \$o$  thf(p1\_type, type)

$p_2: \$i \rightarrow \$o$  thf(p2\_type, type)

ivalid@(iimplies@(iand@(ior@(iatom@p<sub>1</sub>))(iatom@p<sub>2</sub>))(iand@(ior@(inot@(iatom@p<sub>1</sub>))(iatom@p<sub>2</sub>))(ior@(iatom@p<sub>1</sub>))(iatom@p<sub>2</sub>)))

**SYN392+1.p** Pelletier 14

$(p_1 \iff p_2) \iff ((p_2 \text{ or } \neg p_1) \text{ and } (\neg p_2 \text{ or } p_1))$  fof(pel<sub>14</sub>, conjecture)

**SYN392^4.p** Pelletier 14

include('Axioms/LCL010^0.ax')

$p_1: \$i \rightarrow \$o$  thf(p1\_type, type)

$p_2: \$i \rightarrow \$o$  thf(p2\_type, type)

ivalid@(iequiv@(iequiv@(iatom@p<sub>1</sub>))(iatom@p<sub>2</sub>))(iand@(ior@(iatom@p<sub>2</sub>))(inot@(iatom@p<sub>1</sub>)))(ior@(inot@(iatom@p<sub>2</sub>))(iatom@p<sub>1</sub>)))

**SYN393+1.003.p** Pelletier 12

$((p_1 \iff p_2) \iff p_3) \iff (p_1 \iff (p_2 \iff p_3))$  fof(pel<sub>12</sub>, conjecture)

**SYN393^4.002.p** ILTP Problem SYJ206+1.002

include('Axioms/LCL010^0.ax')

$a_1: \$i \rightarrow \$o$  thf(a1\_type, type)

$a_2: \$i \rightarrow \$o$  thf(a2\_type, type)

ivalid@(iequiv@(iequiv@(iatom@a<sub>1</sub>))(iatom@a<sub>2</sub>))(iequiv@(iatom@a<sub>2</sub>))(iatom@a<sub>1</sub>)) thf(con, conjecture)

**SYN393^4.003.p** Pelletier 12

include('Axioms/LCL010^0.ax')

$p_1: \$i \rightarrow \$o$  thf(p1\_type, type)

$p_2: \$i \rightarrow \$o$  thf(p2\_type, type)

$p_3: \$i \rightarrow \$o$  thf(p3\_type, type)

ivalid@(iequiv@(iequiv@(iequiv@(iatom@p<sub>1</sub>))(iatom@p<sub>2</sub>))(iatom@p<sub>3</sub>))(iequiv@(iatom@p<sub>1</sub>))(iequiv@(iatom@p<sub>2</sub>))(iatom@p<sub>3</sub>))

**SYN393^4.004.p** ILTP Problem SYJ206+1.004

include('Axioms/LCL010^0.ax')

$a_1: \$i \rightarrow \$o$  thf(a1\_type, type)

$a_2: \$i \rightarrow \$o$  thf(a2\_type, type)

$a_3: \$i \rightarrow \$o$  thf(a3\_type, type)

$a_4: \$i \rightarrow \$o$  thf(a4\_type, type)

ivalid@(iequiv@(iequiv@(iequiv@(iequiv@(iatom@a<sub>1</sub>))(iatom@a<sub>2</sub>))(iatom@a<sub>3</sub>))(iatom@a<sub>4</sub>))(iequiv@(iatom@a<sub>4</sub>))(iequiv@(iequiv@(iequiv@(iequiv@(iatom@a<sub>1</sub>))(iatom@a<sub>2</sub>))(iatom@a<sub>3</sub>))(iatom@a<sub>4</sub>)))

**SYN394+1.p** Kalish and Montague Problem 201

Laws of distribution.

$\forall x: (f(x) \Rightarrow g(x)) \Rightarrow (\forall y: f(y) \Rightarrow \forall z: g(z))$  fof(kalish<sub>201</sub>, conjecture)

**SYN395+1.p** Kalish and Montague Problem 202

Laws of distribution.

$\forall x: (f(x) \Rightarrow g(x)) \Rightarrow (\exists y: f(y) \Rightarrow \exists z: g(z))$  fof(kalish<sub>202</sub>, conjecture)

**SYN396+1.p** Kalish and Montague Problem 203

Laws of quantifier negation.

$\neg \forall x: f(x) \iff \exists y: \neg f(y)$  fof(kalish<sub>203</sub>, conjecture)

**SYN397+1.p** Kalish and Montague Problem 204

Laws of quantifier negation.

$\neg \exists x: f(x) \iff \forall y: \neg f(y)$  fof(kalish<sub>204</sub>, conjecture)

**SYN397^7.p** Kalish and Montague Problem 204

include('Axioms/LCL015^0.ax')

include('Axioms/LCL013^5.ax')

include('Axioms/LCL015^1.ax')

$f: \mu \rightarrow \$i \rightarrow \$o$     thf(f\_type, type)

mvalid@(mand@(mbox\_s4@(mimplies@(mbox\_s4@(mnnot@(mexists\_ind@ $\lambda x: \mu: (\text{mbox\_s4}@ (f@x))))))\text{@}(\text{mbox\_s4}@(\text{mforall\_in}$

**SYN398+1.p** Kalish and Montague Problem 215

Laws of confinement.

$\forall x: (p \text{ and } f(x)) \iff (p \text{ and } \forall y: f(y))$     fof(kalish215, conjecture)

**SYN399+1.p** Kalish and Montague Problem 223

Laws of confinement.

$\forall x: (f(x) \iff p) \Rightarrow (\forall y: f(y) \iff p)$     fof(kalish223, conjecture)

**SYN400+1.p** Kalish and Montague Problem 227

Laws of vacuous quantification.

$\forall x: p \iff p$     fof(kalish227, conjecture)

**SYN401+1.p** Kalish and Montague Problem 229

Laws of vacuous quantification.

$\forall x: (\forall y: f(y) \Rightarrow f(x))$     fof(kalish229, conjecture)

**SYN402+1.p** Kalish and Montague Problem 230

Laws of vacuous quantification.

$\forall x: (f(x) \Rightarrow \exists y: f(y))$     fof(kalish230, conjecture)

**SYN403+1.p** Kalish and Montague Problem 234

Laws of alphabetic variance.

$\forall x: (((f(x) \Rightarrow g(x)) \text{ and } (g(x) \Rightarrow h(x))) \Rightarrow (f(x) \Rightarrow h(x)))$     fof(kalish234, conjecture)

**SYN404+1.p** Kalish and Montague Problem 238

Laws of alphabetic variance.

$\forall x: f(x) \Rightarrow \exists y: f(y)$     fof(kalish238, conjecture)

**SYN405+1.p** Kalish and Montague Problem 239

Laws of alphabetic variance.

$(\forall x: f(x) \text{ and } \exists y: g(y)) \Rightarrow \exists z: (f(z) \text{ and } g(z))$     fof(kalish239, conjecture)

**SYN406+1.p** Kalish and Montague Problem 240

Laws of alphabetic variance.

$(\forall x: (f(x) \Rightarrow g(x)) \text{ and } \exists y: (f(y) \text{ and } h(y))) \Rightarrow \exists z: (g(z) \text{ and } h(z))$     fof(kalish240, conjecture)

**SYN407+1.p** Kalish and Montague Problem 241

Laws of alphabetic variance.

$\forall x: (f(x) \Rightarrow (g(x) \text{ or } h(x))) \Rightarrow (\forall y: (f(y) \Rightarrow g(y)) \text{ or } \exists z: (f(z) \text{ and } h(z)))$     fof(kalish241, conjecture)

**SYN407^7.p** Kalish and Montague Problem 241

include('Axioms/LCL015^0.ax')

include('Axioms/LCL013^5.ax')

include('Axioms/LCL015^1.ax')

$h: \mu \rightarrow \$i \rightarrow \$o$     thf(h\_type, type)

$g: \mu \rightarrow \$i \rightarrow \$o$     thf(g\_type, type)

$f: \mu \rightarrow \$i \rightarrow \$o$     thf(f\_type, type)

mvalid@(mbox\_s4@(mimplies@(mbox\_s4@(mforall\_ind@ $\lambda x: \mu: (\text{mbox\_s4}@ (\text{mimplies}@ (\text{mbox\_s4}@ (f@x))\text{@}(\text{mor}@ (\text{mbox\_s4}@$

**SYN408+1.p** Kalish and Montague Problem 244

Laws of alphabetic variance.

$\neg \exists x: f(x) \Rightarrow \forall y: (f(y) \Rightarrow g(y))$     fof(kalish244, conjecture)

**SYN409+1.p** Kalish and Montague Problem 246

Laws of alphabetic variance.

$\forall x: f(x) \iff \forall y, z: (f(y) \text{ and } f(z))$     fof(kalish246, conjecture)

**SYN410+1.p** Kalish and Montague Problem 249

$\forall x, y: f(x, y) \Rightarrow \exists u, v: f(u, v)$     fof(kalish249, conjecture)

**SYN411+1.p** Kalish and Montague Problem 250

$\forall x, y, z: f(x, y, z) \iff \neg \exists u, v, w: \neg f(u, v, w)$     fof(kalish250, conjecture)

**SYN412+1.p** Kalish and Montague Problem 255

$\neg \exists x: \forall y: (f(x, y) \iff \neg f(x, x))$     fof(kalish<sub>255</sub>, conjecture)

**SYN413+1.p** Kalish and Montague Problem 256

$\forall z: \exists y: \forall x: (f(x, y) \iff (f(x, z) \text{ and } \neg f(x, x))) \Rightarrow \neg \exists v: \forall u: f(u, v)$     fof(kalish<sub>256</sub>, conjecture)

**SYN414+1.p** Kalish and Montague Problem 265

$\forall x: (\exists y: (h(x, y) \text{ and } f(y)) \Rightarrow \exists z: (h(x, z) \text{ and } g(z))) \iff \forall u, v, w: ((h(u, v) \text{ and } f(v)) \Rightarrow (h(u, w) \text{ and } g(w)))$     fof(kalish<sub>265</sub>, conjecture)

**SYN415+1.p** Kalish and Montague Problem 317

$(\exists x: f(x) \text{ and } \forall y, z: ((f(y) \text{ and } f(z)) \Rightarrow y = z)) \iff \exists u: (f(u) \text{ and } \forall v: (f(v) \Rightarrow u = v))$     fof(kalish<sub>317</sub>, conjecture)

**SYN416+1.p** Pelletier Problem 16

16:A surprising theorem of propositional logic.

$(p \Rightarrow q) \text{ or } (q \Rightarrow p)$     fof(pel<sub>16</sub>, conjecture)

**SYN416^4.p** Pelletier Problem 16

include('Axioms/LCL010^0.ax')

$p: \$i \rightarrow \$o$     thf(p\_type, type)

$q: \$i \rightarrow \$o$     thf(q\_type, type)

ivalid@(ior@(iimplies@(iatom@p)@(iatom@q))@(iimplies@(iatom@q)@(iatom@p)))    thf(pel<sub>16</sub>, conjecture)

**SYN416^7.p** Pelletier Problem 16

include('Axioms/LCL015^0.ax')

include('Axioms/LCL013^5.ax')

include('Axioms/LCL015^1.ax')

$q: \$i \rightarrow \$o$     thf(q\_type, type)

$p: \$i \rightarrow \$o$     thf(p\_type, type)

mvalid@(mor@(mbox\_s4@(mimplies@(mbox\_s4@p)@(mbox\_s4@q))@(mbox\_s4@(mimplies@(mbox\_s4@q)@(mbox\_s4@p))))

**SYN417+1.p** Harrison's cute problem

$\exists x: (x = f(g(x)) \text{ and } \forall y: (y = f(g(y)) \Rightarrow x = y)) \iff \exists x: (x = g(f(x)) \text{ and } \forall y: (y = g(f(y)) \Rightarrow x = y))$     fof(cute, conjecture)

**SYN548+1.p** dia box (box (p or box q)  $\leq$  box p or box q)

$\forall x: \text{reachable}(x, x)$     fof(reflexivity\_of\_reachable, axiom)

$\forall x, y, z: ((\text{reachable}(x, y) \text{ and } \text{reachable}(y, z)) \Rightarrow \text{reachable}(x, z))$     fof(transitivity\_of\_reachable, axiom)

$\exists x: (\text{reachable}(\text{initial\_world}, x) \text{ and } \forall y: (\text{reachable}(x, y) \Rightarrow (\forall z: (\text{reachable}(y, z) \Rightarrow (p(z) \text{ or } \forall v: (\text{reachable}(z, v) \Rightarrow q(v)))) \iff (\forall w: (\text{reachable}(y, w) \Rightarrow p(w)) \text{ or } \forall w: (\text{reachable}(y, w) \Rightarrow q(w))))))$     fof(prove\_this, conjecture)

**SYN549+1.p** dia box(dia(p or dia q)  $\leq$  (dia p or dia q))

$\forall x: \text{reachable}(x, x)$     fof(reflexivity\_of\_reachable, axiom)

$\forall x, y, z: ((\text{reachable}(x, y) \text{ and } \text{reachable}(y, z)) \Rightarrow \text{reachable}(x, z))$     fof(transitivity\_of\_reachable, axiom)

$\exists x: (\text{reachable}(\text{initial\_world}, x) \text{ and } \forall y: (\text{reachable}(x, y) \Rightarrow (\exists z: (\text{reachable}(y, z) \text{ and } (p(z) \text{ or } \exists v: (\text{reachable}(z, v) \text{ and } q(v)))) \iff (\exists w: (\text{reachable}(y, w) \text{ and } p(w)) \text{ or } \exists w: (\text{reachable}(y, w) \text{ and } q(w))))))$     fof(prove\_this, conjecture)

**SYN550+1.p** dia box p  $\leq$  dia box dia box p

$\forall x: \text{reachable}(x, x)$     fof(reflexivity\_of\_reachable, axiom)

$\forall x, y, z: ((\text{reachable}(x, y) \text{ and } \text{reachable}(y, z)) \Rightarrow \text{reachable}(x, z))$     fof(transitivity\_of\_reachable, axiom)

$\exists x: (\text{reachable}(\text{initial\_world}, x) \text{ and } \forall y: (\text{reachable}(x, y) \Rightarrow p(y))) \iff \exists x: (\text{reachable}(\text{initial\_world}, x) \text{ and } \forall y: (\text{reachable}(x, y) \Rightarrow (\exists z: (\text{reachable}(y, z) \text{ and } \forall w: (\text{reachable}(z, w) \Rightarrow p(w))))))$     fof(prove\_this, conjecture)

**SYN551+1.p** Cute Little Problem

$(\exists x: x = f(g(x)) \text{ and } \forall y, z: ((y = f(g(y)) \text{ and } z = f(g(z))) \Rightarrow y = z)) \iff (\exists x: x = g(f(x)) \text{ and } \forall y, z: ((y = g(f(y)) \text{ and } z = g(f(z))) \Rightarrow y = z))$     fof(prove\_this\_cute\_thing, conjecture)

**SYN551+2.p** Cute Little Problem

$\exists x: \forall y: (y = f(g(y)) \iff x = y) \iff \exists x: \forall y: (y = g(f(y)) \iff x = y)$     fof(prove\_this\_cute\_thing, conjecture)

**SYN551+3.p** Cute Little Problem

$\exists x: (x = f(g(x)) \text{ and } \forall y: (y = f(g(y)) \Rightarrow y = x)) \iff \exists x: (x = g(f(x)) \text{ and } \forall y: (y = g(f(y)) \Rightarrow y = x))$     fof(prove\_this\_cute\_thing, conjecture)

**SYN552-1.p** The E Killer

$g(x_1) = g(x_2)$     cnf(c<sub>1</sub>, axiom)

$f(g(b), b) \neq f(g(a), a)$     cnf(c<sub>2</sub>, axiom)

**SYN553-1.p** Harrison problem 1630

$p_2(x_0, x_0)$     cnf(p<sub>2</sub><sub>1</sub>, negated\_conjecture)

$p_2(c_3, c_4) \quad \text{cnf}(p2_2, \text{negated\_conjecture})$   
 $\neg p_2(c_4, f_5(f_6(c_7))) \quad \text{cnf}(\text{not\_}p2_3, \text{negated\_conjecture})$   
 $\neg p_2(c_3, f_5(f_6(c_7))) \quad \text{cnf}(\text{not\_}p2_4, \text{negated\_conjecture})$   
 $p_2(f_8(x_{11}, x_{12}), f_8(x_{12}, x_{11})) \quad \text{cnf}(p2_5, \text{negated\_conjecture})$   
 $(p_2(x_1, x_3) \text{ and } p_2(x_3, x_2)) \Rightarrow p_2(x_1, x_2) \quad \text{cnf}(p2_6, \text{negated\_conjecture})$   
 $p_2(f_8(x_8, f_8(x_9, x_{10})), f_8(f_8(x_8, x_9), x_{10})) \quad \text{cnf}(p2_7, \text{negated\_conjecture})$   
 $(p_2(x_4, x_6) \text{ and } p_2(x_5, x_7)) \Rightarrow p_2(f_8(x_4, x_5), f_8(x_6, x_7)) \quad \text{cnf}(p2_8, \text{negated\_conjecture})$   
 $\neg p_2(f_8(f_8(f_9(c_4), c_4), f_9(c_3)), f_8(f_9(c_4), f_8(f_9(c_3), c_4))) \quad \text{cnf}(\text{not\_}p2_9, \text{negated\_conjecture})$

**SYN554-1.p** Harrison problem 1667

$p_2(x_2, x_2) \quad \text{cnf}(p2_1, \text{negated\_conjecture})$   
 $\neg p_4(x_{15}, x_{15}) \quad \text{cnf}(\text{not\_}p4_2, \text{negated\_conjecture})$   
 $\neg p_2(c_6, c_7) \quad \text{cnf}(\text{not\_}p2_3, \text{negated\_conjecture})$   
 $p_2(f_3(c_5, c_6), f_3(c_5, c_7)) \quad \text{cnf}(p2_4, \text{negated\_conjecture})$   
 $p_2(x_0, x_1) \text{ or } p_4(x_0, x_1) \text{ or } p_4(x_1, x_0) \quad \text{cnf}(p2_5, \text{negated\_conjecture})$   
 $(p_2(x_2, x_4) \text{ and } p_2(x_2, x_3)) \Rightarrow p_2(x_3, x_4) \quad \text{cnf}(p2_6, \text{negated\_conjecture})$   
 $p_4(x_{13}, x_{14}) \Rightarrow p_4(f_3(c_5, x_{13}), f_3(c_5, x_{14})) \quad \text{cnf}(p4_7, \text{negated\_conjecture})$   
 $(p_2(x_{12}, x_{10}) \text{ and } p_4(x_{11}, x_{12}) \text{ and } p_2(x_{11}, x_9)) \Rightarrow p_4(x_9, x_{10}) \quad \text{cnf}(p4_8, \text{negated\_conjecture})$   
 $(p_2(x_5, x_7) \text{ and } p_2(x_6, x_8)) \Rightarrow p_2(f_3(x_5, x_6), f_3(x_7, x_8)) \quad \text{cnf}(p2_9, \text{negated\_conjecture})$

**SYN555-1.p** Harrison problem 2162

$p_2(x_0, x_0) \quad \text{cnf}(p2_1, \text{negated\_conjecture})$   
 $p_4(x_{12}, x_{12}) \quad \text{cnf}(p4_2, \text{negated\_conjecture})$   
 $p_3(x_3, x_3) \quad \text{cnf}(p3_3, \text{negated\_conjecture})$   
 $p_4(f_5(c_7, c_{10}, c_9), c_9) \quad \text{cnf}(p4_4, \text{negated\_conjecture})$   
 $\neg p_4(f_5(c_7, c_{10}, c_8), c_8) \quad \text{cnf}(\text{not\_}p4_5, \text{negated\_conjecture})$   
 $p_4(f_5(c_7, x_{24}, c_8), f_5(c_7, x_{24}, c_9)) \quad \text{cnf}(p4_6, \text{negated\_conjecture})$   
 $(p_2(x_0, x_1) \text{ and } p_2(x_0, x_2)) \Rightarrow p_2(x_1, x_2) \quad \text{cnf}(p2_7, \text{negated\_conjecture})$   
 $(p_4(x_{12}, x_{13}) \text{ and } p_4(x_{12}, x_{14})) \Rightarrow p_4(x_{13}, x_{14}) \quad \text{cnf}(p4_8, \text{negated\_conjecture})$   
 $(p_3(x_3, x_4) \text{ and } p_3(x_3, x_5)) \Rightarrow p_3(x_4, x_5) \quad \text{cnf}(p3_9, \text{negated\_conjecture})$   
 $(p_4(x_8, x_{11}) \text{ and } p_4(x_7, x_{10}) \text{ and } p_3(x_6, x_9)) \Rightarrow p_3(f_6(x_6, x_7, x_8), f_6(x_9, x_{10}, x_{11})) \quad \text{cnf}(p3_{10}, \text{negated\_conjecture})$   
 $(p_3(x_{16}, x_{19}) \text{ and } p_4(x_{17}, x_{20}) \text{ and } p_2(x_{15}, x_{18})) \Rightarrow p_4(f_5(x_{15}, x_{16}, x_{17}), f_5(x_{18}, x_{19}, x_{20})) \quad \text{cnf}(p4_{11}, \text{negated\_conjecture})$   
 $(p_4(f_5(c_7, x_{21}, x_{23}), x_{23}) \text{ and } p_4(f_5(c_7, f_6(x_{21}, x_{23}, x_{22}), x_{23}), f_5(c_7, f_6(x_{21}, x_{23}, x_{22}), x_{22}))) \Rightarrow p_4(f_5(c_7, x_{21}, x_{22}), x_{22}) \quad \text{cnf}(\text{not\_}p4_{12}, \text{negated\_conjecture})$

**SYN556-1.p** Harrison problem 2167

$p_2(x_0, x_0) \quad \text{cnf}(p2_1, \text{negated\_conjecture})$   
 $p_3(x_{15}, x_{15}) \quad \text{cnf}(p3_2, \text{negated\_conjecture})$   
 $p_2(c_{10}, c_{13}) \quad \text{cnf}(p2_3, \text{negated\_conjecture})$   
 $p_2(x_9, x_{10}) \Rightarrow p_2(f_7(x_9), f_7(x_{10})) \quad \text{cnf}(p2_4, \text{negated\_conjecture})$   
 $p_2(x_7, x_8) \Rightarrow p_2(f_6(x_7), f_6(x_8)) \quad \text{cnf}(p2_5, \text{negated\_conjecture})$   
 $(p_2(x_0, x_1) \text{ and } p_2(x_0, x_2)) \Rightarrow p_2(x_1, x_2) \quad \text{cnf}(p2_6, \text{negated\_conjecture})$   
 $(p_3(x_{15}, x_{16}) \text{ and } p_3(x_{15}, x_{17})) \Rightarrow p_3(x_{16}, x_{17}) \quad \text{cnf}(p3_7, \text{negated\_conjecture})$   
 $p_3(c_9, f_4(c_{13}, f_5(f_8(c_{11}, c_{13}), f_6(f_7(c_{12}))), c_{11})) \quad \text{cnf}(p3_8, \text{negated\_conjecture})$   
 $\neg p_3(c_9, f_4(c_{10}, f_5(f_8(c_{11}, c_{10}), f_6(f_7(c_{12}))), c_{11})) \quad \text{cnf}(\text{not\_}p3_9, \text{negated\_conjecture})$   
 $(p_2(x_3, x_5) \text{ and } p_2(x_4, x_6)) \Rightarrow p_2(f_5(x_3, x_4), f_5(x_5, x_6)) \quad \text{cnf}(p2_{10}, \text{negated\_conjecture})$   
 $(p_2(x_{12}, x_{14}) \text{ and } p_3(x_{11}, x_{13})) \Rightarrow p_2(f_8(x_{11}, x_{12}), f_8(x_{13}, x_{14})) \quad \text{cnf}(p2_{11}, \text{negated\_conjecture})$   
 $(p_2(x_{19}, x_{22}) \text{ and } p_3(x_{20}, x_{23}) \text{ and } p_2(x_{18}, x_{21})) \Rightarrow p_3(f_4(x_{18}, x_{19}, x_{20}), f_4(x_{21}, x_{22}, x_{23})) \quad \text{cnf}(p3_{12}, \text{negated\_conjecture})$

**SYN557-1.p** Harrison problem 2313

$p_2(x_3, x_3) \quad \text{cnf}(p2_1, \text{negated\_conjecture})$   
 $p_4(x_{19}, x_{19}) \quad \text{cnf}(p4_2, \text{negated\_conjecture})$   
 $\neg p_2(c_6, f_3(c_8, f_5(c_9))) \quad \text{cnf}(\text{not\_}p2_3, \text{negated\_conjecture})$   
 $p_2(f_3(x_{10}, x_{11}), f_3(x_{11}, x_{10})) \quad \text{cnf}(p2_4, \text{negated\_conjecture})$   
 $p_4(x_{15}, x_{16}) \Rightarrow p_2(f_5(x_{15}), f_5(x_{16})) \quad \text{cnf}(p2_5, \text{negated\_conjecture})$   
 $(p_2(x_3, x_4) \text{ and } p_2(x_3, x_5)) \Rightarrow p_2(x_4, x_5) \quad \text{cnf}(p2_6, \text{negated\_conjecture})$   
 $(p_4(x_{19}, x_{17}) \text{ and } p_4(x_{19}, x_{18})) \Rightarrow p_4(x_{17}, x_{18}) \quad \text{cnf}(p4_7, \text{negated\_conjecture})$   
 $p_2(f_3(x_0, x_2), f_3(x_1, x_2)) \Rightarrow p_2(x_0, x_1) \quad \text{cnf}(p2_8, \text{negated\_conjecture})$   
 $p_2(x_0, x_1) \Rightarrow p_2(f_3(x_0, x_2), f_3(x_1, x_2)) \quad \text{cnf}(p2_9, \text{negated\_conjecture})$   
 $p_2(f_3(x_{12}, f_3(x_{13}, x_{14})), f_3(x_{13}, f_3(x_{12}, x_{14}))) \quad \text{cnf}(p2_{10}, \text{negated\_conjecture})$   
 $p_2(f_3(f_3(x_{12}, x_{13}), x_{14}), f_3(x_{12}, f_3(x_{13}, x_{14}))) \quad \text{cnf}(p2_{11}, \text{negated\_conjecture})$   
 $p_2(f_3(c_6, f_5(c_7)), f_3(c_8, f_3(f_5(c_7), f_5(c_9)))) \quad \text{cnf}(p2_{12}, \text{negated\_conjecture})$



$(p_2(x_6, x_8) \text{ and } p_2(x_7, x_9)) \Rightarrow p_2(f_3(x_6, x_7), f_3(x_8, x_9)) \quad \text{cnf}(p_{2_{13}}, \text{negated\_conjecture})$

**SYN558-1.p** Harrison problem 2379

$p_2(x_0, x_0) \quad \text{cnf}(p_{2_1}, \text{negated\_conjecture})$   
 $p_4(x_8, x_8) \quad \text{cnf}(p_{4_2}, \text{negated\_conjecture})$   
 $p_6(c_7, f_3(x_{21})) \quad \text{cnf}(p_{6_3}, \text{negated\_conjecture})$   
 $p_5(c_7, c_{10}, c_9) \quad \text{cnf}(p_{5_4}, \text{negated\_conjecture})$   
 $p_5(c_7, c_{10}, c_8) \quad \text{cnf}(p_{5_5}, \text{negated\_conjecture})$   
 $p_5(c_7, x_{21}, f_3(x_{21})) \quad \text{cnf}(p_{5_6}, \text{negated\_conjecture})$   
 $p_2(x_6, x_7) \Rightarrow p_2(f_3(x_6), f_3(x_7)) \quad \text{cnf}(p_{2_7}, \text{negated\_conjecture})$   
 $p_5(c_7, c_8, x_{26}) \Rightarrow \neg p_5(c_7, c_9, x_{26}) \quad \text{cnf}(\text{not\_}p_{5_8}, \text{negated\_conjecture})$   
 $(p_2(x_0, x_1) \text{ and } p_2(x_0, x_2)) \Rightarrow p_2(x_1, x_2) \quad \text{cnf}(p_{2_9}, \text{negated\_conjecture})$   
 $(p_4(x_8, x_9) \text{ and } p_4(x_8, x_{10})) \Rightarrow p_4(x_9, x_{10}) \quad \text{cnf}(p_{4_{10}}, \text{negated\_conjecture})$   
 $(p_5(x_{11}, x_{12}, x_{14}) \text{ and } p_5(x_{11}, x_{14}, x_{13})) \Rightarrow p_5(x_{11}, x_{12}, x_{13}) \quad \text{cnf}(p_{5_{11}}, \text{negated\_conjecture})$   
 $(p_4(x_{25}, x_{22}) \text{ and } p_6(x_{25}, x_{24}) \text{ and } p_2(x_{24}, x_{23})) \Rightarrow p_6(x_{22}, x_{23}) \quad \text{cnf}(p_{6_{12}}, \text{negated\_conjecture})$   
 $(p_6(c_7, x_4) \text{ and } p_6(c_7, x_3) \text{ and } p_5(c_7, x_5, x_4) \text{ and } p_5(c_7, x_5, x_3)) \Rightarrow p_2(x_3, x_4) \quad \text{cnf}(p_{2_{13}}, \text{negated\_conjecture})$   
 $(p_2(x_{18}, x_{16}) \text{ and } p_2(x_{19}, x_{17}) \text{ and } p_4(x_{20}, x_{15}) \text{ and } p_5(x_{20}, x_{18}, x_{19})) \Rightarrow p_5(x_{15}, x_{16}, x_{17}) \quad \text{cnf}(p_{5_{14}}, \text{negated\_conjecture})$

**SYN559-1.p** Harrison problem 2418

$p_2(x_0, x_0) \quad \text{cnf}(p_{2_1}, \text{negated\_conjecture})$   
 $p_8(c_{13}, c_9) \quad \text{cnf}(p_{8_2}, \text{negated\_conjecture})$   
 $p_7(c_{10}, c_{13}) \quad \text{cnf}(p_{7_3}, \text{negated\_conjecture})$   
 $p_2(f_6(c_9, c_{13}), c_{14}) \quad \text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $p_2(f_5(c_{14}, c_{10}), c_{15}) \quad \text{cnf}(p_{2_5}, \text{negated\_conjecture})$   
 $p_2(f_3(f_4(c_{11}), c_{12}), c_{15}) \quad \text{cnf}(p_{2_6}, \text{negated\_conjecture})$   
 $p_2(x_7, x_8) \Rightarrow p_2(f_4(x_7), f_4(x_8)) \quad \text{cnf}(p_{2_7}, \text{negated\_conjecture})$   
 $(p_2(x_0, x_1) \text{ and } p_2(x_0, x_2)) \Rightarrow p_2(x_1, x_2) \quad \text{cnf}(p_{2_8}, \text{negated\_conjecture})$   
 $(p_2(x_{24}, x_{22}) \text{ and } p_8(x_{23}, x_{24}) \text{ and } p_2(x_{23}, x_{21})) \Rightarrow p_8(x_{21}, x_{22}) \quad \text{cnf}(p_{8_9}, \text{negated\_conjecture})$   
 $(p_2(x_{20}, x_{18}) \text{ and } p_7(x_{19}, x_{20}) \text{ and } p_2(x_{19}, x_{17})) \Rightarrow p_7(x_{17}, x_{18}) \quad \text{cnf}(p_{7_{10}}, \text{negated\_conjecture})$   
 $(p_2(x_3, x_5) \text{ and } p_2(x_4, x_6)) \Rightarrow p_2(f_3(x_3, x_4), f_3(x_5, x_6)) \quad \text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $(p_2(x_{13}, x_{15}) \text{ and } p_2(x_{14}, x_{16})) \Rightarrow p_2(f_6(x_{13}, x_{14}), f_6(x_{15}, x_{16})) \quad \text{cnf}(p_{2_{12}}, \text{negated\_conjecture})$   
 $(p_2(x_9, x_{11}) \text{ and } p_2(x_{10}, x_{12})) \Rightarrow p_2(f_5(x_9, x_{10}), f_5(x_{11}, x_{12})) \quad \text{cnf}(p_{2_{13}}, \text{negated\_conjecture})$   
 $(p_8(x_{26}, c_9) \text{ and } p_7(c_{10}, x_{26}) \text{ and } p_2(f_6(c_9, x_{26}), x_{25})) \Rightarrow \neg p_2(f_5(x_{25}, c_{10}), f_3(f_4(c_{11}), c_{12})) \quad \text{cnf}(\text{not\_}p_{8_{14}}, \text{negated\_conjecture})$

**SYN560-1.p** Harrison problem 2529

$p_2(x_0, x_0) \quad \text{cnf}(p_{2_1}, \text{negated\_conjecture})$   
 $\neg p_2(c_9, f_3(c_{10})) \quad \text{cnf}(\text{not\_}p_{2_2}, \text{negated\_conjecture})$   
 $p_2(c_{11}, f_4(f_5(c_{12}, c_{13}))) \quad \text{cnf}(p_{2_3}, \text{negated\_conjecture})$   
 $p_2(f_4(x_9), f_5(x_9, f_3(f_7(c_{10})))) \quad \text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $p_2(x_{18}, x_{19}) \Rightarrow p_2(f_7(x_{18}), f_7(x_{19})) \quad \text{cnf}(p_{2_5}, \text{negated\_conjecture})$   
 $p_2(x_5, x_6) \Rightarrow p_2(f_3(x_5), f_3(x_6)) \quad \text{cnf}(p_{2_6}, \text{negated\_conjecture})$   
 $p_2(x_7, x_8) \Rightarrow p_2(f_4(x_7), f_4(x_8)) \quad \text{cnf}(p_{2_7}, \text{negated\_conjecture})$   
 $(p_2(x_0, x_1) \text{ and } p_2(x_0, x_2)) \Rightarrow p_2(x_1, x_2) \quad \text{cnf}(p_{2_8}, \text{negated\_conjecture})$   
 $(p_8(x_{24}, x_{26}) \text{ and } p_8(x_{26}, x_{25})) \Rightarrow p_8(x_{24}, x_{25}) \quad \text{cnf}(p_{8_9}, \text{negated\_conjecture})$   
 $p_8(f_6(c_9, f_4(c_{12})), f_6(c_9, f_4(f_5(c_{12}, c_{14})))) \quad \text{cnf}(p_{8_{10}}, \text{negated\_conjecture})$   
 $\neg p_8(f_6(c_9, f_4(c_{12})), f_6(c_9, f_4(f_4(f_5(c_{12}, c_{14})))))) \quad \text{cnf}(\text{not\_}p_{8_{11}}, \text{negated\_conjecture})$   
 $(p_2(x_{23}, x_{21}) \text{ and } p_8(x_{22}, x_{23}) \text{ and } p_2(x_{22}, x_{20})) \Rightarrow p_8(x_{20}, x_{21}) \quad \text{cnf}(p_{8_{12}}, \text{negated\_conjecture})$   
 $(p_2(x_{10}, x_{12}) \text{ and } p_2(x_{11}, x_{13})) \Rightarrow p_2(f_5(x_{10}, x_{11}), f_5(x_{12}, x_{13})) \quad \text{cnf}(p_{2_{13}}, \text{negated\_conjecture})$   
 $(p_2(x_{15}, x_{17}) \text{ and } p_2(x_{14}, x_{16})) \Rightarrow p_2(f_6(x_{14}, x_{15}), f_6(x_{16}, x_{17})) \quad \text{cnf}(p_{2_{14}}, \text{negated\_conjecture})$   
 $p_2(x_3, f_3(c_{10})) \text{ or } p_8(f_6(x_3, x_4), f_6(x_3, f_5(x_4, f_3(f_7(c_{10})))))) \quad \text{cnf}(p_{2_{15}}, \text{negated\_conjecture})$

**SYN561-1.p** Harrison problem 2539

$p_2(x_0, x_0) \quad \text{cnf}(p_{2_1}, \text{negated\_conjecture})$   
 $p_9(c_{14}, c_{10}) \quad \text{cnf}(p_{9_2}, \text{negated\_conjecture})$   
 $p_8(c_{11}, c_{14}) \quad \text{cnf}(p_{8_3}, \text{negated\_conjecture})$   
 $p_2(f_7(c_{10}, c_{14}), c_{15}) \quad \text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $p_2(f_6(c_{15}, c_{11}), c_{16}) \quad \text{cnf}(p_{2_5}, \text{negated\_conjecture})$   
 $p_2(f_3(f_4(f_5(c_{12})), c_{13}), c_{16}) \quad \text{cnf}(p_{2_6}, \text{negated\_conjecture})$   
 $p_2(x_9, x_{10}) \Rightarrow p_2(f_5(x_9), f_5(x_{10})) \quad \text{cnf}(p_{2_7}, \text{negated\_conjecture})$   
 $p_2(x_7, x_8) \Rightarrow p_2(f_4(x_7), f_4(x_8)) \quad \text{cnf}(p_{2_8}, \text{negated\_conjecture})$   
 $(p_2(x_0, x_1) \text{ and } p_2(x_0, x_2)) \Rightarrow p_2(x_1, x_2) \quad \text{cnf}(p_{2_9}, \text{negated\_conjecture})$



$(p_2(x_{19}, x_{21}) \text{ and } p_2(x_{20}, x_{22})) \Rightarrow p_2(f_9(x_{19}, x_{20}), f_9(x_{21}, x_{22}))$      $\text{cnf}(p_{2_{17}}, \text{negated\_conjecture})$   
 $(p_4(x_{26}, x_{28}) \text{ and } p_4(x_{27}, x_{29})) \Rightarrow p_4(f_6(x_{26}, x_{27}), f_6(x_{28}, x_{29}))$      $\text{cnf}(p_{4_{18}}, \text{negated\_conjecture})$

**SYN565-1.p** Harrison problem 2889

$p_2(x_9, x_9)$      $\text{cnf}(p_{2_1}, \text{negated\_conjecture})$   
 $p_4(x_{23}, x_{23})$      $\text{cnf}(p_{4_2}, \text{negated\_conjecture})$   
 $p_2(f_5(f_7(x_{18})), f_5(x_{18}))$      $\text{cnf}(p_{2_3}, \text{negated\_conjecture})$   
 $p_4(f_8(x_{38}, x_{39}), f_6(x_{38}, f_7(x_{39})))$      $\text{cnf}(p_{4_4}, \text{negated\_conjecture})$   
 $p_4(f_7(f_8(x_{32}, x_{33})), f_8(x_{33}, x_{32}))$      $\text{cnf}(p_{4_5}, \text{negated\_conjecture})$   
 $p_4(x_{16}, x_{17}) \Rightarrow p_2(f_5(x_{16}), f_5(x_{17}))$      $\text{cnf}(p_{2_6}, \text{negated\_conjecture})$   
 $p_4(x_{30}, x_{31}) \Rightarrow p_4(f_7(x_{30}), f_7(x_{31}))$      $\text{cnf}(p_{4_7}, \text{negated\_conjecture})$   
 $(p_2(x_9, x_{10}) \text{ and } p_2(x_9, x_{11})) \Rightarrow p_2(x_{10}, x_{11})$      $\text{cnf}(p_{2_8}, \text{negated\_conjecture})$   
 $(p_4(x_{23}, x_{24}) \text{ and } p_4(x_{23}, x_{25})) \Rightarrow p_4(x_{24}, x_{25})$      $\text{cnf}(p_{4_9}, \text{negated\_conjecture})$   
 $p_{10}(f_5(x_7), f_3(f_5(f_6(x_7, x_8)), f_5(x_8)))$      $\text{cnf}(p_{10_{10}}, \text{negated\_conjecture})$   
 $\neg p_{10}(f_9(f_5(c_{11}), f_5(c_{12})), f_5(f_8(c_{12}, c_{11})))$      $\text{cnf}(\text{not\_}p_{10_{11}}, \text{negated\_conjecture})$   
 $p_{10}(f_9(x_4, x_6), x_5) \Rightarrow p_{10}(x_4, f_3(x_5, x_6))$      $\text{cnf}(p_{10_{12}}, \text{negated\_conjecture})$   
 $p_{10}(x_4, f_3(x_5, x_6)) \Rightarrow p_{10}(f_9(x_4, x_6), x_5)$      $\text{cnf}(p_{10_{13}}, \text{negated\_conjecture})$   
 $(p_2(x_2, x_0) \text{ and } p_2(x_3, x_1) \text{ and } p_{10}(x_2, x_3)) \Rightarrow p_{10}(x_0, x_1)$      $\text{cnf}(p_{10_{14}}, \text{negated\_conjecture})$   
 $(p_4(x_{34}, x_{36}) \text{ and } p_4(x_{35}, x_{37})) \Rightarrow p_4(f_8(x_{34}, x_{35}), f_8(x_{36}, x_{37}))$      $\text{cnf}(p_{4_{15}}, \text{negated\_conjecture})$   
 $(p_2(x_{12}, x_{14}) \text{ and } p_2(x_{13}, x_{15})) \Rightarrow p_2(f_3(x_{12}, x_{13}), f_3(x_{14}, x_{15}))$      $\text{cnf}(p_{2_{16}}, \text{negated\_conjecture})$   
 $(p_2(x_{19}, x_{21}) \text{ and } p_2(x_{20}, x_{22})) \Rightarrow p_2(f_9(x_{19}, x_{20}), f_9(x_{21}, x_{22}))$      $\text{cnf}(p_{2_{17}}, \text{negated\_conjecture})$   
 $(p_4(x_{26}, x_{28}) \text{ and } p_4(x_{27}, x_{29})) \Rightarrow p_4(f_6(x_{26}, x_{27}), f_6(x_{28}, x_{29}))$      $\text{cnf}(p_{4_{18}}, \text{negated\_conjecture})$

**SYN566-1.p** Harrison problem 2967

$p_9(x_{25}, x_{25})$      $\text{cnf}(p_{9_1}, \text{negated\_conjecture})$   
 $p_2(x_4, x_4)$      $\text{cnf}(p_{2_2}, \text{negated\_conjecture})$   
 $p_3(x_{11}, x_{11})$      $\text{cnf}(p_{3_3}, \text{negated\_conjecture})$   
 $p_7(x_{16}, x_{16})$      $\text{cnf}(p_{7_4}, \text{negated\_conjecture})$   
 $p_{10}(c_{15}, c_{11})$      $\text{cnf}(p_{10_5}, \text{negated\_conjecture})$   
 $p_8(c_{12}, c_{13})$      $\text{cnf}(p_{8_6}, \text{negated\_conjecture})$   
 $p_2(c_{14}, f_6(c_{15}))$      $\text{cnf}(p_{2_7}, \text{negated\_conjecture})$   
 $p_3(c_{13}, f_4(c_{14}))$      $\text{cnf}(p_{3_8}, \text{negated\_conjecture})$   
 $p_2(x_{14}, x_{15}) \Rightarrow p_3(f_4(x_{14}), f_4(x_{15}))$      $\text{cnf}(p_{3_9}, \text{negated\_conjecture})$   
 $p_2(x_7, x_8) \Rightarrow p_2(f_5(x_7), f_5(x_8))$      $\text{cnf}(p_{2_{10}}, \text{negated\_conjecture})$   
 $p_2(x_9, x_{10}) \Rightarrow p_2(f_6(x_9), f_6(x_{10}))$      $\text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $(p_9(x_{25}, x_{26}) \text{ and } p_9(x_{25}, x_{27})) \Rightarrow p_9(x_{26}, x_{27})$      $\text{cnf}(p_{9_{12}}, \text{negated\_conjecture})$   
 $(p_2(x_4, x_5) \text{ and } p_2(x_4, x_6)) \Rightarrow p_2(x_5, x_6)$      $\text{cnf}(p_{2_{13}}, \text{negated\_conjecture})$   
 $(p_3(x_{11}, x_{12}) \text{ and } p_3(x_{11}, x_{13})) \Rightarrow p_3(x_{12}, x_{13})$      $\text{cnf}(p_{3_{14}}, \text{negated\_conjecture})$   
 $(p_7(x_{16}, x_{17}) \text{ and } p_7(x_{16}, x_{18})) \Rightarrow p_7(x_{17}, x_{18})$      $\text{cnf}(p_{7_{15}}, \text{negated\_conjecture})$   
 $p_8(x_{19}, f_4(f_6(x_{20}))) \Rightarrow p_8(x_{19}, f_4(f_5(x_{20})))$      $\text{cnf}(p_{8_{16}}, \text{negated\_conjecture})$   
 $(p_2(x_2, x_0) \text{ and } p_9(x_3, x_1) \text{ and } p_{10}(x_2, x_3)) \Rightarrow p_{10}(x_0, x_1)$      $\text{cnf}(p_{10_{17}}, \text{negated\_conjecture})$   
 $(p_7(x_{24}, x_{21}) \text{ and } p_8(x_{24}, x_{23}) \text{ and } p_3(x_{23}, x_{22})) \Rightarrow p_8(x_{21}, x_{22})$      $\text{cnf}(p_{8_{18}}, \text{negated\_conjecture})$   
 $(p_{10}(x_{28}, c_{11}) \text{ and } p_8(c_{12}, x_{30}) \text{ and } p_3(x_{30}, f_4(x_{29}))) \Rightarrow \neg p_2(x_{29}, f_5(x_{28}))$      $\text{cnf}(\text{not\_}p_{10_{19}}, \text{negated\_conjecture})$

**SYN567-1.p** Harrison problem 3022

$p_2(x_0, x_0)$      $\text{cnf}(p_{2_1}, \text{negated\_conjecture})$   
 $p_5(x_{12}, x_{12})$      $\text{cnf}(p_{5_2}, \text{negated\_conjecture})$   
 $p_5(f_8(f_6(x_{17})), x_{17})$      $\text{cnf}(p_{5_3}, \text{negated\_conjecture})$   
 $\neg p_2(f_6(c_9), f_3(f_4(c_{10})))$      $\text{cnf}(\text{not\_}p_{2_4}, \text{negated\_conjecture})$   
 $\neg p_2(f_6(c_9), f_3(f_7(f_4(c_{10}))))$      $\text{cnf}(\text{not\_}p_{2_5}, \text{negated\_conjecture})$   
 $\neg p_2(f_6(c_9), f_3(f_7(f_7(f_4(c_{10}))))))$      $\text{cnf}(\text{not\_}p_{2_6}, \text{negated\_conjecture})$   
 $p_2(x_4, x_5) \Rightarrow p_2(f_3(x_4), f_3(x_5))$      $\text{cnf}(p_{2_7}, \text{negated\_conjecture})$   
 $p_2(x_{15}, x_{16}) \Rightarrow p_5(f_8(x_{15}), f_8(x_{16}))$      $\text{cnf}(p_{5_8}, \text{negated\_conjecture})$   
 $p_2(x_{10}, x_{11}) \Rightarrow p_2(f_7(x_{10}), f_7(x_{11}))$      $\text{cnf}(p_{2_9}, \text{negated\_conjecture})$   
 $p_5(x_8, x_9) \Rightarrow p_2(f_6(x_8), f_6(x_9))$      $\text{cnf}(p_{2_{10}}, \text{negated\_conjecture})$   
 $p_2(x_6, x_7) \Rightarrow p_2(f_4(x_6), f_4(x_7))$      $\text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $\neg p_2(f_6(c_9), f_3(f_7(f_7(f_7(f_4(c_{10}))))))$      $\text{cnf}(\text{not\_}p_{2_{12}}, \text{negated\_conjecture})$   
 $(p_2(x_0, x_1) \text{ and } p_2(x_0, x_2)) \Rightarrow p_2(x_1, x_2)$      $\text{cnf}(p_{2_{13}}, \text{negated\_conjecture})$   
 $(p_5(x_{12}, x_{13}) \text{ and } p_5(x_{12}, x_{14})) \Rightarrow p_5(x_{13}, x_{14})$      $\text{cnf}(p_{5_{14}}, \text{negated\_conjecture})$   
 $p_2(x_3, f_3(f_4(c_{10}))) \Rightarrow p_2(f_6(f_8(x_3)), x_3)$      $\text{cnf}(p_{2_{15}}, \text{negated\_conjecture})$   
 $p_2(x_3, f_3(f_7(f_4(c_{10})))) \Rightarrow p_2(f_6(f_8(x_3)), x_3)$      $\text{cnf}(p_{2_{16}}, \text{negated\_conjecture})$

$p_2(x_3, f_3(f_7(f_7(f_4(c_{10})))))) \Rightarrow p_2(f_6(f_8(x_3)), x_3)$     cnf(p2<sub>17</sub>, negated\_conjecture)  
 $p_2(x_3, f_3(f_7(f_7(f_7(f_4(c_{10})))))) \Rightarrow p_2(f_6(f_8(x_3)), x_3)$     cnf(p2<sub>18</sub>, negated\_conjecture)  
 $p_2(f_6(f_8(x_3)), x_3) \Rightarrow (p_2(x_3, f_3(f_4(c_{10}))) \text{ or } p_2(x_3, f_3(f_7(f_4(c_{10})))) \text{ or } p_2(x_3, f_3(f_7(f_7(f_4(c_{10})))))) \text{ or } p_2(x_3, f_3(f_7(f_7(f_7(f_4(c_{10}))))))$

**SYN568-1.p** Harrison problem 3076

$p_2(x_{17}, x_{17})$     cnf(p2<sub>1</sub>, negated\_conjecture)  
 $p_3(x_{28}, x_{28})$     cnf(p3<sub>2</sub>, negated\_conjecture)  
 $\neg p_{11}(f_9(c_{13}), f_9(c_{14}))$     cnf(not\_p11<sub>3</sub>, negated\_conjecture)  
 $p_{11}(f_5(f_6(c_{12})), f_9(x_{16}))$     cnf(p11<sub>4</sub>, negated\_conjecture)  
 $p_{10}(x_4, x_5) \text{ or } p_{11}(x_5, x_4)$     cnf(p10<sub>5</sub>, negated\_conjecture)  
 $p_{10}(x_4, x_5) \Rightarrow \neg p_{11}(x_5, x_4)$     cnf(not\_p10<sub>6</sub>, negated\_conjecture)  
 $\neg p_3(f_6(f_7(f_8(c_{12}))), f_6(c_{12}))$     cnf(not\_p3<sub>7</sub>, negated\_conjecture)  
 $p_3(x_{35}, x_{36}) \Rightarrow p_3(f_8(x_{35}), f_8(x_{36}))$     cnf(p3<sub>8</sub>, negated\_conjecture)  
 $p_3(x_{24}, x_{25}) \Rightarrow p_2(f_5(x_{24}), f_5(x_{25}))$     cnf(p2<sub>9</sub>, negated\_conjecture)  
 $p_2(x_{26}, x_{27}) \Rightarrow p_2(f_9(x_{26}), f_9(x_{27}))$     cnf(p2<sub>10</sub>, negated\_conjecture)  
 $p_3(x_{31}, x_{32}) \Rightarrow p_3(f_6(x_{31}), f_6(x_{32}))$     cnf(p3<sub>11</sub>, negated\_conjecture)  
 $p_3(x_{33}, x_{34}) \Rightarrow p_3(f_7(x_{33}), f_7(x_{34}))$     cnf(p3<sub>12</sub>, negated\_conjecture)  
 $(p_2(x_{17}, x_{18}) \text{ and } p_2(x_{17}, x_{19})) \Rightarrow p_2(x_{18}, x_{19})$     cnf(p2<sub>13</sub>, negated\_conjecture)  
 $(p_3(x_{28}, x_{29}) \text{ and } p_3(x_{28}, x_{30})) \Rightarrow p_3(x_{29}, x_{30})$     cnf(p3<sub>14</sub>, negated\_conjecture)  
 $(p_2(x_2, x_0) \text{ and } p_2(x_3, x_1) \text{ and } p_{10}(x_2, x_3)) \Rightarrow p_{10}(x_0, x_1)$     cnf(p10<sub>15</sub>, negated\_conjecture)  
 $(p_2(x_{11}, x_9) \text{ and } p_2(x_{12}, x_{10}) \text{ and } p_{11}(x_{11}, x_{12})) \Rightarrow p_{11}(x_9, x_{10})$     cnf(p11<sub>16</sub>, negated\_conjecture)  
 $(p_2(x_{20}, x_{22}) \text{ and } p_3(x_{21}, x_{23})) \Rightarrow p_2(f_4(x_{20}, x_{21}), f_4(x_{22}, x_{23}))$     cnf(p2<sub>17</sub>, negated\_conjecture)  
 $p_{11}(f_4(f_9(c_{13}), f_6(f_7(f_8(c_{12}))))), f_4(f_9(c_{14}), f_6(f_7(f_8(c_{12}))))))$     cnf(p11<sub>18</sub>, negated\_conjecture)  
 $(p_{11}(x_{13}, x_{15}) \text{ and } p_{11}(f_5(f_6(c_{12})), x_{13})) \Rightarrow p_{11}(f_4(x_{13}, x_{14}), f_4(x_{15}, x_{14}))$     cnf(p11<sub>19</sub>, negated\_conjecture)  
 $(p_{10}(x_6, x_8) \text{ and } p_{11}(f_5(f_6(c_{12})), x_6)) \Rightarrow (p_3(x_7, f_6(c_{12})) \text{ or } p_{10}(f_4(x_6, x_7), f_4(x_8, x_7)))$     cnf(p3<sub>20</sub>, negated\_conjecture)

**SYN569-1.p** Harrison problem 3088

$p_2(x_6, x_6)$     cnf(p2<sub>1</sub>, negated\_conjecture)  
 $p_6(x_{27}, x_{27})$     cnf(p6<sub>2</sub>, negated\_conjecture)  
 $p_8(c_{14}, c_{12})$     cnf(p8<sub>3</sub>, negated\_conjecture)  
 $p_8(c_{11}, c_{12})$     cnf(p8<sub>4</sub>, negated\_conjecture)  
 $p_8(c_{11}, c_{14})$     cnf(p8<sub>5</sub>, negated\_conjecture)  
 $p_9(c_{13}, c_{15}, c_{14})$     cnf(p9<sub>6</sub>, negated\_conjecture)  
 $p_8(x_4, x_5) \Rightarrow p_{10}(x_4, x_5)$     cnf(p10<sub>7</sub>, negated\_conjecture)  
 $p_2(x_{13}, x_{14}) \Rightarrow p_2(f_3(x_{13}), f_3(x_{14}))$     cnf(p2<sub>8</sub>, negated\_conjecture)  
 $(p_6(x_{27}, x_{28}) \text{ and } p_6(x_{27}, x_{29})) \Rightarrow p_6(x_{28}, x_{29})$     cnf(p6<sub>9</sub>, negated\_conjecture)  
 $(p_2(x_6, x_7) \text{ and } p_2(x_6, x_8)) \Rightarrow p_2(x_7, x_8)$     cnf(p2<sub>10</sub>, negated\_conjecture)  
 $(p_9(x_{11}, x_9, x_{12}) \text{ and } p_9(x_{11}, x_{10}, x_{12})) \Rightarrow p_2(x_9, x_{10})$     cnf(p2<sub>11</sub>, negated\_conjecture)  
 $(p_{10}(x_{40}, c_{12}) \text{ and } p_{10}(c_{11}, x_{40})) \Rightarrow p_9(c_{13}, f_3(x_{40}), x_{40})$     cnf(p9<sub>12</sub>, negated\_conjecture)  
 $(p_2(x_2, x_0) \text{ and } p_2(x_3, x_1) \text{ and } p_{10}(x_2, x_3)) \Rightarrow p_{10}(x_0, x_1)$     cnf(p10<sub>13</sub>, negated\_conjecture)  
 $(p_2(x_{33}, x_{31}) \text{ and } p_8(x_{32}, x_{33}) \text{ and } p_2(x_{32}, x_{30})) \Rightarrow p_8(x_{30}, x_{31})$     cnf(p8<sub>14</sub>, negated\_conjecture)  
 $p_2(f_5(f_7(c_{13}, c_{12}), f_7(c_{13}, c_{11})), f_4(f_5(c_{12}, c_{11}), c_{15}))$     cnf(p2<sub>15</sub>, negated\_conjecture)  
 $(p_2(x_{15}, x_{17}) \text{ and } p_2(x_{16}, x_{18})) \Rightarrow p_2(f_4(x_{15}, x_{16}), f_4(x_{17}, x_{18}))$     cnf(p2<sub>16</sub>, negated\_conjecture)  
 $(p_2(x_{24}, x_{26}) \text{ and } p_6(x_{23}, x_{25})) \Rightarrow p_2(f_7(x_{23}, x_{24}), f_7(x_{25}, x_{26}))$     cnf(p2<sub>17</sub>, negated\_conjecture)  
 $(p_2(x_{19}, x_{21}) \text{ and } p_2(x_{20}, x_{22})) \Rightarrow p_2(f_5(x_{19}, x_{20}), f_5(x_{21}, x_{22}))$     cnf(p2<sub>18</sub>, negated\_conjecture)  
 $(p_2(x_{37}, x_{35}) \text{ and } p_2(x_{38}, x_{36}) \text{ and } p_6(x_{39}, x_{34}) \text{ and } p_9(x_{39}, x_{37}, x_{38})) \Rightarrow p_9(x_{34}, x_{35}, x_{36})$     cnf(p9<sub>19</sub>, negated\_conjecture)  
 $(p_8(x_{41}, c_{12}) \text{ and } p_8(c_{11}, x_{41})) \Rightarrow \neg p_2(f_5(f_7(c_{13}, c_{12}), f_7(c_{13}, c_{11})), f_4(f_5(c_{12}, c_{11}), f_3(x_{41})))$     cnf(not\_p8<sub>20</sub>, negated\_conjecture)

**SYN570-1.p** Harrison problem 3089

$p_{10}(x_0, x_0)$     cnf(p10<sub>1</sub>, negated\_conjecture)  
 $p_7(x_{21}, x_{21})$     cnf(p7<sub>2</sub>, negated\_conjecture)  
 $p_6(x_{18}, x_{18})$     cnf(p6<sub>3</sub>, negated\_conjecture)  
 $p_3(x_{12}, x_{12})$     cnf(p3<sub>4</sub>, negated\_conjecture)  
 $p_2(x_7, x_7)$     cnf(p2<sub>5</sub>, negated\_conjecture)  
 $p_{11}(c_{12}, c_{14})$     cnf(p11<sub>6</sub>, negated\_conjecture)  
 $p_9(c_{15}, f_8(c_{13}))$     cnf(p9<sub>7</sub>, negated\_conjecture)  
 $p_2(c_{12}, f_5(c_{15}))$     cnf(p2<sub>8</sub>, negated\_conjecture)  
 $p_3(f_4(f_5(x_{17})), x_{17})$     cnf(p3<sub>9</sub>, negated\_conjecture)  
 $\neg p_9(f_4(c_{12}), f_8(c_{13}))$     cnf(not\_p9<sub>10</sub>, negated\_conjecture)  
 $p_6(x_{24}, x_{25}) \Rightarrow p_7(f_8(x_{24}), f_8(x_{25}))$     cnf(p7<sub>11</sub>, negated\_conjecture)  
 $p_3(x_{10}, x_{11}) \Rightarrow p_2(f_5(x_{10}), f_5(x_{11}))$     cnf(p2<sub>12</sub>, negated\_conjecture)

$p_2(x_{15}, x_{16}) \Rightarrow p_3(f_4(x_{15}), f_4(x_{16}))$      $\text{cnf}(p_{3_{13}}, \text{negated\_conjecture})$   
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2)$      $\text{cnf}(p_{10_{14}}, \text{negated\_conjecture})$   
 $(p_7(x_{21}, x_{22}) \text{ and } p_7(x_{21}, x_{23})) \Rightarrow p_7(x_{22}, x_{23})$      $\text{cnf}(p_{7_{15}}, \text{negated\_conjecture})$   
 $(p_6(x_{18}, x_{19}) \text{ and } p_6(x_{18}, x_{20})) \Rightarrow p_6(x_{19}, x_{20})$      $\text{cnf}(p_{6_{16}}, \text{negated\_conjecture})$   
 $(p_3(x_{12}, x_{13}) \text{ and } p_3(x_{12}, x_{14})) \Rightarrow p_3(x_{13}, x_{14})$      $\text{cnf}(p_{3_{17}}, \text{negated\_conjecture})$   
 $(p_2(x_7, x_8) \text{ and } p_2(x_7, x_9)) \Rightarrow p_2(x_8, x_9)$      $\text{cnf}(p_{2_{18}}, \text{negated\_conjecture})$   
 $(p_7(x_{29}, x_{27}) \text{ and } p_9(x_{28}, x_{29}) \text{ and } p_3(x_{28}, x_{26})) \Rightarrow p_9(x_{26}, x_{27})$      $\text{cnf}(p_{9_{19}}, \text{negated\_conjecture})$   
 $(p_{11}(x_6, x_5) \text{ and } p_2(x_6, x_3) \text{ and } p_{10}(x_5, x_4)) \Rightarrow p_{11}(x_3, x_4)$      $\text{cnf}(p_{11_{20}}, \text{negated\_conjecture})$

**SYN571-1.p** Harrison problem 3108

$p_4(x_{26}, x_{26})$      $\text{cnf}(p_{4_1}, \text{negated\_conjecture})$   
 $p_2(x_{11}, x_{11})$      $\text{cnf}(p_{2_2}, \text{negated\_conjecture})$   
 $p_{11}(f_5(x_{10}), c_{14})$      $\text{cnf}(p_{11_3}, \text{negated\_conjecture})$   
 $\neg p_{11}(c_{13}, f_5(x_{40}))$      $\text{cnf}(\text{not\_}p_{11_4}, \text{negated\_conjecture})$   
 $p_{11}(x_4, x_5) \text{ or } p_{11}(x_5, x_4)$      $\text{cnf}(p_{11_5}, \text{negated\_conjecture})$   
 $\neg p_{11}(x_{39}, f_3(x_{39}, f_5(f_6(f_7(c_{12}))))))$      $\text{cnf}(\text{not\_}p_{11_6}, \text{negated\_conjecture})$   
 $p_{11}(f_5(f_{10}(x_9)), x_9) \Rightarrow p_{11}(c_{14}, x_9)$      $\text{cnf}(p_{11_7}, \text{negated\_conjecture})$   
 $p_4(x_{33}, x_{34}) \Rightarrow p_4(f_7(x_{33}), f_7(x_{34}))$      $\text{cnf}(p_{4_8}, \text{negated\_conjecture})$   
 $p_4(x_{18}, x_{19}) \Rightarrow p_2(f_5(x_{18}), f_5(x_{19}))$      $\text{cnf}(p_{2_9}, \text{negated\_conjecture})$   
 $p_2(x_{29}, x_{30}) \Rightarrow p_4(f_{10}(x_{29}), f_{10}(x_{30}))$      $\text{cnf}(p_{4_{10}}, \text{negated\_conjecture})$   
 $p_4(x_{31}, x_{32}) \Rightarrow p_4(f_6(x_{31}), f_6(x_{32}))$      $\text{cnf}(p_{4_{11}}, \text{negated\_conjecture})$   
 $(p_2(x_{11}, x_{12}) \text{ and } p_2(x_{11}, x_{13})) \Rightarrow p_2(x_{12}, x_{13})$      $\text{cnf}(p_{2_{12}}, \text{negated\_conjecture})$   
 $(p_4(x_{26}, x_{27}) \text{ and } p_4(x_{26}, x_{28})) \Rightarrow p_4(x_{27}, x_{28})$      $\text{cnf}(p_{4_{13}}, \text{negated\_conjecture})$   
 $p_2(f_9(f_5(x_{24}), f_5(x_{25})), f_5(f_8(x_{24}, x_{25})))$      $\text{cnf}(p_{2_{14}}, \text{negated\_conjecture})$   
 $p_{11}(f_9(x_6, x_8), x_7) \Rightarrow p_{11}(x_6, f_3(x_7, x_8))$      $\text{cnf}(p_{11_{15}}, \text{negated\_conjecture})$   
 $p_{11}(x_6, f_3(x_7, x_8)) \Rightarrow p_{11}(f_9(x_6, x_8), x_7)$      $\text{cnf}(p_{11_{16}}, \text{negated\_conjecture})$   
 $(p_2(x_2, x_0) \text{ and } p_2(x_3, x_1) \text{ and } p_{11}(x_2, x_3)) \Rightarrow p_{11}(x_0, x_1)$      $\text{cnf}(p_{11_{17}}, \text{negated\_conjecture})$   
 $(p_4(x_{35}, x_{37}) \text{ and } p_4(x_{36}, x_{38})) \Rightarrow p_4(f_8(x_{35}, x_{36}), f_8(x_{37}, x_{38}))$      $\text{cnf}(p_{4_{18}}, \text{negated\_conjecture})$   
 $(p_2(x_{14}, x_{16}) \text{ and } p_2(x_{15}, x_{17})) \Rightarrow p_2(f_3(x_{14}, x_{15}), f_3(x_{16}, x_{17}))$      $\text{cnf}(p_{2_{19}}, \text{negated\_conjecture})$   
 $(p_2(x_{20}, x_{22}) \text{ and } p_2(x_{21}, x_{23})) \Rightarrow p_2(f_9(x_{20}, x_{21}), f_9(x_{22}, x_{23}))$      $\text{cnf}(p_{2_{20}}, \text{negated\_conjecture})$

**SYN572-1.p** Harrison problem 3112

$p_2(x_6, x_6)$      $\text{cnf}(p_{2_1}, \text{negated\_conjecture})$   
 $p_6(x_{34}, x_{34})$      $\text{cnf}(p_{6_2}, \text{negated\_conjecture})$   
 $p_4(x_{22}, x_{22})$      $\text{cnf}(p_{4_3}, \text{negated\_conjecture})$   
 $p_4(f_{10}(f_9(x_{27})), f_{10}(x_{27}))$      $\text{cnf}(p_{4_4}, \text{negated\_conjecture})$   
 $p_2(f_3(x_{13}, f_5(f_7(f_8(c_{13}))))), x_{13})$      $\text{cnf}(p_{2_5}, \text{negated\_conjecture})$   
 $p_6(x_{37}, x_{38}) \Rightarrow p_6(f_8(x_{37}), f_8(x_{38}))$      $\text{cnf}(p_{6_6}, \text{negated\_conjecture})$   
 $p_4(x_{18}, x_{19}) \Rightarrow p_2(f_5(x_{18}), f_5(x_{19}))$      $\text{cnf}(p_{2_7}, \text{negated\_conjecture})$   
 $p_2(x_{20}, x_{21}) \Rightarrow p_2(f_9(x_{20}), f_9(x_{21}))$      $\text{cnf}(p_{2_8}, \text{negated\_conjecture})$   
 $p_2(x_{25}, x_{26}) \Rightarrow p_4(f_{10}(x_{25}), f_{10}(x_{26}))$      $\text{cnf}(p_{4_9}, \text{negated\_conjecture})$   
 $p_6(x_{32}, x_{33}) \Rightarrow p_4(f_7(x_{32}), f_7(x_{33}))$      $\text{cnf}(p_{4_{10}}, \text{negated\_conjecture})$   
 $p_2(f_3(x_{14}, f_9(x_{14})), f_5(f_7(f_8(c_{13}))))$      $\text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $(p_2(x_6, x_7) \text{ and } p_2(x_6, x_8)) \Rightarrow p_2(x_7, x_8)$      $\text{cnf}(p_{2_{12}}, \text{negated\_conjecture})$   
 $(p_6(x_{34}, x_{35}) \text{ and } p_6(x_{34}, x_{36})) \Rightarrow p_6(x_{35}, x_{36})$      $\text{cnf}(p_{6_{13}}, \text{negated\_conjecture})$   
 $(p_4(x_{22}, x_{23}) \text{ and } p_4(x_{22}, x_{24})) \Rightarrow p_4(x_{23}, x_{24})$      $\text{cnf}(p_{4_{14}}, \text{negated\_conjecture})$   
 $p_{12}(f_{10}(f_3(x_4, x_5)), f_{11}(f_{10}(x_4), f_{10}(x_5)))$      $\text{cnf}(p_{12_{15}}, \text{negated\_conjecture})$   
 $\neg p_{12}(f_{10}(c_{14}), f_{11}(f_{10}(f_3(c_{14}, c_{15})), f_{10}(c_{15})))$      $\text{cnf}(\text{not\_}p_{12_{16}}, \text{negated\_conjecture})$   
 $p_2(f_3(x_{15}, f_3(x_{16}, x_{17})), f_3(f_3(x_{15}, x_{16}), x_{17}))$      $\text{cnf}(p_{2_{17}}, \text{negated\_conjecture})$   
 $(p_4(x_2, x_0) \text{ and } p_4(x_3, x_1) \text{ and } p_{12}(x_2, x_3)) \Rightarrow p_{12}(x_0, x_1)$      $\text{cnf}(p_{12_{18}}, \text{negated\_conjecture})$   
 $(p_4(x_{28}, x_{30}) \text{ and } p_4(x_{29}, x_{31})) \Rightarrow p_4(f_{11}(x_{28}, x_{29}), f_{11}(x_{30}, x_{31}))$      $\text{cnf}(p_{4_{19}}, \text{negated\_conjecture})$   
 $(p_2(x_9, x_{11}) \text{ and } p_2(x_{10}, x_{12})) \Rightarrow p_2(f_3(x_9, x_{10}), f_3(x_{11}, x_{12}))$      $\text{cnf}(p_{2_{20}}, \text{negated\_conjecture})$

**SYN573-1.p** Harrison problem 3208

$p_{12}(c_{15})$      $\text{cnf}(c_{15\_is\_}p_{12_1}, \text{negated\_conjecture})$   
 $p_4(x_{30}, x_{30})$      $\text{cnf}(p_{4_2}, \text{negated\_conjecture})$   
 $p_2(x_{17}, x_{17})$      $\text{cnf}(p_{2_3}, \text{negated\_conjecture})$   
 $p_{12}(x_{16}) \Rightarrow p_2(x_{16}, f_9(f_{10}(x_{16})))$      $\text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $(p_{12}(x_{11}) \text{ and } p_2(x_{11}, x_{10})) \Rightarrow p_{12}(x_{10})$      $\text{cnf}(p_{12_5}, \text{negated\_conjecture})$   
 $p_4(x_{37}, x_{38}) \Rightarrow p_4(f_7(x_{37}), f_7(x_{38}))$      $\text{cnf}(p_{4_6}, \text{negated\_conjecture})$   
 $p_4(x_{24}, x_{25}) \Rightarrow p_2(f_5(x_{24}), f_5(x_{25}))$      $\text{cnf}(p_{2_7}, \text{negated\_conjecture})$

$p_2(x_{26}, x_{27}) \Rightarrow p_2(f_8(x_{26}), f_8(x_{27}))$      $\text{cnf}(p_{2_8}, \text{negated\_conjecture})$   
 $p_4(x_{28}, x_{29}) \Rightarrow p_2(f_9(x_{28}), f_9(x_{29}))$      $\text{cnf}(p_{2_9}, \text{negated\_conjecture})$   
 $p_2(x_{33}, x_{34}) \Rightarrow p_4(f_{10}(x_{33}), f_{10}(x_{34}))$      $\text{cnf}(p_{4_{10}}, \text{negated\_conjecture})$   
 $p_4(x_{35}, x_{36}) \Rightarrow p_4(f_6(x_{35}), f_6(x_{36}))$      $\text{cnf}(p_{4_{11}}, \text{negated\_conjecture})$   
 $(p_4(x_{30}, x_{31}) \text{ and } p_4(x_{30}, x_{32})) \Rightarrow p_4(x_{31}, x_{32})$      $\text{cnf}(p_{4_{12}}, \text{negated\_conjecture})$   
 $(p_2(x_{17}, x_{18}) \text{ and } p_2(x_{17}, x_{19})) \Rightarrow p_2(x_{18}, x_{19})$      $\text{cnf}(p_{2_{13}}, \text{negated\_conjecture})$   
 $p_{12}(x_9) \Rightarrow (p_{11}(x_9, c_{16}) \text{ or } p_2(x_9, f_9(c_{17})))$      $\text{cnf}(p_{11_{14}}, \text{negated\_conjecture})$   
 $p_{12}(x_{16}) \Rightarrow (p_{13}(f_{10}(x_{16}), c_{17}) \text{ or } p_4(f_{10}(x_{16}), c_{17}))$      $\text{cnf}(p_{13_{15}}, \text{negated\_conjecture})$   
 $p_{11}(x_7, f_3(f_8(x_8), f_3(f_8(x_7), f_5(f_6(f_7(c_{14}))))))$      $\text{cnf}(p_{11_{16}}, \text{negated\_conjecture})$   
 $(p_2(x_2, x_0) \text{ and } p_2(x_3, x_1) \text{ and } p_{11}(x_2, x_3)) \Rightarrow p_{11}(x_0, x_1)$      $\text{cnf}(p_{11_{17}}, \text{negated\_conjecture})$   
 $(p_4(x_{14}, x_{12}) \text{ and } p_4(x_{15}, x_{13}) \text{ and } p_{13}(x_{14}, x_{15})) \Rightarrow p_{13}(x_{12}, x_{13})$      $\text{cnf}(p_{13_{18}}, \text{negated\_conjecture})$   
 $\neg p_{11}(c_{15}, f_3(f_8(c_{16}), f_3(f_8(f_9(c_{17})), f_5(f_6(f_7(c_{14}))))))$      $\text{cnf}(\text{not\_}p_{11_{19}}, \text{negated\_conjecture})$   
 $(p_2(x_{20}, x_{22}) \text{ and } p_2(x_{21}, x_{23})) \Rightarrow p_2(f_3(x_{20}, x_{21}), f_3(x_{22}, x_{23}))$      $\text{cnf}(p_{2_{20}}, \text{negated\_conjecture})$   
 $p_{11}(x_4, x_5) \Rightarrow p_{11}(x_4, f_3(f_8(x_5), f_3(f_8(x_6), f_5(f_6(f_7(c_{14}))))))$      $\text{cnf}(p_{11_{21}}, \text{negated\_conjecture})$

### SYN574-1.p Harrison problem 3263

$p_{10}(x_0, x_0)$      $\text{cnf}(p_{10_1}, \text{negated\_conjecture})$   
 $p_7(x_{21}, x_{21})$      $\text{cnf}(p_{7_2}, \text{negated\_conjecture})$   
 $p_3(x_{12}, x_{12})$      $\text{cnf}(p_{3_3}, \text{negated\_conjecture})$   
 $p_2(x_7, x_7)$      $\text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $p_9(c_{12}, c_{13})$      $\text{cnf}(p_{9_5}, \text{negated\_conjecture})$   
 $p_{11}(c_{14}, c_{15})$      $\text{cnf}(p_{11_6}, \text{negated\_conjecture})$   
 $p_3(f_4(f_5(x_{17})), f_4(x_{17}))$      $\text{cnf}(p_{3_7}, \text{negated\_conjecture})$   
 $p_3(f_6(f_5(x_{20})), f_6(x_{20}))$      $\text{cnf}(p_{3_8}, \text{negated\_conjecture})$   
 $p_9(x_{32}, f_4(c_{14})) \Rightarrow p_9(x_{32}, c_{13})$      $\text{cnf}(p_{9_9}, \text{negated\_conjecture})$   
 $p_9(x_{32}, c_{13}) \Rightarrow p_9(x_{32}, f_4(c_{14}))$      $\text{cnf}(p_{9_{10}}, \text{negated\_conjecture})$   
 $p_2(x_{10}, x_{11}) \Rightarrow p_2(f_5(x_{10}), f_5(x_{11}))$      $\text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $p_2(x_{18}, x_{19}) \Rightarrow p_3(f_6(x_{18}), f_6(x_{19}))$      $\text{cnf}(p_{3_{12}}, \text{negated\_conjecture})$   
 $p_2(x_{15}, x_{16}) \Rightarrow p_3(f_4(x_{15}), f_4(x_{16}))$      $\text{cnf}(p_{3_{13}}, \text{negated\_conjecture})$   
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2)$      $\text{cnf}(p_{10_{14}}, \text{negated\_conjecture})$   
 $(p_7(x_{21}, x_{22}) \text{ and } p_7(x_{21}, x_{23})) \Rightarrow p_7(x_{22}, x_{23})$      $\text{cnf}(p_{7_{15}}, \text{negated\_conjecture})$   
 $(p_3(x_{12}, x_{13}) \text{ and } p_3(x_{12}, x_{14})) \Rightarrow p_3(x_{13}, x_{14})$      $\text{cnf}(p_{3_{16}}, \text{negated\_conjecture})$   
 $(p_2(x_7, x_8) \text{ and } p_2(x_7, x_9)) \Rightarrow p_2(x_8, x_9)$      $\text{cnf}(p_{2_{17}}, \text{negated\_conjecture})$   
 $(p_{11}(x_6, x_5) \text{ and } p_2(x_6, x_3) \text{ and } p_{10}(x_5, x_4)) \Rightarrow p_{11}(x_3, x_4)$      $\text{cnf}(p_{11_{18}}, \text{negated\_conjecture})$   
 $(p_7(x_{31}, x_{28}) \text{ and } p_9(x_{31}, x_{30}) \text{ and } p_3(x_{30}, x_{29})) \Rightarrow p_9(x_{28}, x_{29})$      $\text{cnf}(p_{9_{19}}, \text{negated\_conjecture})$   
 $(p_2(x_{25}, x_{27}) \text{ and } p_3(x_{24}, x_{26})) \Rightarrow p_7(f_8(x_{24}, x_{25}), f_8(x_{26}, x_{27}))$      $\text{cnf}(p_{7_{20}}, \text{negated\_conjecture})$   
 $(p_{11}(x_{35}, c_{15}) \text{ and } p_9(c_{12}, x_{33}) \text{ and } p_2(x_{34}, f_5(x_{35}))) \Rightarrow (p_9(f_8(x_{33}, x_{34}), x_{33}) \text{ or } p_9(f_8(x_{33}, x_{34}), f_4(x_{34})))$      $\text{cnf}(p_{9_{21}}, \text{negated\_conjecture})$   
 $(p_{11}(x_{35}, c_{15}) \text{ and } p_9(c_{12}, x_{33}) \text{ and } p_2(x_{34}, f_5(x_{35})) \text{ and } p_9(f_8(x_{33}, x_{34}), x_{33})) \Rightarrow \neg p_9(f_8(x_{33}, x_{34}), f_4(x_{34}))$      $\text{cnf}(\text{not\_}p_{11_{22}}, \text{negated\_conjecture})$

### SYN575-1.p Harrison problem 3265

$p_{10}(x_0, x_0)$      $\text{cnf}(p_{10_1}, \text{negated\_conjecture})$   
 $p_7(x_{21}, x_{21})$      $\text{cnf}(p_{7_2}, \text{negated\_conjecture})$   
 $p_3(x_{12}, x_{12})$      $\text{cnf}(p_{3_3}, \text{negated\_conjecture})$   
 $p_2(x_7, x_7)$      $\text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $p_9(c_{12}, c_{13})$      $\text{cnf}(p_{9_5}, \text{negated\_conjecture})$   
 $p_{11}(c_{14}, c_{15})$      $\text{cnf}(p_{11_6}, \text{negated\_conjecture})$   
 $p_3(f_4(f_5(x_{17})), f_4(x_{17}))$      $\text{cnf}(p_{3_7}, \text{negated\_conjecture})$   
 $p_3(f_6(f_5(x_{20})), f_6(x_{20}))$      $\text{cnf}(p_{3_8}, \text{negated\_conjecture})$   
 $p_9(x_{32}, f_6(c_{14})) \Rightarrow p_9(x_{32}, c_{13})$      $\text{cnf}(p_{9_9}, \text{negated\_conjecture})$   
 $p_9(x_{32}, c_{13}) \Rightarrow p_9(x_{32}, f_6(c_{14}))$      $\text{cnf}(p_{9_{10}}, \text{negated\_conjecture})$   
 $p_2(x_{10}, x_{11}) \Rightarrow p_2(f_5(x_{10}), f_5(x_{11}))$      $\text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $p_2(x_{18}, x_{19}) \Rightarrow p_3(f_6(x_{18}), f_6(x_{19}))$      $\text{cnf}(p_{3_{12}}, \text{negated\_conjecture})$   
 $p_2(x_{15}, x_{16}) \Rightarrow p_3(f_4(x_{15}), f_4(x_{16}))$      $\text{cnf}(p_{3_{13}}, \text{negated\_conjecture})$   
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2)$      $\text{cnf}(p_{10_{14}}, \text{negated\_conjecture})$   
 $(p_7(x_{21}, x_{22}) \text{ and } p_7(x_{21}, x_{23})) \Rightarrow p_7(x_{22}, x_{23})$      $\text{cnf}(p_{7_{15}}, \text{negated\_conjecture})$   
 $(p_3(x_{12}, x_{13}) \text{ and } p_3(x_{12}, x_{14})) \Rightarrow p_3(x_{13}, x_{14})$      $\text{cnf}(p_{3_{16}}, \text{negated\_conjecture})$   
 $(p_2(x_7, x_8) \text{ and } p_2(x_7, x_9)) \Rightarrow p_2(x_8, x_9)$      $\text{cnf}(p_{2_{17}}, \text{negated\_conjecture})$   
 $(p_{11}(x_6, x_5) \text{ and } p_2(x_6, x_3) \text{ and } p_{10}(x_5, x_4)) \Rightarrow p_{11}(x_3, x_4)$      $\text{cnf}(p_{11_{18}}, \text{negated\_conjecture})$   
 $(p_7(x_{31}, x_{28}) \text{ and } p_9(x_{31}, x_{30}) \text{ and } p_3(x_{30}, x_{29})) \Rightarrow p_9(x_{28}, x_{29})$      $\text{cnf}(p_{9_{19}}, \text{negated\_conjecture})$   
 $(p_2(x_{25}, x_{27}) \text{ and } p_3(x_{24}, x_{26})) \Rightarrow p_7(f_8(x_{24}, x_{25}), f_8(x_{26}, x_{27}))$      $\text{cnf}(p_{7_{20}}, \text{negated\_conjecture})$

$(p_{11}(x_{35}, c_{15}) \text{ and } p_9(c_{12}, x_{33}) \text{ and } p_2(x_{34}, f_5(x_{35}))) \Rightarrow (p_9(f_8(x_{33}, x_{34}), x_{33}) \text{ or } p_9(f_8(x_{33}, x_{34}), f_6(x_{34})))$     cnf(p9<sub>21</sub>, negated\_conjecture)  
 $(p_{11}(x_{35}, c_{15}) \text{ and } p_9(c_{12}, x_{33}) \text{ and } p_2(x_{34}, f_5(x_{35})) \text{ and } p_9(f_8(x_{33}, x_{34}), x_{33})) \Rightarrow \neg p_9(f_8(x_{33}, x_{34}), f_6(x_{34}))$     cnf(not\_p11<sub>22</sub>, negated\_conjecture)

**SYN576-1.p** Harrison problem 3280

$p_8(x_{42}, x_{42})$     cnf(p8<sub>1</sub>, negated\_conjecture)  
 $p_2(x_{13}, x_{13})$     cnf(p2<sub>2</sub>, negated\_conjecture)  
 $p_4(x_{34}, x_{34})$     cnf(p4<sub>3</sub>, negated\_conjecture)  
 $p_5(x_{37}, x_{37})$     cnf(p5<sub>4</sub>, negated\_conjecture)  
 $p_{12}(c_{15}, f_6(c_{13}))$     cnf(p12<sub>5</sub>, negated\_conjecture)  
 $p_{12}(c_{16}, f_6(c_{13}))$     cnf(p12<sub>6</sub>, negated\_conjecture)  
 $p_{11}(x_4, x_5) \text{ or } p_{11}(x_5, x_4)$     cnf(p11<sub>7</sub>, negated\_conjecture)  
 $p_2(f_3(x_{22}, x_{23}), f_3(x_{23}, x_{22}))$     cnf(p2<sub>8</sub>, negated\_conjecture)  
 $p_4(x_{40}, x_{41}) \Rightarrow p_5(f_6(x_{40}), f_6(x_{41}))$     cnf(p5<sub>9</sub>, negated\_conjecture)  
 $p_2(x_{16}, x_{17}) \Rightarrow p_2(f_{10}(x_{16}), f_{10}(x_{17}))$     cnf(p2<sub>10</sub>, negated\_conjecture)  
 $(p_8(x_{42}, x_{43}) \text{ and } p_8(x_{42}, x_{44})) \Rightarrow p_8(x_{43}, x_{44})$     cnf(p8<sub>11</sub>, negated\_conjecture)  
 $(p_2(x_{13}, x_{14}) \text{ and } p_2(x_{13}, x_{15})) \Rightarrow p_2(x_{14}, x_{15})$     cnf(p2<sub>12</sub>, negated\_conjecture)  
 $(p_4(x_{34}, x_{35}) \text{ and } p_4(x_{34}, x_{36})) \Rightarrow p_4(x_{35}, x_{36})$     cnf(p4<sub>13</sub>, negated\_conjecture)  
 $(p_5(x_{37}, x_{38}) \text{ and } p_5(x_{37}, x_{39})) \Rightarrow p_5(x_{38}, x_{39})$     cnf(p5<sub>14</sub>, negated\_conjecture)  
 $(p_2(x_2, x_0) \text{ and } p_2(x_3, x_1) \text{ and } p_{11}(x_2, x_3)) \Rightarrow p_{11}(x_0, x_1)$     cnf(p11<sub>15</sub>, negated\_conjecture)  
 $(p_2(x_8, x_6) \text{ and } p_5(x_9, x_7) \text{ and } p_{12}(x_8, x_9)) \Rightarrow p_{12}(x_6, x_7)$     cnf(p12<sub>16</sub>, negated\_conjecture)  
 $\neg p_{12}(f_7(f_9(c_{13}, c_{14}), f_3(c_{15}, c_{16})), f_3(c_{15}, c_{16})), f_6(c_{13}))$     cnf(not\_p12<sub>17</sub>, negated\_conjecture)  
 $(p_2(x_{18}, x_{20}) \text{ and } p_2(x_{19}, x_{21})) \Rightarrow p_2(f_3(x_{18}, x_{19}), f_3(x_{20}, x_{21}))$     cnf(p2<sub>18</sub>, negated\_conjecture)  
 $(p_2(x_{24}, x_{26}) \text{ and } p_2(x_{25}, x_{27})) \Rightarrow p_2(f_7(x_{24}, x_{25}), f_7(x_{26}, x_{27}))$     cnf(p2<sub>19</sub>, negated\_conjecture)  
 $(p_4(x_{28}, x_{31}) \text{ and } p_8(x_{29}, x_{32}) \text{ and } p_2(x_{30}, x_{33})) \Rightarrow p_2(f_9(x_{28}, x_{29}, x_{30}), f_9(x_{31}, x_{32}, x_{33}))$     cnf(p2<sub>20</sub>, negated\_conjecture)  
 $(p_{12}(x_{12}, f_6(x_{10})) \text{ and } p_{12}(x_{11}, f_6(x_{10})) \text{ and } p_{11}(f_{10}(x_{11}), f_{10}(x_{12}))) \Rightarrow p_{12}(f_7(f_9(x_{10}, c_{14}), f_3(x_{11}, x_{12})), x_{12}), f_6(x_{10}))$     cnf(p12<sub>21</sub>, negated\_conjecture)  
 $(p_{12}(x_{12}, f_6(x_{10})) \text{ and } p_{12}(x_{11}, f_6(x_{10})) \text{ and } p_{11}(f_{10}(x_{11}), f_{10}(x_{12}))) \Rightarrow p_{12}(f_7(f_9(x_{10}, c_{14}), f_3(x_{11}, x_{12})), f_3(x_{11}, x_{12})), f_6(x_{10}))$     cnf(p12<sub>22</sub>, negated\_conjecture)

**SYN577-1.p** Harrison problem 3300

$p_2(x_0, x_0)$     cnf(p2<sub>1</sub>, negated\_conjecture)  
 $p_8(c_{14}, c_{13})$     cnf(p8<sub>2</sub>, negated\_conjecture)  
 $p_7(c_{11}, c_{12})$     cnf(p7<sub>3</sub>, negated\_conjecture)  
 $p_7(c_{13}, c_{12})$     cnf(p7<sub>4</sub>, negated\_conjecture)  
 $p_7(c_9, c_{10})$     cnf(p7<sub>5</sub>, negated\_conjecture)  
 $p_8(c_{14}, c_{11})$     cnf(p8<sub>6</sub>, negated\_conjecture)  
 $p_2(f_3(c_{12}, c_{11}), c_{15})$     cnf(p2<sub>7</sub>, negated\_conjecture)  
 $p_2(f_4(c_{16}, c_{14}), c_{18})$     cnf(p2<sub>8</sub>, negated\_conjecture)  
 $p_2(f_4(c_{15}, c_{14}), c_{17})$     cnf(p2<sub>9</sub>, negated\_conjecture)  
 $p_2(f_3(c_{12}, c_{13}), c_{16})$     cnf(p2<sub>10</sub>, negated\_conjecture)  
 $p_2(f_5(f_6(c_9), c_{19}), c_{17})$     cnf(p2<sub>11</sub>, negated\_conjecture)  
 $p_2(f_5(f_6(c_9), c_{20}), c_{18})$     cnf(p2<sub>12</sub>, negated\_conjecture)  
 $p_2(x_{22}, x_{23}) \Rightarrow p_2(f_6(x_{22}), f_6(x_{23}))$     cnf(p2<sub>13</sub>, negated\_conjecture)  
 $(p_2(x_0, x_1) \text{ and } p_2(x_0, x_2)) \Rightarrow p_2(x_1, x_2)$     cnf(p2<sub>14</sub>, negated\_conjecture)  
 $(p_2(x_{31}, x_{29}) \text{ and } p_8(x_{30}, x_{31}) \text{ and } p_2(x_{30}, x_{28})) \Rightarrow p_8(x_{28}, x_{29})$     cnf(p8<sub>15</sub>, negated\_conjecture)  
 $(p_2(x_{27}, x_{25}) \text{ and } p_7(x_{26}, x_{27}) \text{ and } p_2(x_{26}, x_{24})) \Rightarrow p_7(x_{24}, x_{25})$     cnf(p7<sub>16</sub>, negated\_conjecture)  
 $(p_2(x_{10}, x_{12}) \text{ and } p_2(x_{11}, x_{13})) \Rightarrow p_2(f_3(x_{10}, x_{11}), f_3(x_{12}, x_{13}))$     cnf(p2<sub>17</sub>, negated\_conjecture)  
 $(p_2(x_{19}, x_{21}) \text{ and } p_2(x_{18}, x_{20})) \Rightarrow p_2(f_5(x_{18}, x_{19}), f_5(x_{20}, x_{21}))$     cnf(p2<sub>18</sub>, negated\_conjecture)  
 $(p_2(x_{14}, x_{16}) \text{ and } p_2(x_{15}, x_{17})) \Rightarrow p_2(f_4(x_{14}, x_{15}), f_4(x_{16}, x_{17}))$     cnf(p2<sub>19</sub>, negated\_conjecture)  
 $(p_7(x_{34}, c_{10}) \text{ and } p_2(c_{15}, x_{32}) \text{ and } p_2(c_{16}, x_{33}) \text{ and } p_2(f_4(x_{32}, c_{14}), f_5(f_6(x_{34}), c_{19}))) \Rightarrow \neg p_2(f_4(x_{33}, c_{14}), f_5(f_6(x_{34}), c_{20}))$   
 $(p_7(x_7, c_{10}) \text{ and } p_7(x_3, c_{12}) \text{ and } p_7(x_4, c_{12}) \text{ and } p_8(c_{14}, x_4) \text{ and } p_8(c_{14}, x_3) \text{ and } p_2(f_3(c_{12}, x_4), x_6) \text{ and } p_2(f_3(c_{12}, x_3), x_5) \text{ and } p_2(x_3, x_4))$     cnf(p2<sub>21</sub>, negated\_conjecture)  
 $(p_7(x_7, c_{10}) \text{ and } p_7(x_3, c_{12}) \text{ and } p_7(x_4, c_{12}) \text{ and } p_8(c_{14}, x_4) \text{ and } p_8(c_{14}, x_3) \text{ and } p_2(f_3(c_{12}, x_4), x_6) \text{ and } p_2(f_3(c_{12}, x_3), x_5) \text{ and } p_2(x_3, x_4))$     cnf(p2<sub>22</sub>, negated\_conjecture)

**SYN578-1.p** Harrison problem 3328

$p_{10}(x_0, x_0)$     cnf(p10<sub>1</sub>, negated\_conjecture)  
 $p_7(x_{21}, x_{21})$     cnf(p7<sub>2</sub>, negated\_conjecture)  
 $p_3(x_{12}, x_{12})$     cnf(p3<sub>3</sub>, negated\_conjecture)  
 $p_2(x_7, x_7)$     cnf(p2<sub>4</sub>, negated\_conjecture)  
 $p_9(c_{12}, c_{13})$     cnf(p9<sub>5</sub>, negated\_conjecture)  
 $p_{11}(c_{14}, c_{15})$     cnf(p11<sub>6</sub>, negated\_conjecture)  
 $p_2(c_{16}, f_5(c_{14}))$     cnf(p2<sub>7</sub>, negated\_conjecture)

$p_3(f_4(f_5(x_{17})), f_4(x_{17})) \quad \text{cnf}(p3_8, \text{negated\_conjecture})$   
 $p_3(f_6(f_5(x_{20})), f_6(x_{20})) \quad \text{cnf}(p3_9, \text{negated\_conjecture})$   
 $p_9(x_{32}, f_4(c_{16})) \Rightarrow p_9(x_{32}, c_{13}) \quad \text{cnf}(p9_{10}, \text{negated\_conjecture})$   
 $p_9(x_{32}, c_{13}) \Rightarrow p_9(x_{32}, f_4(c_{16})) \quad \text{cnf}(p9_{11}, \text{negated\_conjecture})$   
 $p_2(x_{10}, x_{11}) \Rightarrow p_2(f_5(x_{10}), f_5(x_{11})) \quad \text{cnf}(p2_{12}, \text{negated\_conjecture})$   
 $p_2(x_{18}, x_{19}) \Rightarrow p_3(f_6(x_{18}), f_6(x_{19})) \quad \text{cnf}(p3_{13}, \text{negated\_conjecture})$   
 $p_2(x_{15}, x_{16}) \Rightarrow p_3(f_4(x_{15}), f_4(x_{16})) \quad \text{cnf}(p3_{14}, \text{negated\_conjecture})$   
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2) \quad \text{cnf}(p10_{15}, \text{negated\_conjecture})$   
 $(p_7(x_{21}, x_{22}) \text{ and } p_7(x_{21}, x_{23})) \Rightarrow p_7(x_{22}, x_{23}) \quad \text{cnf}(p7_{16}, \text{negated\_conjecture})$   
 $(p_3(x_{12}, x_{13}) \text{ and } p_3(x_{12}, x_{14})) \Rightarrow p_3(x_{13}, x_{14}) \quad \text{cnf}(p3_{17}, \text{negated\_conjecture})$   
 $(p_2(x_7, x_8) \text{ and } p_2(x_7, x_9)) \Rightarrow p_2(x_8, x_9) \quad \text{cnf}(p2_{18}, \text{negated\_conjecture})$   
 $(p_{11}(x_6, x_5) \text{ and } p_2(x_6, x_3) \text{ and } p_{10}(x_5, x_4)) \Rightarrow p_{11}(x_3, x_4) \quad \text{cnf}(p11_{19}, \text{negated\_conjecture})$   
 $(p_7(x_{31}, x_{28}) \text{ and } p_9(x_{31}, x_{30}) \text{ and } p_3(x_{30}, x_{29})) \Rightarrow p_9(x_{28}, x_{29}) \quad \text{cnf}(p9_{20}, \text{negated\_conjecture})$   
 $(p_2(x_{25}, x_{27}) \text{ and } p_3(x_{24}, x_{26})) \Rightarrow p_7(f_8(x_{24}, x_{25}), f_8(x_{26}, x_{27})) \quad \text{cnf}(p7_{21}, \text{negated\_conjecture})$   
 $(p_{11}(x_{34}, c_{15}) \text{ and } p_9(c_{12}, x_{33})) \Rightarrow (p_9(f_8(x_{33}, x_{34}), x_{33}) \text{ or } p_9(f_8(x_{33}, x_{34}), f_4(x_{34}))) \quad \text{cnf}(p9_{22}, \text{negated\_conjecture})$   
 $(p_{11}(x_{34}, c_{15}) \text{ and } p_9(c_{12}, x_{33}) \text{ and } p_9(f_8(x_{33}, x_{34}), x_{33})) \Rightarrow \neg p_9(f_8(x_{33}, x_{34}), f_4(x_{34})) \quad \text{cnf}(\text{not\_p11}_{23}, \text{negated\_conjecture})$

### SYN579-1.p Harrison problem 3330

$p_{10}(x_0, x_0) \quad \text{cnf}(p10_1, \text{negated\_conjecture})$   
 $p_7(x_{21}, x_{21}) \quad \text{cnf}(p7_2, \text{negated\_conjecture})$   
 $p_3(x_{12}, x_{12}) \quad \text{cnf}(p3_3, \text{negated\_conjecture})$   
 $p_2(x_7, x_7) \quad \text{cnf}(p2_4, \text{negated\_conjecture})$   
 $p_9(c_{12}, c_{13}) \quad \text{cnf}(p9_5, \text{negated\_conjecture})$   
 $p_{11}(c_{14}, c_{15}) \quad \text{cnf}(p11_6, \text{negated\_conjecture})$   
 $p_2(c_{16}, f_5(c_{14})) \quad \text{cnf}(p2_7, \text{negated\_conjecture})$   
 $p_3(f_4(f_5(x_{17})), f_4(x_{17})) \quad \text{cnf}(p3_8, \text{negated\_conjecture})$   
 $p_3(f_6(f_5(x_{20})), f_6(x_{20})) \quad \text{cnf}(p3_9, \text{negated\_conjecture})$   
 $p_9(x_{32}, f_6(c_{16})) \Rightarrow p_9(x_{32}, c_{13}) \quad \text{cnf}(p9_{10}, \text{negated\_conjecture})$   
 $p_9(x_{32}, c_{13}) \Rightarrow p_9(x_{32}, f_6(c_{16})) \quad \text{cnf}(p9_{11}, \text{negated\_conjecture})$   
 $p_2(x_{10}, x_{11}) \Rightarrow p_2(f_5(x_{10}), f_5(x_{11})) \quad \text{cnf}(p2_{12}, \text{negated\_conjecture})$   
 $p_2(x_{18}, x_{19}) \Rightarrow p_3(f_6(x_{18}), f_6(x_{19})) \quad \text{cnf}(p3_{13}, \text{negated\_conjecture})$   
 $p_2(x_{15}, x_{16}) \Rightarrow p_3(f_4(x_{15}), f_4(x_{16})) \quad \text{cnf}(p3_{14}, \text{negated\_conjecture})$   
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2) \quad \text{cnf}(p10_{15}, \text{negated\_conjecture})$   
 $(p_7(x_{21}, x_{22}) \text{ and } p_7(x_{21}, x_{23})) \Rightarrow p_7(x_{22}, x_{23}) \quad \text{cnf}(p7_{16}, \text{negated\_conjecture})$   
 $(p_3(x_{12}, x_{13}) \text{ and } p_3(x_{12}, x_{14})) \Rightarrow p_3(x_{13}, x_{14}) \quad \text{cnf}(p3_{17}, \text{negated\_conjecture})$   
 $(p_2(x_7, x_8) \text{ and } p_2(x_7, x_9)) \Rightarrow p_2(x_8, x_9) \quad \text{cnf}(p2_{18}, \text{negated\_conjecture})$   
 $(p_{11}(x_6, x_5) \text{ and } p_2(x_6, x_3) \text{ and } p_{10}(x_5, x_4)) \Rightarrow p_{11}(x_3, x_4) \quad \text{cnf}(p11_{19}, \text{negated\_conjecture})$   
 $(p_7(x_{31}, x_{28}) \text{ and } p_9(x_{31}, x_{30}) \text{ and } p_3(x_{30}, x_{29})) \Rightarrow p_9(x_{28}, x_{29}) \quad \text{cnf}(p9_{20}, \text{negated\_conjecture})$   
 $(p_2(x_{25}, x_{27}) \text{ and } p_3(x_{24}, x_{26})) \Rightarrow p_7(f_8(x_{24}, x_{25}), f_8(x_{26}, x_{27})) \quad \text{cnf}(p7_{21}, \text{negated\_conjecture})$   
 $(p_{11}(x_{34}, c_{15}) \text{ and } p_9(c_{12}, x_{33})) \Rightarrow (p_9(f_8(x_{33}, x_{34}), x_{33}) \text{ or } p_9(f_8(x_{33}, x_{34}), f_6(x_{34}))) \quad \text{cnf}(p9_{22}, \text{negated\_conjecture})$   
 $(p_{11}(x_{34}, c_{15}) \text{ and } p_9(c_{12}, x_{33}) \text{ and } p_9(f_8(x_{33}, x_{34}), x_{33})) \Rightarrow \neg p_9(f_8(x_{33}, x_{34}), f_6(x_{34})) \quad \text{cnf}(\text{not\_p11}_{23}, \text{negated\_conjecture})$

### SYN580-1.p Harrison problem 3332

$p_{10}(x_0, x_0) \quad \text{cnf}(p10_1, \text{negated\_conjecture})$   
 $p_7(x_{19}, x_{19}) \quad \text{cnf}(p7_2, \text{negated\_conjecture})$   
 $p_4(x_{12}, x_{12}) \quad \text{cnf}(p4_3, \text{negated\_conjecture})$   
 $p_2(x_7, x_7) \quad \text{cnf}(p2_4, \text{negated\_conjecture})$   
 $p_{11}(c_{15}, c_{16}) \quad \text{cnf}(p11_5, \text{negated\_conjecture})$   
 $p_9(c_{12}, c_{13}) \quad \text{cnf}(p9_6, \text{negated\_conjecture})$   
 $p_2(c_{14}, f_3(c_{15})) \quad \text{cnf}(p2_7, \text{negated\_conjecture})$   
 $\neg p_8(c_{12}, c_{13}, c_{14}) \quad \text{cnf}(\text{not\_p8}_8, \text{negated\_conjecture})$   
 $p_2(x_{17}, x_{18}) \Rightarrow p_4(f_6(x_{17}), f_6(x_{18})) \quad \text{cnf}(p4_9, \text{negated\_conjecture})$   
 $p_2(x_{10}, x_{11}) \Rightarrow p_2(f_3(x_{10}), f_3(x_{11})) \quad \text{cnf}(p2_{10}, \text{negated\_conjecture})$   
 $p_2(x_{15}, x_{16}) \Rightarrow p_4(f_5(x_{15}), f_5(x_{16})) \quad \text{cnf}(p4_{11}, \text{negated\_conjecture})$   
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2) \quad \text{cnf}(p10_{12}, \text{negated\_conjecture})$   
 $(p_7(x_{19}, x_{20}) \text{ and } p_7(x_{19}, x_{21})) \Rightarrow p_7(x_{20}, x_{21}) \quad \text{cnf}(p7_{13}, \text{negated\_conjecture})$   
 $(p_4(x_{12}, x_{13}) \text{ and } p_4(x_{12}, x_{14})) \Rightarrow p_4(x_{13}, x_{14}) \quad \text{cnf}(p4_{14}, \text{negated\_conjecture})$   
 $(p_2(x_7, x_8) \text{ and } p_2(x_7, x_9)) \Rightarrow p_2(x_8, x_9) \quad \text{cnf}(p2_{15}, \text{negated\_conjecture})$   
 $(p_{11}(x_{29}, c_{16}) \text{ and } p_9(c_{12}, x_{28})) \Rightarrow p_8(c_{12}, x_{28}, x_{29}) \quad \text{cnf}(p8_{16}, \text{negated\_conjecture})$   
 $p_9(c_{12}, x_{30}) \Rightarrow (p_9(c_{12}, f_5(x_{31})) \text{ or } p_8(c_{12}, x_{30}, x_{31})) \quad \text{cnf}(p9_{17}, \text{negated\_conjecture})$



$p_9(c_{12}, x_{30}) \Rightarrow (p_9(c_{12}, f_6(x_{31})) \text{ or } p_8(c_{12}, x_{30}, f_3(x_{31})))$      $\text{cnf}(p9_{18}, \text{negated\_conjecture})$   
 $(p_7(x_{35}, x_{32}) \text{ and } p_9(x_{35}, x_{34}) \text{ and } p_4(x_{34}, x_{33})) \Rightarrow p_9(x_{32}, x_{33})$      $\text{cnf}(p9_{19}, \text{negated\_conjecture})$   
 $(p_{11}(x_6, x_5) \text{ and } p_2(x_6, x_3) \text{ and } p_{10}(x_5, x_4)) \Rightarrow p_{11}(x_3, x_4)$      $\text{cnf}(p11_{20}, \text{negated\_conjecture})$   
 $(p_9(c_{12}, x_{30}) \text{ and } p_8(c_{12}, f_5(x_{31}), f_3(x_{31}))) \Rightarrow p_8(c_{12}, x_{30}, x_{31})$      $\text{cnf}(p8_{21}, \text{negated\_conjecture})$   
 $(p_9(c_{12}, x_{30}) \text{ and } p_8(c_{12}, f_6(x_{31}), x_{31})) \Rightarrow p_8(c_{12}, x_{30}, f_3(x_{31}))$      $\text{cnf}(p8_{22}, \text{negated\_conjecture})$   
 $(p_2(x_{25}, x_{24}) \text{ and } p_4(x_{26}, x_{23}) \text{ and } p_7(x_{27}, x_{22}) \text{ and } p_8(x_{27}, x_{26}, x_{25})) \Rightarrow p_8(x_{22}, x_{23}, x_{24})$      $\text{cnf}(p8_{23}, \text{negated\_conjecture})$

**SYN581-1.p** Harrison problem 3466

$p_7(x_{34}, x_{34})$      $\text{cnf}(p7_1, \text{negated\_conjecture})$   
 $p_2(x_{18}, x_{18})$      $\text{cnf}(p2_2, \text{negated\_conjecture})$   
 $p_5(x_{31}, x_{31})$      $\text{cnf}(p5_3, \text{negated\_conjecture})$   
 $p_{12}(c_{13}, c_{18})$      $\text{cnf}(p12_4, \text{negated\_conjecture})$   
 $p_2(c_{18}, c_{14})$      $\text{cnf}(p2_5, \text{negated\_conjecture})$   
 $p_2(f_3(c_{18}), f_8(f_9(c_{17})))$      $\text{cnf}(p2_6, \text{negated\_conjecture})$   
 $p_{11}(f_4(f_6(c_{15}, c_{13})), c_{16})$      $\text{cnf}(p11_7, \text{negated\_conjecture})$   
 $p_{11}(f_4(f_6(c_{15}, c_{14})), c_{16})$      $\text{cnf}(p11_8, \text{negated\_conjecture})$   
 $\neg p_{11}(f_4(f_6(c_{15}, c_{18})), c_{16})$      $\text{cnf}(\text{not\_}p11_9, \text{negated\_conjecture})$   
 $p_{12}(x_{11}, x_{12}) \Rightarrow p_{11}(x_{11}, x_{12})$      $\text{cnf}(p11_{10}, \text{negated\_conjecture})$   
 $p_2(x_{11}, x_{12}) \Rightarrow p_{11}(x_{11}, x_{12})$      $\text{cnf}(p11_{11}, \text{negated\_conjecture})$   
 $p_7(x_{37}, x_{38}) \Rightarrow p_7(f_9(x_{37}), f_9(x_{38}))$      $\text{cnf}(p7_{12}, \text{negated\_conjecture})$   
 $p_2(x_{21}, x_{22}) \Rightarrow p_2(f_3(x_{21}), f_3(x_{22}))$      $\text{cnf}(p2_{13}, \text{negated\_conjecture})$   
 $p_2(x_{23}, x_{24}) \Rightarrow p_2(f_4(x_{23}), f_4(x_{24}))$      $\text{cnf}(p2_{14}, \text{negated\_conjecture})$   
 $p_7(x_{29}, x_{30}) \Rightarrow p_2(f_8(x_{29}), f_8(x_{30}))$      $\text{cnf}(p2_{15}, \text{negated\_conjecture})$   
 $p_{11}(x_{11}, x_{12}) \Rightarrow (p_{12}(x_{11}, x_{12}) \text{ or } p_2(x_{11}, x_{12}))$      $\text{cnf}(p12_{16}, \text{negated\_conjecture})$   
 $(p_7(x_{34}, x_{35}) \text{ and } p_7(x_{34}, x_{36})) \Rightarrow p_7(x_{35}, x_{36})$      $\text{cnf}(p7_{17}, \text{negated\_conjecture})$   
 $(p_2(x_{18}, x_{19}) \text{ and } p_2(x_{18}, x_{20})) \Rightarrow p_2(x_{19}, x_{20})$      $\text{cnf}(p2_{18}, \text{negated\_conjecture})$   
 $(p_5(x_{31}, x_{32}) \text{ and } p_5(x_{31}, x_{33})) \Rightarrow p_5(x_{32}, x_{33})$      $\text{cnf}(p5_{19}, \text{negated\_conjecture})$   
 $(p_{11}(x_6, c_{14}) \text{ and } p_{11}(c_{13}, x_6)) \Rightarrow p_{10}(c_{15}, f_3(x_6), x_6)$      $\text{cnf}(p10_{20}, \text{negated\_conjecture})$   
 $(p_2(x_9, x_7) \text{ and } p_2(x_{10}, x_8) \text{ and } p_{11}(x_9, x_{10})) \Rightarrow p_{11}(x_7, x_8)$      $\text{cnf}(p11_{21}, \text{negated\_conjecture})$   
 $(p_2(x_{16}, x_{14}) \text{ and } p_2(x_{17}, x_{15}) \text{ and } p_{12}(x_{16}, x_{17})) \Rightarrow p_{12}(x_{14}, x_{15})$      $\text{cnf}(p12_{22}, \text{negated\_conjecture})$   
 $(p_2(x_{26}, x_{28}) \text{ and } p_5(x_{25}, x_{27})) \Rightarrow p_2(f_6(x_{25}, x_{26}), f_6(x_{27}, x_{28}))$      $\text{cnf}(p2_{23}, \text{negated\_conjecture})$   
 $(p_5(x_3, x_0) \text{ and } p_2(x_5, x_2) \text{ and } p_2(x_4, x_1) \text{ and } p_{10}(x_3, x_4, x_5)) \Rightarrow p_{10}(x_0, x_1, x_2)$      $\text{cnf}(p10_{24}, \text{negated\_conjecture})$   
 $(p_{12}(x_{13}, c_{14}) \text{ and } p_{12}(c_{13}, x_{13}) \text{ and } p_2(f_3(x_{13}), f_8(f_9(c_{17})))) \Rightarrow p_{11}(f_4(f_6(c_{15}, x_{13})), c_{16})$      $\text{cnf}(p11_{25}, \text{negated\_conjecture})$

**SYN582-1.p** Harrison problem 3467

$p_7(x_{34}, x_{34})$      $\text{cnf}(p7_1, \text{negated\_conjecture})$   
 $p_2(x_{18}, x_{18})$      $\text{cnf}(p2_2, \text{negated\_conjecture})$   
 $p_5(x_{31}, x_{31})$      $\text{cnf}(p5_3, \text{negated\_conjecture})$   
 $p_{12}(c_{18}, c_{14})$      $\text{cnf}(p12_4, \text{negated\_conjecture})$   
 $p_2(c_{13}, c_{18})$      $\text{cnf}(p2_5, \text{negated\_conjecture})$   
 $p_2(f_3(c_{18}), f_8(f_9(c_{17})))$      $\text{cnf}(p2_6, \text{negated\_conjecture})$   
 $p_{11}(f_4(f_6(c_{15}, c_{13})), c_{16})$      $\text{cnf}(p11_7, \text{negated\_conjecture})$   
 $p_{11}(f_4(f_6(c_{15}, c_{14})), c_{16})$      $\text{cnf}(p11_8, \text{negated\_conjecture})$   
 $\neg p_{11}(f_4(f_6(c_{15}, c_{18})), c_{16})$      $\text{cnf}(\text{not\_}p11_9, \text{negated\_conjecture})$   
 $p_{12}(x_{11}, x_{12}) \Rightarrow p_{11}(x_{11}, x_{12})$      $\text{cnf}(p11_{10}, \text{negated\_conjecture})$   
 $p_2(x_{11}, x_{12}) \Rightarrow p_{11}(x_{11}, x_{12})$      $\text{cnf}(p11_{11}, \text{negated\_conjecture})$   
 $p_7(x_{37}, x_{38}) \Rightarrow p_7(f_9(x_{37}), f_9(x_{38}))$      $\text{cnf}(p7_{12}, \text{negated\_conjecture})$   
 $p_2(x_{21}, x_{22}) \Rightarrow p_2(f_3(x_{21}), f_3(x_{22}))$      $\text{cnf}(p2_{13}, \text{negated\_conjecture})$   
 $p_2(x_{23}, x_{24}) \Rightarrow p_2(f_4(x_{23}), f_4(x_{24}))$      $\text{cnf}(p2_{14}, \text{negated\_conjecture})$   
 $p_7(x_{29}, x_{30}) \Rightarrow p_2(f_8(x_{29}), f_8(x_{30}))$      $\text{cnf}(p2_{15}, \text{negated\_conjecture})$   
 $p_{11}(x_{11}, x_{12}) \Rightarrow (p_{12}(x_{11}, x_{12}) \text{ or } p_2(x_{11}, x_{12}))$      $\text{cnf}(p12_{16}, \text{negated\_conjecture})$   
 $(p_7(x_{34}, x_{35}) \text{ and } p_7(x_{34}, x_{36})) \Rightarrow p_7(x_{35}, x_{36})$      $\text{cnf}(p7_{17}, \text{negated\_conjecture})$   
 $(p_2(x_{18}, x_{19}) \text{ and } p_2(x_{18}, x_{20})) \Rightarrow p_2(x_{19}, x_{20})$      $\text{cnf}(p2_{18}, \text{negated\_conjecture})$   
 $(p_5(x_{31}, x_{32}) \text{ and } p_5(x_{31}, x_{33})) \Rightarrow p_5(x_{32}, x_{33})$      $\text{cnf}(p5_{19}, \text{negated\_conjecture})$   
 $(p_{11}(x_6, c_{14}) \text{ and } p_{11}(c_{13}, x_6)) \Rightarrow p_{10}(c_{15}, f_3(x_6), x_6)$      $\text{cnf}(p10_{20}, \text{negated\_conjecture})$   
 $(p_2(x_9, x_7) \text{ and } p_2(x_{10}, x_8) \text{ and } p_{11}(x_9, x_{10})) \Rightarrow p_{11}(x_7, x_8)$      $\text{cnf}(p11_{21}, \text{negated\_conjecture})$   
 $(p_2(x_{16}, x_{14}) \text{ and } p_2(x_{17}, x_{15}) \text{ and } p_{12}(x_{16}, x_{17})) \Rightarrow p_{12}(x_{14}, x_{15})$      $\text{cnf}(p12_{22}, \text{negated\_conjecture})$   
 $(p_2(x_{26}, x_{28}) \text{ and } p_5(x_{25}, x_{27})) \Rightarrow p_2(f_6(x_{25}, x_{26}), f_6(x_{27}, x_{28}))$      $\text{cnf}(p2_{23}, \text{negated\_conjecture})$   
 $(p_5(x_3, x_0) \text{ and } p_2(x_5, x_2) \text{ and } p_2(x_4, x_1) \text{ and } p_{10}(x_3, x_4, x_5)) \Rightarrow p_{10}(x_0, x_1, x_2)$      $\text{cnf}(p10_{24}, \text{negated\_conjecture})$   
 $(p_{12}(x_{13}, c_{14}) \text{ and } p_{12}(c_{13}, x_{13}) \text{ and } p_2(f_3(x_{13}), f_8(f_9(c_{17})))) \Rightarrow p_{11}(f_4(f_6(c_{15}, x_{13})), c_{16})$      $\text{cnf}(p11_{25}, \text{negated\_conjecture})$

**SYN583-1.p** Harrison problem 3468

$p_7(x_{34}, x_{34}) \quad \text{cnf}(p_{7_1}, \text{negated\_conjecture})$   
 $p_2(x_{18}, x_{18}) \quad \text{cnf}(p_{2_2}, \text{negated\_conjecture})$   
 $p_5(x_{31}, x_{31}) \quad \text{cnf}(p_{5_3}, \text{negated\_conjecture})$   
 $p_2(c_{13}, c_{18}) \quad \text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $p_2(c_{18}, c_{14}) \quad \text{cnf}(p_{2_5}, \text{negated\_conjecture})$   
 $p_2(f_3(c_{18}), f_8(f_9(c_{17}))) \quad \text{cnf}(p_{2_6}, \text{negated\_conjecture})$   
 $p_{11}(f_4(f_6(c_{15}, c_{13})), c_{16}) \quad \text{cnf}(p_{11_7}, \text{negated\_conjecture})$   
 $p_{11}(f_4(f_6(c_{15}, c_{14})), c_{16}) \quad \text{cnf}(p_{11_8}, \text{negated\_conjecture})$   
 $\neg p_{11}(f_4(f_6(c_{15}, c_{18})), c_{16}) \quad \text{cnf}(\text{not\_p}_{11_9}, \text{negated\_conjecture})$   
 $p_{12}(x_{11}, x_{12}) \Rightarrow p_{11}(x_{11}, x_{12}) \quad \text{cnf}(p_{11_{10}}, \text{negated\_conjecture})$   
 $p_2(x_{11}, x_{12}) \Rightarrow p_{11}(x_{11}, x_{12}) \quad \text{cnf}(p_{11_{11}}, \text{negated\_conjecture})$   
 $p_7(x_{37}, x_{38}) \Rightarrow p_7(f_9(x_{37}), f_9(x_{38})) \quad \text{cnf}(p_{7_{12}}, \text{negated\_conjecture})$   
 $p_2(x_{21}, x_{22}) \Rightarrow p_2(f_3(x_{21}), f_3(x_{22})) \quad \text{cnf}(p_{2_{13}}, \text{negated\_conjecture})$   
 $p_2(x_{23}, x_{24}) \Rightarrow p_2(f_4(x_{23}), f_4(x_{24})) \quad \text{cnf}(p_{2_{14}}, \text{negated\_conjecture})$   
 $p_7(x_{29}, x_{30}) \Rightarrow p_2(f_8(x_{29}), f_8(x_{30})) \quad \text{cnf}(p_{2_{15}}, \text{negated\_conjecture})$   
 $p_{11}(x_{11}, x_{12}) \Rightarrow (p_{12}(x_{11}, x_{12}) \text{ or } p_2(x_{11}, x_{12})) \quad \text{cnf}(p_{12_{16}}, \text{negated\_conjecture})$   
 $(p_7(x_{34}, x_{35}) \text{ and } p_7(x_{34}, x_{36})) \Rightarrow p_7(x_{35}, x_{36}) \quad \text{cnf}(p_{7_{17}}, \text{negated\_conjecture})$   
 $(p_2(x_{18}, x_{19}) \text{ and } p_2(x_{18}, x_{20})) \Rightarrow p_2(x_{19}, x_{20}) \quad \text{cnf}(p_{2_{18}}, \text{negated\_conjecture})$   
 $(p_5(x_{31}, x_{32}) \text{ and } p_5(x_{31}, x_{33})) \Rightarrow p_5(x_{32}, x_{33}) \quad \text{cnf}(p_{5_{19}}, \text{negated\_conjecture})$   
 $(p_{11}(x_6, c_{14}) \text{ and } p_{11}(c_{13}, x_6)) \Rightarrow p_{10}(c_{15}, f_3(x_6), x_6) \quad \text{cnf}(p_{10_{20}}, \text{negated\_conjecture})$   
 $(p_2(x_9, x_7) \text{ and } p_2(x_{10}, x_8) \text{ and } p_{11}(x_9, x_{10})) \Rightarrow p_{11}(x_7, x_8) \quad \text{cnf}(p_{11_{21}}, \text{negated\_conjecture})$   
 $(p_2(x_{16}, x_{14}) \text{ and } p_2(x_{17}, x_{15}) \text{ and } p_{12}(x_{16}, x_{17})) \Rightarrow p_{12}(x_{14}, x_{15}) \quad \text{cnf}(p_{12_{22}}, \text{negated\_conjecture})$   
 $(p_2(x_{26}, x_{28}) \text{ and } p_5(x_{25}, x_{27})) \Rightarrow p_2(f_6(x_{25}, x_{26}), f_6(x_{27}, x_{28})) \quad \text{cnf}(p_{2_{23}}, \text{negated\_conjecture})$   
 $(p_5(x_3, x_0) \text{ and } p_2(x_5, x_2) \text{ and } p_2(x_4, x_1) \text{ and } p_{10}(x_3, x_4, x_5)) \Rightarrow p_{10}(x_0, x_1, x_2) \quad \text{cnf}(p_{10_{24}}, \text{negated\_conjecture})$   
 $(p_{12}(x_{13}, c_{14}) \text{ and } p_{12}(c_{13}, x_{13}) \text{ and } p_2(f_3(x_{13}), f_8(f_9(c_{17})))) \Rightarrow p_{11}(f_4(f_6(c_{15}, x_{13})), c_{16}) \quad \text{cnf}(p_{11_{25}}, \text{negated\_conjecture})$

**SYN584-1.p** Harrison problem 3511

$p_{12}(x_0, x_0) \quad \text{cnf}(p_{12_1}, \text{negated\_conjecture})$   
 $p_6(x_{42}, x_{42}) \quad \text{cnf}(p_{6_2}, \text{negated\_conjecture})$   
 $p_5(x_{31}, x_{31}) \quad \text{cnf}(p_{5_3}, \text{negated\_conjecture})$   
 $p_3(x_{26}, x_{26}) \quad \text{cnf}(p_{3_4}, \text{negated\_conjecture})$   
 $p_2(x_{19}, x_{19}) \quad \text{cnf}(p_{2_5}, \text{negated\_conjecture})$   
 $p_5(x_{36}, x_{37}) \Rightarrow p_5(f_{11}(x_{36}), f_{11}(x_{37})) \quad \text{cnf}(p_{5_6}, \text{negated\_conjecture})$   
 $p_2(x_{29}, x_{30}) \Rightarrow p_3(f_4(x_{29}), f_4(x_{30})) \quad \text{cnf}(p_{3_7}, \text{negated\_conjecture})$   
 $p_5(x_{34}, x_{35}) \Rightarrow p_5(f_{10}(x_{34}), f_{10}(x_{35})) \quad \text{cnf}(p_{5_8}, \text{negated\_conjecture})$   
 $(p_{12}(x_0, x_1) \text{ and } p_{12}(x_0, x_2)) \Rightarrow p_{12}(x_1, x_2) \quad \text{cnf}(p_{12_9}, \text{negated\_conjecture})$   
 $(p_6(x_{42}, x_{43}) \text{ and } p_6(x_{42}, x_{44})) \Rightarrow p_6(x_{43}, x_{44}) \quad \text{cnf}(p_{6_{10}}, \text{negated\_conjecture})$   
 $(p_5(x_{31}, x_{32}) \text{ and } p_5(x_{31}, x_{33})) \Rightarrow p_5(x_{32}, x_{33}) \quad \text{cnf}(p_{5_{11}}, \text{negated\_conjecture})$   
 $(p_3(x_{26}, x_{27}) \text{ and } p_3(x_{26}, x_{28})) \Rightarrow p_3(x_{27}, x_{28}) \quad \text{cnf}(p_{3_{12}}, \text{negated\_conjecture})$   
 $(p_2(x_{19}, x_{20}) \text{ and } p_2(x_{19}, x_{21})) \Rightarrow p_2(x_{20}, x_{21}) \quad \text{cnf}(p_{2_{13}}, \text{negated\_conjecture})$   
 $(p_{12}(x_{18}, x_{16}) \text{ and } p_{16}(x_{17}, x_{18}) \text{ and } p_{12}(x_{17}, x_{15})) \Rightarrow p_{16}(x_{15}, x_{16}) \quad \text{cnf}(p_{16_{14}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{13}, x_{14}) \text{ and } p_3(x_{14}, x_{12}) \text{ and } p_{12}(x_{13}, x_{11})) \Rightarrow p_{15}(x_{11}, x_{12}) \quad \text{cnf}(p_{15_{15}}, \text{negated\_conjecture})$   
 $(p_{12}(x_3, x_5) \text{ and } p_{12}(x_4, x_6)) \Rightarrow p_{12}(f_{13}(x_3, x_4), f_{13}(x_5, x_6)) \quad \text{cnf}(p_{12_{16}}, \text{negated\_conjecture})$   
 $(p_5(x_{45}, x_{47}) \text{ and } p_5(x_{46}, x_{48})) \Rightarrow p_6(f_8(x_{45}, x_{46}), f_8(x_{47}, x_{48})) \quad \text{cnf}(p_{6_{17}}, \text{negated\_conjecture})$   
 $(p_5(x_{38}, x_{40}) \text{ and } p_5(x_{39}, x_{41})) \Rightarrow p_5(f_9(x_{38}, x_{39}), f_9(x_{40}, x_{41})) \quad \text{cnf}(p_{5_{18}}, \text{negated\_conjecture})$   
 $(p_5(x_{22}, x_{24}) \text{ and } p_6(x_{23}, x_{25})) \Rightarrow p_2(f_7(x_{22}, x_{23}), f_7(x_{24}, x_{25})) \quad \text{cnf}(p_{2_{19}}, \text{negated\_conjecture})$   
 $(p_{12}(x_8, x_{10}) \text{ and } p_2(x_7, x_9)) \Rightarrow p_{12}(f_{14}(x_7, x_8), f_{14}(x_9, x_{10})) \quad \text{cnf}(p_{12_{20}}, \text{negated\_conjecture})$   
 $p_{15}(c_{22}, f_4(f_7(c_{18}, f_8(f_9(c_{19}, f_{10}(f_{11}(c_{20}))))), f_9(c_{21}, f_{10}(f_{11}(c_{20})))))) \quad \text{cnf}(p_{15_{21}}, \text{negated\_conjecture})$   
 $p_{15}(c_{17}, f_4(f_7(c_{18}, f_8(f_9(c_{19}, f_{10}(f_{11}(c_{20}))))), f_9(c_{21}, f_{10}(f_{11}(c_{20})))))) \quad \text{cnf}(p_{15_{22}}, \text{negated\_conjecture})$   
 $p_{12}(f_{13}(c_{17}, f_{14}(f_7(c_{18}, f_8(f_9(c_{19}, f_{10}(f_{11}(c_{20}))))), f_9(c_{21}, f_{10}(f_{11}(c_{20}))))), c_{17}), c_{22}) \quad \text{cnf}(p_{12_{23}}, \text{negated\_conjecture})$   
 $(p_{16}(x_{49}, c_{17}) \text{ and } p_{16}(c_{22}, x_{49})) \Rightarrow \neg p_{15}(x_{49}, f_4(f_7(c_{18}, f_8(f_9(c_{19}, f_{10}(f_{11}(c_{20}))))), f_9(c_{21}, f_{10}(f_{11}(c_{20})))))) \quad \text{cnf}(\text{not\_p}_{16_{24}}, \text{negated\_conjecture})$   
 $\neg p_{15}(f_{13}(c_{17}, f_{14}(f_7(c_{18}, f_8(f_9(c_{19}, f_{10}(f_{11}(c_{20}))))), f_9(c_{21}, f_{10}(f_{11}(c_{20}))))), c_{17}), f_4(f_7(c_{18}, f_8(f_9(c_{19}, f_{10}(f_{11}(c_{20}))))), f_9(c_{21}, f_{10}(f_{11}(c_{20})))))) \quad \text{cnf}(\text{not\_p}_{16_{24}}, \text{negated\_conjecture})$

**SYN585-1.p** Harrison problem 3538

$p_2(x_{18}, x_{18}) \quad \text{cnf}(p_{2_1}, \text{negated\_conjecture})$   
 $p_{11}(x_8, x_8) \quad \text{cnf}(p_{11_2}, \text{negated\_conjecture})$   
 $p_{10}(c_{14}, c_{15}) \quad \text{cnf}(p_{10_3}, \text{negated\_conjecture})$   
 $p_{10}(c_{17}, c_{14}) \quad \text{cnf}(p_{10_4}, \text{negated\_conjecture})$   
 $\neg p_2(c_{14}, f_3(c_{13})) \quad \text{cnf}(\text{not\_p}_{2_5}, \text{negated\_conjecture})$

$\neg p_2(c_{12}, f_3(c_{13})) \quad \text{cnf}(\text{not\_p2}_6, \text{negated\_conjecture})$   
 $p_{11}(c_{18}, f_9(c_{12}, c_{14})) \quad \text{cnf}(p_{11}_7, \text{negated\_conjecture})$   
 $p_2(f_6(c_{15}, c_{14}), c_{17}) \quad \text{cnf}(p_{28}, \text{negated\_conjecture})$   
 $p_2(f_5(c_{15}, c_{14}), c_{16}) \quad \text{cnf}(p_{29}, \text{negated\_conjecture})$   
 $\neg p_2(c_{12}, f_3(f_4(c_{13}))) \quad \text{cnf}(\text{not\_p2}_{10}, \text{negated\_conjecture})$   
 $p_2(f_7(f_8(c_{16}, c_{14}), c_{17}), c_{15}) \quad \text{cnf}(p_{211}, \text{negated\_conjecture})$   
 $\neg p_{11}(c_{18}, f_9(c_{12}, f_8(c_{16}, c_{14}))) \quad \text{cnf}(\text{not\_p11}_{12}, \text{negated\_conjecture})$   
 $p_{11}(x_9, x_{11}) \Rightarrow p_{11}(x_9, f_8(x_{10}, x_{11})) \quad \text{cnf}(p_{11}_{13}, \text{negated\_conjecture})$   
 $p_2(x_{23}, x_{24}) \Rightarrow p_2(f_4(x_{23}), f_4(x_{24})) \quad \text{cnf}(p_{214}, \text{negated\_conjecture})$   
 $p_2(x_{21}, x_{22}) \Rightarrow p_2(f_3(x_{21}), f_3(x_{22})) \quad \text{cnf}(p_{215}, \text{negated\_conjecture})$   
 $(p_{11}(x_{12}, x_{14}) \text{ and } p_{11}(x_{14}, x_{13})) \Rightarrow p_{11}(x_{12}, x_{13}) \quad \text{cnf}(p_{11}_{16}, \text{negated\_conjecture})$   
 $(p_2(x_{18}, x_{19}) \text{ and } p_2(x_{18}, x_{20})) \Rightarrow p_2(x_{19}, x_{20}) \quad \text{cnf}(p_{217}, \text{negated\_conjecture})$   
 $(p_2(x_2, x_0) \text{ and } p_2(x_3, x_1) \text{ and } p_{10}(x_2, x_3)) \Rightarrow p_{10}(x_0, x_1) \quad \text{cnf}(p_{10}_{18}, \text{negated\_conjecture})$   
 $(p_2(x_6, x_4) \text{ and } p_2(x_7, x_5) \text{ and } p_{11}(x_6, x_7)) \Rightarrow p_{11}(x_4, x_5) \quad \text{cnf}(p_{11}_{19}, \text{negated\_conjecture})$   
 $(p_2(x_{41}, x_{43}) \text{ and } p_2(x_{42}, x_{44})) \Rightarrow p_2(f_9(x_{41}, x_{42}), f_9(x_{43}, x_{44})) \quad \text{cnf}(p_{220}, \text{negated\_conjecture})$   
 $(p_2(x_{25}, x_{27}) \text{ and } p_2(x_{26}, x_{28})) \Rightarrow p_2(f_5(x_{25}, x_{26}), f_5(x_{27}, x_{28})) \quad \text{cnf}(p_{221}, \text{negated\_conjecture})$   
 $(p_2(x_{30}, x_{32}) \text{ and } p_2(x_{29}, x_{31})) \Rightarrow p_2(f_6(x_{29}, x_{30}), f_6(x_{31}, x_{32})) \quad \text{cnf}(p_{222}, \text{negated\_conjecture})$   
 $(p_2(x_{33}, x_{35}) \text{ and } p_2(x_{34}, x_{36})) \Rightarrow p_2(f_7(x_{33}, x_{34}), f_7(x_{35}, x_{36})) \quad \text{cnf}(p_{223}, \text{negated\_conjecture})$   
 $(p_2(x_{37}, x_{39}) \text{ and } p_2(x_{38}, x_{40})) \Rightarrow p_2(f_8(x_{37}, x_{38}), f_8(x_{39}, x_{40})) \quad \text{cnf}(p_{224}, \text{negated\_conjecture})$   
 $p_{11}(f_9(x_{17}, x_{15}), f_9(x_{17}, x_{16})) \Rightarrow (p_{11}(x_{15}, x_{16}) \text{ or } p_2(x_{17}, f_3(c_{13}))) \quad \text{cnf}(p_{11}_{25}, \text{negated\_conjecture})$   
 $p_{11}(x_{15}, x_{16}) \Rightarrow (p_2(x_{17}, f_3(c_{13})) \text{ or } p_{11}(f_9(x_{17}, x_{15}), f_9(x_{17}, x_{16}))) \quad \text{cnf}(p_{226}, \text{negated\_conjecture})$

### SYN586-1.p Harrison problem 3571

$p_{12}(x_0, x_0) \quad \text{cnf}(p_{12}_1, \text{negated\_conjecture})$   
 $p_5(x_{37}, x_{37}) \quad \text{cnf}(p_{52}, \text{negated\_conjecture})$   
 $p_3(x_{24}, x_{24}) \quad \text{cnf}(p_{33}, \text{negated\_conjecture})$   
 $p_2(x_{13}, x_{13}) \quad \text{cnf}(p_{24}, \text{negated\_conjecture})$   
 $p_3(c_{21}, c_{19}) \quad \text{cnf}(p_{35}, \text{negated\_conjecture})$   
 $\neg p_{12}(f_{13}(c_{20}), f_{13}(c_{18})) \quad \text{cnf}(\text{not\_p12}_6, \text{negated\_conjecture})$   
 $p_2(x_3, x_4) \Rightarrow p_{12}(f_{13}(x_3), f_{13}(x_4)) \quad \text{cnf}(p_{12}_7, \text{negated\_conjecture})$   
 $p_3(x_{42}, x_{43}) \Rightarrow p_5(f_7(x_{42}), f_7(x_{43})) \quad \text{cnf}(p_{58}, \text{negated\_conjecture})$   
 $p_5(x_{40}, x_{41}) \Rightarrow p_5(f_{10}(x_{40}), f_{10}(x_{41})) \quad \text{cnf}(p_{59}, \text{negated\_conjecture})$   
 $p_3(x_{35}, x_{36}) \Rightarrow p_3(f_9(x_{35}), f_9(x_{36})) \quad \text{cnf}(p_{310}, \text{negated\_conjecture})$   
 $p_3(x_{33}, x_{34}) \Rightarrow p_3(f_8(x_{33}), f_8(x_{34})) \quad \text{cnf}(p_{311}, \text{negated\_conjecture})$   
 $p_3(x_{27}, x_{28}) \Rightarrow p_3(f_{11}(x_{27}), f_{11}(x_{28})) \quad \text{cnf}(p_{312}, \text{negated\_conjecture})$   
 $(p_{12}(x_0, x_1) \text{ and } p_{12}(x_0, x_2)) \Rightarrow p_{12}(x_1, x_2) \quad \text{cnf}(p_{12}_{13}, \text{negated\_conjecture})$   
 $(p_5(x_{37}, x_{38}) \text{ and } p_5(x_{37}, x_{39})) \Rightarrow p_5(x_{38}, x_{39}) \quad \text{cnf}(p_{514}, \text{negated\_conjecture})$   
 $(p_3(x_{24}, x_{25}) \text{ and } p_3(x_{24}, x_{26})) \Rightarrow p_3(x_{25}, x_{26}) \quad \text{cnf}(p_{315}, \text{negated\_conjecture})$   
 $(p_2(x_{13}, x_{14}) \text{ and } p_2(x_{13}, x_{15})) \Rightarrow p_2(x_{14}, x_{15}) \quad \text{cnf}(p_{216}, \text{negated\_conjecture})$   
 $(p_2(x_{11}, x_9) \text{ and } p_2(x_{12}, x_{10}) \text{ and } p_{15}(x_{11}, x_{12})) \Rightarrow p_{15}(x_9, x_{10}) \quad \text{cnf}(p_{15}_{17}, \text{negated\_conjecture})$   
 $p_{15}(f_4(f_6(f_{10}(c_{16}), f_6(f_7(f_8(f_9(c_{17}))), c_{18})), c_{19}), c_{20}) \quad \text{cnf}(p_{15}_{18}, \text{negated\_conjecture})$   
 $(p_2(x_{29}, x_{31}) \text{ and } p_5(x_{30}, x_{32})) \Rightarrow p_3(f_{14}(x_{29}, x_{30}), f_{14}(x_{31}, x_{32})) \quad \text{cnf}(p_{319}, \text{negated\_conjecture})$   
 $(p_2(x_{16}, x_{18}) \text{ and } p_3(x_{17}, x_{19})) \Rightarrow p_2(f_4(x_{16}, x_{17}), f_4(x_{18}, x_{19})) \quad \text{cnf}(p_{220}, \text{negated\_conjecture})$   
 $(p_2(x_{21}, x_{23}) \text{ and } p_5(x_{20}, x_{22})) \Rightarrow p_2(f_6(x_{20}, x_{21}), f_6(x_{22}, x_{23})) \quad \text{cnf}(p_{221}, \text{negated\_conjecture})$   
 $p_{15}(f_4(f_6(f_{10}(c_{16}), f_6(f_7(f_8(f_9(c_{17}))), c_{18})), f_{11}(c_{21}), c_{20}) \quad \text{cnf}(p_{15}_{22}, \text{negated\_conjecture})$   
 $\neg p_{15}(f_4(f_6(f_{10}(c_{16}), f_6(f_7(f_8(f_9(c_{17}))), c_{18})), f_{11}(c_{19}), c_{20}) \quad \text{cnf}(\text{not\_p15}_{23}, \text{negated\_conjecture})$   
 $p_{12}(f_{13}(x_5), f_{13}(c_{18})) \text{ or } p_{15}(f_4(f_6(f_{10}(x_6), f_6(f_7(f_8(f_9(c_{17}))), c_{18})), f_{14}(x_5, x_6)), x_5) \quad \text{cnf}(p_{12}_{24}, \text{negated\_conjecture})$   
 $p_{15}(f_4(f_6(f_{10}(x_6), f_6(f_7(f_8(f_9(c_{17}))), c_{18})), f_{11}(f_{14}(x_5, x_6))), x_5) \Rightarrow p_{12}(f_{13}(x_5), f_{13}(c_{18})) \quad \text{cnf}(p_{12}_{25}, \text{negated\_conjecture})$   
 $(p_{15}(f_4(f_6(f_{10}(x_6), f_6(f_7(f_8(f_9(c_{17}))), c_{18})), x_7), x_5) \text{ and } p_{15}(f_4(f_6(f_{10}(x_6), f_6(f_7(f_8(f_9(c_{17}))), c_{18})), x_8), x_5)) \Rightarrow (p_3(x_7, x_8) \text{ or } p_2(x_7, x_8))$

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$p_{12}(x_0, x_0) \quad \text{cnf}(p_{12}_1, \text{negated\_conjecture})$   
 $p_5(x_{37}, x_{37}) \quad \text{cnf}(p_{52}, \text{negated\_conjecture})$   
 $p_3(x_{24}, x_{24}) \quad \text{cnf}(p_{33}, \text{negated\_conjecture})$   
 $p_2(x_{13}, x_{13}) \quad \text{cnf}(p_{24}, \text{negated\_conjecture})$   
 $p_3(c_{21}, c_{19}) \quad \text{cnf}(p_{35}, \text{negated\_conjecture})$   
 $\neg p_{12}(f_{13}(c_{20}), f_{13}(c_{18})) \quad \text{cnf}(\text{not\_p12}_6, \text{negated\_conjecture})$   
 $p_2(x_3, x_4) \Rightarrow p_{12}(f_{13}(x_3), f_{13}(x_4)) \quad \text{cnf}(p_{12}_7, \text{negated\_conjecture})$   
 $p_3(x_{42}, x_{43}) \Rightarrow p_5(f_7(x_{42}), f_7(x_{43})) \quad \text{cnf}(p_{58}, \text{negated\_conjecture})$   
 $p_5(x_{40}, x_{41}) \Rightarrow p_5(f_{10}(x_{40}), f_{10}(x_{41})) \quad \text{cnf}(p_{59}, \text{negated\_conjecture})$

$p_3(x_{35}, x_{36}) \Rightarrow p_3(f_9(x_{35}), f_9(x_{36})) \quad \text{cnf}(p_{3_{10}}, \text{negated\_conjecture})$   
 $p_3(x_{33}, x_{34}) \Rightarrow p_3(f_8(x_{33}), f_8(x_{34})) \quad \text{cnf}(p_{3_{11}}, \text{negated\_conjecture})$   
 $p_3(x_{27}, x_{28}) \Rightarrow p_3(f_{11}(x_{27}), f_{11}(x_{28})) \quad \text{cnf}(p_{3_{12}}, \text{negated\_conjecture})$   
 $(p_{12}(x_0, x_1) \text{ and } p_{12}(x_0, x_2)) \Rightarrow p_{12}(x_1, x_2) \quad \text{cnf}(p_{12_{13}}, \text{negated\_conjecture})$   
 $(p_5(x_{37}, x_{38}) \text{ and } p_5(x_{37}, x_{39})) \Rightarrow p_5(x_{38}, x_{39}) \quad \text{cnf}(p_{5_{14}}, \text{negated\_conjecture})$   
 $(p_3(x_{24}, x_{25}) \text{ and } p_3(x_{24}, x_{26})) \Rightarrow p_3(x_{25}, x_{26}) \quad \text{cnf}(p_{3_{15}}, \text{negated\_conjecture})$   
 $(p_2(x_{13}, x_{14}) \text{ and } p_2(x_{13}, x_{15})) \Rightarrow p_2(x_{14}, x_{15}) \quad \text{cnf}(p_{2_{16}}, \text{negated\_conjecture})$   
 $(p_2(x_{11}, x_9) \text{ and } p_2(x_{12}, x_{10}) \text{ and } p_{15}(x_{11}, x_{12})) \Rightarrow p_{15}(x_9, x_{10}) \quad \text{cnf}(p_{15_{17}}, \text{negated\_conjecture})$   
 $p_{15}(f_4(f_6(f_{10}(c_{16}), f_6(f_7(f_8(f_9(c_{17})))), c_{18})), c_{19}), c_{20}) \quad \text{cnf}(p_{15_{18}}, \text{negated\_conjecture})$   
 $\neg p_{15}(f_4(f_6(f_{10}(c_{16}), f_6(f_7(f_8(f_9(c_{17})))), c_{18})), c_{21}), c_{20}) \quad \text{cnf}(\text{not\_}p_{15_{19}}, \text{negated\_conjecture})$   
 $(p_2(x_{16}, x_{18}) \text{ and } p_3(x_{17}, x_{19})) \Rightarrow p_2(f_4(x_{16}, x_{17}), f_4(x_{18}, x_{19})) \quad \text{cnf}(p_{2_{20}}, \text{negated\_conjecture})$   
 $(p_2(x_{29}, x_{31}) \text{ and } p_5(x_{30}, x_{32})) \Rightarrow p_3(f_{14}(x_{29}, x_{30}), f_{14}(x_{31}, x_{32})) \quad \text{cnf}(p_{3_{21}}, \text{negated\_conjecture})$   
 $(p_2(x_{21}, x_{23}) \text{ and } p_5(x_{20}, x_{22})) \Rightarrow p_2(f_6(x_{20}, x_{21}), f_6(x_{22}, x_{23})) \quad \text{cnf}(p_{2_{22}}, \text{negated\_conjecture})$   
 $\neg p_{15}(f_4(f_6(f_{10}(c_{16}), f_6(f_7(f_8(f_9(c_{17})))), c_{18})), f_{11}(c_{19}), c_{20}) \quad \text{cnf}(\text{not\_}p_{15_{23}}, \text{negated\_conjecture})$   
 $p_{12}(f_{13}(x_5), f_{13}(c_{18})) \text{ or } p_{15}(f_4(f_6(f_{10}(x_6), f_6(f_7(f_8(f_9(c_{17})))), c_{18})), f_{14}(x_5, x_6), x_5) \quad \text{cnf}(p_{12_{24}}, \text{negated\_conjecture})$   
 $p_{15}(f_4(f_6(f_{10}(x_6), f_6(f_7(f_8(f_9(c_{17})))), c_{18})), f_{11}(f_{14}(x_5, x_6))), x_5) \Rightarrow p_{12}(f_{13}(x_5), f_{13}(c_{18})) \quad \text{cnf}(p_{12_{25}}, \text{negated\_conjecture})$   
 $(p_{15}(f_4(f_6(f_{10}(x_6), f_6(f_7(f_8(f_9(c_{17})))), c_{18})), x_7), x_5) \text{ and } p_{15}(f_4(f_6(f_{10}(x_6), f_6(f_7(f_8(f_9(c_{17})))), c_{18})), x_8), x_5) \Rightarrow (p_3(x_7, x_8) \text{ or } p_3(x_7, x_8))$

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$p_2(x_8, x_8) \quad \text{cnf}(p_{2_1}, \text{negated\_conjecture})$   
 $p_7(x_{25}, x_{25}) \quad \text{cnf}(p_{7_2}, \text{negated\_conjecture})$   
 $p_2(c_{25}, f_3(c_{17})) \quad \text{cnf}(p_{2_3}, \text{negated\_conjecture})$   
 $\neg p_2(c_{16}, f_3(c_{17})) \quad \text{cnf}(\text{not\_}p_{2_4}, \text{negated\_conjecture})$   
 $p_{14}(c_{18}, f_3(f_4(f_5(c_{17})))) \quad \text{cnf}(p_{14_5}, \text{negated\_conjecture})$   
 $p_{14}(c_{23}, f_3(f_4(f_5(c_{17})))) \quad \text{cnf}(p_{14_6}, \text{negated\_conjecture})$   
 $p_{14}(c_{19}, f_6(f_3(f_4(f_5(c_{17}))), c_{16})) \quad \text{cnf}(p_{14_7}, \text{negated\_conjecture})$   
 $p_{14}(c_{24}, f_6(f_3(f_4(f_5(c_{17}))), c_{16})) \quad \text{cnf}(p_{14_8}, \text{negated\_conjecture})$   
 $p_7(x_{34}, x_{35}) \Rightarrow p_7(f_{12}(x_{34}), f_{12}(x_{35})) \quad \text{cnf}(p_{7_9}, \text{negated\_conjecture})$   
 $p_2(x_{15}, x_{16}) \Rightarrow p_2(f_3(x_{15}), f_3(x_{16})) \quad \text{cnf}(p_{2_{10}}, \text{negated\_conjecture})$   
 $p_2(x_{17}, x_{18}) \Rightarrow p_2(f_4(x_{17}), f_4(x_{18})) \quad \text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $p_2(x_{19}, x_{20}) \Rightarrow p_2(f_5(x_{19}), f_5(x_{20})) \quad \text{cnf}(p_{2_{12}}, \text{negated\_conjecture})$   
 $p_2(x_{32}, x_{33}) \Rightarrow p_7(f_{11}(x_{32}), f_{11}(x_{33})) \quad \text{cnf}(p_{7_{13}}, \text{negated\_conjecture})$   
 $(p_7(x_{25}, x_{26}) \text{ and } p_7(x_{25}, x_{27})) \Rightarrow p_7(x_{26}, x_{27}) \quad \text{cnf}(p_{7_{14}}, \text{negated\_conjecture})$   
 $(p_2(x_8, x_9) \text{ and } p_2(x_8, x_{10})) \Rightarrow p_2(x_9, x_{10}) \quad \text{cnf}(p_{2_{15}}, \text{negated\_conjecture})$   
 $p_{15}(f_6(f_3(f_4(f_5(c_{17}))), f_{13}(c_{16}, f_3(f_5(c_{17}))))), c_{19}) \quad \text{cnf}(p_{15_{16}}, \text{negated\_conjecture})$   
 $(p_2(x_2, x_0) \text{ and } p_2(x_3, x_1) \text{ and } p_{14}(x_2, x_3)) \Rightarrow p_{14}(x_0, x_1) \quad \text{cnf}(p_{14_{17}}, \text{negated\_conjecture})$   
 $(p_2(x_6, x_4) \text{ and } p_2(x_7, x_5) \text{ and } p_{15}(x_6, x_7)) \Rightarrow p_{15}(x_4, x_5) \quad \text{cnf}(p_{15_{18}}, \text{negated\_conjecture})$   
 $(p_2(x_{11}, x_{13}) \text{ and } p_2(x_{12}, x_{14})) \Rightarrow p_2(f_{13}(x_{11}, x_{12}), f_{13}(x_{13}, x_{14})) \quad \text{cnf}(p_{2_{19}}, \text{negated\_conjecture})$   
 $(p_7(x_{40}, x_{42}) \text{ and } p_7(x_{41}, x_{43})) \Rightarrow p_7(f_9(x_{40}, x_{41}), f_9(x_{42}, x_{43})) \quad \text{cnf}(p_{7_{20}}, \text{negated\_conjecture})$   
 $(p_7(x_{36}, x_{38}) \text{ and } p_7(x_{37}, x_{39})) \Rightarrow p_7(f_8(x_{36}, x_{37}), f_8(x_{38}, x_{39})) \quad \text{cnf}(p_{7_{21}}, \text{negated\_conjecture})$   
 $(p_2(x_{29}, x_{31}) \text{ and } p_7(x_{28}, x_{30})) \Rightarrow p_7(f_{10}(x_{28}, x_{29}), f_{10}(x_{30}, x_{31})) \quad \text{cnf}(p_{7_{22}}, \text{negated\_conjecture})$   
 $(p_2(x_{21}, x_{23}) \text{ and } p_2(x_{22}, x_{24})) \Rightarrow p_2(f_6(x_{21}, x_{22}), f_6(x_{23}, x_{24})) \quad \text{cnf}(p_{2_{23}}, \text{negated\_conjecture})$   
 $p_7(c_{20}, f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{17}))))), c_{23}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{25}), f_9(f_{11}(c_{24}), f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{22})))))) \quad \text{cnf}(p_{7_{24}}, \text{negated\_conjecture})$   
 $p_7(c_{20}, f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{17}))))), c_{18}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{21}), f_9(f_{11}(c_{19}), f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{22})))))) \quad \text{cnf}(p_{7_{25}}, \text{negated\_conjecture})$   
 $\neg p_7(f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{17}))))), c_{18}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{21}), f_9(f_{11}(c_{19}), f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{22}))))), f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{17}))))), c_{18}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{21}), f_9(f_{11}(c_{19}), f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{22}))))))$

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$p_2(x_8, x_8) \quad \text{cnf}(p_{2_1}, \text{negated\_conjecture})$   
 $p_7(x_{25}, x_{25}) \quad \text{cnf}(p_{7_2}, \text{negated\_conjecture})$   
 $p_2(c_{21}, f_3(c_{17})) \quad \text{cnf}(p_{2_3}, \text{negated\_conjecture})$   
 $\neg p_2(c_{16}, f_3(c_{17})) \quad \text{cnf}(\text{not\_}p_{2_4}, \text{negated\_conjecture})$   
 $p_{14}(c_{18}, f_3(f_4(f_5(c_{17})))) \quad \text{cnf}(p_{14_5}, \text{negated\_conjecture})$   
 $p_{14}(c_{23}, f_3(f_4(f_5(c_{17})))) \quad \text{cnf}(p_{14_6}, \text{negated\_conjecture})$   
 $p_{14}(c_{19}, f_6(f_3(f_4(f_5(c_{17}))), c_{16})) \quad \text{cnf}(p_{14_7}, \text{negated\_conjecture})$   
 $p_{14}(c_{24}, f_6(f_3(f_4(f_5(c_{17}))), c_{16})) \quad \text{cnf}(p_{14_8}, \text{negated\_conjecture})$   
 $p_7(x_{34}, x_{35}) \Rightarrow p_7(f_{12}(x_{34}), f_{12}(x_{35})) \quad \text{cnf}(p_{7_9}, \text{negated\_conjecture})$   
 $p_2(x_{15}, x_{16}) \Rightarrow p_2(f_3(x_{15}), f_3(x_{16})) \quad \text{cnf}(p_{2_{10}}, \text{negated\_conjecture})$   
 $p_2(x_{17}, x_{18}) \Rightarrow p_2(f_4(x_{17}), f_4(x_{18})) \quad \text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $p_2(x_{19}, x_{20}) \Rightarrow p_2(f_5(x_{19}), f_5(x_{20})) \quad \text{cnf}(p_{2_{12}}, \text{negated\_conjecture})$   
 $p_2(x_{32}, x_{33}) \Rightarrow p_7(f_{11}(x_{32}), f_{11}(x_{33})) \quad \text{cnf}(p_{7_{13}}, \text{negated\_conjecture})$

$(p_7(x_{25}, x_{26}) \text{ and } p_7(x_{25}, x_{27})) \Rightarrow p_7(x_{26}, x_{27})$      $\text{cnf}(p_{7_{14}}, \text{negated\_conjecture})$   
 $(p_2(x_8, x_9) \text{ and } p_2(x_8, x_{10})) \Rightarrow p_2(x_9, x_{10})$      $\text{cnf}(p_{2_{15}}, \text{negated\_conjecture})$   
 $p_{15}(f_6(f_3(f_4(f_5(c_{17}))))), f_{13}(c_{16}, f_3(f_5(c_{17}))))), c_{24})$      $\text{cnf}(p_{15_{16}}, \text{negated\_conjecture})$   
 $(p_2(x_2, x_0) \text{ and } p_2(x_3, x_1) \text{ and } p_{14}(x_2, x_3)) \Rightarrow p_{14}(x_0, x_1)$      $\text{cnf}(p_{14_{17}}, \text{negated\_conjecture})$   
 $(p_2(x_6, x_4) \text{ and } p_2(x_7, x_5) \text{ and } p_{15}(x_6, x_7)) \Rightarrow p_{15}(x_4, x_5)$      $\text{cnf}(p_{15_{18}}, \text{negated\_conjecture})$   
 $(p_2(x_{11}, x_{13}) \text{ and } p_2(x_{12}, x_{14})) \Rightarrow p_2(f_{13}(x_{11}, x_{12}), f_{13}(x_{13}, x_{14}))$      $\text{cnf}(p_{2_{19}}, \text{negated\_conjecture})$   
 $(p_7(x_{40}, x_{42}) \text{ and } p_7(x_{41}, x_{43})) \Rightarrow p_7(f_9(x_{40}, x_{41}), f_9(x_{42}, x_{43}))$      $\text{cnf}(p_{7_{20}}, \text{negated\_conjecture})$   
 $(p_7(x_{36}, x_{38}) \text{ and } p_7(x_{37}, x_{39})) \Rightarrow p_7(f_8(x_{36}, x_{37}), f_8(x_{38}, x_{39}))$      $\text{cnf}(p_{7_{21}}, \text{negated\_conjecture})$   
 $(p_2(x_{29}, x_{31}) \text{ and } p_7(x_{28}, x_{30})) \Rightarrow p_7(f_{10}(x_{28}, x_{29}), f_{10}(x_{30}, x_{31}))$      $\text{cnf}(p_{7_{22}}, \text{negated\_conjecture})$   
 $(p_2(x_{21}, x_{23}) \text{ and } p_2(x_{22}, x_{24})) \Rightarrow p_2(f_6(x_{21}, x_{22}), f_6(x_{23}, x_{24}))$      $\text{cnf}(p_{2_{23}}, \text{negated\_conjecture})$   
 $p_7(c_{20}, f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{17}))))), c_{23}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{25}), f_9(f_{11}(c_{24}), f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{22}))))))$      $\text{cnf}$   
 $p_7(c_{20}, f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{17}))))), c_{18}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{21}), f_9(f_{11}(c_{19}), f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{22}))))))$      $\text{cnf}$   
 $\neg p_7(f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{17}))))), c_{18}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{21}), f_9(f_{11}(c_{19}), f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{22}))))), f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{17}))))), c_{23}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{25}), f_9(f_{11}(c_{24}), f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{22}))))))$

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$p_{11}(c_{14})$      $\text{cnf}(c_{14\_is\_p11_1}, \text{negated\_conjecture})$   
 $p_{11}(c_{17})$      $\text{cnf}(c_{17\_is\_p11_2}, \text{negated\_conjecture})$   
 $p_{11}(c_{16})$      $\text{cnf}(c_{16\_is\_p11_3}, \text{negated\_conjecture})$   
 $p_5(x_{27}, x_{27})$      $\text{cnf}(p_{5_4}, \text{negated\_conjecture})$   
 $p_2(x_{14}, x_{14})$      $\text{cnf}(p_{2_5}, \text{negated\_conjecture})$   
 $p_3(x_{19}, x_{19})$      $\text{cnf}(p_{3_6}, \text{negated\_conjecture})$   
 $p_3(f_4(c_{17}), f_6(c_{18}))$      $\text{cnf}(p_{3_7}, \text{negated\_conjecture})$   
 $p_3(f_4(c_{16}), f_6(c_{15}))$      $\text{cnf}(p_{3_8}, \text{negated\_conjecture})$   
 $p_{11}(x_4) \Rightarrow p_{11}(f_9(x_4))$      $\text{cnf}(p_{11_9}, \text{negated\_conjecture})$   
 $(p_{11}(x_9) \text{ and } p_2(x_9, x_8)) \Rightarrow p_{11}(x_8)$      $\text{cnf}(p_{11_{10}}, \text{negated\_conjecture})$   
 $p_{10}(f_6(x_5), f_6(x_6)) \Rightarrow p_{12}(x_5, x_6)$      $\text{cnf}(p_{12_{11}}, \text{negated\_conjecture})$   
 $p_2(x_{32}, x_{33}) \Rightarrow p_5(f_8(x_{32}), f_8(x_{33}))$      $\text{cnf}(p_{5_{12}}, \text{negated\_conjecture})$   
 $p_{12}(x_5, x_6) \Rightarrow p_{10}(f_6(x_5), f_6(x_6))$      $\text{cnf}(p_{10_{13}}, \text{negated\_conjecture})$   
 $p_2(x_{17}, x_{18}) \Rightarrow p_2(f_9(x_{17}), f_9(x_{18}))$      $\text{cnf}(p_{2_{14}}, \text{negated\_conjecture})$   
 $p_2(x_{22}, x_{23}) \Rightarrow p_3(f_4(x_{22}), f_4(x_{23}))$      $\text{cnf}(p_{3_{15}}, \text{negated\_conjecture})$   
 $p_5(x_{25}, x_{26}) \Rightarrow p_3(f_6(x_{25}), f_6(x_{26}))$      $\text{cnf}(p_{3_{16}}, \text{negated\_conjecture})$   
 $p_5(x_{30}, x_{31}) \Rightarrow p_5(f_7(x_{30}), f_7(x_{31}))$      $\text{cnf}(p_{5_{17}}, \text{negated\_conjecture})$   
 $p_{11}(x_{24}) \Rightarrow p_3(f_4(x_{24}), f_6(f_8(x_{24})))$      $\text{cnf}(p_{3_{18}}, \text{negated\_conjecture})$   
 $p_{11}(x_4) \Rightarrow p_{10}(f_4(f_9(x_4)), f_4(x_4))$      $\text{cnf}(p_{10_{19}}, \text{negated\_conjecture})$   
 $p_{11}(x_7) \Rightarrow p_{10}(f_6(f_7(c_{13})), f_4(x_7))$      $\text{cnf}(p_{10_{20}}, \text{negated\_conjecture})$   
 $p_{11}(x_4) \Rightarrow p_{10}(f_6(f_7(c_{13})), f_4(x_4))$      $\text{cnf}(p_{10_{21}}, \text{negated\_conjecture})$   
 $(p_5(x_{27}, x_{28}) \text{ and } p_5(x_{27}, x_{29})) \Rightarrow p_5(x_{28}, x_{29})$      $\text{cnf}(p_{5_{22}}, \text{negated\_conjecture})$   
 $(p_2(x_{14}, x_{15}) \text{ and } p_2(x_{14}, x_{16})) \Rightarrow p_2(x_{15}, x_{16})$      $\text{cnf}(p_{2_{23}}, \text{negated\_conjecture})$   
 $(p_3(x_{19}, x_{20}) \text{ and } p_3(x_{19}, x_{21})) \Rightarrow p_3(x_{20}, x_{21})$      $\text{cnf}(p_{3_{24}}, \text{negated\_conjecture})$   
 $(p_{11}(x_{34}) \text{ and } p_{12}(x_{35}, c_{15})) \Rightarrow \neg p_3(f_4(x_{34}), f_6(x_{35}))$      $\text{cnf}(\text{not\_}p_{11_{25}}, \text{negated\_conjecture})$   
 $(p_3(x_2, x_0) \text{ and } p_3(x_3, x_1) \text{ and } p_{10}(x_2, x_3)) \Rightarrow p_{10}(x_0, x_1)$      $\text{cnf}(p_{10_{26}}, \text{negated\_conjecture})$   
 $(p_5(x_{12}, x_{10}) \text{ and } p_5(x_{13}, x_{11}) \text{ and } p_{12}(x_{12}, x_{13})) \Rightarrow p_{12}(x_{10}, x_{11})$      $\text{cnf}(p_{12_{27}}, \text{negated\_conjecture})$

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$p_9(c_{14})$      $\text{cnf}(c_{14\_is\_p9_1}, \text{negated\_conjecture})$   
 $p_8(c_{13})$      $\text{cnf}(c_{13\_is\_p8_2}, \text{negated\_conjecture})$   
 $p_7(x_{30}, x_{30})$      $\text{cnf}(p_{7_3}, \text{negated\_conjecture})$   
 $p_2(x_{15}, x_{15})$      $\text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $p_3(x_{23}, x_{23})$      $\text{cnf}(p_{3_5}, \text{negated\_conjecture})$   
 $p_{10}(c_{14}, x_4)$      $\text{cnf}(p_{10_6}, \text{negated\_conjecture})$   
 $p_{10}(c_{13}, c_{15})$      $\text{cnf}(p_{10_7}, \text{negated\_conjecture})$   
 $p_{10}(c_{13}, c_{17})$      $\text{cnf}(p_{10_8}, \text{negated\_conjecture})$   
 $p_{10}(c_{13}, c_{16})$      $\text{cnf}(p_{10_9}, \text{negated\_conjecture})$   
 $\neg p_2(c_{15}, c_{17})$      $\text{cnf}(\text{not\_}p_{2_{10}}, \text{negated\_conjecture})$   
 $p_{12}(c_{14}, f_4(c_{18}, c_{17}))$      $\text{cnf}(p_{12_{11}}, \text{negated\_conjecture})$   
 $\neg p_{11}(c_{13}, f_4(c_{17}, f_6(c_{18})))$      $\text{cnf}(\text{not\_}p_{11_{12}}, \text{negated\_conjecture})$   
 $\neg p_{11}(c_{13}, f_4(f_6(c_{18}), c_{17}))$      $\text{cnf}(\text{not\_}p_{11_{13}}, \text{negated\_conjecture})$   
 $(p_8(x_{34}) \text{ and } p_7(x_{34}, x_{33})) \Rightarrow p_8(x_{33})$      $\text{cnf}(p_{8_{14}}, \text{negated\_conjecture})$   
 $(p_9(x_{36}) \text{ and } p_7(x_{36}, x_{35})) \Rightarrow p_9(x_{35})$      $\text{cnf}(p_{9_{15}}, \text{negated\_conjecture})$   
 $p_{10}(c_{13}, x_{10}) \Rightarrow p_{11}(c_{14}, f_4(c_{15}, x_{10}))$      $\text{cnf}(p_{11_{16}}, \text{negated\_conjecture})$

$p_2(x_{18}, x_{19}) \Rightarrow p_2(f_5(x_{18}), f_5(x_{19}))$      $\text{cnf}(p_{2_{17}}, \text{negated\_conjecture})$   
 $p_2(x_{21}, x_{22}) \Rightarrow p_2(f_6(x_{21}), f_6(x_{22}))$      $\text{cnf}(p_{2_{18}}, \text{negated\_conjecture})$   
 $(p_7(x_{30}, x_{31}) \text{ and } p_7(x_{30}, x_{32})) \Rightarrow p_7(x_{31}, x_{32})$      $\text{cnf}(p_{7_{19}}, \text{negated\_conjecture})$   
 $(p_2(x_{15}, x_{16}) \text{ and } p_2(x_{15}, x_{17})) \Rightarrow p_2(x_{16}, x_{17})$      $\text{cnf}(p_{2_{20}}, \text{negated\_conjecture})$   
 $(p_3(x_{23}, x_{24}) \text{ and } p_3(x_{23}, x_{25})) \Rightarrow p_3(x_{24}, x_{25})$      $\text{cnf}(p_{3_{21}}, \text{negated\_conjecture})$   
 $p_{12}(c_{14}, f_4(x_{20}, c_{17})) \Rightarrow p_2(f_6(x_{20}), f_5(x_{20}))$      $\text{cnf}(p_{2_{22}}, \text{negated\_conjecture})$   
 $(p_2(x_3, x_1) \text{ and } p_7(x_2, x_0) \text{ and } p_{10}(x_2, x_3)) \Rightarrow p_{10}(x_0, x_1)$      $\text{cnf}(p_{10_{23}}, \text{negated\_conjecture})$   
 $(p_3(x_{14}, x_{12}) \text{ and } p_7(x_{13}, x_{11}) \text{ and } p_{12}(x_{13}, x_{14})) \Rightarrow p_{12}(x_{11}, x_{12})$      $\text{cnf}(p_{12_{24}}, \text{negated\_conjecture})$   
 $(p_3(x_8, x_6) \text{ and } p_7(x_7, x_5) \text{ and } p_{11}(x_7, x_8)) \Rightarrow p_{11}(x_5, x_6)$      $\text{cnf}(p_{11_{25}}, \text{negated\_conjecture})$   
 $(p_2(x_{26}, x_{28}) \text{ and } p_2(x_{27}, x_{29})) \Rightarrow p_3(f_4(x_{26}, x_{27}), f_4(x_{28}, x_{29}))$      $\text{cnf}(p_{3_{26}}, \text{negated\_conjecture})$   
 $p_{12}(c_{14}, f_4(x_9, c_{17})) \Rightarrow (p_{11}(c_{13}, f_4(c_{17}, f_5(x_9))) \text{ or } p_{11}(c_{13}, f_4(f_5(x_9), c_{17})))$      $\text{cnf}(p_{11_{27}}, \text{negated\_conjecture})$

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$p_9(c_{14})$      $\text{cnf}(c_{14\_is\_p9_1}, \text{negated\_conjecture})$   
 $p_8(c_{13})$      $\text{cnf}(c_{13\_is\_p8_2}, \text{negated\_conjecture})$   
 $p_7(x_{30}, x_{30})$      $\text{cnf}(p_{7_3}, \text{negated\_conjecture})$   
 $p_2(x_{15}, x_{15})$      $\text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $p_3(x_{23}, x_{23})$      $\text{cnf}(p_{3_5}, \text{negated\_conjecture})$   
 $p_{10}(c_{14}, x_4)$      $\text{cnf}(p_{10_6}, \text{negated\_conjecture})$   
 $p_{10}(c_{13}, c_{15})$      $\text{cnf}(p_{10_7}, \text{negated\_conjecture})$   
 $p_{10}(c_{13}, c_{17})$      $\text{cnf}(p_{10_8}, \text{negated\_conjecture})$   
 $p_{10}(c_{13}, c_{16})$      $\text{cnf}(p_{10_9}, \text{negated\_conjecture})$   
 $\neg p_2(c_{17}, c_{15})$      $\text{cnf}(\text{not\_p2}_{10}, \text{negated\_conjecture})$   
 $p_{12}(c_{14}, f_4(c_{18}, c_{17}))$      $\text{cnf}(p_{12_{11}}, \text{negated\_conjecture})$   
 $\neg p_{11}(c_{13}, f_4(c_{17}, f_5(c_{18})))$      $\text{cnf}(\text{not\_p11}_{12}, \text{negated\_conjecture})$   
 $\neg p_{11}(c_{13}, f_4(f_5(c_{18}), c_{17}))$      $\text{cnf}(\text{not\_p11}_{13}, \text{negated\_conjecture})$   
 $(p_8(x_{34}) \text{ and } p_7(x_{34}, x_{33})) \Rightarrow p_8(x_{33})$      $\text{cnf}(p_{8_{14}}, \text{negated\_conjecture})$   
 $(p_9(x_{36}) \text{ and } p_7(x_{36}, x_{35})) \Rightarrow p_9(x_{35})$      $\text{cnf}(p_{9_{15}}, \text{negated\_conjecture})$   
 $p_{10}(c_{13}, x_{10}) \Rightarrow p_{11}(c_{14}, f_4(c_{15}, x_{10}))$      $\text{cnf}(p_{11_{16}}, \text{negated\_conjecture})$   
 $p_2(x_{18}, x_{19}) \Rightarrow p_2(f_5(x_{18}), f_5(x_{19}))$      $\text{cnf}(p_{2_{17}}, \text{negated\_conjecture})$   
 $p_2(x_{21}, x_{22}) \Rightarrow p_2(f_6(x_{21}), f_6(x_{22}))$      $\text{cnf}(p_{2_{18}}, \text{negated\_conjecture})$   
 $(p_7(x_{30}, x_{31}) \text{ and } p_7(x_{30}, x_{32})) \Rightarrow p_7(x_{31}, x_{32})$      $\text{cnf}(p_{7_{19}}, \text{negated\_conjecture})$   
 $(p_2(x_{15}, x_{16}) \text{ and } p_2(x_{15}, x_{17})) \Rightarrow p_2(x_{16}, x_{17})$      $\text{cnf}(p_{2_{20}}, \text{negated\_conjecture})$   
 $(p_3(x_{23}, x_{24}) \text{ and } p_3(x_{23}, x_{25})) \Rightarrow p_3(x_{24}, x_{25})$      $\text{cnf}(p_{3_{21}}, \text{negated\_conjecture})$   
 $p_{12}(c_{14}, f_4(x_{20}, c_{17})) \Rightarrow p_2(f_6(x_{20}), f_5(x_{20}))$      $\text{cnf}(p_{2_{22}}, \text{negated\_conjecture})$   
 $(p_2(x_3, x_1) \text{ and } p_7(x_2, x_0) \text{ and } p_{10}(x_2, x_3)) \Rightarrow p_{10}(x_0, x_1)$      $\text{cnf}(p_{10_{23}}, \text{negated\_conjecture})$   
 $(p_3(x_{14}, x_{12}) \text{ and } p_7(x_{13}, x_{11}) \text{ and } p_{12}(x_{13}, x_{14})) \Rightarrow p_{12}(x_{11}, x_{12})$      $\text{cnf}(p_{12_{24}}, \text{negated\_conjecture})$   
 $(p_3(x_8, x_6) \text{ and } p_7(x_7, x_5) \text{ and } p_{11}(x_7, x_8)) \Rightarrow p_{11}(x_5, x_6)$      $\text{cnf}(p_{11_{25}}, \text{negated\_conjecture})$   
 $(p_2(x_{26}, x_{28}) \text{ and } p_2(x_{27}, x_{29})) \Rightarrow p_3(f_4(x_{26}, x_{27}), f_4(x_{28}, x_{29}))$      $\text{cnf}(p_{3_{26}}, \text{negated\_conjecture})$   
 $p_{12}(c_{14}, f_4(x_9, c_{17})) \Rightarrow (p_{11}(c_{13}, f_4(c_{17}, f_6(x_9))) \text{ or } p_{11}(c_{13}, f_4(f_6(x_9), c_{17})))$      $\text{cnf}(p_{11_{27}}, \text{negated\_conjecture})$

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$p_{12}(x_0, x_0)$      $\text{cnf}(p_{12_1}, \text{negated\_conjecture})$   
 $p_5(x_{37}, x_{37})$      $\text{cnf}(p_{5_2}, \text{negated\_conjecture})$   
 $p_3(x_{24}, x_{24})$      $\text{cnf}(p_{3_3}, \text{negated\_conjecture})$   
 $p_2(x_{13}, x_{13})$      $\text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $\neg p_3(c_{21}, c_{19})$      $\text{cnf}(\text{not\_p3}_5, \text{negated\_conjecture})$   
 $\neg p_{12}(f_{13}(c_{20}), f_{13}(c_{18}))$      $\text{cnf}(\text{not\_p12}_6, \text{negated\_conjecture})$   
 $p_2(x_3, x_4) \Rightarrow p_{12}(f_{13}(x_3), f_{13}(x_4))$      $\text{cnf}(p_{12_7}, \text{negated\_conjecture})$   
 $p_3(x_{42}, x_{43}) \Rightarrow p_5(f_7(x_{42}), f_7(x_{43}))$      $\text{cnf}(p_{5_8}, \text{negated\_conjecture})$   
 $p_5(x_{40}, x_{41}) \Rightarrow p_5(f_{10}(x_{40}), f_{10}(x_{41}))$      $\text{cnf}(p_{5_9}, \text{negated\_conjecture})$   
 $p_3(x_{35}, x_{36}) \Rightarrow p_3(f_9(x_{35}), f_9(x_{36}))$      $\text{cnf}(p_{3_{10}}, \text{negated\_conjecture})$   
 $p_3(x_{33}, x_{34}) \Rightarrow p_3(f_8(x_{33}), f_8(x_{34}))$      $\text{cnf}(p_{3_{11}}, \text{negated\_conjecture})$   
 $p_3(x_{27}, x_{28}) \Rightarrow p_3(f_{11}(x_{27}), f_{11}(x_{28}))$      $\text{cnf}(p_{3_{12}}, \text{negated\_conjecture})$   
 $(p_{12}(x_0, x_1) \text{ and } p_{12}(x_0, x_2)) \Rightarrow p_{12}(x_1, x_2)$      $\text{cnf}(p_{12_{13}}, \text{negated\_conjecture})$   
 $(p_5(x_{37}, x_{38}) \text{ and } p_5(x_{37}, x_{39})) \Rightarrow p_5(x_{38}, x_{39})$      $\text{cnf}(p_{5_{14}}, \text{negated\_conjecture})$   
 $(p_3(x_{24}, x_{25}) \text{ and } p_3(x_{24}, x_{26})) \Rightarrow p_3(x_{25}, x_{26})$      $\text{cnf}(p_{3_{15}}, \text{negated\_conjecture})$   
 $(p_2(x_{13}, x_{14}) \text{ and } p_2(x_{13}, x_{15})) \Rightarrow p_2(x_{14}, x_{15})$      $\text{cnf}(p_{2_{16}}, \text{negated\_conjecture})$   
 $(p_2(x_{11}, x_9) \text{ and } p_2(x_{12}, x_{10}) \text{ and } p_{15}(x_{11}, x_{12})) \Rightarrow p_{15}(x_9, x_{10})$      $\text{cnf}(p_{15_{17}}, \text{negated\_conjecture})$   
 $p_{15}(f_4(f_6(f_{10}(c_{16}), f_6(f_7(f_8(f_9(c_{17}))), c_{18})), c_{19}), c_{20})$      $\text{cnf}(p_{15_{18}}, \text{negated\_conjecture})$

$p_{15}(f_4(f_6(f_{10}(c_{16}), f_6(f_7(f_8(f_9(c_{17}))))), c_{18})), c_{21}), c_{20}) \quad \text{cnf}(p_{15_{19}}, \text{negated\_conjecture})$   
 $(p_2(x_{29}, x_{31}) \text{ and } p_5(x_{30}, x_{32})) \Rightarrow p_3(f_{14}(x_{29}, x_{30}), f_{14}(x_{31}, x_{32})) \quad \text{cnf}(p_{3_{20}}, \text{negated\_conjecture})$   
 $(p_2(x_{16}, x_{18}) \text{ and } p_3(x_{17}, x_{19})) \Rightarrow p_2(f_4(x_{16}, x_{17}), f_4(x_{18}, x_{19})) \quad \text{cnf}(p_{2_{21}}, \text{negated\_conjecture})$   
 $(p_2(x_{21}, x_{23}) \text{ and } p_5(x_{20}, x_{22})) \Rightarrow p_2(f_6(x_{20}, x_{21}), f_6(x_{22}, x_{23})) \quad \text{cnf}(p_{2_{22}}, \text{negated\_conjecture})$   
 $\neg p_{15}(f_4(f_6(f_{10}(c_{16}), f_6(f_7(f_8(f_9(c_{17}))))), c_{18})), f_{11}(c_{21}), c_{20}) \quad \text{cnf}(\text{not\_}p_{15_{23}}, \text{negated\_conjecture})$   
 $\neg p_{15}(f_4(f_6(f_{10}(c_{16}), f_6(f_7(f_8(f_9(c_{17}))))), c_{18})), f_{11}(c_{19}), c_{20}) \quad \text{cnf}(\text{not\_}p_{15_{24}}, \text{negated\_conjecture})$   
 $p_{12}(f_{13}(x_5), f_{13}(c_{18})) \text{ or } p_{15}(f_4(f_6(f_{10}(x_6), f_6(f_7(f_8(f_9(c_{17}))))), c_{18})), f_{14}(x_5, x_6), x_5) \quad \text{cnf}(p_{12_{25}}, \text{negated\_conjecture})$   
 $p_{15}(f_4(f_6(f_{10}(x_6), f_6(f_7(f_8(f_9(c_{17}))))), c_{18})), f_{11}(f_{14}(x_5, x_6)), x_5) \Rightarrow p_{12}(f_{13}(x_5), f_{13}(c_{18})) \quad \text{cnf}(p_{12_{26}}, \text{negated\_conjecture})$   
 $(p_{15}(f_4(f_6(f_{10}(x_6), f_6(f_7(f_8(f_9(c_{17}))))), c_{18})), x_7, x_5) \text{ and } p_{15}(f_4(f_6(f_{10}(x_6), f_6(f_7(f_8(f_9(c_{17}))))), c_{18})), x_8, x_5) \Rightarrow (p_3(x_7, x_8) \text{ or } p_5(x_7, x_8))$

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$p_2(x_{10}, x_{10}) \quad \text{cnf}(p_{2_1}, \text{negated\_conjecture})$   
 $p_7(x_{27}, x_{27}) \quad \text{cnf}(p_{7_2}, \text{negated\_conjecture})$   
 $\neg p_2(c_{16}, f_3(c_{17})) \quad \text{cnf}(\text{not\_}p_{2_3}, \text{negated\_conjecture})$   
 $p_{14}(c_{18}, f_3(f_4(f_5(c_{17})))) \quad \text{cnf}(p_{14_4}, \text{negated\_conjecture})$   
 $p_{14}(x_4, x_5) \Rightarrow p_{15}(x_4, x_5) \quad \text{cnf}(p_{15_5}, \text{negated\_conjecture})$   
 $p_{14}(x_4, x_5) \Rightarrow \neg p_2(x_4, x_5) \quad \text{cnf}(\text{not\_}p_{14_6}, \text{negated\_conjecture})$   
 $p_{14}(c_{19}, f_6(f_3(f_4(f_5(c_{17}))))), c_{16})) \quad \text{cnf}(p_{14_7}, \text{negated\_conjecture})$   
 $p_7(x_{36}, x_{37}) \Rightarrow p_7(f_{12}(x_{36}), f_{12}(x_{37})) \quad \text{cnf}(p_{7_8}, \text{negated\_conjecture})$   
 $p_2(x_{17}, x_{18}) \Rightarrow p_2(f_3(x_{17}), f_3(x_{18})) \quad \text{cnf}(p_{2_9}, \text{negated\_conjecture})$   
 $p_2(x_{19}, x_{20}) \Rightarrow p_2(f_4(x_{19}), f_4(x_{20})) \quad \text{cnf}(p_{2_{10}}, \text{negated\_conjecture})$   
 $p_2(x_{21}, x_{22}) \Rightarrow p_2(f_5(x_{21}), f_5(x_{22})) \quad \text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $p_2(x_{34}, x_{35}) \Rightarrow p_7(f_{11}(x_{34}), f_{11}(x_{35})) \quad \text{cnf}(p_{7_{12}}, \text{negated\_conjecture})$   
 $p_{15}(x_4, x_5) \Rightarrow (p_{14}(x_4, x_5) \text{ or } p_2(x_4, x_5)) \quad \text{cnf}(p_{14_{13}}, \text{negated\_conjecture})$   
 $(p_7(x_{27}, x_{28}) \text{ and } p_7(x_{27}, x_{29})) \Rightarrow p_7(x_{28}, x_{29}) \quad \text{cnf}(p_{7_{14}}, \text{negated\_conjecture})$   
 $(p_2(x_{10}, x_{11}) \text{ and } p_2(x_{10}, x_{12})) \Rightarrow p_2(x_{11}, x_{12}) \quad \text{cnf}(p_{2_{15}}, \text{negated\_conjecture})$   
 $p_{15}(f_6(f_3(f_4(f_5(c_{17}))))), f_{13}(c_{16}, f_3(f_5(c_{17}))))), c_{19}) \quad \text{cnf}(p_{15_{16}}, \text{negated\_conjecture})$   
 $\neg p_2(c_{19}, f_6(f_3(f_4(f_5(c_{17}))))), f_{13}(c_{16}, f_3(f_5(c_{17})))))) \quad \text{cnf}(\text{not\_}p_{2_{17}}, \text{negated\_conjecture})$   
 $(p_2(x_2, x_0) \text{ and } p_2(x_3, x_1) \text{ and } p_{14}(x_2, x_3)) \Rightarrow p_{14}(x_0, x_1) \quad \text{cnf}(p_{14_{18}}, \text{negated\_conjecture})$   
 $(p_2(x_8, x_6) \text{ and } p_2(x_9, x_7) \text{ and } p_{15}(x_8, x_9)) \Rightarrow p_{15}(x_6, x_7) \quad \text{cnf}(p_{15_{19}}, \text{negated\_conjecture})$   
 $(p_2(x_{13}, x_{15}) \text{ and } p_2(x_{14}, x_{16})) \Rightarrow p_2(f_{13}(x_{13}, x_{14}), f_{13}(x_{15}, x_{16})) \quad \text{cnf}(p_{2_{20}}, \text{negated\_conjecture})$   
 $(p_7(x_{42}, x_{44}) \text{ and } p_7(x_{43}, x_{45})) \Rightarrow p_7(f_9(x_{42}, x_{43}), f_9(x_{44}, x_{45})) \quad \text{cnf}(p_{7_{21}}, \text{negated\_conjecture})$   
 $(p_7(x_{38}, x_{40}) \text{ and } p_7(x_{39}, x_{41})) \Rightarrow p_7(f_8(x_{38}, x_{39}), f_8(x_{40}, x_{41})) \quad \text{cnf}(p_{7_{22}}, \text{negated\_conjecture})$   
 $(p_2(x_{31}, x_{33}) \text{ and } p_7(x_{30}, x_{32})) \Rightarrow p_7(f_{10}(x_{30}, x_{31}), f_{10}(x_{32}, x_{33})) \quad \text{cnf}(p_{7_{23}}, \text{negated\_conjecture})$   
 $(p_2(x_{23}, x_{25}) \text{ and } p_2(x_{24}, x_{26})) \Rightarrow p_2(f_6(x_{23}, x_{24}), f_6(x_{25}, x_{26})) \quad \text{cnf}(p_{2_{24}}, \text{negated\_conjecture})$   
 $p_7(c_{20}, f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{17}))))), c_{18}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{21}), f_9(f_{11}(c_{19}), f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{22})))))) \quad \text{cnf}(p_{7_{25}}, \text{negated\_conjecture})$   
 $(p_2(x_{48}, f_3(c_{17})) \text{ and } p_{14}(x_{46}, f_3(f_4(f_5(c_{17})))) \text{ and } p_{15}(x_{47}, f_6(f_3(f_4(f_5(c_{17}))))), c_{16})) \Rightarrow \neg p_7(c_{20}, f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{17}))))), c_{18}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{21}), f_9(f_{11}(c_{19}), f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{22})))))) \quad \text{cnf}(\text{not\_}p_{7_{26}}, \text{negated\_conjecture})$   
 $(p_{14}(x_{46}, f_3(f_4(f_5(c_{17})))) \text{ and } p_{15}(x_{47}, f_6(f_3(f_4(f_5(c_{17}))))), c_{16})) \text{ and } p_{14}(f_6(f_3(f_4(f_5(c_{17}))))), f_{13}(c_{16}, f_3(f_5(c_{17}))))), x_{47})) \Rightarrow \neg p_7(c_{20}, f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{17}))))), c_{18}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{21}), f_9(f_{11}(c_{19}), f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{22})))))) \quad \text{cnf}(\text{not\_}p_{7_{27}}, \text{negated\_conjecture})$

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$p_2(x_{10}, x_{10}) \quad \text{cnf}(p_{2_1}, \text{negated\_conjecture})$   
 $p_7(x_{27}, x_{27}) \quad \text{cnf}(p_{7_2}, \text{negated\_conjecture})$   
 $p_2(c_{21}, f_3(c_{17})) \quad \text{cnf}(p_{2_3}, \text{negated\_conjecture})$   
 $\neg p_2(c_{16}, f_3(c_{17})) \quad \text{cnf}(\text{not\_}p_{2_4}, \text{negated\_conjecture})$   
 $p_{14}(c_{18}, f_3(f_4(f_5(c_{17})))) \quad \text{cnf}(p_{14_5}, \text{negated\_conjecture})$   
 $p_{14}(x_4, x_5) \Rightarrow p_{15}(x_4, x_5) \quad \text{cnf}(p_{15_6}, \text{negated\_conjecture})$   
 $p_{14}(x_4, x_5) \Rightarrow \neg p_2(x_4, x_5) \quad \text{cnf}(\text{not\_}p_{14_7}, \text{negated\_conjecture})$   
 $p_{14}(c_{19}, f_6(f_3(f_4(f_5(c_{17}))))), c_{16})) \quad \text{cnf}(p_{14_8}, \text{negated\_conjecture})$   
 $p_7(x_{36}, x_{37}) \Rightarrow p_7(f_{12}(x_{36}), f_{12}(x_{37})) \quad \text{cnf}(p_{7_9}, \text{negated\_conjecture})$   
 $p_2(x_{17}, x_{18}) \Rightarrow p_2(f_3(x_{17}), f_3(x_{18})) \quad \text{cnf}(p_{2_{10}}, \text{negated\_conjecture})$   
 $p_2(x_{19}, x_{20}) \Rightarrow p_2(f_4(x_{19}), f_4(x_{20})) \quad \text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $p_2(x_{21}, x_{22}) \Rightarrow p_2(f_5(x_{21}), f_5(x_{22})) \quad \text{cnf}(p_{2_{12}}, \text{negated\_conjecture})$   
 $p_2(x_{34}, x_{35}) \Rightarrow p_7(f_{11}(x_{34}), f_{11}(x_{35})) \quad \text{cnf}(p_{7_{13}}, \text{negated\_conjecture})$   
 $p_{15}(x_4, x_5) \Rightarrow (p_{14}(x_4, x_5) \text{ or } p_2(x_4, x_5)) \quad \text{cnf}(p_{14_{14}}, \text{negated\_conjecture})$   
 $(p_7(x_{27}, x_{28}) \text{ and } p_7(x_{27}, x_{29})) \Rightarrow p_7(x_{28}, x_{29}) \quad \text{cnf}(p_{7_{15}}, \text{negated\_conjecture})$   
 $(p_2(x_{10}, x_{11}) \text{ and } p_2(x_{10}, x_{12})) \Rightarrow p_2(x_{11}, x_{12}) \quad \text{cnf}(p_{2_{16}}, \text{negated\_conjecture})$   
 $p_2(c_{19}, f_6(f_3(f_4(f_5(c_{17}))))), f_{13}(c_{16}, f_3(f_5(c_{17})))))) \quad \text{cnf}(p_{2_{17}}, \text{negated\_conjecture})$   
 $(p_2(x_2, x_0) \text{ and } p_2(x_3, x_1) \text{ and } p_{14}(x_2, x_3)) \Rightarrow p_{14}(x_0, x_1) \quad \text{cnf}(p_{14_{18}}, \text{negated\_conjecture})$   
 $(p_2(x_8, x_6) \text{ and } p_2(x_9, x_7) \text{ and } p_{15}(x_8, x_9)) \Rightarrow p_{15}(x_6, x_7) \quad \text{cnf}(p_{15_{19}}, \text{negated\_conjecture})$

$(p_2(x_{13}, x_{15}) \text{ and } p_2(x_{14}, x_{16})) \Rightarrow p_2(f_{13}(x_{13}, x_{14}), f_{13}(x_{15}, x_{16}))$      $\text{cnf}(p_{20}, \text{negated\_conjecture})$   
 $(p_7(x_{42}, x_{44}) \text{ and } p_7(x_{43}, x_{45})) \Rightarrow p_7(f_9(x_{42}, x_{43}), f_9(x_{44}, x_{45}))$      $\text{cnf}(p_{721}, \text{negated\_conjecture})$   
 $(p_7(x_{38}, x_{40}) \text{ and } p_7(x_{39}, x_{41})) \Rightarrow p_7(f_8(x_{38}, x_{39}), f_8(x_{40}, x_{41}))$      $\text{cnf}(p_{722}, \text{negated\_conjecture})$   
 $(p_2(x_{31}, x_{33}) \text{ and } p_7(x_{30}, x_{32})) \Rightarrow p_7(f_{10}(x_{30}, x_{31}), f_{10}(x_{32}, x_{33}))$      $\text{cnf}(p_{723}, \text{negated\_conjecture})$   
 $(p_2(x_{23}, x_{25}) \text{ and } p_2(x_{24}, x_{26})) \Rightarrow p_2(f_6(x_{23}, x_{24}), f_6(x_{25}, x_{26}))$      $\text{cnf}(p_{224}, \text{negated\_conjecture})$   
 $p_7(c_{20}, f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{17}))))), c_{18}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{21}), f_9(f_{11}(c_{19}), f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), c_{22}))))))$      $\text{cnf}(p_{724}, \text{negated\_conjecture})$   
 $(p_2(x_{48}, f_3(c_{17})) \text{ and } p_{14}(x_{46}, f_3(f_4(f_5(c_{17})))) \text{ and } p_{15}(x_{47}, f_6(f_3(f_4(f_5(c_{17}))))), c_{16})) \Rightarrow \neg p_7(f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{17}))))), c_{18}),$   
 $(p_{14}(x_{46}, f_3(f_4(f_5(c_{17})))) \text{ and } p_{15}(x_{47}, f_6(f_3(f_4(f_5(c_{17}))))), c_{16})) \text{ and } p_{14}(f_6(f_3(f_4(f_5(c_{17}))))), f_{13}(c_{16}, f_3(f_5(c_{17}))), x_{47})) \Rightarrow$   
 $\neg p_7(f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{17}))))), c_{18}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{17}))))), f_3(c_{17})), f_9(f_{11}(f_6(f_3(f_4(f_5(c_{17}))))), f_{13}(c_{16}, f_3(f_5(c_{17}))))), f_3(c_{17})),$

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$p_{10}(x_0, x_0)$      $\text{cnf}(p_{101}, \text{negated\_conjecture})$   
 $p_9(x_{50}, x_{50})$      $\text{cnf}(p_{92}, \text{negated\_conjecture})$   
 $p_3(x_{35}, x_{35})$      $\text{cnf}(p_{33}, \text{negated\_conjecture})$   
 $p_2(x_{28}, x_{28})$      $\text{cnf}(p_{24}, \text{negated\_conjecture})$   
 $p_{12}(x_9, x_9)$      $\text{cnf}(p_{125}, \text{negated\_conjecture})$   
 $p_{16}(c_{21}, c_{22})$      $\text{cnf}(p_{166}, \text{negated\_conjecture})$   
 $p_{17}(c_{21}, f_8(c_{20}))$      $\text{cnf}(p_{177}, \text{negated\_conjecture})$   
 $p_{16}(f_5(f_6(f_7(c_{19}))), f_4(c_{20}))$      $\text{cnf}(p_{168}, \text{negated\_conjecture})$   
 $p_2(x_{48}, x_{49}) \Rightarrow p_3(f_8(x_{48}), f_8(x_{49}))$      $\text{cnf}(p_{39}, \text{negated\_conjecture})$   
 $p_2(x_{38}, x_{39}) \Rightarrow p_3(f_{15}(x_{38}), f_{15}(x_{39}))$      $\text{cnf}(p_{310}, \text{negated\_conjecture})$   
 $p_2(x_{40}, x_{41}) \Rightarrow p_3(f_4(x_{40}), f_4(x_{41}))$      $\text{cnf}(p_{311}, \text{negated\_conjecture})$   
 $p_3(x_{42}, x_{43}) \Rightarrow p_3(f_5(x_{42}), f_5(x_{43}))$      $\text{cnf}(p_{312}, \text{negated\_conjecture})$   
 $p_3(x_{44}, x_{45}) \Rightarrow p_3(f_6(x_{44}), f_6(x_{45}))$      $\text{cnf}(p_{313}, \text{negated\_conjecture})$   
 $p_3(x_{46}, x_{47}) \Rightarrow p_3(f_7(x_{46}), f_7(x_{47}))$      $\text{cnf}(p_{314}, \text{negated\_conjecture})$   
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2)$      $\text{cnf}(p_{1015}, \text{negated\_conjecture})$   
 $(p_9(x_{50}, x_{51}) \text{ and } p_9(x_{50}, x_{52})) \Rightarrow p_9(x_{51}, x_{52})$      $\text{cnf}(p_{916}, \text{negated\_conjecture})$   
 $(p_3(x_{35}, x_{36}) \text{ and } p_3(x_{35}, x_{37})) \Rightarrow p_3(x_{36}, x_{37})$      $\text{cnf}(p_{317}, \text{negated\_conjecture})$   
 $(p_2(x_{28}, x_{29}) \text{ and } p_2(x_{28}, x_{30})) \Rightarrow p_2(x_{29}, x_{30})$      $\text{cnf}(p_{218}, \text{negated\_conjecture})$   
 $(p_{12}(x_9, x_{10}) \text{ and } p_{12}(x_9, x_{11})) \Rightarrow p_{12}(x_{10}, x_{11})$      $\text{cnf}(p_{1219}, \text{negated\_conjecture})$   
 $p_{18}(c_{20}, f_{11}(f_{13}(f_{15}(c_{20}), f_{14}(f_4(c_{20}), c_{21})), c_{23}, c_{24}))$      $\text{cnf}(p_{1820}, \text{negated\_conjecture})$   
 $\neg p_{18}(c_{20}, f_{11}(f_{13}(f_{15}(c_{20}), f_{14}(f_4(c_{20}), c_{22})), c_{23}, c_{24}))$      $\text{cnf}(\text{not\_}p_{1821}, \text{negated\_conjecture})$   
 $(p_3(x_{18}, x_{16}) \text{ and } p_3(x_{19}, x_{17}) \text{ and } p_{16}(x_{18}, x_{19})) \Rightarrow p_{16}(x_{16}, x_{17})$      $\text{cnf}(p_{1622}, \text{negated\_conjecture})$   
 $(p_{18}(x_{27}, x_{26}) \text{ and } p_2(x_{27}, x_{24}) \text{ and } p_{10}(x_{26}, x_{25})) \Rightarrow p_{18}(x_{24}, x_{25})$      $\text{cnf}(p_{1823}, \text{negated\_conjecture})$   
 $(p_3(x_{22}, x_{20}) \text{ and } p_3(x_{23}, x_{21}) \text{ and } p_{17}(x_{22}, x_{23})) \Rightarrow p_{17}(x_{20}, x_{21})$      $\text{cnf}(p_{1724}, \text{negated\_conjecture})$   
 $(p_{12}(x_{32}, x_{34}) \text{ and } p_3(x_{31}, x_{33})) \Rightarrow p_2(f_{13}(x_{31}, x_{32}), f_{13}(x_{33}, x_{34}))$      $\text{cnf}(p_{225}, \text{negated\_conjecture})$   
 $(p_3(x_{12}, x_{14}) \text{ and } p_3(x_{13}, x_{15})) \Rightarrow p_{12}(f_{14}(x_{12}, x_{13}), f_{14}(x_{14}, x_{15}))$      $\text{cnf}(p_{1226}, \text{negated\_conjecture})$   
 $(p_2(x_3, x_6) \text{ and } p_9(x_4, x_7) \text{ and } p_{10}(x_5, x_8)) \Rightarrow p_{10}(f_{11}(x_3, x_4, x_5), f_{11}(x_6, x_7, x_8))$      $\text{cnf}(p_{1027}, \text{negated\_conjecture})$   
 $p_{10}(f_{11}(f_{13}(f_{15}(c_{20}), f_{14}(f_4(c_{20}), c_{22})), c_{23}, c_{24}), f_{11}(f_{13}(f_{15}(c_{20}), f_{14}(f_4(c_{20}), c_{21})), c_{23}, c_{24}))$      $\text{cnf}(p_{1028}, \text{negated\_conjecture})$

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$p_{10}(x_0, x_0)$      $\text{cnf}(p_{101}, \text{negated\_conjecture})$   
 $p_9(x_{50}, x_{50})$      $\text{cnf}(p_{92}, \text{negated\_conjecture})$   
 $p_3(x_{35}, x_{35})$      $\text{cnf}(p_{33}, \text{negated\_conjecture})$   
 $p_2(x_{28}, x_{28})$      $\text{cnf}(p_{24}, \text{negated\_conjecture})$   
 $p_{12}(x_9, x_9)$      $\text{cnf}(p_{125}, \text{negated\_conjecture})$   
 $p_{16}(c_{21}, c_{22})$      $\text{cnf}(p_{166}, \text{negated\_conjecture})$   
 $p_3(c_{21}, c_{22})$      $\text{cnf}(p_{37}, \text{negated\_conjecture})$   
 $p_{17}(c_{21}, f_8(c_{20}))$      $\text{cnf}(p_{178}, \text{negated\_conjecture})$   
 $p_{16}(f_5(f_6(f_7(c_{19}))), f_4(c_{20}))$      $\text{cnf}(p_{169}, \text{negated\_conjecture})$   
 $p_2(x_{48}, x_{49}) \Rightarrow p_3(f_8(x_{48}), f_8(x_{49}))$      $\text{cnf}(p_{310}, \text{negated\_conjecture})$   
 $p_2(x_{38}, x_{39}) \Rightarrow p_3(f_{15}(x_{38}), f_{15}(x_{39}))$      $\text{cnf}(p_{311}, \text{negated\_conjecture})$   
 $p_2(x_{40}, x_{41}) \Rightarrow p_3(f_4(x_{40}), f_4(x_{41}))$      $\text{cnf}(p_{312}, \text{negated\_conjecture})$   
 $p_3(x_{42}, x_{43}) \Rightarrow p_3(f_5(x_{42}), f_5(x_{43}))$      $\text{cnf}(p_{313}, \text{negated\_conjecture})$   
 $p_3(x_{44}, x_{45}) \Rightarrow p_3(f_6(x_{44}), f_6(x_{45}))$      $\text{cnf}(p_{314}, \text{negated\_conjecture})$   
 $p_3(x_{46}, x_{47}) \Rightarrow p_3(f_7(x_{46}), f_7(x_{47}))$      $\text{cnf}(p_{315}, \text{negated\_conjecture})$   
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2)$      $\text{cnf}(p_{1016}, \text{negated\_conjecture})$   
 $(p_9(x_{50}, x_{51}) \text{ and } p_9(x_{50}, x_{52})) \Rightarrow p_9(x_{51}, x_{52})$      $\text{cnf}(p_{917}, \text{negated\_conjecture})$   
 $(p_3(x_{35}, x_{36}) \text{ and } p_3(x_{35}, x_{37})) \Rightarrow p_3(x_{36}, x_{37})$      $\text{cnf}(p_{318}, \text{negated\_conjecture})$   
 $(p_2(x_{28}, x_{29}) \text{ and } p_2(x_{28}, x_{30})) \Rightarrow p_2(x_{29}, x_{30})$      $\text{cnf}(p_{219}, \text{negated\_conjecture})$



$(p_{12}(x_9, x_{10}) \text{ and } p_{12}(x_9, x_{11})) \Rightarrow p_{12}(x_{10}, x_{11})$      $\text{cnf}(p_{12_{20}}, \text{negated\_conjecture})$   
 $p_{18}(c_{20}, f_{11}(f_{13}(f_{15}(c_{20}), f_{14}(f_4(c_{20}), c_{21})), c_{23}, c_{24}))$      $\text{cnf}(p_{18_{21}}, \text{negated\_conjecture})$   
 $\neg p_{18}(c_{20}, f_{11}(f_{13}(f_{15}(c_{20}), f_{14}(f_4(c_{20}), c_{22})), c_{23}, c_{24}))$      $\text{cnf}(\text{not\_}p_{18_{22}}, \text{negated\_conjecture})$   
 $(p_3(x_{18}, x_{16}) \text{ and } p_3(x_{19}, x_{17}) \text{ and } p_{16}(x_{18}, x_{19})) \Rightarrow p_{16}(x_{16}, x_{17})$      $\text{cnf}(p_{16_{23}}, \text{negated\_conjecture})$   
 $(p_{18}(x_{27}, x_{26}) \text{ and } p_2(x_{27}, x_{24}) \text{ and } p_{10}(x_{26}, x_{25})) \Rightarrow p_{18}(x_{24}, x_{25})$      $\text{cnf}(p_{18_{24}}, \text{negated\_conjecture})$   
 $(p_3(x_{22}, x_{20}) \text{ and } p_3(x_{23}, x_{21}) \text{ and } p_{17}(x_{22}, x_{23})) \Rightarrow p_{17}(x_{20}, x_{21})$      $\text{cnf}(p_{17_{25}}, \text{negated\_conjecture})$   
 $(p_{12}(x_{32}, x_{34}) \text{ and } p_3(x_{31}, x_{33})) \Rightarrow p_2(f_{13}(x_{31}, x_{32}), f_{13}(x_{33}, x_{34}))$      $\text{cnf}(p_{2_{26}}, \text{negated\_conjecture})$   
 $(p_3(x_{12}, x_{14}) \text{ and } p_3(x_{13}, x_{15})) \Rightarrow p_{12}(f_{14}(x_{12}, x_{13}), f_{14}(x_{14}, x_{15}))$      $\text{cnf}(p_{12_{27}}, \text{negated\_conjecture})$   
 $(p_2(x_3, x_6) \text{ and } p_9(x_4, x_7) \text{ and } p_{10}(x_5, x_8)) \Rightarrow p_{10}(f_{11}(x_3, x_4, x_5), f_{11}(x_6, x_7, x_8))$      $\text{cnf}(p_{10_{28}}, \text{negated\_conjecture})$

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$p_{17}(c_{21})$      $\text{cnf}(c_{21\_is\_}p_{17_1}, \text{negated\_conjecture})$   
 $p_{18}(c_{21})$      $\text{cnf}(c_{21\_is\_}p_{18_2}, \text{negated\_conjecture})$   
 $p_7(x_{34}, x_{34})$      $\text{cnf}(p_{7_3}, \text{negated\_conjecture})$   
 $p_2(x_9, x_9)$      $\text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $p_3(x_{18}, x_{18})$      $\text{cnf}(p_{3_5}, \text{negated\_conjecture})$   
 $p_5(x_{31}, x_{31})$      $\text{cnf}(p_{5_6}, \text{negated\_conjecture})$   
 $p_3(f_4(f_6(c_{21})), c_{22})$      $\text{cnf}(p_{3_7}, \text{negated\_conjecture})$   
 $(p_{17}(x_1) \text{ and } p_5(x_1, x_0)) \Rightarrow p_{17}(x_0)$      $\text{cnf}(p_{17_8}, \text{negated\_conjecture})$   
 $(p_{18}(x_3) \text{ and } p_5(x_3, x_2)) \Rightarrow p_{18}(x_2)$      $\text{cnf}(p_{18_9}, \text{negated\_conjecture})$   
 $p_5(x_{49}, x_{50}) \Rightarrow p_7(f_9(x_{49}), f_9(x_{50}))$      $\text{cnf}(p_{7_{10}}, \text{negated\_conjecture})$   
 $p_5(x_{12}, x_{13}) \Rightarrow p_2(f_6(x_{12}), f_6(x_{13}))$      $\text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $p_3(x_{21}, x_{22}) \Rightarrow p_3(f_{12}(x_{21}), f_{12}(x_{22}))$      $\text{cnf}(p_{3_{12}}, \text{negated\_conjecture})$   
 $p_3(x_{23}, x_{24}) \Rightarrow p_3(f_{13}(x_{23}), f_{13}(x_{24}))$      $\text{cnf}(p_{3_{13}}, \text{negated\_conjecture})$   
 $p_3(x_{25}, x_{26}) \Rightarrow p_3(f_{15}(x_{25}), f_{15}(x_{26}))$      $\text{cnf}(p_{3_{14}}, \text{negated\_conjecture})$   
 $p_3(x_{27}, x_{28}) \Rightarrow p_3(f_{16}(x_{27}), f_{16}(x_{28}))$      $\text{cnf}(p_{3_{15}}, \text{negated\_conjecture})$   
 $p_2(x_{29}, x_{30}) \Rightarrow p_3(f_4(x_{29}), f_4(x_{30}))$      $\text{cnf}(p_{3_{16}}, \text{negated\_conjecture})$   
 $p_3(x_{45}, x_{46}) \Rightarrow p_7(f_{14}(x_{45}), f_{14}(x_{46}))$      $\text{cnf}(p_{7_{17}}, \text{negated\_conjecture})$   
 $p_7(x_{47}, x_{48}) \Rightarrow p_7(f_8(x_{47}), f_8(x_{48}))$      $\text{cnf}(p_{7_{18}}, \text{negated\_conjecture})$   
 $(p_2(x_9, x_{10}) \text{ and } p_2(x_9, x_{11})) \Rightarrow p_2(x_{10}, x_{11})$      $\text{cnf}(p_{2_{19}}, \text{negated\_conjecture})$   
 $(p_7(x_{34}, x_{35}) \text{ and } p_7(x_{34}, x_{36})) \Rightarrow p_7(x_{35}, x_{36})$      $\text{cnf}(p_{7_{20}}, \text{negated\_conjecture})$   
 $(p_5(x_{31}, x_{32}) \text{ and } p_5(x_{31}, x_{33})) \Rightarrow p_5(x_{32}, x_{33})$      $\text{cnf}(p_{5_{21}}, \text{negated\_conjecture})$   
 $(p_3(x_{18}, x_{19}) \text{ and } p_3(x_{18}, x_{20})) \Rightarrow p_3(x_{19}, x_{20})$      $\text{cnf}(p_{3_{22}}, \text{negated\_conjecture})$   
 $(p_7(x_6, x_4) \text{ and } p_7(x_7, x_5) \text{ and } p_{19}(x_6, x_7)) \Rightarrow p_{19}(x_4, x_5)$      $\text{cnf}(p_{19_{23}}, \text{negated\_conjecture})$   
 $(p_7(x_{16}, x_{14}) \text{ and } p_7(x_{17}, x_{15}) \text{ and } p_{20}(x_{16}, x_{17})) \Rightarrow p_{20}(x_{14}, x_{15})$      $\text{cnf}(p_{20_{24}}, \text{negated\_conjecture})$   
 $(p_3(x_{42}, x_{44}) \text{ and } p_7(x_{41}, x_{43})) \Rightarrow p_7(f_{11}(x_{41}, x_{42}), f_{11}(x_{43}, x_{44}))$      $\text{cnf}(p_{7_{25}}, \text{negated\_conjecture})$   
 $(p_7(x_{38}, x_{40}) \text{ and } p_7(x_{37}, x_{39})) \Rightarrow p_7(f_{10}(x_{37}, x_{38}), f_{10}(x_{39}, x_{40}))$      $\text{cnf}(p_{7_{26}}, \text{negated\_conjecture})$   
 $\neg p_{19}(f_{10}(f_{11}(f_{14}(f_{12}(f_{15}(f_{13}(c_{23}))))), c_{22}), f_{11}(f_{14}(f_{12}(f_{15}(f_{13}(c_{23}))))), f_{12}(f_{13}(f_{13}(f_{13}(f_{13}(f_{13}(f_{13}(c_{23}))))))))))$ ,  $f_8(f_9(c_{21}))$   
 $p_{18}(x_8) \Rightarrow p_{19}(f_{10}(f_{11}(f_{14}(f_{12}(f_{15}(f_{13}(c_{23}))))), f_4(f_6(x_8))), f_{11}(f_{14}(f_{12}(f_{15}(f_{13}(c_{23}))))), f_{12}(f_{13}(f_{13}(f_{13}(f_{13}(f_{13}(f_{13}(c_{23}))))))))))$   
 $p_{18}(x_8) \Rightarrow p_{20}(f_8(f_9(x_8)), f_{10}(f_{11}(f_{14}(f_{12}(f_{15}(f_{13}(c_{23}))))), f_{16}(f_4(f_6(x_8))), f_{11}(f_{14}(f_{12}(f_{15}(f_{13}(c_{23}))))), f_{12}(f_{13}(f_{13}(f_{13}(f_{13}(f_{13}(f_{13}(c_{23}))))))))))$

### SYN599-1.p Harrison problem 3757

$p_{17}(c_{21})$      $\text{cnf}(c_{21\_is\_}p_{17_1}, \text{negated\_conjecture})$   
 $p_{18}(c_{21})$      $\text{cnf}(c_{21\_is\_}p_{18_2}, \text{negated\_conjecture})$   
 $p_7(x_{34}, x_{34})$      $\text{cnf}(p_{7_3}, \text{negated\_conjecture})$   
 $p_2(x_9, x_9)$      $\text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $p_3(x_{18}, x_{18})$      $\text{cnf}(p_{3_5}, \text{negated\_conjecture})$   
 $p_5(x_{31}, x_{31})$      $\text{cnf}(p_{5_6}, \text{negated\_conjecture})$   
 $p_3(f_4(f_6(c_{21})), c_{22})$      $\text{cnf}(p_{3_7}, \text{negated\_conjecture})$   
 $(p_{17}(x_1) \text{ and } p_5(x_1, x_0)) \Rightarrow p_{17}(x_0)$      $\text{cnf}(p_{17_8}, \text{negated\_conjecture})$   
 $(p_{18}(x_3) \text{ and } p_5(x_3, x_2)) \Rightarrow p_{18}(x_2)$      $\text{cnf}(p_{18_9}, \text{negated\_conjecture})$   
 $p_5(x_{41}, x_{42}) \Rightarrow p_7(f_{16}(x_{41}), f_{16}(x_{42}))$      $\text{cnf}(p_{7_{10}}, \text{negated\_conjecture})$   
 $p_5(x_{12}, x_{13}) \Rightarrow p_2(f_6(x_{12}), f_6(x_{13}))$      $\text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $p_3(x_{21}, x_{22}) \Rightarrow p_3(f_{10}(x_{21}), f_{10}(x_{22}))$      $\text{cnf}(p_{3_{12}}, \text{negated\_conjecture})$   
 $p_3(x_{23}, x_{24}) \Rightarrow p_3(f_{11}(x_{23}), f_{11}(x_{24}))$      $\text{cnf}(p_{3_{13}}, \text{negated\_conjecture})$   
 $p_3(x_{25}, x_{26}) \Rightarrow p_3(f_{13}(x_{25}), f_{13}(x_{26}))$      $\text{cnf}(p_{3_{14}}, \text{negated\_conjecture})$   
 $p_3(x_{27}, x_{28}) \Rightarrow p_3(f_{14}(x_{27}), f_{14}(x_{28}))$      $\text{cnf}(p_{3_{15}}, \text{negated\_conjecture})$   
 $p_2(x_{29}, x_{30}) \Rightarrow p_3(f_4(x_{29}), f_4(x_{30}))$      $\text{cnf}(p_{3_{16}}, \text{negated\_conjecture})$   
 $p_3(x_{37}, x_{38}) \Rightarrow p_7(f_{12}(x_{37}), f_{12}(x_{38}))$      $\text{cnf}(p_{7_{17}}, \text{negated\_conjecture})$   
 $p_7(x_{39}, x_{40}) \Rightarrow p_7(f_{15}(x_{39}), f_{15}(x_{40}))$      $\text{cnf}(p_{7_{18}}, \text{negated\_conjecture})$

$(p_2(x_9, x_{10}) \text{ and } p_2(x_9, x_{11})) \Rightarrow p_2(x_{10}, x_{11})$      $\text{cnf}(p_{2_{19}}, \text{negated\_conjecture})$   
 $(p_7(x_{34}, x_{35}) \text{ and } p_7(x_{34}, x_{36})) \Rightarrow p_7(x_{35}, x_{36})$      $\text{cnf}(p_{7_{20}}, \text{negated\_conjecture})$   
 $(p_5(x_{31}, x_{32}) \text{ and } p_5(x_{31}, x_{33})) \Rightarrow p_5(x_{32}, x_{33})$      $\text{cnf}(p_{5_{21}}, \text{negated\_conjecture})$   
 $(p_3(x_{18}, x_{19}) \text{ and } p_3(x_{18}, x_{20})) \Rightarrow p_3(x_{19}, x_{20})$      $\text{cnf}(p_{3_{22}}, \text{negated\_conjecture})$   
 $(p_7(x_6, x_4) \text{ and } p_7(x_7, x_5) \text{ and } p_{19}(x_6, x_7)) \Rightarrow p_{19}(x_4, x_5)$      $\text{cnf}(p_{19_{23}}, \text{negated\_conjecture})$   
 $(p_7(x_{16}, x_{14}) \text{ and } p_7(x_{17}, x_{15}) \text{ and } p_{20}(x_{16}, x_{17})) \Rightarrow p_{20}(x_{14}, x_{15})$      $\text{cnf}(p_{20_{24}}, \text{negated\_conjecture})$   
 $(p_3(x_{48}, x_{50}) \text{ and } p_7(x_{47}, x_{49})) \Rightarrow p_7(f_9(x_{47}, x_{48}), f_9(x_{49}, x_{50}))$      $\text{cnf}(p_{7_{25}}, \text{negated\_conjecture})$   
 $(p_7(x_{43}, x_{45}) \text{ and } p_7(x_{44}, x_{46})) \Rightarrow p_7(f_8(x_{43}, x_{44}), f_8(x_{45}, x_{46}))$      $\text{cnf}(p_{7_{26}}, \text{negated\_conjecture})$   
 $\neg p_{19}(f_{15}(f_{16}(c_{21})), f_8(f_9(f_{12}(f_{10}(f_{13}(f_{11}(c_{23}))))), f_{14}(c_{22})), f_9(f_{12}(f_{10}(f_{13}(f_{11}(c_{23}))))), f_{10}(f_{11}(f_{11}(f_{11}(f_{11}(f_{11}(f_{11}(c_{23}))))))))))$   
 $p_{18}(x_8) \Rightarrow p_{20}(f_8(f_9(f_{12}(f_{10}(f_{13}(f_{11}(c_{23}))))), f_4(f_6(x_8))), f_9(f_{12}(f_{10}(f_{13}(f_{11}(c_{23}))))), f_{10}(f_{11}(f_{11}(f_{11}(f_{11}(f_{11}(f_{11}(c_{23}))))))))))$   
 $p_{18}(x_8) \Rightarrow p_{19}(f_{15}(f_{16}(x_8)), f_8(f_9(f_{12}(f_{10}(f_{13}(f_{11}(c_{23}))))), f_{14}(f_4(f_6(x_8))), f_9(f_{12}(f_{10}(f_{13}(f_{11}(c_{23}))))), f_{10}(f_{11}(f_{11}(f_{11}(f_{11}(f_{11}(f_{11}(c_{23}))))))))))$

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$p_{19}(c_{21})$      $\text{cnf}(c_{21\_is\_p19_1}, \text{negated\_conjecture})$   
 $p_{19}(c_{22})$      $\text{cnf}(c_{22\_is\_p19_2}, \text{negated\_conjecture})$   
 $p_2(x_{11}, x_{11})$      $\text{cnf}(p_{2_3}, \text{negated\_conjecture})$   
 $p_7(x_{32}, x_{32})$      $\text{cnf}(p_{7_4}, \text{negated\_conjecture})$   
 $p_5(x_{29}, x_{29})$      $\text{cnf}(p_{5_5}, \text{negated\_conjecture})$   
 $p_3(x_{16}, x_{16})$      $\text{cnf}(p_{3_6}, \text{negated\_conjecture})$   
 $p_7(f_{16}(c_{21}), f_{16}(c_{22}))$      $\text{cnf}(p_{7_7}, \text{negated\_conjecture})$   
 $\neg p_3(f_4(f_6(c_{21})), f_4(f_6(c_{22})))$      $\text{cnf}(\text{not\_p3}_8, \text{negated\_conjecture})$   
 $(p_{19}(x_{10}) \text{ and } p_5(x_{10}, x_9)) \Rightarrow p_{19}(x_9)$      $\text{cnf}(p_{19_9}, \text{negated\_conjecture})$   
 $p_5(x_{43}, x_{44}) \Rightarrow p_7(f_{16}(x_{43}), f_{16}(x_{44}))$      $\text{cnf}(p_{7_{10}}, \text{negated\_conjecture})$   
 $p_5(x_{14}, x_{15}) \Rightarrow p_2(f_6(x_{14}), f_6(x_{15}))$      $\text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $p_3(x_{19}, x_{20}) \Rightarrow p_3(f_{11}(x_{19}), f_{11}(x_{20}))$      $\text{cnf}(p_{3_{12}}, \text{negated\_conjecture})$   
 $p_3(x_{21}, x_{22}) \Rightarrow p_3(f_{12}(x_{21}), f_{12}(x_{22}))$      $\text{cnf}(p_{3_{13}}, \text{negated\_conjecture})$   
 $p_3(x_{23}, x_{24}) \Rightarrow p_3(f_{14}(x_{23}), f_{14}(x_{24}))$      $\text{cnf}(p_{3_{14}}, \text{negated\_conjecture})$   
 $p_2(x_{25}, x_{26}) \Rightarrow p_3(f_4(x_{25}), f_4(x_{26}))$      $\text{cnf}(p_{3_{15}}, \text{negated\_conjecture})$   
 $p_3(x_{39}, x_{40}) \Rightarrow p_7(f_{13}(x_{39}), f_{13}(x_{40}))$      $\text{cnf}(p_{7_{16}}, \text{negated\_conjecture})$   
 $p_7(x_{41}, x_{42}) \Rightarrow p_7(f_{15}(x_{41}), f_{15}(x_{42}))$      $\text{cnf}(p_{7_{17}}, \text{negated\_conjecture})$   
 $(p_2(x_{11}, x_{12}) \text{ and } p_2(x_{11}, x_{13})) \Rightarrow p_2(x_{12}, x_{13})$      $\text{cnf}(p_{2_{18}}, \text{negated\_conjecture})$   
 $(p_7(x_{32}, x_{33}) \text{ and } p_7(x_{32}, x_{34})) \Rightarrow p_7(x_{33}, x_{34})$      $\text{cnf}(p_{7_{19}}, \text{negated\_conjecture})$   
 $(p_5(x_{29}, x_{30}) \text{ and } p_5(x_{29}, x_{31})) \Rightarrow p_5(x_{30}, x_{31})$      $\text{cnf}(p_{5_{20}}, \text{negated\_conjecture})$   
 $(p_3(x_{16}, x_{17}) \text{ and } p_3(x_{16}, x_{18})) \Rightarrow p_3(x_{17}, x_{18})$      $\text{cnf}(p_{3_{21}}, \text{negated\_conjecture})$   
 $(p_7(x_2, x_0) \text{ and } p_7(x_3, x_1) \text{ and } p_{17}(x_2, x_3)) \Rightarrow p_{17}(x_0, x_1)$      $\text{cnf}(p_{17_{22}}, \text{negated\_conjecture})$   
 $(p_7(x_7, x_5) \text{ and } p_7(x_8, x_6) \text{ and } p_{18}(x_7, x_8)) \Rightarrow p_{18}(x_5, x_6)$      $\text{cnf}(p_{18_{23}}, \text{negated\_conjecture})$   
 $(p_7(x_{50}, x_{52}) \text{ and } p_7(x_{49}, x_{51})) \Rightarrow p_7(f_9(x_{49}, x_{50}), f_9(x_{51}, x_{52}))$      $\text{cnf}(p_{7_{24}}, \text{negated\_conjecture})$   
 $(p_3(x_{36}, x_{38}) \text{ and } p_7(x_{35}, x_{37})) \Rightarrow p_7(f_{10}(x_{35}, x_{36}), f_{10}(x_{37}, x_{38}))$      $\text{cnf}(p_{7_{25}}, \text{negated\_conjecture})$   
 $(p_7(x_{45}, x_{47}) \text{ and } p_7(x_{46}, x_{48})) \Rightarrow p_7(f_8(x_{45}, x_{46}), f_8(x_{47}, x_{48}))$      $\text{cnf}(p_{7_{26}}, \text{negated\_conjecture})$   
 $p_{19}(x_4) \Rightarrow p_{18}(f_9(f_{10}(f_{13}(f_{11}(f_{14}(f_{12}(c_{20}))))), f_4(f_6(x_4))), f_{10}(f_{13}(f_{11}(f_{14}(f_{12}(c_{20}))))), f_{11}(f_{12}(f_{12}(f_{12}(f_{12}(f_{12}(f_{12}(f_{12}(c_{20}))))))))))$   
 $p_{19}(x_4) \Rightarrow p_{17}(f_{15}(f_{16}(x_4)), f_8(f_{13}(f_{11}(f_{14}(f_{12}(c_{20}))))), f_9(f_{10}(f_{13}(f_{11}(f_{14}(f_{12}(c_{20}))))), f_4(f_6(x_4))), f_{10}(f_{13}(f_{11}(f_{14}(f_{12}(c_{20}))))), (p_{19}(x_{27}) \text{ and } p_{18}(f_9(f_{10}(f_{13}(f_{11}(f_{14}(f_{12}(c_{20}))))), x_{28}), f_{10}(f_{13}(f_{11}(f_{14}(f_{12}(c_{20}))))), f_{11}(f_{12}(f_{12}(f_{12}(f_{12}(f_{12}(f_{12}(f_{12}(c_{20}))))))))))$   
 $p_3(f_4(f_6(x_{27})), x_{28})$      $\text{cnf}(p_{3_{29}}, \text{negated\_conjecture})$

### SYN601-1.p Harrison problem 3799

$p_{10}(x_0, x_0)$      $\text{cnf}(p_{10_1}, \text{negated\_conjecture})$   
 $p_9(x_{52}, x_{52})$      $\text{cnf}(p_{9_2}, \text{negated\_conjecture})$   
 $p_3(x_{37}, x_{37})$      $\text{cnf}(p_{3_3}, \text{negated\_conjecture})$   
 $p_2(x_{30}, x_{30})$      $\text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $p_{12}(x_{11}, x_{11})$      $\text{cnf}(p_{12_5}, \text{negated\_conjecture})$   
 $p_{17}(c_{22}, c_{23})$      $\text{cnf}(p_{17_6}, \text{negated\_conjecture})$   
 $p_3(c_{22}, c_{23})$      $\text{cnf}(p_{3_7}, \text{negated\_conjecture})$   
 $p_{18}(c_{22}, f_8(c_{21}))$      $\text{cnf}(p_{18_8}, \text{negated\_conjecture})$   
 $p_{17}(f_5(f_6(f_7(c_{20}))), f_4(c_{21}))$      $\text{cnf}(p_{17_9}, \text{negated\_conjecture})$   
 $p_2(x_{50}, x_{51}) \Rightarrow p_3(f_8(x_{50}), f_8(x_{51}))$      $\text{cnf}(p_{3_{10}}, \text{negated\_conjecture})$   
 $p_3(x_9, x_{10}) \Rightarrow p_{10}(f_{16}(x_9), f_{16}(x_{10}))$      $\text{cnf}(p_{10_{11}}, \text{negated\_conjecture})$   
 $p_2(x_{40}, x_{41}) \Rightarrow p_3(f_{15}(x_{40}), f_{15}(x_{41}))$      $\text{cnf}(p_{3_{12}}, \text{negated\_conjecture})$   
 $p_2(x_{42}, x_{43}) \Rightarrow p_3(f_4(x_{42}), f_4(x_{43}))$      $\text{cnf}(p_{3_{13}}, \text{negated\_conjecture})$   
 $p_3(x_{44}, x_{45}) \Rightarrow p_3(f_5(x_{44}), f_5(x_{45}))$      $\text{cnf}(p_{3_{14}}, \text{negated\_conjecture})$   
 $p_3(x_{46}, x_{47}) \Rightarrow p_3(f_6(x_{46}), f_6(x_{47}))$      $\text{cnf}(p_{3_{15}}, \text{negated\_conjecture})$

$p_3(x_{48}, x_{49}) \Rightarrow p_3(f_7(x_{48}), f_7(x_{49})) \quad \text{cnf}(p_{3_{16}}, \text{negated\_conjecture})$   
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2) \quad \text{cnf}(p_{10_{17}}, \text{negated\_conjecture})$   
 $(p_9(x_{52}, x_{53}) \text{ and } p_9(x_{52}, x_{54})) \Rightarrow p_9(x_{53}, x_{54}) \quad \text{cnf}(p_{9_{18}}, \text{negated\_conjecture})$   
 $(p_3(x_{37}, x_{38}) \text{ and } p_3(x_{37}, x_{39})) \Rightarrow p_3(x_{38}, x_{39}) \quad \text{cnf}(p_{3_{19}}, \text{negated\_conjecture})$   
 $(p_2(x_{30}, x_{31}) \text{ and } p_2(x_{30}, x_{32})) \Rightarrow p_2(x_{31}, x_{32}) \quad \text{cnf}(p_{2_{20}}, \text{negated\_conjecture})$   
 $(p_{12}(x_{11}, x_{12}) \text{ and } p_{12}(x_{11}, x_{13})) \Rightarrow p_{12}(x_{12}, x_{13}) \quad \text{cnf}(p_{12_{21}}, \text{negated\_conjecture})$   
 $p_{19}(c_{21}, f_{11}(f_{13}(f_{15}(c_{21}), f_{14}(f_4(c_{21}), c_{22})), c_{24}, c_{25})) \quad \text{cnf}(p_{19_{22}}, \text{negated\_conjecture})$   
 $\neg p_{19}(c_{21}, f_{11}(f_{13}(f_{15}(c_{21}), f_{14}(f_4(c_{21}), c_{23})), c_{24}, c_{25})) \quad \text{cnf}(\text{not\_}p_{19_{23}}, \text{negated\_conjecture})$   
 $(p_{19}(x_{29}, x_{28}) \text{ and } p_2(x_{29}, x_{26}) \text{ and } p_{10}(x_{28}, x_{27})) \Rightarrow p_{19}(x_{26}, x_{27}) \quad \text{cnf}(p_{19_{24}}, \text{negated\_conjecture})$   
 $(p_3(x_{20}, x_{18}) \text{ and } p_3(x_{21}, x_{19}) \text{ and } p_{17}(x_{20}, x_{21})) \Rightarrow p_{17}(x_{18}, x_{19}) \quad \text{cnf}(p_{17_{25}}, \text{negated\_conjecture})$   
 $(p_3(x_{24}, x_{22}) \text{ and } p_3(x_{25}, x_{23}) \text{ and } p_{18}(x_{24}, x_{25})) \Rightarrow p_{18}(x_{22}, x_{23}) \quad \text{cnf}(p_{18_{26}}, \text{negated\_conjecture})$   
 $(p_3(x_{14}, x_{16}) \text{ and } p_3(x_{15}, x_{17})) \Rightarrow p_{12}(f_{14}(x_{14}, x_{15}), f_{14}(x_{16}, x_{17})) \quad \text{cnf}(p_{12_{27}}, \text{negated\_conjecture})$   
 $(p_{12}(x_{34}, x_{36}) \text{ and } p_3(x_{33}, x_{35})) \Rightarrow p_2(f_{13}(x_{33}, x_{34}), f_{13}(x_{35}, x_{36})) \quad \text{cnf}(p_{2_{28}}, \text{negated\_conjecture})$   
 $\neg p_{10}(f_{11}(f_{13}(f_{15}(c_{21}), f_{14}(f_4(c_{21}), c_{23})), c_{24}, c_{25}), f_{16}(f_5(c_{20}))) \quad \text{cnf}(\text{not\_}p_{10_{29}}, \text{negated\_conjecture})$   
 $(p_2(x_3, x_6) \text{ and } p_9(x_4, x_7) \text{ and } p_{10}(x_5, x_8)) \Rightarrow p_{10}(f_{11}(x_3, x_4, x_5), f_{11}(x_6, x_7, x_8)) \quad \text{cnf}(p_{10_{30}}, \text{negated\_conjecture})$

### SYN602-1.p Harrison problem 3811

$p_{14}(c_{20}) \quad \text{cnf}(c_{20\_is\_}p_{14_1}, \text{negated\_conjecture})$   
 $p_2(x_{18}, x_{18}) \quad \text{cnf}(p_{2_2}, \text{negated\_conjecture})$   
 $p_{15}(c_{22}, c_{21}) \quad \text{cnf}(p_{15_3}, \text{negated\_conjecture})$   
 $p_2(f_3(c_{18}), c_{19}) \quad \text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $p_2(c_{22}, f_9(c_{20}, c_{23})) \quad \text{cnf}(p_{2_5}, \text{negated\_conjecture})$   
 $p_2(f_3(f_4(c_{16})), c_{17}) \quad \text{cnf}(p_{2_6}, \text{negated\_conjecture})$   
 $(p_{14}(x_{12}) \text{ and } p_2(x_{12}, x_{11})) \Rightarrow p_{14}(x_{11}) \quad \text{cnf}(p_{14_7}, \text{negated\_conjecture})$   
 $p_{13}(x_{17}, f_5(c_{18})) \Rightarrow p_{15}(f_{10}(x_{17}), c_{21}) \quad \text{cnf}(p_{15_8}, \text{negated\_conjecture})$   
 $p_2(x_{35}, x_{36}) \Rightarrow p_2(f_5(x_{35}), f_5(x_{36})) \quad \text{cnf}(p_{2_9}, \text{negated\_conjecture})$   
 $p_2(x_{27}, x_{28}) \Rightarrow p_2(f_{10}(x_{27}), f_{10}(x_{28})) \quad \text{cnf}(p_{2_{10}}, \text{negated\_conjecture})$   
 $p_2(x_{29}, x_{30}) \Rightarrow p_2(f_{11}(x_{29}), f_{11}(x_{30})) \quad \text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $p_2(x_{31}, x_{32}) \Rightarrow p_2(f_3(x_{31}), f_3(x_{32})) \quad \text{cnf}(p_{2_{12}}, \text{negated\_conjecture})$   
 $p_2(x_{33}, x_{34}) \Rightarrow p_2(f_4(x_{33}), f_4(x_{34})) \quad \text{cnf}(p_{2_{13}}, \text{negated\_conjecture})$   
 $(p_2(x_{18}, x_{19}) \text{ and } p_2(x_{18}, x_{20})) \Rightarrow p_2(x_{19}, x_{20}) \quad \text{cnf}(p_{2_{14}}, \text{negated\_conjecture})$   
 $p_{13}(x_6, c_{18}) \Rightarrow p_{12}(x_6, f_3(x_6), f_3(f_5(x_6))) \quad \text{cnf}(p_{12_{15}}, \text{negated\_conjecture})$   
 $p_2(f_7(f_8(c_{21}, c_{22}), c_{20}), f_6(f_5(c_{18}), f_3(c_{18}))) \quad \text{cnf}(p_{2_{16}}, \text{negated\_conjecture})$   
 $p_{13}(x_{17}, f_5(c_{18})) \Rightarrow p_2(f_{10}(x_{17}), f_9(c_{20}, f_{11}(x_{17}))) \quad \text{cnf}(p_{2_{17}}, \text{negated\_conjecture})$   
 $(p_2(x_9, x_7) \text{ and } p_2(x_{10}, x_8) \text{ and } p_{13}(x_9, x_{10})) \Rightarrow p_{13}(x_7, x_8) \quad \text{cnf}(p_{13_{18}}, \text{negated\_conjecture})$   
 $(p_2(x_{15}, x_{13}) \text{ and } p_2(x_{16}, x_{14}) \text{ and } p_{15}(x_{15}, x_{16})) \Rightarrow p_{15}(x_{13}, x_{14}) \quad \text{cnf}(p_{15_{19}}, \text{negated\_conjecture})$   
 $(p_2(x_{49}, x_{51}) \text{ and } p_2(x_{50}, x_{52})) \Rightarrow p_2(f_9(x_{49}, x_{50}), f_9(x_{51}, x_{52})) \quad \text{cnf}(p_{2_{20}}, \text{negated\_conjecture})$   
 $(p_2(x_{37}, x_{39}) \text{ and } p_2(x_{38}, x_{40})) \Rightarrow p_2(f_6(x_{37}, x_{38}), f_6(x_{39}, x_{40})) \quad \text{cnf}(p_{2_{21}}, \text{negated\_conjecture})$   
 $(p_2(x_{41}, x_{43}) \text{ and } p_2(x_{42}, x_{44})) \Rightarrow p_2(f_7(x_{41}, x_{42}), f_7(x_{43}, x_{44})) \quad \text{cnf}(p_{2_{22}}, \text{negated\_conjecture})$   
 $(p_2(x_{45}, x_{47}) \text{ and } p_2(x_{46}, x_{48})) \Rightarrow p_2(f_8(x_{45}, x_{46}), f_8(x_{47}, x_{48})) \quad \text{cnf}(p_{2_{23}}, \text{negated\_conjecture})$   
 $p_{13}(x_{17}, f_5(c_{18})) \Rightarrow p_2(f_7(f_8(c_{21}, f_{10}(x_{17})), c_{20}), f_6(f_5(x_{17}), f_3(x_{17}))) \quad \text{cnf}(p_{2_{24}}, \text{negated\_conjecture})$   
 $(p_2(x_5, x_2) \text{ and } p_2(x_4, x_1) \text{ and } p_2(x_3, x_0) \text{ and } p_{12}(x_3, x_4, x_5)) \Rightarrow p_{12}(x_0, x_1, x_2) \quad \text{cnf}(p_{12_{25}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{53}, c_{21}) \text{ and } p_2(x_{53}, f_9(c_{20}, x_{54}))) \Rightarrow \neg p_2(f_7(f_8(c_{21}, x_{53}), c_{20}), f_6(f_5(c_{18}), c_{19})) \quad \text{cnf}(\text{not\_}p_{15_{26}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{21}, c_{21}) \text{ and } p_2(x_{21}, f_9(c_{20}, x_{22})) \text{ and } p_2(f_7(f_8(c_{21}, x_{21}), c_{20}), f_6(f_5(c_{18}), x_{23}))) \Rightarrow p_2(x_{21}, c_{22}) \quad \text{cnf}(p_{2_{27}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{21}, c_{21}) \text{ and } p_2(x_{21}, f_9(c_{20}, x_{22})) \text{ and } p_2(f_7(f_8(c_{21}, x_{21}), c_{20}), f_6(f_5(c_{18}), x_{23}))) \Rightarrow p_2(x_{23}, f_3(c_{18})) \quad \text{cnf}(p_{2_{28}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{24}, c_{21}) \text{ and } p_{13}(x_{17}, f_5(c_{18})) \text{ and } p_2(x_{24}, f_9(c_{20}, x_{25})) \text{ and } p_2(f_7(f_8(c_{21}, x_{24}), c_{20}), f_6(f_5(x_{17}), x_{26}))) \Rightarrow p_2(x_{26}, f_3(x_{17}))$   
 $(p_{15}(x_{24}, c_{21}) \text{ and } p_{13}(x_{17}, f_5(c_{18})) \text{ and } p_2(x_{24}, f_9(c_{20}, x_{25})) \text{ and } p_2(f_7(f_8(c_{21}, x_{24}), c_{20}), f_6(f_5(x_{17}), x_{26}))) \Rightarrow p_2(x_{24}, f_{10}(x_{17}))$

### SYN603-1.p Harrison problem 3812

$p_{14}(c_{20}) \quad \text{cnf}(c_{20\_is\_}p_{14_1}, \text{negated\_conjecture})$   
 $p_2(x_{18}, x_{18}) \quad \text{cnf}(p_{2_2}, \text{negated\_conjecture})$   
 $p_{15}(c_{22}, c_{21}) \quad \text{cnf}(p_{15_3}, \text{negated\_conjecture})$   
 $p_2(f_3(c_{18}), c_{19}) \quad \text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $p_2(c_{22}, f_9(c_{20}, c_{23})) \quad \text{cnf}(p_{2_5}, \text{negated\_conjecture})$   
 $p_2(f_3(f_4(c_{16})), c_{17}) \quad \text{cnf}(p_{2_6}, \text{negated\_conjecture})$   
 $(p_{14}(x_{12}) \text{ and } p_2(x_{12}, x_{11})) \Rightarrow p_{14}(x_{11}) \quad \text{cnf}(p_{14_7}, \text{negated\_conjecture})$   
 $p_{13}(x_{17}, f_5(c_{18})) \Rightarrow p_{15}(f_{10}(x_{17}), c_{21}) \quad \text{cnf}(p_{15_8}, \text{negated\_conjecture})$   
 $p_2(x_{35}, x_{36}) \Rightarrow p_2(f_5(x_{35}), f_5(x_{36})) \quad \text{cnf}(p_{2_9}, \text{negated\_conjecture})$   
 $p_2(x_{27}, x_{28}) \Rightarrow p_2(f_{10}(x_{27}), f_{10}(x_{28})) \quad \text{cnf}(p_{2_{10}}, \text{negated\_conjecture})$   
 $p_2(x_{29}, x_{30}) \Rightarrow p_2(f_{11}(x_{29}), f_{11}(x_{30})) \quad \text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$

$p_2(x_{31}, x_{32}) \Rightarrow p_2(f_3(x_{31}), f_3(x_{32}))$     cnf(p2<sub>12</sub>, negated\_conjecture)  
 $p_2(x_{33}, x_{34}) \Rightarrow p_2(f_4(x_{33}), f_4(x_{34}))$     cnf(p2<sub>13</sub>, negated\_conjecture)  
 $(p_2(x_{18}, x_{19}) \text{ and } p_2(x_{18}, x_{20})) \Rightarrow p_2(x_{19}, x_{20})$     cnf(p2<sub>14</sub>, negated\_conjecture)  
 $p_{13}(x_6, c_{18}) \Rightarrow p_{12}(x_6, f_3(x_6), f_3(f_5(x_6)))$     cnf(p12<sub>15</sub>, negated\_conjecture)  
 $p_{13}(x_{17}, f_5(c_{18})) \Rightarrow p_2(f_{10}(x_{17}), f_9(c_{20}, f_{11}(x_{17})))$     cnf(p2<sub>16</sub>, negated\_conjecture)  
 $(p_2(x_9, x_7) \text{ and } p_2(x_{10}, x_8) \text{ and } p_{13}(x_9, x_{10})) \Rightarrow p_{13}(x_7, x_8)$     cnf(p13<sub>17</sub>, negated\_conjecture)  
 $(p_2(x_{15}, x_{13}) \text{ and } p_2(x_{16}, x_{14}) \text{ and } p_{15}(x_{15}, x_{16})) \Rightarrow p_{15}(x_{13}, x_{14})$     cnf(p15<sub>18</sub>, negated\_conjecture)  
 $p_2(f_7(f_8(c_{21}, c_{22}), c_{20}), f_6(f_5(f_4(c_{16}))), f_3(f_4(c_{16})))$     cnf(p2<sub>19</sub>, negated\_conjecture)  
 $(p_2(x_{49}, x_{51}) \text{ and } p_2(x_{50}, x_{52})) \Rightarrow p_2(f_9(x_{49}, x_{50}), f_9(x_{51}, x_{52}))$     cnf(p2<sub>20</sub>, negated\_conjecture)  
 $(p_2(x_{37}, x_{39}) \text{ and } p_2(x_{38}, x_{40})) \Rightarrow p_2(f_6(x_{37}, x_{38}), f_6(x_{39}, x_{40}))$     cnf(p2<sub>21</sub>, negated\_conjecture)  
 $(p_2(x_{41}, x_{43}) \text{ and } p_2(x_{42}, x_{44})) \Rightarrow p_2(f_7(x_{41}, x_{42}), f_7(x_{43}, x_{44}))$     cnf(p2<sub>22</sub>, negated\_conjecture)  
 $(p_2(x_{45}, x_{47}) \text{ and } p_2(x_{46}, x_{48})) \Rightarrow p_2(f_8(x_{45}, x_{46}), f_8(x_{47}, x_{48}))$     cnf(p2<sub>23</sub>, negated\_conjecture)  
 $p_{13}(x_{17}, f_5(c_{18})) \Rightarrow p_2(f_7(f_8(c_{21}, f_{10}(x_{17})), c_{20}), f_6(f_5(x_{17}), f_3(x_{17})))$     cnf(p2<sub>24</sub>, negated\_conjecture)  
 $(p_2(x_5, x_2) \text{ and } p_2(x_4, x_1) \text{ and } p_2(x_3, x_0) \text{ and } p_{12}(x_3, x_4, x_5)) \Rightarrow p_{12}(x_0, x_1, x_2)$     cnf(p12<sub>25</sub>, negated\_conjecture)  
 $(p_{15}(x_{53}, c_{21}) \text{ and } p_2(x_{53}, f_9(c_{20}, x_{54}))) \Rightarrow \neg p_2(f_7(f_8(c_{21}, x_{53}), c_{20}), f_6(f_5(f_4(c_{16}))), c_{17}))$     cnf(not\_p15<sub>26</sub>, negated\_conjecture)  
 $(p_{15}(x_{21}, c_{21}) \text{ and } p_2(x_{21}, f_9(c_{20}, x_{22})) \text{ and } p_2(f_7(f_8(c_{21}, x_{21}), c_{20}), f_6(f_5(f_4(c_{16}))), x_{23}))) \Rightarrow p_2(x_{21}, c_{22})$     cnf(p2<sub>27</sub>, negated.  
 $(p_{15}(x_{21}, c_{21}) \text{ and } p_2(x_{21}, f_9(c_{20}, x_{22})) \text{ and } p_2(f_7(f_8(c_{21}, x_{21}), c_{20}), f_6(f_5(f_4(c_{16}))), x_{23}))) \Rightarrow p_2(x_{23}, f_3(f_4(c_{16})))$     cnf(p2<sub>28</sub>,  
 $(p_{15}(x_{24}, c_{21}) \text{ and } p_{13}(x_{17}, f_5(c_{18})) \text{ and } p_2(x_{24}, f_9(c_{20}, x_{25})) \text{ and } p_2(f_7(f_8(c_{21}, x_{24}), c_{20}), f_6(f_5(x_{17}), x_{26}))) \Rightarrow p_2(x_{26}, f_3(x_{17}))$   
 $(p_{15}(x_{24}, c_{21}) \text{ and } p_{13}(x_{17}, f_5(c_{18})) \text{ and } p_2(x_{24}, f_9(c_{20}, x_{25})) \text{ and } p_2(f_7(f_8(c_{21}, x_{24}), c_{20}), f_6(f_5(x_{17}), x_{26}))) \Rightarrow p_2(x_{24}, f_{10}(x_{17}))$

### SYN604-1.p Harrison problem 3820

$p_{14}(x_0, x_0)$     cnf(p14<sub>1</sub>, negated\_conjecture)  
 $p_9(x_{49}, x_{49})$     cnf(p9<sub>2</sub>, negated\_conjecture)  
 $p_5(x_{42}, x_{42})$     cnf(p5<sub>3</sub>, negated\_conjecture)  
 $p_3(x_{31}, x_{31})$     cnf(p3<sub>4</sub>, negated\_conjecture)  
 $p_2(x_{20}, x_{20})$     cnf(p2<sub>5</sub>, negated\_conjecture)  
 $p_{15}(c_{17}, c_{18})$     cnf(p15<sub>6</sub>, negated\_conjecture)  
 $p_3(f_4(f_8(x_{41})), f_{12}(x_{41}))$     cnf(p3<sub>7</sub>, negated\_conjecture)  
 $p_3(f_{12}(f_{10}(x_{38})), f_{10}(x_{38}))$     cnf(p3<sub>8</sub>, negated\_conjecture)  
 $p_{16}(f_{10}(f_{11}(c_{21})), f_{12}(x_{16}))$     cnf(p16<sub>9</sub>, negated\_conjecture)  
 $p_{16}(x_{14}, x_{15}) \text{ or } p_{16}(x_{15}, f_{12}(x_{14}))$     cnf(p16<sub>10</sub>, negated\_conjecture)  
 $p_9(x_{52}, x_{53}) \Rightarrow p_9(f_{11}(x_{52}), f_{11}(x_{53}))$     cnf(p9<sub>11</sub>, negated\_conjecture)  
 $p_2(x_{23}, x_{24}) \Rightarrow p_2(f_{13}(x_{23}), f_{13}(x_{24}))$     cnf(p2<sub>12</sub>, negated\_conjecture)  
 $p_3(x_{29}, x_{30}) \Rightarrow p_2(f_8(x_{29}), f_8(x_{30}))$     cnf(p2<sub>13</sub>, negated\_conjecture)  
 $p_9(x_{34}, x_{35}) \Rightarrow p_3(f_{10}(x_{34}), f_{10}(x_{35}))$     cnf(p3<sub>14</sub>, negated\_conjecture)  
 $p_3(x_{36}, x_{37}) \Rightarrow p_3(f_{12}(x_{36}), f_{12}(x_{37}))$     cnf(p3<sub>15</sub>, negated\_conjecture)  
 $p_2(x_{39}, x_{40}) \Rightarrow p_3(f_4(x_{39}), f_4(x_{40}))$     cnf(p3<sub>16</sub>, negated\_conjecture)  
 $p_{16}(f_4(f_6(c_{18}, c_{22})), f_4(f_6(c_{18}, x_{17})))$     cnf(p16<sub>17</sub>, negated\_conjecture)  
 $(p_{14}(x_0, x_1) \text{ and } p_{14}(x_0, x_2)) \Rightarrow p_{14}(x_1, x_2)$     cnf(p14<sub>18</sub>, negated\_conjecture)  
 $(p_9(x_{49}, x_{50}) \text{ and } p_9(x_{49}, x_{51})) \Rightarrow p_9(x_{50}, x_{51})$     cnf(p9<sub>19</sub>, negated\_conjecture)  
 $(p_5(x_{42}, x_{43}) \text{ and } p_5(x_{42}, x_{44})) \Rightarrow p_5(x_{43}, x_{44})$     cnf(p5<sub>20</sub>, negated\_conjecture)  
 $(p_3(x_{31}, x_{32}) \text{ and } p_3(x_{31}, x_{33})) \Rightarrow p_3(x_{32}, x_{33})$     cnf(p3<sub>21</sub>, negated\_conjecture)  
 $(p_2(x_{20}, x_{21}) \text{ and } p_2(x_{20}, x_{22})) \Rightarrow p_2(x_{21}, x_{22})$     cnf(p2<sub>22</sub>, negated\_conjecture)  
 $(p_{16}(x_{11}, x_{13}) \text{ and } p_{16}(x_{13}, x_{12})) \Rightarrow p_{16}(x_{11}, x_{12})$     cnf(p16<sub>23</sub>, negated\_conjecture)  
 $(p_{15}(x_5, x_6) \text{ and } p_5(x_6, x_4) \text{ and } p_{14}(x_5, x_3)) \Rightarrow p_{15}(x_3, x_4)$     cnf(p15<sub>24</sub>, negated\_conjecture)  
 $(p_3(x_9, x_7) \text{ and } p_3(x_{10}, x_8) \text{ and } p_{16}(x_9, x_{10})) \Rightarrow p_{16}(x_7, x_8)$     cnf(p16<sub>25</sub>, negated\_conjecture)  
 $(p_2(x_{45}, x_{47}) \text{ and } p_5(x_{46}, x_{48})) \Rightarrow p_5(f_7(x_{45}, x_{46}), f_7(x_{47}, x_{48}))$     cnf(p5<sub>26</sub>, negated\_conjecture)  
 $(p_2(x_{26}, x_{28}) \text{ and } p_5(x_{25}, x_{27})) \Rightarrow p_2(f_6(x_{25}, x_{26}), f_6(x_{27}, x_{28}))$     cnf(p2<sub>27</sub>, negated\_conjecture)  
 $\neg p_{16}(f_4(f_6(f_7(c_{20}, c_{18}), x_{54})), f_4(f_6(f_7(c_{20}, c_{18}), f_{13}(x_{54}))))$     cnf(not\_p16<sub>28</sub>, negated\_conjecture)  
 $p_{16}(f_4(x_{18}), f_{12}(c_{19})) \Rightarrow p_{16}(f_4(f_6(f_7(c_{20}, c_{18}), c_{23})), f_4(f_6(f_7(c_{20}, c_{18}), x_{18})))$     cnf(p16<sub>29</sub>, negated\_conjecture)  
 $p_{16}(c_{19}, f_4(x_{19})) \Rightarrow p_{16}(f_4(f_6(f_7(c_{20}, c_{18}), f_8(f_{10}(f_{11}(c_{21}))))), f_4(f_6(f_7(c_{20}, c_{18}), x_{19})))$     cnf(p16<sub>30</sub>, negated\_conjecture)

### SYN605-1.p Harrison problem 3825

$\neg p_{16}(c_{21})$     cnf(c21\_is\_not\_p16<sub>1</sub>, negated\_conjecture)  
 $p_2(x_{11}, x_{11})$     cnf(p2<sub>2</sub>, negated\_conjecture)  
 $p_5(x_{43}, x_{43})$     cnf(p5<sub>3</sub>, negated\_conjecture)  
 $p_3(x_{18}, x_{18})$     cnf(p3<sub>4</sub>, negated\_conjecture)  
 $\neg p_5(c_{21}, f_7(c_{20}))$     cnf(not\_p5<sub>5</sub>, negated\_conjecture)  
 $p_3(f_{12}(c_{22}, c_{21}), c_{22})$     cnf(p3<sub>6</sub>, negated\_conjecture)  
 $\neg p_3(c_{19}, f_4(f_6(f_7(c_{20}))))$     cnf(not\_p3<sub>7</sub>, negated\_conjecture)

$p_3(f_{12}(f_{15}(c_{22}), c_{21}), f_{15}(c_{22})) \quad \text{cnf}(p_{3_8}, \text{negated\_conjecture})$   
 $(p_{16}(x_1) \text{ and } p_5(x_1, x_0)) \Rightarrow p_{16}(x_0) \quad \text{cnf}(p_{16_9}, \text{negated\_conjecture})$   
 $p_5(x_{48}, x_{49}) \Rightarrow p_5(f_8(x_{48}), f_8(x_{49})) \quad \text{cnf}(p_{5_{10}}, \text{negated\_conjecture})$   
 $p_5(x_{14}, x_{15}) \Rightarrow p_2(f_6(x_{14}), f_6(x_{15})) \quad \text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $p_3(x_{16}, x_{17}) \Rightarrow p_2(f_9(x_{16}), f_9(x_{17})) \quad \text{cnf}(p_{2_{12}}, \text{negated\_conjecture})$   
 $p_5(x_{33}, x_{34}) \Rightarrow p_3(f_{13}(x_{33}), f_{13}(x_{34})) \quad \text{cnf}(p_{3_{13}}, \text{negated\_conjecture})$   
 $p_3(x_{39}, x_{40}) \Rightarrow p_3(f_{15}(x_{39}), f_{15}(x_{40})) \quad \text{cnf}(p_{3_{14}}, \text{negated\_conjecture})$   
 $p_2(x_{41}, x_{42}) \Rightarrow p_3(f_4(x_{41}), f_4(x_{42})) \quad \text{cnf}(p_{3_{15}}, \text{negated\_conjecture})$   
 $p_5(x_{46}, x_{47}) \Rightarrow p_5(f_7(x_{46}), f_7(x_{47})) \quad \text{cnf}(p_{5_{16}}, \text{negated\_conjecture})$   
 $(p_2(x_{11}, x_{12}) \text{ and } p_2(x_{11}, x_{13})) \Rightarrow p_2(x_{12}, x_{13}) \quad \text{cnf}(p_{2_{17}}, \text{negated\_conjecture})$   
 $(p_5(x_{43}, x_{44}) \text{ and } p_5(x_{43}, x_{45})) \Rightarrow p_5(x_{44}, x_{45}) \quad \text{cnf}(p_{5_{18}}, \text{negated\_conjecture})$   
 $(p_3(x_{18}, x_{19}) \text{ and } p_3(x_{18}, x_{20})) \Rightarrow p_3(x_{19}, x_{20}) \quad \text{cnf}(p_{3_{19}}, \text{negated\_conjecture})$   
 $(p_2(x_4, x_2) \text{ and } p_2(x_5, x_3) \text{ and } p_{17}(x_4, x_5)) \Rightarrow p_{17}(x_2, x_3) \quad \text{cnf}(p_{17_{20}}, \text{negated\_conjecture})$   
 $(p_5(x_9, x_7) \text{ and } p_5(x_{10}, x_8) \text{ and } p_{18}(x_9, x_{10})) \Rightarrow p_{18}(x_7, x_8) \quad \text{cnf}(p_{18_{21}}, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_4(f_6(f_7(f_8(c_{20}))))), c_{21}), f_4(f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(p_{3_{22}}, \text{negated\_conjecture})$   
 $p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), c_{22}), f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(p_{17_{23}}, \text{negated\_conjecture})$   
 $(p_3(x_{35}, x_{37}) \text{ and } p_3(x_{36}, x_{38})) \Rightarrow p_3(f_{14}(x_{35}, x_{36}), f_{14}(x_{37}, x_{38})) \quad \text{cnf}(p_{3_{24}}, \text{negated\_conjecture})$   
 $(p_3(x_{21}, x_{23}) \text{ and } p_3(x_{22}, x_{24})) \Rightarrow p_3(f_{10}(x_{21}, x_{22}), f_{10}(x_{23}, x_{24})) \quad \text{cnf}(p_{3_{25}}, \text{negated\_conjecture})$   
 $(p_3(x_{25}, x_{27}) \text{ and } p_3(x_{26}, x_{28})) \Rightarrow p_3(f_{11}(x_{25}, x_{26}), f_{11}(x_{27}, x_{28})) \quad \text{cnf}(p_{3_{26}}, \text{negated\_conjecture})$   
 $(p_3(x_{29}, x_{31}) \text{ and } p_5(x_{30}, x_{32})) \Rightarrow p_3(f_{12}(x_{29}, x_{30}), f_{12}(x_{31}, x_{32})) \quad \text{cnf}(p_{3_{27}}, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_{15}(f_4(f_6(f_7(f_8(c_{20}))))), c_{21}), f_{15}(f_4(f_6(f_7(f_8(c_{20})))))) \quad \text{cnf}(p_{3_{28}}, \text{negated\_conjecture})$   
 $\neg p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), f_{12}(x_{50}, c_{21})), f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(\text{not\_p}_{17_{29}}, \text{negated\_conjecture})$   
 $p_{18}(x_6, c_{21}) \Rightarrow (p_5(x_6, f_7(c_{20})) \text{ or } p_3(c_{19}, f_4(f_6(f_7(c_{20})))) \text{ or } p_{17}(f_9(f_{10}(f_4(f_6(f_7(f_8(c_{20}))))), f_{11}(c_{19}, f_{12}(f_{13}(x_6), x_6))))), f_6(f_7($

#### SYN606-1.p Harrison problem 3826

$\neg p_{16}(c_{21}) \quad \text{cnf}(c_{21\_is\_not\_p}_{16_1}, \text{negated\_conjecture})$   
 $p_2(x_{11}, x_{11}) \quad \text{cnf}(p_{2_2}, \text{negated\_conjecture})$   
 $p_5(x_{43}, x_{43}) \quad \text{cnf}(p_{5_3}, \text{negated\_conjecture})$   
 $p_3(x_{18}, x_{18}) \quad \text{cnf}(p_{3_4}, \text{negated\_conjecture})$   
 $\neg p_5(c_{21}, f_7(c_{20})) \quad \text{cnf}(\text{not\_p}_{5_5}, \text{negated\_conjecture})$   
 $p_3(f_{12}(c_{22}, c_{21}), f_{15}(c_{22})) \quad \text{cnf}(p_{3_6}, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_{15}(c_{22}), c_{21}), c_{22}) \quad \text{cnf}(p_{3_7}, \text{negated\_conjecture})$   
 $\neg p_3(c_{19}, f_4(f_6(f_7(c_{20})))) \quad \text{cnf}(\text{not\_p}_{3_8}, \text{negated\_conjecture})$   
 $(p_{16}(x_1) \text{ and } p_5(x_1, x_0)) \Rightarrow p_{16}(x_0) \quad \text{cnf}(p_{16_9}, \text{negated\_conjecture})$   
 $p_5(x_{48}, x_{49}) \Rightarrow p_5(f_8(x_{48}), f_8(x_{49})) \quad \text{cnf}(p_{5_{10}}, \text{negated\_conjecture})$   
 $p_5(x_{14}, x_{15}) \Rightarrow p_2(f_6(x_{14}), f_6(x_{15})) \quad \text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $p_3(x_{16}, x_{17}) \Rightarrow p_2(f_9(x_{16}), f_9(x_{17})) \quad \text{cnf}(p_{2_{12}}, \text{negated\_conjecture})$   
 $p_5(x_{33}, x_{34}) \Rightarrow p_3(f_{13}(x_{33}), f_{13}(x_{34})) \quad \text{cnf}(p_{3_{13}}, \text{negated\_conjecture})$   
 $p_3(x_{39}, x_{40}) \Rightarrow p_3(f_{15}(x_{39}), f_{15}(x_{40})) \quad \text{cnf}(p_{3_{14}}, \text{negated\_conjecture})$   
 $p_2(x_{41}, x_{42}) \Rightarrow p_3(f_4(x_{41}), f_4(x_{42})) \quad \text{cnf}(p_{3_{15}}, \text{negated\_conjecture})$   
 $p_5(x_{46}, x_{47}) \Rightarrow p_5(f_7(x_{46}), f_7(x_{47})) \quad \text{cnf}(p_{5_{16}}, \text{negated\_conjecture})$   
 $(p_2(x_{11}, x_{12}) \text{ and } p_2(x_{11}, x_{13})) \Rightarrow p_2(x_{12}, x_{13}) \quad \text{cnf}(p_{2_{17}}, \text{negated\_conjecture})$   
 $(p_5(x_{43}, x_{44}) \text{ and } p_5(x_{43}, x_{45})) \Rightarrow p_5(x_{44}, x_{45}) \quad \text{cnf}(p_{5_{18}}, \text{negated\_conjecture})$   
 $(p_3(x_{18}, x_{19}) \text{ and } p_3(x_{18}, x_{20})) \Rightarrow p_3(x_{19}, x_{20}) \quad \text{cnf}(p_{3_{19}}, \text{negated\_conjecture})$   
 $(p_2(x_4, x_2) \text{ and } p_2(x_5, x_3) \text{ and } p_{17}(x_4, x_5)) \Rightarrow p_{17}(x_2, x_3) \quad \text{cnf}(p_{17_{20}}, \text{negated\_conjecture})$   
 $(p_5(x_9, x_7) \text{ and } p_5(x_{10}, x_8) \text{ and } p_{18}(x_9, x_{10})) \Rightarrow p_{18}(x_7, x_8) \quad \text{cnf}(p_{18_{21}}, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_4(f_6(f_7(f_8(c_{20}))))), c_{21}), f_4(f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(p_{3_{22}}, \text{negated\_conjecture})$   
 $p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), c_{22}), f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(p_{17_{23}}, \text{negated\_conjecture})$   
 $(p_3(x_{35}, x_{37}) \text{ and } p_3(x_{36}, x_{38})) \Rightarrow p_3(f_{14}(x_{35}, x_{36}), f_{14}(x_{37}, x_{38})) \quad \text{cnf}(p_{3_{24}}, \text{negated\_conjecture})$   
 $(p_3(x_{21}, x_{23}) \text{ and } p_3(x_{22}, x_{24})) \Rightarrow p_3(f_{10}(x_{21}, x_{22}), f_{10}(x_{23}, x_{24})) \quad \text{cnf}(p_{3_{25}}, \text{negated\_conjecture})$   
 $(p_3(x_{25}, x_{27}) \text{ and } p_3(x_{26}, x_{28})) \Rightarrow p_3(f_{11}(x_{25}, x_{26}), f_{11}(x_{27}, x_{28})) \quad \text{cnf}(p_{3_{26}}, \text{negated\_conjecture})$   
 $(p_3(x_{29}, x_{31}) \text{ and } p_5(x_{30}, x_{32})) \Rightarrow p_3(f_{12}(x_{29}, x_{30}), f_{12}(x_{31}, x_{32})) \quad \text{cnf}(p_{3_{27}}, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_{15}(f_4(f_6(f_7(f_8(c_{20}))))), c_{21}), f_{15}(f_4(f_6(f_7(f_8(c_{20})))))) \quad \text{cnf}(p_{3_{28}}, \text{negated\_conjecture})$   
 $\neg p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), f_{12}(x_{50}, c_{21})), f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(\text{not\_p}_{17_{29}}, \text{negated\_conjecture})$   
 $p_{18}(x_6, c_{21}) \Rightarrow (p_5(x_6, f_7(c_{20})) \text{ or } p_3(c_{19}, f_4(f_6(f_7(c_{20})))) \text{ or } p_{17}(f_9(f_{10}(f_4(f_6(f_7(f_8(c_{20}))))), f_{11}(c_{19}, f_{12}(f_{13}(x_6), x_6))))), f_6(f_7($

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$\neg p_{16}(c_{21}) \quad \text{cnf}(c_{21\_is\_not\_p}_{16_1}, \text{negated\_conjecture})$   
 $p_2(x_{11}, x_{11}) \quad \text{cnf}(p_{2_2}, \text{negated\_conjecture})$   
 $p_5(x_{43}, x_{43}) \quad \text{cnf}(p_{5_3}, \text{negated\_conjecture})$

$p_3(x_{18}, x_{18}) \quad \text{cnf}(p3_4, \text{negated\_conjecture})$   
 $\neg p_5(c_{21}, f_7(c_{20})) \quad \text{cnf}(\text{not\_p5}_5, \text{negated\_conjecture})$   
 $p_3(f_{12}(c_{22}, c_{21}), c_{22}) \quad \text{cnf}(p3_6, \text{negated\_conjecture})$   
 $\neg p_3(c_{19}, f_4(f_6(f_7(c_{20})))) \quad \text{cnf}(\text{not\_p3}_7, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_{15}(c_{22}), c_{21}), f_{15}(c_{22})) \quad \text{cnf}(p3_8, \text{negated\_conjecture})$   
 $(p_{16}(x_1) \text{ and } p_5(x_1, x_0)) \Rightarrow p_{16}(x_0) \quad \text{cnf}(p16_9, \text{negated\_conjecture})$   
 $p_5(x_{48}, x_{49}) \Rightarrow p_5(f_8(x_{48}), f_8(x_{49})) \quad \text{cnf}(p5_{10}, \text{negated\_conjecture})$   
 $p_5(x_{14}, x_{15}) \Rightarrow p_2(f_6(x_{14}), f_6(x_{15})) \quad \text{cnf}(p2_{11}, \text{negated\_conjecture})$   
 $p_3(x_{16}, x_{17}) \Rightarrow p_2(f_9(x_{16}), f_9(x_{17})) \quad \text{cnf}(p2_{12}, \text{negated\_conjecture})$   
 $p_5(x_{33}, x_{34}) \Rightarrow p_3(f_{13}(x_{33}), f_{13}(x_{34})) \quad \text{cnf}(p3_{13}, \text{negated\_conjecture})$   
 $p_3(x_{39}, x_{40}) \Rightarrow p_3(f_{15}(x_{39}), f_{15}(x_{40})) \quad \text{cnf}(p3_{14}, \text{negated\_conjecture})$   
 $p_2(x_{41}, x_{42}) \Rightarrow p_3(f_4(x_{41}), f_4(x_{42})) \quad \text{cnf}(p3_{15}, \text{negated\_conjecture})$   
 $p_5(x_{46}, x_{47}) \Rightarrow p_5(f_7(x_{46}), f_7(x_{47})) \quad \text{cnf}(p5_{16}, \text{negated\_conjecture})$   
 $(p_2(x_{11}, x_{12}) \text{ and } p_2(x_{11}, x_{13})) \Rightarrow p_2(x_{12}, x_{13}) \quad \text{cnf}(p2_{17}, \text{negated\_conjecture})$   
 $(p_5(x_{43}, x_{44}) \text{ and } p_5(x_{43}, x_{45})) \Rightarrow p_5(x_{44}, x_{45}) \quad \text{cnf}(p5_{18}, \text{negated\_conjecture})$   
 $(p_3(x_{18}, x_{19}) \text{ and } p_3(x_{18}, x_{20})) \Rightarrow p_3(x_{19}, x_{20}) \quad \text{cnf}(p3_{19}, \text{negated\_conjecture})$   
 $(p_2(x_4, x_2) \text{ and } p_2(x_5, x_3) \text{ and } p_{17}(x_4, x_5)) \Rightarrow p_{17}(x_2, x_3) \quad \text{cnf}(p17_{20}, \text{negated\_conjecture})$   
 $(p_5(x_9, x_7) \text{ and } p_5(x_{10}, x_8) \text{ and } p_{18}(x_9, x_{10})) \Rightarrow p_{18}(x_7, x_8) \quad \text{cnf}(p18_{21}, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_4(f_6(f_7(f_8(c_{20}))))), c_{21}), f_4(f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(p3_{22}, \text{negated\_conjecture})$   
 $(p_3(x_{35}, x_{37}) \text{ and } p_3(x_{36}, x_{38})) \Rightarrow p_3(f_{14}(x_{35}, x_{36}), f_{14}(x_{37}, x_{38})) \quad \text{cnf}(p3_{23}, \text{negated\_conjecture})$   
 $(p_3(x_{21}, x_{23}) \text{ and } p_3(x_{22}, x_{24})) \Rightarrow p_3(f_{10}(x_{21}, x_{22}), f_{10}(x_{23}, x_{24})) \quad \text{cnf}(p3_{24}, \text{negated\_conjecture})$   
 $(p_3(x_{25}, x_{27}) \text{ and } p_3(x_{26}, x_{28})) \Rightarrow p_3(f_{11}(x_{25}, x_{26}), f_{11}(x_{27}, x_{28})) \quad \text{cnf}(p3_{25}, \text{negated\_conjecture})$   
 $(p_3(x_{29}, x_{31}) \text{ and } p_5(x_{30}, x_{32})) \Rightarrow p_3(f_{12}(x_{29}, x_{30}), f_{12}(x_{31}, x_{32})) \quad \text{cnf}(p3_{26}, \text{negated\_conjecture})$   
 $p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), f_{15}(c_{22}))), f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(p17_{27}, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_{15}(f_4(f_6(f_7(f_8(c_{20}))))), c_{21}), f_{15}(f_4(f_6(f_7(f_8(c_{20})))))) \quad \text{cnf}(p3_{28}, \text{negated\_conjecture})$   
 $\neg p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), f_{12}(x_{50}, c_{21}))), f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(\text{not\_p17}_{29}, \text{negated\_conjecture})$   
 $p_{18}(x_6, c_{21}) \Rightarrow (p_5(x_6, f_7(c_{20})) \text{ or } p_3(c_{19}, f_4(f_6(f_7(c_{20})))) \text{ or } p_{17}(f_9(f_{10}(f_4(f_6(f_7(f_8(c_{20}))))), f_{11}(c_{19}, f_{12}(f_{13}(x_6), x_6))))), f_6(f_7(c_{20})))$

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$\neg p_{16}(c_{21}) \quad \text{cnf}(c21\_is\_not\_p16_1, \text{negated\_conjecture})$   
 $p_2(x_{11}, x_{11}) \quad \text{cnf}(p2_2, \text{negated\_conjecture})$   
 $p_5(x_{43}, x_{43}) \quad \text{cnf}(p5_3, \text{negated\_conjecture})$   
 $p_3(x_{18}, x_{18}) \quad \text{cnf}(p3_4, \text{negated\_conjecture})$   
 $\neg p_5(c_{21}, f_7(c_{20})) \quad \text{cnf}(\text{not\_p5}_5, \text{negated\_conjecture})$   
 $p_3(f_{12}(c_{22}, c_{21}), f_{15}(c_{22})) \quad \text{cnf}(p3_6, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_{15}(c_{22}), c_{21}), c_{22}) \quad \text{cnf}(p3_7, \text{negated\_conjecture})$   
 $\neg p_3(c_{19}, f_4(f_6(f_7(c_{20})))) \quad \text{cnf}(\text{not\_p3}_8, \text{negated\_conjecture})$   
 $(p_{16}(x_1) \text{ and } p_5(x_1, x_0)) \Rightarrow p_{16}(x_0) \quad \text{cnf}(p16_9, \text{negated\_conjecture})$   
 $p_5(x_{48}, x_{49}) \Rightarrow p_5(f_8(x_{48}), f_8(x_{49})) \quad \text{cnf}(p5_{10}, \text{negated\_conjecture})$   
 $p_5(x_{14}, x_{15}) \Rightarrow p_2(f_6(x_{14}), f_6(x_{15})) \quad \text{cnf}(p2_{11}, \text{negated\_conjecture})$   
 $p_3(x_{16}, x_{17}) \Rightarrow p_2(f_9(x_{16}), f_9(x_{17})) \quad \text{cnf}(p2_{12}, \text{negated\_conjecture})$   
 $p_5(x_{33}, x_{34}) \Rightarrow p_3(f_{13}(x_{33}), f_{13}(x_{34})) \quad \text{cnf}(p3_{13}, \text{negated\_conjecture})$   
 $p_3(x_{39}, x_{40}) \Rightarrow p_3(f_{15}(x_{39}), f_{15}(x_{40})) \quad \text{cnf}(p3_{14}, \text{negated\_conjecture})$   
 $p_2(x_{41}, x_{42}) \Rightarrow p_3(f_4(x_{41}), f_4(x_{42})) \quad \text{cnf}(p3_{15}, \text{negated\_conjecture})$   
 $p_5(x_{46}, x_{47}) \Rightarrow p_5(f_7(x_{46}), f_7(x_{47})) \quad \text{cnf}(p5_{16}, \text{negated\_conjecture})$   
 $(p_2(x_{11}, x_{12}) \text{ and } p_2(x_{11}, x_{13})) \Rightarrow p_2(x_{12}, x_{13}) \quad \text{cnf}(p2_{17}, \text{negated\_conjecture})$   
 $(p_5(x_{43}, x_{44}) \text{ and } p_5(x_{43}, x_{45})) \Rightarrow p_5(x_{44}, x_{45}) \quad \text{cnf}(p5_{18}, \text{negated\_conjecture})$   
 $(p_3(x_{18}, x_{19}) \text{ and } p_3(x_{18}, x_{20})) \Rightarrow p_3(x_{19}, x_{20}) \quad \text{cnf}(p3_{19}, \text{negated\_conjecture})$   
 $(p_2(x_4, x_2) \text{ and } p_2(x_5, x_3) \text{ and } p_{17}(x_4, x_5)) \Rightarrow p_{17}(x_2, x_3) \quad \text{cnf}(p17_{20}, \text{negated\_conjecture})$   
 $(p_5(x_9, x_7) \text{ and } p_5(x_{10}, x_8) \text{ and } p_{18}(x_9, x_{10})) \Rightarrow p_{18}(x_7, x_8) \quad \text{cnf}(p18_{21}, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_4(f_6(f_7(f_8(c_{20}))))), c_{21}), f_4(f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(p3_{22}, \text{negated\_conjecture})$   
 $(p_3(x_{35}, x_{37}) \text{ and } p_3(x_{36}, x_{38})) \Rightarrow p_3(f_{14}(x_{35}, x_{36}), f_{14}(x_{37}, x_{38})) \quad \text{cnf}(p3_{23}, \text{negated\_conjecture})$   
 $(p_3(x_{21}, x_{23}) \text{ and } p_3(x_{22}, x_{24})) \Rightarrow p_3(f_{10}(x_{21}, x_{22}), f_{10}(x_{23}, x_{24})) \quad \text{cnf}(p3_{24}, \text{negated\_conjecture})$   
 $(p_3(x_{25}, x_{27}) \text{ and } p_3(x_{26}, x_{28})) \Rightarrow p_3(f_{11}(x_{25}, x_{26}), f_{11}(x_{27}, x_{28})) \quad \text{cnf}(p3_{25}, \text{negated\_conjecture})$   
 $(p_3(x_{29}, x_{31}) \text{ and } p_5(x_{30}, x_{32})) \Rightarrow p_3(f_{12}(x_{29}, x_{30}), f_{12}(x_{31}, x_{32})) \quad \text{cnf}(p3_{26}, \text{negated\_conjecture})$   
 $p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), f_{15}(c_{22}))), f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(p17_{27}, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_{15}(f_4(f_6(f_7(f_8(c_{20}))))), c_{21}), f_{15}(f_4(f_6(f_7(f_8(c_{20})))))) \quad \text{cnf}(p3_{28}, \text{negated\_conjecture})$   
 $\neg p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), f_{12}(x_{50}, c_{21}))), f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(\text{not\_p17}_{29}, \text{negated\_conjecture})$   
 $p_{18}(x_6, c_{21}) \Rightarrow (p_5(x_6, f_7(c_{20})) \text{ or } p_3(c_{19}, f_4(f_6(f_7(c_{20})))) \text{ or } p_{17}(f_9(f_{10}(f_4(f_6(f_7(f_8(c_{20}))))), f_{11}(c_{19}, f_{12}(f_{13}(x_6), x_6))))), f_6(f_7(c_{20})))$

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$\neg p_{16}(c_{21}) \quad \text{cnf}(c_{21\_is\_not\_p16_1, \text{negated\_conjecture})}$   
 $p_2(x_{11}, x_{11}) \quad \text{cnf}(p_{2_2, \text{negated\_conjecture})}$   
 $p_5(x_{43}, x_{43}) \quad \text{cnf}(p_{5_3, \text{negated\_conjecture})}$   
 $p_3(x_{18}, x_{18}) \quad \text{cnf}(p_{3_4, \text{negated\_conjecture})}$   
 $\neg p_5(c_{21}, f_7(c_{20})) \quad \text{cnf}(\text{not\_p5}_5, \text{negated\_conjecture})$   
 $p_3(f_{12}(c_{22}, c_{21}), c_{22}) \quad \text{cnf}(p_{3_6, \text{negated\_conjecture})}$   
 $\neg p_3(c_{19}, f_4(f_6(f_7(c_{20})))) \quad \text{cnf}(\text{not\_p3}_7, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_{15}(c_{22}), c_{21}), f_{15}(c_{22})) \quad \text{cnf}(p_{3_8, \text{negated\_conjecture})}$   
 $(p_{16}(x_1) \text{ and } p_5(x_1, x_0)) \Rightarrow p_{16}(x_0) \quad \text{cnf}(p_{16_9, \text{negated\_conjecture})}$   
 $p_5(x_{48}, x_{49}) \Rightarrow p_5(f_8(x_{48}), f_8(x_{49})) \quad \text{cnf}(p_{5_{10}, \text{negated\_conjecture})}$   
 $p_5(x_{14}, x_{15}) \Rightarrow p_2(f_6(x_{14}), f_6(x_{15})) \quad \text{cnf}(p_{2_{11}, \text{negated\_conjecture})}$   
 $p_3(x_{16}, x_{17}) \Rightarrow p_2(f_9(x_{16}), f_9(x_{17})) \quad \text{cnf}(p_{2_{12}, \text{negated\_conjecture})}$   
 $p_5(x_{33}, x_{34}) \Rightarrow p_3(f_{13}(x_{33}), f_{13}(x_{34})) \quad \text{cnf}(p_{3_{13}, \text{negated\_conjecture})}$   
 $p_3(x_{39}, x_{40}) \Rightarrow p_3(f_{15}(x_{39}), f_{15}(x_{40})) \quad \text{cnf}(p_{3_{14}, \text{negated\_conjecture})}$   
 $p_2(x_{41}, x_{42}) \Rightarrow p_3(f_4(x_{41}), f_4(x_{42})) \quad \text{cnf}(p_{3_{15}, \text{negated\_conjecture})}$   
 $p_5(x_{46}, x_{47}) \Rightarrow p_5(f_7(x_{46}), f_7(x_{47})) \quad \text{cnf}(p_{5_{16}, \text{negated\_conjecture})}$   
 $(p_2(x_{11}, x_{12}) \text{ and } p_2(x_{11}, x_{13})) \Rightarrow p_2(x_{12}, x_{13}) \quad \text{cnf}(p_{2_{17}, \text{negated\_conjecture})}$   
 $(p_5(x_{43}, x_{44}) \text{ and } p_5(x_{43}, x_{45})) \Rightarrow p_5(x_{44}, x_{45}) \quad \text{cnf}(p_{5_{18}, \text{negated\_conjecture})}$   
 $(p_3(x_{18}, x_{19}) \text{ and } p_3(x_{18}, x_{20})) \Rightarrow p_3(x_{19}, x_{20}) \quad \text{cnf}(p_{3_{19}, \text{negated\_conjecture})}$   
 $(p_2(x_4, x_2) \text{ and } p_2(x_5, x_3) \text{ and } p_{17}(x_4, x_5)) \Rightarrow p_{17}(x_2, x_3) \quad \text{cnf}(p_{17_{20}, \text{negated\_conjecture})}$   
 $(p_5(x_9, x_7) \text{ and } p_5(x_{10}, x_8) \text{ and } p_{18}(x_9, x_{10})) \Rightarrow p_{18}(x_7, x_8) \quad \text{cnf}(p_{18_{21}, \text{negated\_conjecture})}$   
 $p_3(f_{12}(f_4(f_6(f_7(f_8(c_{20}))))), c_{21}), f_4(f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(p_{3_{22}, \text{negated\_conjecture})}$   
 $(p_3(x_{35}, x_{37}) \text{ and } p_3(x_{36}, x_{38})) \Rightarrow p_3(f_{14}(x_{35}, x_{36}), f_{14}(x_{37}, x_{38})) \quad \text{cnf}(p_{3_{23}, \text{negated\_conjecture})}$   
 $(p_3(x_{21}, x_{23}) \text{ and } p_3(x_{22}, x_{24})) \Rightarrow p_3(f_{10}(x_{21}, x_{22}), f_{10}(x_{23}, x_{24})) \quad \text{cnf}(p_{3_{24}, \text{negated\_conjecture})}$   
 $(p_3(x_{25}, x_{27}) \text{ and } p_3(x_{26}, x_{28})) \Rightarrow p_3(f_{11}(x_{25}, x_{26}), f_{11}(x_{27}, x_{28})) \quad \text{cnf}(p_{3_{25}, \text{negated\_conjecture})}$   
 $(p_3(x_{29}, x_{31}) \text{ and } p_5(x_{30}, x_{32})) \Rightarrow p_3(f_{12}(x_{29}, x_{30}), f_{12}(x_{31}, x_{32})) \quad \text{cnf}(p_{3_{26}, \text{negated\_conjecture})}$   
 $p_3(f_{12}(f_{15}(f_4(f_6(f_7(f_8(c_{20}))))), c_{21}), f_{15}(f_4(f_6(f_7(f_8(c_{20})))))) \quad \text{cnf}(p_{3_{27}, \text{negated\_conjecture})}$   
 $\neg p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), f_{12}(x_{50}, c_{21})), f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(\text{not\_p17}_{28}, \text{negated\_conjecture})$   
 $p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), f_{15}(f_4(f_6(f_7(f_8(c_{20}))))), f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(p_{17_{29}, \text{negated\_conjecture})}$   
 $p_{18}(x_6, c_{21}) \Rightarrow (p_5(x_6, f_7(c_{20})) \text{ or } p_3(c_{19}, f_4(f_6(f_7(c_{20})))) \text{ or } p_{17}(f_9(f_{10}(f_4(f_6(f_7(f_8(c_{20}))))), f_{11}(c_{19}, f_{12}(f_{13}(x_6), x_6))))), f_6(f_7(c_{20})))$

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$\neg p_{16}(c_{21}) \quad \text{cnf}(c_{21\_is\_not\_p16_1, \text{negated\_conjecture})}$   
 $p_2(x_{11}, x_{11}) \quad \text{cnf}(p_{2_2, \text{negated\_conjecture})}$   
 $p_5(x_{43}, x_{43}) \quad \text{cnf}(p_{5_3, \text{negated\_conjecture})}$   
 $p_3(x_{18}, x_{18}) \quad \text{cnf}(p_{3_4, \text{negated\_conjecture})}$   
 $\neg p_5(c_{21}, f_7(c_{20})) \quad \text{cnf}(\text{not\_p5}_5, \text{negated\_conjecture})$   
 $p_3(f_{12}(c_{22}, c_{21}), f_{15}(c_{22})) \quad \text{cnf}(p_{3_6, \text{negated\_conjecture})}$   
 $p_3(f_{12}(f_{15}(c_{22}), c_{21}), c_{22}) \quad \text{cnf}(p_{3_7, \text{negated\_conjecture})}$   
 $\neg p_3(c_{19}, f_4(f_6(f_7(c_{20})))) \quad \text{cnf}(\text{not\_p3}_8, \text{negated\_conjecture})$   
 $(p_{16}(x_1) \text{ and } p_5(x_1, x_0)) \Rightarrow p_{16}(x_0) \quad \text{cnf}(p_{16_9, \text{negated\_conjecture})}$   
 $p_5(x_{48}, x_{49}) \Rightarrow p_5(f_8(x_{48}), f_8(x_{49})) \quad \text{cnf}(p_{5_{10}, \text{negated\_conjecture})}$   
 $p_5(x_{14}, x_{15}) \Rightarrow p_2(f_6(x_{14}), f_6(x_{15})) \quad \text{cnf}(p_{2_{11}, \text{negated\_conjecture})}$   
 $p_3(x_{16}, x_{17}) \Rightarrow p_2(f_9(x_{16}), f_9(x_{17})) \quad \text{cnf}(p_{2_{12}, \text{negated\_conjecture})}$   
 $p_5(x_{33}, x_{34}) \Rightarrow p_3(f_{13}(x_{33}), f_{13}(x_{34})) \quad \text{cnf}(p_{3_{13}, \text{negated\_conjecture})}$   
 $p_3(x_{39}, x_{40}) \Rightarrow p_3(f_{15}(x_{39}), f_{15}(x_{40})) \quad \text{cnf}(p_{3_{14}, \text{negated\_conjecture})}$   
 $p_2(x_{41}, x_{42}) \Rightarrow p_3(f_4(x_{41}), f_4(x_{42})) \quad \text{cnf}(p_{3_{15}, \text{negated\_conjecture})}$   
 $p_5(x_{46}, x_{47}) \Rightarrow p_5(f_7(x_{46}), f_7(x_{47})) \quad \text{cnf}(p_{5_{16}, \text{negated\_conjecture})}$   
 $(p_2(x_{11}, x_{12}) \text{ and } p_2(x_{11}, x_{13})) \Rightarrow p_2(x_{12}, x_{13}) \quad \text{cnf}(p_{2_{17}, \text{negated\_conjecture})}$   
 $(p_5(x_{43}, x_{44}) \text{ and } p_5(x_{43}, x_{45})) \Rightarrow p_5(x_{44}, x_{45}) \quad \text{cnf}(p_{5_{18}, \text{negated\_conjecture})}$   
 $(p_3(x_{18}, x_{19}) \text{ and } p_3(x_{18}, x_{20})) \Rightarrow p_3(x_{19}, x_{20}) \quad \text{cnf}(p_{3_{19}, \text{negated\_conjecture})}$   
 $(p_2(x_4, x_2) \text{ and } p_2(x_5, x_3) \text{ and } p_{17}(x_4, x_5)) \Rightarrow p_{17}(x_2, x_3) \quad \text{cnf}(p_{17_{20}, \text{negated\_conjecture})}$   
 $(p_5(x_9, x_7) \text{ and } p_5(x_{10}, x_8) \text{ and } p_{18}(x_9, x_{10})) \Rightarrow p_{18}(x_7, x_8) \quad \text{cnf}(p_{18_{21}, \text{negated\_conjecture})}$   
 $p_3(f_{12}(f_4(f_6(f_7(f_8(c_{20}))))), c_{21}), f_4(f_6(f_7(f_8(c_{20})))) \quad \text{cnf}(p_{3_{22}, \text{negated\_conjecture})}$   
 $(p_3(x_{35}, x_{37}) \text{ and } p_3(x_{36}, x_{38})) \Rightarrow p_3(f_{14}(x_{35}, x_{36}), f_{14}(x_{37}, x_{38})) \quad \text{cnf}(p_{3_{23}, \text{negated\_conjecture})}$   
 $(p_3(x_{21}, x_{23}) \text{ and } p_3(x_{22}, x_{24})) \Rightarrow p_3(f_{10}(x_{21}, x_{22}), f_{10}(x_{23}, x_{24})) \quad \text{cnf}(p_{3_{24}, \text{negated\_conjecture})}$   
 $(p_3(x_{25}, x_{27}) \text{ and } p_3(x_{26}, x_{28})) \Rightarrow p_3(f_{11}(x_{25}, x_{26}), f_{11}(x_{27}, x_{28})) \quad \text{cnf}(p_{3_{25}, \text{negated\_conjecture})}$   
 $(p_3(x_{29}, x_{31}) \text{ and } p_5(x_{30}, x_{32})) \Rightarrow p_3(f_{12}(x_{29}, x_{30}), f_{12}(x_{31}, x_{32})) \quad \text{cnf}(p_{3_{26}, \text{negated\_conjecture})}$   
 $p_3(f_{12}(f_{15}(f_4(f_6(f_7(f_8(c_{20}))))), c_{21}), f_{15}(f_4(f_6(f_7(f_8(c_{20})))))) \quad \text{cnf}(p_{3_{27}, \text{negated\_conjecture})}$

$\neg p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), f_{12}(x_{50}, c_{21}))), f_6(f_7(f_8(c_{20}))))$      $\text{cnf}(\text{not\_p17}_{28}, \text{negated\_conjecture})$   
 $p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), f_{15}(f_4(f_6(f_7(f_8(c_{20})))))), f_6(f_7(f_8(c_{20}))))$      $\text{cnf}(\text{p17}_{29}, \text{negated\_conjecture})$   
 $p_{18}(x_6, c_{21}) \Rightarrow (p_5(x_6, f_7(c_{20})) \text{ or } p_3(c_{19}, f_4(f_6(f_7(c_{20})))) \text{ or } p_{17}(f_9(f_{10}(f_4(f_6(f_7(f_8(c_{20}))))), f_{11}(c_{19}, f_{12}(f_{13}(x_6), x_6))), f_6(f_7($

### SYN611-1.p Harrison problem 3831

$\neg p_{16}(c_{21})$      $\text{cnf}(\text{c21\_is\_not\_p16}_1, \text{negated\_conjecture})$   
 $p_2(x_{11}, x_{11})$      $\text{cnf}(\text{p2}_2, \text{negated\_conjecture})$   
 $p_5(x_{43}, x_{43})$      $\text{cnf}(\text{p5}_3, \text{negated\_conjecture})$   
 $p_3(x_{18}, x_{18})$      $\text{cnf}(\text{p3}_4, \text{negated\_conjecture})$   
 $\neg p_5(c_{21}, f_7(c_{20}))$      $\text{cnf}(\text{not\_p5}_5, \text{negated\_conjecture})$   
 $p_3(f_{12}(c_{22}, c_{21}), c_{22})$      $\text{cnf}(\text{p3}_6, \text{negated\_conjecture})$   
 $\neg p_3(c_{19}, f_4(f_6(f_7(c_{20}))))$      $\text{cnf}(\text{not\_p3}_7, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_{15}(c_{22}), c_{21}), f_{15}(c_{22}))$      $\text{cnf}(\text{p3}_8, \text{negated\_conjecture})$   
 $(p_{16}(x_1) \text{ and } p_5(x_1, x_0)) \Rightarrow p_{16}(x_0)$      $\text{cnf}(\text{p16}_9, \text{negated\_conjecture})$   
 $p_5(x_{48}, x_{49}) \Rightarrow p_5(f_8(x_{48}), f_8(x_{49}))$      $\text{cnf}(\text{p5}_{10}, \text{negated\_conjecture})$   
 $p_5(x_{14}, x_{15}) \Rightarrow p_2(f_6(x_{14}), f_6(x_{15}))$      $\text{cnf}(\text{p2}_{11}, \text{negated\_conjecture})$   
 $p_3(x_{16}, x_{17}) \Rightarrow p_2(f_9(x_{16}), f_9(x_{17}))$      $\text{cnf}(\text{p2}_{12}, \text{negated\_conjecture})$   
 $p_5(x_{33}, x_{34}) \Rightarrow p_3(f_{13}(x_{33}), f_{13}(x_{34}))$      $\text{cnf}(\text{p3}_{13}, \text{negated\_conjecture})$   
 $p_3(x_{39}, x_{40}) \Rightarrow p_3(f_{15}(x_{39}), f_{15}(x_{40}))$      $\text{cnf}(\text{p3}_{14}, \text{negated\_conjecture})$   
 $p_2(x_{41}, x_{42}) \Rightarrow p_3(f_4(x_{41}), f_4(x_{42}))$      $\text{cnf}(\text{p3}_{15}, \text{negated\_conjecture})$   
 $p_5(x_{46}, x_{47}) \Rightarrow p_5(f_7(x_{46}), f_7(x_{47}))$      $\text{cnf}(\text{p5}_{16}, \text{negated\_conjecture})$   
 $(p_2(x_{11}, x_{12}) \text{ and } p_2(x_{11}, x_{13})) \Rightarrow p_2(x_{12}, x_{13})$      $\text{cnf}(\text{p2}_{17}, \text{negated\_conjecture})$   
 $(p_5(x_{43}, x_{44}) \text{ and } p_5(x_{43}, x_{45})) \Rightarrow p_5(x_{44}, x_{45})$      $\text{cnf}(\text{p5}_{18}, \text{negated\_conjecture})$   
 $(p_3(x_{18}, x_{19}) \text{ and } p_3(x_{18}, x_{20})) \Rightarrow p_3(x_{19}, x_{20})$      $\text{cnf}(\text{p3}_{19}, \text{negated\_conjecture})$   
 $(p_2(x_4, x_2) \text{ and } p_2(x_5, x_3) \text{ and } p_{17}(x_4, x_5)) \Rightarrow p_{17}(x_2, x_3)$      $\text{cnf}(\text{p17}_{20}, \text{negated\_conjecture})$   
 $(p_5(x_9, x_7) \text{ and } p_5(x_{10}, x_8) \text{ and } p_{18}(x_9, x_{10})) \Rightarrow p_{18}(x_7, x_8)$      $\text{cnf}(\text{p18}_{21}, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_4(f_6(f_7(f_8(c_{20}))))), c_{21}), f_4(f_6(f_7(f_8(c_{20}))))$      $\text{cnf}(\text{p3}_{22}, \text{negated\_conjecture})$   
 $(p_3(x_{35}, x_{37}) \text{ and } p_3(x_{36}, x_{38})) \Rightarrow p_3(f_{14}(x_{35}, x_{36}), f_{14}(x_{37}, x_{38}))$      $\text{cnf}(\text{p3}_{23}, \text{negated\_conjecture})$   
 $(p_3(x_{21}, x_{23}) \text{ and } p_3(x_{22}, x_{24})) \Rightarrow p_3(f_{10}(x_{21}, x_{22}), f_{10}(x_{23}, x_{24}))$      $\text{cnf}(\text{p3}_{24}, \text{negated\_conjecture})$   
 $(p_3(x_{25}, x_{27}) \text{ and } p_3(x_{26}, x_{28})) \Rightarrow p_3(f_{11}(x_{25}, x_{26}), f_{11}(x_{27}, x_{28}))$      $\text{cnf}(\text{p3}_{25}, \text{negated\_conjecture})$   
 $(p_3(x_{29}, x_{31}) \text{ and } p_5(x_{30}, x_{32})) \Rightarrow p_3(f_{12}(x_{29}, x_{30}), f_{12}(x_{31}, x_{32}))$      $\text{cnf}(\text{p3}_{26}, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_{15}(f_4(f_6(f_7(f_8(c_{20}))))), c_{21}), f_{15}(f_4(f_6(f_7(f_8(c_{20}))))))$      $\text{cnf}(\text{p3}_{27}, \text{negated\_conjecture})$   
 $\neg p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), f_{12}(x_{50}, c_{21}))), f_6(f_7(f_8(c_{20}))))$      $\text{cnf}(\text{not\_p17}_{28}, \text{negated\_conjecture})$   
 $p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), f_4(f_6(f_7(f_8(c_{20}))))), f_6(f_7(f_8(c_{20}))))$      $\text{cnf}(\text{p17}_{29}, \text{negated\_conjecture})$   
 $p_{18}(x_6, c_{21}) \Rightarrow (p_5(x_6, f_7(c_{20})) \text{ or } p_3(c_{19}, f_4(f_6(f_7(c_{20})))) \text{ or } p_{17}(f_9(f_{10}(f_4(f_6(f_7(f_8(c_{20}))))), f_{11}(c_{19}, f_{12}(f_{13}(x_6), x_6))), f_6(f_7($

### SYN612-1.p Harrison problem 3832

$\neg p_{16}(c_{21})$      $\text{cnf}(\text{c21\_is\_not\_p16}_1, \text{negated\_conjecture})$   
 $p_2(x_{11}, x_{11})$      $\text{cnf}(\text{p2}_2, \text{negated\_conjecture})$   
 $p_5(x_{43}, x_{43})$      $\text{cnf}(\text{p5}_3, \text{negated\_conjecture})$   
 $p_3(x_{18}, x_{18})$      $\text{cnf}(\text{p3}_4, \text{negated\_conjecture})$   
 $\neg p_5(c_{21}, f_7(c_{20}))$      $\text{cnf}(\text{not\_p5}_5, \text{negated\_conjecture})$   
 $p_3(f_{12}(c_{22}, c_{21}), f_{15}(c_{22}))$      $\text{cnf}(\text{p3}_6, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_{15}(c_{22}), c_{21}), c_{22})$      $\text{cnf}(\text{p3}_7, \text{negated\_conjecture})$   
 $\neg p_3(c_{19}, f_4(f_6(f_7(c_{20}))))$      $\text{cnf}(\text{not\_p3}_8, \text{negated\_conjecture})$   
 $(p_{16}(x_1) \text{ and } p_5(x_1, x_0)) \Rightarrow p_{16}(x_0)$      $\text{cnf}(\text{p16}_9, \text{negated\_conjecture})$   
 $p_5(x_{48}, x_{49}) \Rightarrow p_5(f_8(x_{48}), f_8(x_{49}))$      $\text{cnf}(\text{p5}_{10}, \text{negated\_conjecture})$   
 $p_5(x_{14}, x_{15}) \Rightarrow p_2(f_6(x_{14}), f_6(x_{15}))$      $\text{cnf}(\text{p2}_{11}, \text{negated\_conjecture})$   
 $p_3(x_{16}, x_{17}) \Rightarrow p_2(f_9(x_{16}), f_9(x_{17}))$      $\text{cnf}(\text{p2}_{12}, \text{negated\_conjecture})$   
 $p_5(x_{33}, x_{34}) \Rightarrow p_3(f_{13}(x_{33}), f_{13}(x_{34}))$      $\text{cnf}(\text{p3}_{13}, \text{negated\_conjecture})$   
 $p_3(x_{39}, x_{40}) \Rightarrow p_3(f_{15}(x_{39}), f_{15}(x_{40}))$      $\text{cnf}(\text{p3}_{14}, \text{negated\_conjecture})$   
 $p_2(x_{41}, x_{42}) \Rightarrow p_3(f_4(x_{41}), f_4(x_{42}))$      $\text{cnf}(\text{p3}_{15}, \text{negated\_conjecture})$   
 $p_5(x_{46}, x_{47}) \Rightarrow p_5(f_7(x_{46}), f_7(x_{47}))$      $\text{cnf}(\text{p5}_{16}, \text{negated\_conjecture})$   
 $(p_2(x_{11}, x_{12}) \text{ and } p_2(x_{11}, x_{13})) \Rightarrow p_2(x_{12}, x_{13})$      $\text{cnf}(\text{p2}_{17}, \text{negated\_conjecture})$   
 $(p_5(x_{43}, x_{44}) \text{ and } p_5(x_{43}, x_{45})) \Rightarrow p_5(x_{44}, x_{45})$      $\text{cnf}(\text{p5}_{18}, \text{negated\_conjecture})$   
 $(p_3(x_{18}, x_{19}) \text{ and } p_3(x_{18}, x_{20})) \Rightarrow p_3(x_{19}, x_{20})$      $\text{cnf}(\text{p3}_{19}, \text{negated\_conjecture})$   
 $(p_2(x_4, x_2) \text{ and } p_2(x_5, x_3) \text{ and } p_{17}(x_4, x_5)) \Rightarrow p_{17}(x_2, x_3)$      $\text{cnf}(\text{p17}_{20}, \text{negated\_conjecture})$   
 $(p_5(x_9, x_7) \text{ and } p_5(x_{10}, x_8) \text{ and } p_{18}(x_9, x_{10})) \Rightarrow p_{18}(x_7, x_8)$      $\text{cnf}(\text{p18}_{21}, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_4(f_6(f_7(f_8(c_{20}))))), c_{21}), f_4(f_6(f_7(f_8(c_{20}))))$      $\text{cnf}(\text{p3}_{22}, \text{negated\_conjecture})$   
 $(p_3(x_{35}, x_{37}) \text{ and } p_3(x_{36}, x_{38})) \Rightarrow p_3(f_{14}(x_{35}, x_{36}), f_{14}(x_{37}, x_{38}))$      $\text{cnf}(\text{p3}_{23}, \text{negated\_conjecture})$



$(p_3(x_{21}, x_{23}) \text{ and } p_3(x_{22}, x_{24})) \Rightarrow p_3(f_{10}(x_{21}, x_{22}), f_{10}(x_{23}, x_{24}))$      $\text{cnf}(p_{3_{24}}, \text{negated\_conjecture})$   
 $(p_3(x_{25}, x_{27}) \text{ and } p_3(x_{26}, x_{28})) \Rightarrow p_3(f_{11}(x_{25}, x_{26}), f_{11}(x_{27}, x_{28}))$      $\text{cnf}(p_{3_{25}}, \text{negated\_conjecture})$   
 $(p_3(x_{29}, x_{31}) \text{ and } p_5(x_{30}, x_{32})) \Rightarrow p_3(f_{12}(x_{29}, x_{30}), f_{12}(x_{31}, x_{32}))$      $\text{cnf}(p_{3_{26}}, \text{negated\_conjecture})$   
 $p_3(f_{12}(f_{15}(f_4(f_6(f_7(f_8(c_{20})))))), c_{21}), f_{15}(f_4(f_6(f_7(f_8(c_{20}))))))$      $\text{cnf}(p_{3_{27}}, \text{negated\_conjecture})$   
 $\neg p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), f_{12}(x_{50}, c_{21}))), f_6(f_7(f_8(c_{20}))))$      $\text{cnf}(\text{not\_}p_{17_{28}}, \text{negated\_conjecture})$   
 $p_{17}(f_9(f_{10}(f_{14}(f_4(f_9(c_{19}))), c_{19}), f_4(f_6(f_7(f_8(c_{20})))))), f_6(f_7(f_8(c_{20}))))$      $\text{cnf}(p_{17_{29}}, \text{negated\_conjecture})$   
 $p_{18}(x_6, c_{21}) \Rightarrow (p_5(x_6, f_7(c_{20})) \text{ or } p_3(c_{19}, f_4(f_6(f_7(c_{20})))) \text{ or } p_{17}(f_9(f_{10}(f_4(f_6(f_7(f_8(c_{20}))))), f_{11}(c_{19}, f_{12}(f_{13}(x_6), x_6))), f_6(f_7($

### SYN613-1.p Harrison problem 3862

$p_{11}(x_0, x_0)$      $\text{cnf}(p_{11_1}, \text{negated\_conjecture})$   
 $p_6(x_{48}, x_{48})$      $\text{cnf}(p_{6_2}, \text{negated\_conjecture})$   
 $p_5(x_{41}, x_{41})$      $\text{cnf}(p_{5_3}, \text{negated\_conjecture})$   
 $p_3(x_{36}, x_{36})$      $\text{cnf}(p_{3_4}, \text{negated\_conjecture})$   
 $p_2(x_{29}, x_{29})$      $\text{cnf}(p_{2_5}, \text{negated\_conjecture})$   
 $p_{16}(x_{14}, x_{14})$      $\text{cnf}(p_{16_6}, \text{negated\_conjecture})$   
 $p_{11}(c_{23}, f_{12}(f_9(c_{21})))$      $\text{cnf}(p_{11_7}, \text{negated\_conjecture})$   
 $p_{11}(c_{24}, f_{12}(f_9(c_{21})))$      $\text{cnf}(p_{11_8}, \text{negated\_conjecture})$   
 $p_5(x_{46}, x_{47}) \Rightarrow p_5(f_9(x_{46}), f_9(x_{47}))$      $\text{cnf}(p_{5_9}, \text{negated\_conjecture})$   
 $p_5(x_3, x_4) \Rightarrow p_{11}(f_{12}(x_3), f_{12}(x_4))$      $\text{cnf}(p_{11_{10}}, \text{negated\_conjecture})$   
 $p_{11}(x_5, x_6) \Rightarrow p_{11}(f_{13}(x_5), f_{13}(x_6))$      $\text{cnf}(p_{11_{11}}, \text{negated\_conjecture})$   
 $p_{11}(x_{11}, x_{12}) \Rightarrow p_{11}(f_{15}(x_{11}), f_{15}(x_{12}))$      $\text{cnf}(p_{11_{12}}, \text{negated\_conjecture})$   
 $p_2(x_{39}, x_{40}) \Rightarrow p_3(f_4(x_{39}), f_4(x_{40}))$      $\text{cnf}(p_{3_{13}}, \text{negated\_conjecture})$   
 $p_2(x_{44}, x_{45}) \Rightarrow p_5(f_{10}(x_{44}), f_{10}(x_{45}))$      $\text{cnf}(p_{5_{14}}, \text{negated\_conjecture})$   
 $(p_{11}(x_0, x_1) \text{ and } p_{11}(x_0, x_2)) \Rightarrow p_{11}(x_1, x_2)$      $\text{cnf}(p_{11_{15}}, \text{negated\_conjecture})$   
 $(p_6(x_{48}, x_{49}) \text{ and } p_6(x_{48}, x_{50})) \Rightarrow p_6(x_{49}, x_{50})$      $\text{cnf}(p_{6_{16}}, \text{negated\_conjecture})$   
 $(p_5(x_{41}, x_{42}) \text{ and } p_5(x_{41}, x_{43})) \Rightarrow p_5(x_{42}, x_{43})$      $\text{cnf}(p_{5_{17}}, \text{negated\_conjecture})$   
 $(p_3(x_{36}, x_{37}) \text{ and } p_3(x_{36}, x_{38})) \Rightarrow p_3(x_{37}, x_{38})$      $\text{cnf}(p_{3_{18}}, \text{negated\_conjecture})$   
 $(p_2(x_{29}, x_{30}) \text{ and } p_2(x_{29}, x_{31})) \Rightarrow p_2(x_{30}, x_{31})$      $\text{cnf}(p_{2_{19}}, \text{negated\_conjecture})$   
 $(p_{16}(x_{14}, x_{15}) \text{ and } p_{16}(x_{14}, x_{16})) \Rightarrow p_{16}(x_{15}, x_{16})$      $\text{cnf}(p_{16_{20}}, \text{negated\_conjecture})$   
 $p_{17}(c_{19}, f_4(f_7(f_{10}(c_{20}), f_8(f_9(c_{21}), c_{22}))), c_{24})$      $\text{cnf}(p_{17_{21}}, \text{negated\_conjecture})$   
 $\neg p_{17}(c_{19}, f_4(f_7(f_{10}(c_{20}), f_8(f_9(c_{21}), c_{22}))), c_{23})$      $\text{cnf}(\text{not\_}p_{17_{22}}, \text{negated\_conjecture})$   
 $(p_{11}(x_{26}, x_{24}) \text{ and } p_{18}(x_{25}, x_{26}) \text{ and } p_{11}(x_{25}, x_{23})) \Rightarrow p_{18}(x_{23}, x_{24})$      $\text{cnf}(p_{18_{23}}, \text{negated\_conjecture})$   
 $(p_{11}(x_7, x_9) \text{ and } p_{11}(x_8, x_{10})) \Rightarrow p_{11}(f_{14}(x_7, x_8), f_{14}(x_9, x_{10}))$      $\text{cnf}(p_{11_{24}}, \text{negated\_conjecture})$   
 $(p_5(x_{51}, x_{53}) \text{ and } p_5(x_{52}, x_{54})) \Rightarrow p_6(f_8(x_{51}, x_{52}), f_8(x_{53}, x_{54}))$      $\text{cnf}(p_{6_{25}}, \text{negated\_conjecture})$   
 $(p_5(x_{32}, x_{34}) \text{ and } p_6(x_{33}, x_{35})) \Rightarrow p_2(f_7(x_{32}, x_{33}), f_7(x_{34}, x_{35}))$      $\text{cnf}(p_{2_{26}}, \text{negated\_conjecture})$   
 $p_{11}(x_{28}, f_{12}(f_9(c_{21}))) \Rightarrow p_{18}(f_{13}(f_{14}(x_{28}, c_{25})), f_{13}(f_{14}(c_{23}, c_{25})))$      $\text{cnf}(p_{18_{27}}, \text{negated\_conjecture})$   
 $p_{11}(x_{27}, f_{12}(f_9(c_{21}))) \Rightarrow p_{18}(f_{13}(f_{14}(x_{27}, c_{25})), f_{13}(f_{14}(c_{24}, c_{25})))$      $\text{cnf}(p_{18_{28}}, \text{negated\_conjecture})$   
 $(p_3(x_{22}, x_{18}) \text{ and } p_{16}(x_{21}, x_{17}) \text{ and } p_{11}(x_{20}, x_{19}) \text{ and } p_{17}(x_{21}, x_{22}, x_{20})) \Rightarrow p_{17}(x_{17}, x_{18}, x_{19})$      $\text{cnf}(p_{17_{29}}, \text{negated\_conjecture})$   
 $(p_{11}(x_{13}, f_{12}(f_9(c_{21}))) \text{ and } p_{17}(c_{19}, f_4(c_{20}), x_{13})) \Rightarrow (p_{17}(c_{19}, f_4(c_{20}), c_{23}) \text{ or } p_{11}(f_{15}(x_{13}), f_{12}(f_9(c_{21}))))$      $\text{cnf}(p_{17_{30}}, \text{negated\_conjecture})$   
 $(p_{11}(x_{13}, f_{12}(f_9(c_{21}))) \text{ and } p_{17}(c_{19}, f_4(c_{20}), x_{13}) \text{ and } p_{18}(f_{13}(f_{14}(f_{15}(x_{13}), c_{25})), f_{13}(f_{14}(x_{13}, c_{25})))) \Rightarrow p_{17}(c_{19}, f_4(c_{20}), c_{23})$

### SYN614-1.p Harrison problem 3878

$p_{13}(x_0, x_0)$      $\text{cnf}(p_{13_1}, \text{negated\_conjecture})$   
 $p_7(x_{43}, x_{43})$      $\text{cnf}(p_{7_2}, \text{negated\_conjecture})$   
 $p_2(x_{18}, x_{18})$      $\text{cnf}(p_{2_3}, \text{negated\_conjecture})$   
 $p_{15}(x_7, x_7)$      $\text{cnf}(p_{15_4}, \text{negated\_conjecture})$   
 $\neg p_2(c_{21}, f_3(c_{22}))$      $\text{cnf}(\text{not\_}p_{2_5}, \text{negated\_conjecture})$   
 $p_{19}(c_{23}, f_3(f_4(f_5(c_{22}))))$      $\text{cnf}(p_{19_6}, \text{negated\_conjecture})$   
 $p_{20}(c_{24}, f_6(f_3(f_4(f_5(c_{22}))), c_{21}))$      $\text{cnf}(p_{20_7}, \text{negated\_conjecture})$   
 $p_7(x_{52}, x_{53}) \Rightarrow p_7(f_{12}(x_{52}), f_{12}(x_{53}))$      $\text{cnf}(p_{7_8}, \text{negated\_conjecture})$   
 $p_2(x_{29}, x_{30}) \Rightarrow p_2(f_3(x_{29}), f_3(x_{30}))$      $\text{cnf}(p_{2_9}, \text{negated\_conjecture})$   
 $p_2(x_{31}, x_{32}) \Rightarrow p_2(f_4(x_{31}), f_4(x_{32}))$      $\text{cnf}(p_{2_{10}}, \text{negated\_conjecture})$   
 $p_2(x_{33}, x_{34}) \Rightarrow p_2(f_5(x_{33}), f_5(x_{34}))$      $\text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $p_2(x_{50}, x_{51}) \Rightarrow p_7(f_{11}(x_{50}), f_{11}(x_{51}))$      $\text{cnf}(p_{7_{12}}, \text{negated\_conjecture})$   
 $p_2(c_{26}, f_{14}(f_{16}(c_{28}, f_{17}(c_{21}, c_{27})), c_{25}))$      $\text{cnf}(p_{2_{13}}, \text{negated\_conjecture})$   
 $(p_{13}(x_0, x_1) \text{ and } p_{13}(x_0, x_2)) \Rightarrow p_{13}(x_1, x_2)$      $\text{cnf}(p_{13_{14}}, \text{negated\_conjecture})$   
 $(p_7(x_{43}, x_{44}) \text{ and } p_7(x_{43}, x_{45})) \Rightarrow p_7(x_{44}, x_{45})$      $\text{cnf}(p_{7_{15}}, \text{negated\_conjecture})$   
 $(p_2(x_{18}, x_{19}) \text{ and } p_2(x_{18}, x_{20})) \Rightarrow p_2(x_{19}, x_{20})$      $\text{cnf}(p_{2_{16}}, \text{negated\_conjecture})$   
 $(p_{15}(x_7, x_8) \text{ and } p_{15}(x_7, x_9)) \Rightarrow p_{15}(x_8, x_9)$      $\text{cnf}(p_{15_{17}}, \text{negated\_conjecture})$   
 $p_{19}(f_6(f_3(f_4(f_5(c_{22}))), f_{18}(c_{21}, f_3(f_5(c_{22}))))), c_{24})$      $\text{cnf}(p_{19_{18}}, \text{negated\_conjecture})$

$(p_2(x_{42}, x_{40}) \text{ and } p_{20}(x_{41}, x_{42}) \text{ and } p_2(x_{41}, x_{39})) \Rightarrow p_{20}(x_{39}, x_{40})$     cnf(p20<sub>19</sub>, negated\_conjecture)  
 $(p_2(x_{16}, x_{14}) \text{ and } p_2(x_{17}, x_{15}) \text{ and } p_{19}(x_{16}, x_{17})) \Rightarrow p_{19}(x_{14}, x_{15})$     cnf(p19<sub>20</sub>, negated\_conjecture)  
 $(p_{15}(x_4, x_6) \text{ and } p_2(x_3, x_5)) \Rightarrow p_{13}(f_{16}(x_3, x_4), f_{16}(x_5, x_6))$     cnf(p13<sub>21</sub>, negated\_conjecture)  
 $(p_7(x_{58}, x_{60}) \text{ and } p_7(x_{59}, x_{61})) \Rightarrow p_7(f_9(x_{58}, x_{59}), f_9(x_{60}, x_{61}))$     cnf(p7<sub>22</sub>, negated\_conjecture)  
 $(p_7(x_{54}, x_{56}) \text{ and } p_7(x_{55}, x_{57})) \Rightarrow p_7(f_8(x_{54}, x_{55}), f_8(x_{56}, x_{57}))$     cnf(p7<sub>23</sub>, negated\_conjecture)  
 $(p_2(x_{47}, x_{49}) \text{ and } p_7(x_{46}, x_{48})) \Rightarrow p_7(f_{10}(x_{46}, x_{47}), f_{10}(x_{48}, x_{49}))$     cnf(p7<sub>24</sub>, negated\_conjecture)  
 $(p_2(x_{35}, x_{37}) \text{ and } p_2(x_{36}, x_{38})) \Rightarrow p_2(f_6(x_{35}, x_{36}), f_6(x_{37}, x_{38}))$     cnf(p2<sub>25</sub>, negated\_conjecture)  
 $(p_2(x_{25}, x_{27}) \text{ and } p_2(x_{26}, x_{28})) \Rightarrow p_2(f_{18}(x_{25}, x_{26}), f_{18}(x_{27}, x_{28}))$     cnf(p2<sub>26</sub>, negated\_conjecture)  
 $(p_{13}(x_{21}, x_{23}) \text{ and } p_7(x_{22}, x_{24})) \Rightarrow p_2(f_{14}(x_{21}, x_{22}), f_{14}(x_{23}, x_{24}))$     cnf(p2<sub>27</sub>, negated\_conjecture)  
 $(p_2(x_{10}, x_{12}) \text{ and } p_2(x_{11}, x_{13})) \Rightarrow p_{15}(f_{17}(x_{10}, x_{11}), f_{17}(x_{12}, x_{13}))$     cnf(p15<sub>28</sub>, negated\_conjecture)  
 $p_7(c_{25}, f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{22}))))), c_{23}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{22}))))), c_{26}), f_9(f_{11}(c_{24}), f_{10}(f_{11}(f_3(f_4(f_5(c_{22}))))), c_{27}))))))$     cnf  
 $(p_{19}(x_{62}, f_3(f_4(f_5(c_{22})))) \text{ and } p_{20}(x_{63}, f_6(f_3(f_4(f_5(c_{22}))))), c_{21}) \text{ and } p_2(f_{14}(f_{16}(c_{28}, f_{17}(c_{21}, c_{27})), c_{25}), f_3(c_{22}))) \Rightarrow \neg p_7(c_{25}, f_8$   
 $(p_{19}(x_{62}, f_3(f_4(f_5(c_{22})))) \text{ and } p_{20}(x_{63}, f_6(f_3(f_4(f_5(c_{22}))))), c_{21}) \text{ and } p_{19}(f_6(f_3(f_4(f_5(c_{22}))), f_{18}(c_{21}, f_3(f_5(c_{22}))), x_{63})) \Rightarrow$   
 $\neg p_7(c_{25}, f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{22}))))), x_{62}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{22}))))), f_{14}(f_{16}(c_{28}, f_{17}(c_{21}, c_{27})), c_{25})), f_9(f_{11}(x_{63}), f_{10}(f_{11}(f_3$

### SYN615-1.p Harrison problem 3879

$p_{13}(x_0, x_0)$     cnf(p13<sub>1</sub>, negated\_conjecture)  
 $p_7(x_{43}, x_{43})$     cnf(p7<sub>2</sub>, negated\_conjecture)  
 $p_2(x_{18}, x_{18})$     cnf(p2<sub>3</sub>, negated\_conjecture)  
 $p_{15}(x_7, x_7)$     cnf(p15<sub>4</sub>, negated\_conjecture)  
 $p_2(c_{26}, f_3(c_{22}))$     cnf(p2<sub>5</sub>, negated\_conjecture)  
 $\neg p_2(c_{21}, f_3(c_{22}))$     cnf(not\_p2<sub>6</sub>, negated\_conjecture)  
 $p_{19}(c_{23}, f_3(f_4(f_5(c_{22}))))$     cnf(p19<sub>7</sub>, negated\_conjecture)  
 $p_{20}(c_{24}, f_6(f_3(f_4(f_5(c_{22}))))), c_{21})$     cnf(p20<sub>8</sub>, negated\_conjecture)  
 $p_7(x_{52}, x_{53}) \Rightarrow p_7(f_{12}(x_{52}), f_{12}(x_{53}))$     cnf(p7<sub>9</sub>, negated\_conjecture)  
 $p_2(x_{29}, x_{30}) \Rightarrow p_2(f_3(x_{29}), f_3(x_{30}))$     cnf(p2<sub>10</sub>, negated\_conjecture)  
 $p_2(x_{31}, x_{32}) \Rightarrow p_2(f_4(x_{31}), f_4(x_{32}))$     cnf(p2<sub>11</sub>, negated\_conjecture)  
 $p_2(x_{33}, x_{34}) \Rightarrow p_2(f_5(x_{33}), f_5(x_{34}))$     cnf(p2<sub>12</sub>, negated\_conjecture)  
 $p_2(x_{50}, x_{51}) \Rightarrow p_7(f_{11}(x_{50}), f_{11}(x_{51}))$     cnf(p7<sub>13</sub>, negated\_conjecture)  
 $p_2(c_{26}, f_{14}(f_{16}(c_{28}, f_{17}(c_{21}, c_{27})), c_{25}))$     cnf(p2<sub>14</sub>, negated\_conjecture)  
 $(p_{13}(x_0, x_1) \text{ and } p_{13}(x_0, x_2)) \Rightarrow p_{13}(x_1, x_2)$     cnf(p13<sub>15</sub>, negated\_conjecture)  
 $(p_7(x_{43}, x_{44}) \text{ and } p_7(x_{43}, x_{45})) \Rightarrow p_7(x_{44}, x_{45})$     cnf(p7<sub>16</sub>, negated\_conjecture)  
 $(p_2(x_{18}, x_{19}) \text{ and } p_2(x_{18}, x_{20})) \Rightarrow p_2(x_{19}, x_{20})$     cnf(p2<sub>17</sub>, negated\_conjecture)  
 $(p_{15}(x_7, x_8) \text{ and } p_{15}(x_7, x_9)) \Rightarrow p_{15}(x_8, x_9)$     cnf(p15<sub>18</sub>, negated\_conjecture)  
 $(p_2(x_{42}, x_{40}) \text{ and } p_{20}(x_{41}, x_{42}) \text{ and } p_2(x_{41}, x_{39})) \Rightarrow p_{20}(x_{39}, x_{40})$     cnf(p20<sub>19</sub>, negated\_conjecture)  
 $(p_2(x_{16}, x_{14}) \text{ and } p_2(x_{17}, x_{15}) \text{ and } p_{19}(x_{16}, x_{17})) \Rightarrow p_{19}(x_{14}, x_{15})$     cnf(p19<sub>20</sub>, negated\_conjecture)  
 $(p_{15}(x_4, x_6) \text{ and } p_2(x_3, x_5)) \Rightarrow p_{13}(f_{16}(x_3, x_4), f_{16}(x_5, x_6))$     cnf(p13<sub>21</sub>, negated\_conjecture)  
 $(p_7(x_{58}, x_{60}) \text{ and } p_7(x_{59}, x_{61})) \Rightarrow p_7(f_9(x_{58}, x_{59}), f_9(x_{60}, x_{61}))$     cnf(p7<sub>22</sub>, negated\_conjecture)  
 $(p_7(x_{54}, x_{56}) \text{ and } p_7(x_{55}, x_{57})) \Rightarrow p_7(f_8(x_{54}, x_{55}), f_8(x_{56}, x_{57}))$     cnf(p7<sub>23</sub>, negated\_conjecture)  
 $(p_2(x_{47}, x_{49}) \text{ and } p_7(x_{46}, x_{48})) \Rightarrow p_7(f_{10}(x_{46}, x_{47}), f_{10}(x_{48}, x_{49}))$     cnf(p7<sub>24</sub>, negated\_conjecture)  
 $(p_2(x_{35}, x_{37}) \text{ and } p_2(x_{36}, x_{38})) \Rightarrow p_2(f_6(x_{35}, x_{36}), f_6(x_{37}, x_{38}))$     cnf(p2<sub>25</sub>, negated\_conjecture)  
 $(p_2(x_{25}, x_{27}) \text{ and } p_2(x_{26}, x_{28})) \Rightarrow p_2(f_{18}(x_{25}, x_{26}), f_{18}(x_{27}, x_{28}))$     cnf(p2<sub>26</sub>, negated\_conjecture)  
 $(p_{13}(x_{21}, x_{23}) \text{ and } p_7(x_{22}, x_{24})) \Rightarrow p_2(f_{14}(x_{21}, x_{22}), f_{14}(x_{23}, x_{24}))$     cnf(p2<sub>27</sub>, negated\_conjecture)  
 $(p_2(x_{10}, x_{12}) \text{ and } p_2(x_{11}, x_{13})) \Rightarrow p_{15}(f_{17}(x_{10}, x_{11}), f_{17}(x_{12}, x_{13}))$     cnf(p15<sub>28</sub>, negated\_conjecture)  
 $p_7(c_{25}, f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{22}))))), c_{23}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{22}))))), c_{26}), f_9(f_{11}(c_{24}), f_{10}(f_{11}(f_3(f_4(f_5(c_{22}))))), c_{27}))))))$     cnf  
 $(p_{19}(x_{62}, f_3(f_4(f_5(c_{22})))) \text{ and } p_{20}(x_{63}, f_6(f_3(f_4(f_5(c_{22}))))), c_{21}) \text{ and } p_2(f_{14}(f_{16}(c_{28}, f_{17}(c_{21}, c_{27})), c_{25}), f_3(c_{22}))) \Rightarrow \neg p_7(c_{25}, f_8$   
 $(p_{19}(x_{62}, f_3(f_4(f_5(c_{22})))) \text{ and } p_{20}(x_{63}, f_6(f_3(f_4(f_5(c_{22}))))), c_{21}) \text{ and } p_{19}(f_6(f_3(f_4(f_5(c_{22}))), f_{18}(c_{21}, f_3(f_5(c_{22}))), x_{63})) \Rightarrow$   
 $\neg p_7(c_{25}, f_8(f_{10}(f_{12}(f_{11}(f_3(f_5(c_{22}))))), x_{62}), f_8(f_{10}(f_{11}(f_3(f_4(f_5(c_{22}))))), f_{14}(f_{16}(c_{28}, f_{17}(c_{21}, c_{27})), c_{25})), f_9(f_{11}(x_{63}), f_{10}(f_{11}(f_3$

### SYN616-1.p Harrison problem 3901

$p_{17}(c_{28})$     cnf(c28\_is\_p17<sub>1</sub>, negated\_conjecture)  
 $p_{10}(x_0, x_0)$     cnf(p10<sub>2</sub>, negated\_conjecture)  
 $p_9(x_{60}, x_{60})$     cnf(p9<sub>3</sub>, negated\_conjecture)  
 $p_2(x_{31}, x_{31})$     cnf(p2<sub>4</sub>, negated\_conjecture)  
 $p_{18}(x_{24}, x_{24})$     cnf(p18<sub>5</sub>, negated\_conjecture)  
 $p_{19}(c_{26}, c_{27})$     cnf(p19<sub>6</sub>, negated\_conjecture)  
 $p_2(c_{25}, c_{28})$     cnf(p2<sub>7</sub>, negated\_conjecture)  
 $\neg p_{15}(c_{25}, c_{27})$     cnf(not\_p15<sub>8</sub>, negated\_conjecture)  
 $p_{13}(f_3(f_4(f_5(c_{20}))), c_{21})$     cnf(p13<sub>9</sub>, negated\_conjecture)  
 $(p_{17}(x_{23}) \text{ and } p_2(x_{23}, x_{22})) \Rightarrow p_{17}(x_{22})$     cnf(p17<sub>10</sub>, negated\_conjecture)

$p_2(x_{50}, x_{51}) \Rightarrow p_2(f_6(x_{50}), f_6(x_{51}))$      $\text{cnf}(p_{2_{11}}, \text{negated\_conjecture})$   
 $p_2(x_{44}, x_{45}) \Rightarrow p_2(f_3(x_{44}), f_3(x_{45}))$      $\text{cnf}(p_{2_{12}}, \text{negated\_conjecture})$   
 $p_2(x_{46}, x_{47}) \Rightarrow p_2(f_4(x_{46}), f_4(x_{47}))$      $\text{cnf}(p_{2_{13}}, \text{negated\_conjecture})$   
 $p_2(x_{48}, x_{49}) \Rightarrow p_2(f_5(x_{48}), f_5(x_{49}))$      $\text{cnf}(p_{2_{14}}, \text{negated\_conjecture})$   
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2)$      $\text{cnf}(p_{10_{15}}, \text{negated\_conjecture})$   
 $(p_9(x_{60}, x_{61}) \text{ and } p_9(x_{60}, x_{62})) \Rightarrow p_9(x_{61}, x_{62})$      $\text{cnf}(p_{9_{16}}, \text{negated\_conjecture})$   
 $(p_2(x_{31}, x_{32}) \text{ and } p_2(x_{31}, x_{33})) \Rightarrow p_2(x_{32}, x_{33})$      $\text{cnf}(p_{2_{17}}, \text{negated\_conjecture})$   
 $(p_{18}(x_{24}, x_{25}) \text{ and } p_{18}(x_{24}, x_{26})) \Rightarrow p_{18}(x_{25}, x_{26})$      $\text{cnf}(p_{18_{18}}, \text{negated\_conjecture})$   
 $p_2(f_{11}(c_{23}, c_{24}, f_3(f_5(c_{20}))), f_8(c_{21}, f_3(f_5(c_{20}))))$      $\text{cnf}(p_{2_{19}}, \text{negated\_conjecture})$   
 $(p_{17}(x_{17}) \text{ and } p_{16}(x_{17}, f_8(c_{21}, f_3(f_5(c_{20})))) \Rightarrow p_{15}(x_{17}, c_{24})$      $\text{cnf}(p_{15_{20}}, \text{negated\_conjecture})$   
 $(p_2(x_5, x_3) \text{ and } p_2(x_6, x_4) \text{ and } p_{13}(x_5, x_6)) \Rightarrow p_{13}(x_3, x_4)$      $\text{cnf}(p_{13_{21}}, \text{negated\_conjecture})$   
 $(p_{18}(x_{30}, x_{27}) \text{ and } p_{19}(x_{30}, x_{29}) \text{ and } p_{10}(x_{29}, x_{28})) \Rightarrow p_{19}(x_{27}, x_{28})$      $\text{cnf}(p_{19_{22}}, \text{negated\_conjecture})$   
 $(p_2(x_{20}, x_{18}) \text{ and } p_2(x_{21}, x_{19}) \text{ and } p_{16}(x_{20}, x_{21})) \Rightarrow p_{16}(x_{18}, x_{19})$      $\text{cnf}(p_{16_{23}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{16}, x_{15}) \text{ and } p_2(x_{16}, x_{13}) \text{ and } p_{10}(x_{15}, x_{14})) \Rightarrow p_{15}(x_{13}, x_{14})$      $\text{cnf}(p_{15_{24}}, \text{negated\_conjecture})$   
 $p_{14}(f_7(c_{22}, f_8(c_{21}, f_3(f_5(c_{20}))))), f_3(f_5(c_{20})), f_6(c_{21}))$      $\text{cnf}(p_{14_{25}}, \text{negated\_conjecture})$   
 $(p_2(x_{56}, x_{58}) \text{ and } p_2(x_{57}, x_{59})) \Rightarrow p_2(f_8(x_{56}, x_{57}), f_8(x_{58}, x_{59}))$      $\text{cnf}(p_{2_{26}}, \text{negated\_conjecture})$   
 $(p_2(x_{40}, x_{42}) \text{ and } p_2(x_{41}, x_{43})) \Rightarrow p_2(f_{12}(x_{40}, x_{41}), f_{12}(x_{42}, x_{43}))$      $\text{cnf}(p_{2_{27}}, \text{negated\_conjecture})$   
 $(p_2(x_{53}, x_{55}) \text{ and } p_2(x_{52}, x_{54})) \Rightarrow p_2(f_7(x_{52}, x_{53}), f_7(x_{54}, x_{55}))$      $\text{cnf}(p_{2_{28}}, \text{negated\_conjecture})$   
 $p_{14}(f_7(c_{22}, f_{12}(f_8(c_{21}, f_3(f_5(c_{20}))), c_{25})), f_3(f_5(c_{20})), f_6(c_{21}))$      $\text{cnf}(p_{14_{29}}, \text{negated\_conjecture})$   
 $\neg p_{14}(f_7(c_{22}, f_{12}(f_8(c_{21}, f_3(f_5(c_{20}))), c_{28})), f_3(f_5(c_{20})), f_6(c_{21}))$      $\text{cnf}(\text{not\_}p_{14_{30}}, \text{negated\_conjecture})$   
 $(p_2(x_{12}, x_9) \text{ and } p_2(x_{11}, x_8) \text{ and } p_2(x_{10}, x_7) \text{ and } p_{14}(x_{10}, x_{11}, x_{12})) \Rightarrow p_{14}(x_7, x_8, x_9)$      $\text{cnf}(p_{14_{31}}, \text{negated\_conjecture})$   
 $(p_2(x_{36}, x_{39}) \text{ and } p_9(x_{34}, x_{37}) \text{ and } p_{10}(x_{35}, x_{38})) \Rightarrow p_2(f_{11}(x_{34}, x_{35}, x_{36}), f_{11}(x_{37}, x_{38}, x_{39}))$      $\text{cnf}(p_{2_{32}}, \text{negated\_conjecture})$

### SYN617-1.p Harrison problem 3908

$p_{11}(x_0, x_0)$      $\text{cnf}(p_{11_1}, \text{negated\_conjecture})$   
 $p_9(x_{53}, x_{53})$      $\text{cnf}(p_{9_2}, \text{negated\_conjecture})$   
 $p_7(x_{42}, x_{42})$      $\text{cnf}(p_{7_3}, \text{negated\_conjecture})$   
 $p_2(x_{27}, x_{27})$      $\text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $p_{13}(x_{11}, x_{11})$      $\text{cnf}(p_{13_5}, \text{negated\_conjecture})$   
 $p_{19}(c_{21}, c_{22})$      $\text{cnf}(p_{19_6}, \text{negated\_conjecture})$   
 $p_{11}(f_{12}(f_{14}(x_5, x_6)), x_6)$      $\text{cnf}(p_{11_7}, \text{negated\_conjecture})$   
 $p_7(f_8(f_{10}(x_{51}, x_{52})), x_{52})$      $\text{cnf}(p_{7_8}, \text{negated\_conjecture})$   
 $p_9(f_{18}(f_5(c_{20}), x_{64}), f_{17}(x_{64}))$      $\text{cnf}(p_{9_9}, \text{negated\_conjecture})$   
 $p_{13}(f_{15}(f_5(c_{20}), x_{20}), f_{16}(x_{20}))$      $\text{cnf}(p_{13_{10}}, \text{negated\_conjecture})$   
 $p_{11}(x_3, x_4) \Rightarrow p_{11}(f_{12}(x_3), f_{12}(x_4))$      $\text{cnf}(p_{11_{11}}, \text{negated\_conjecture})$   
 $p_7(x_{56}, x_{57}) \Rightarrow p_9(f_{17}(x_{56}), f_{17}(x_{57}))$      $\text{cnf}(p_{9_{12}}, \text{negated\_conjecture})$   
 $p_7(x_{49}, x_{50}) \Rightarrow p_7(f_8(x_{49}), f_8(x_{50}))$      $\text{cnf}(p_{7_{13}}, \text{negated\_conjecture})$   
 $p_2(x_{40}, x_{41}) \Rightarrow p_2(f_6(x_{40}), f_6(x_{41}))$      $\text{cnf}(p_{2_{14}}, \text{negated\_conjecture})$   
 $p_2(x_{38}, x_{39}) \Rightarrow p_2(f_5(x_{38}), f_5(x_{39}))$      $\text{cnf}(p_{2_{15}}, \text{negated\_conjecture})$   
 $p_2(x_{30}, x_{31}) \Rightarrow p_2(f_3(x_{30}), f_3(x_{31}))$      $\text{cnf}(p_{2_{16}}, \text{negated\_conjecture})$   
 $p_{11}(x_{21}, x_{22}) \Rightarrow p_{13}(f_{16}(x_{21}), f_{16}(x_{22}))$      $\text{cnf}(p_{13_{17}}, \text{negated\_conjecture})$   
 $p_9(f_{18}(f_3(x_{62}), x_{63}), f_{18}(x_{62}, f_8(x_{63})))$      $\text{cnf}(p_{9_{18}}, \text{negated\_conjecture})$   
 $p_{13}(f_{15}(f_3(x_{18}), x_{19}), f_{15}(x_{18}, f_{12}(x_{19})))$      $\text{cnf}(p_{13_{19}}, \text{negated\_conjecture})$   
 $(p_{11}(x_0, x_1) \text{ and } p_{11}(x_0, x_2)) \Rightarrow p_{11}(x_1, x_2)$      $\text{cnf}(p_{11_{20}}, \text{negated\_conjecture})$   
 $(p_9(x_{53}, x_{54}) \text{ and } p_9(x_{53}, x_{55})) \Rightarrow p_9(x_{54}, x_{55})$      $\text{cnf}(p_{9_{21}}, \text{negated\_conjecture})$   
 $(p_7(x_{42}, x_{43}) \text{ and } p_7(x_{42}, x_{44})) \Rightarrow p_7(x_{43}, x_{44})$      $\text{cnf}(p_{7_{22}}, \text{negated\_conjecture})$   
 $(p_2(x_{27}, x_{28}) \text{ and } p_2(x_{27}, x_{29})) \Rightarrow p_2(x_{28}, x_{29})$      $\text{cnf}(p_{2_{23}}, \text{negated\_conjecture})$   
 $(p_{13}(x_{11}, x_{12}) \text{ and } p_{13}(x_{11}, x_{13})) \Rightarrow p_{13}(x_{12}, x_{13})$      $\text{cnf}(p_{13_{24}}, \text{negated\_conjecture})$   
 $(p_2(x_{25}, x_{23}) \text{ and } p_2(x_{26}, x_{24}) \text{ and } p_{19}(x_{25}, x_{26})) \Rightarrow p_{19}(x_{23}, x_{24})$      $\text{cnf}(p_{19_{25}}, \text{negated\_conjecture})$   
 $(p_2(x_{58}, x_{60}) \text{ and } p_7(x_{59}, x_{61})) \Rightarrow p_9(f_{18}(x_{58}, x_{59}), f_{18}(x_{60}, x_{61}))$      $\text{cnf}(p_{9_{26}}, \text{negated\_conjecture})$   
 $(p_{11}(x_8, x_{10}) \text{ and } p_{13}(x_7, x_9)) \Rightarrow p_{11}(f_{14}(x_7, x_8), f_{14}(x_9, x_{10}))$      $\text{cnf}(p_{11_{27}}, \text{negated\_conjecture})$   
 $(p_{11}(x_{15}, x_{17}) \text{ and } p_2(x_{14}, x_{16})) \Rightarrow p_{13}(f_{15}(x_{14}, x_{15}), f_{15}(x_{16}, x_{17}))$      $\text{cnf}(p_{13_{28}}, \text{negated\_conjecture})$   
 $(p_2(x_{32}, x_{34}) \text{ and } p_2(x_{33}, x_{35})) \Rightarrow p_2(f_4(x_{32}, x_{33}), f_4(x_{34}, x_{35}))$      $\text{cnf}(p_{2_{29}}, \text{negated\_conjecture})$   
 $(p_7(x_{46}, x_{48}) \text{ and } p_9(x_{45}, x_{47})) \Rightarrow p_7(f_{10}(x_{45}, x_{46}), f_{10}(x_{47}, x_{48}))$      $\text{cnf}(p_{7_{30}}, \text{negated\_conjecture})$   
 $p_{19}(x_{37}, x_{36}) \Rightarrow p_2(f_4(f_4(f_3(x_{36}), f_5(f_6(c_{20}))), x_{37}), f_3(f_4(f_4(x_{36}, f_5(f_6(c_{20}))), x_{37})))$      $\text{cnf}(p_{2_{31}}, \text{negated\_conjecture})$   
 $\neg p_{13}(f_{15}(f_4(f_4(f_3(c_{22}), f_5(f_6(c_{20}))), c_{21}), f_{14}(c_{23}, c_{24}), f_{15}(f_4(f_4(c_{22}, f_5(f_6(c_{20}))), c_{21}), c_{24}))$      $\text{cnf}(\text{not\_}p_{13_{32}}, \text{negated\_conjecture})$

### SYN618-1.p Harrison problem 3944

$p_9(c_{16})$      $\text{cnf}(c_{16.\text{is\_}p_{9_1}}, \text{negated\_conjecture})$   
 $p_{10}(x_0, x_0)$      $\text{cnf}(p_{10_2}, \text{negated\_conjecture})$

$p_5(x_{34}, x_{34})$     cnf(p5<sub>3</sub>, negated\_conjecture)  
 $p_4(x_{29}, x_{29})$     cnf(p4<sub>4</sub>, negated\_conjecture)  
 $p_2(x_{24}, x_{24})$     cnf(p2<sub>5</sub>, negated\_conjecture)  
 $p_{14}(x_{17}, x_{17})$     cnf(p14<sub>6</sub>, negated\_conjecture)  
 $p_{12}(c_{19}, c_{20})$     cnf(p12<sub>7</sub>, negated\_conjecture)  
 $p_{13}(c_{23}, c_{21})$     cnf(p13<sub>8</sub>, negated\_conjecture)  
 $p_{13}(c_{19}, c_{23})$     cnf(p13<sub>9</sub>, negated\_conjecture)  
 $p_{13}(c_{19}, c_{21})$     cnf(p13<sub>10</sub>, negated\_conjecture)  
 $p_{12}(c_{20}, c_{21})$     cnf(p12<sub>11</sub>, negated\_conjecture)  
 $p_2(c_{17}, f_3(c_{16}))$     cnf(p2<sub>12</sub>, negated\_conjecture)  
 $p_{11}(c_{16}, c_{17}, c_{18})$     cnf(p11<sub>13</sub>, negated\_conjecture)  
 $p_5(f_8(c_{16}, c_{20}), f_6(f_7(c_{22})))$     cnf(p5<sub>14</sub>, negated\_conjecture)  
 $(p_9(x_{45}) \text{ and } p_2(x_{45}, x_{44})) \Rightarrow p_9(x_{44})$     cnf(p9<sub>15</sub>, negated\_conjecture)  
 $p_5(f_8(f_3(c_{16}), c_{23}), f_6(f_7(c_{22})))$     cnf(p5<sub>16</sub>, negated\_conjecture)  
 $\neg p_5(f_8(f_3(c_{16}), c_{20}), f_6(f_7(c_{22})))$     cnf(not\_p5<sub>17</sub>, negated\_conjecture)  
 $p_4(x_{38}, x_{39}) \Rightarrow p_5(f_6(x_{38}), f_6(x_{39}))$     cnf(p5<sub>18</sub>, negated\_conjecture)  
 $p_2(x_{27}, x_{28}) \Rightarrow p_2(f_3(x_{27}), f_3(x_{28}))$     cnf(p2<sub>19</sub>, negated\_conjecture)  
 $p_4(x_{32}, x_{33}) \Rightarrow p_4(f_7(x_{32}), f_7(x_{33}))$     cnf(p4<sub>20</sub>, negated\_conjecture)  
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2)$     cnf(p10<sub>21</sub>, negated\_conjecture)  
 $(p_5(x_{34}, x_{35}) \text{ and } p_5(x_{34}, x_{36})) \Rightarrow p_5(x_{35}, x_{36})$     cnf(p5<sub>22</sub>, negated\_conjecture)  
 $(p_4(x_{29}, x_{30}) \text{ and } p_4(x_{29}, x_{31})) \Rightarrow p_4(x_{30}, x_{31})$     cnf(p4<sub>23</sub>, negated\_conjecture)  
 $(p_2(x_{24}, x_{25}) \text{ and } p_2(x_{24}, x_{26})) \Rightarrow p_2(x_{25}, x_{26})$     cnf(p2<sub>24</sub>, negated\_conjecture)  
 $(p_{14}(x_{17}, x_{18}) \text{ and } p_{14}(x_{17}, x_{19})) \Rightarrow p_{14}(x_{18}, x_{19})$     cnf(p14<sub>25</sub>, negated\_conjecture)  
 $(p_5(x_{11}, x_9) \text{ and } p_5(x_{12}, x_{10}) \text{ and } p_{12}(x_{11}, x_{12})) \Rightarrow p_{12}(x_9, x_{10})$     cnf(p12<sub>26</sub>, negated\_conjecture)  
 $(p_{14}(x_{23}, x_{20}) \text{ and } p_{15}(x_{23}, x_{22}) \text{ and } p_{10}(x_{22}, x_{21})) \Rightarrow p_{15}(x_{20}, x_{21})$     cnf(p15<sub>27</sub>, negated\_conjecture)  
 $(p_5(x_{15}, x_{13}) \text{ and } p_5(x_{16}, x_{14}) \text{ and } p_{13}(x_{15}, x_{16})) \Rightarrow p_{13}(x_{13}, x_{14})$     cnf(p13<sub>28</sub>, negated\_conjecture)  
 $(p_{13}(x_{37}, c_{21}) \text{ and } p_{13}(c_{19}, x_{37}) \text{ and } p_{15}(c_{24}, c_{18})) \Rightarrow p_5(x_{37}, c_{20})$     cnf(p5<sub>29</sub>, negated\_conjecture)  
 $(p_2(x_{40}, x_{42}) \text{ and } p_5(x_{41}, x_{43})) \Rightarrow p_5(f_8(x_{40}, x_{41}), f_8(x_{42}, x_{43}))$     cnf(p5<sub>30</sub>, negated\_conjecture)  
 $(p_{13}(x_{37}, c_{21}) \text{ and } p_{13}(c_{19}, x_{37}) \text{ and } p_5(f_8(c_{17}, x_{37}), f_6(f_7(c_{22})))) \Rightarrow p_5(x_{37}, c_{20})$     cnf(p5<sub>31</sub>, negated\_conjecture)  
 $(p_{13}(x_{37}, c_{21}) \text{ and } p_{13}(c_{19}, x_{37}) \text{ and } p_5(f_8(c_{16}, x_{37}), f_6(f_7(c_{22})))) \Rightarrow p_5(x_{37}, c_{20})$     cnf(p5<sub>32</sub>, negated\_conjecture)  
 $(p_2(x_8, x_4) \text{ and } p_2(x_7, x_3) \text{ and } p_{10}(x_6, x_5) \text{ and } p_{11}(x_7, x_8, x_6)) \Rightarrow p_{11}(x_3, x_4, x_5)$     cnf(p11<sub>33</sub>, negated\_conjecture)

### SYN619-1.p Harrison problem 3992

$p_{10}(x_0, x_0)$     cnf(p10<sub>1</sub>, negated\_conjecture)  
 $p_8(x_{51}, x_{51})$     cnf(p8<sub>2</sub>, negated\_conjecture)  
 $p_5(x_{46}, x_{46})$     cnf(p5<sub>3</sub>, negated\_conjecture)  
 $p_4(x_{39}, x_{39})$     cnf(p4<sub>4</sub>, negated\_conjecture)  
 $p_2(x_{18}, x_{18})$     cnf(p2<sub>5</sub>, negated\_conjecture)  
 $p_{17}(x_9, x_9)$     cnf(p17<sub>6</sub>, negated\_conjecture)  
 $p_{18}(c_{24}, f_6(c_{25}))$     cnf(p18<sub>7</sub>, negated\_conjecture)  
 $\neg p_{18}(c_{24}, f_6(f_7(c_{22}), c_{23}))$     cnf(not\_p18<sub>8</sub>, negated\_conjecture)  
 $p_{17}(f_3(x_{10}), x_{11}) \Rightarrow p_{17}(x_{10}, x_{11})$     cnf(p17<sub>9</sub>, negated\_conjecture)  
 $p_4(x_{49}, x_{50}) \Rightarrow p_5(f_6(x_{49}), f_6(x_{50}))$     cnf(p5<sub>10</sub>, negated\_conjecture)  
 $p_4(x_3, x_4) \Rightarrow p_{10}(f_{12}(x_3), f_{12}(x_4))$     cnf(p10<sub>11</sub>, negated\_conjecture)  
 $p_{10}(x_{25}, x_{26}) \Rightarrow p_2(f_{11}(x_{25}), f_{11}(x_{26}))$     cnf(p2<sub>12</sub>, negated\_conjecture)  
 $p_8(x_{31}, x_{32}) \Rightarrow p_2(f_{14}(x_{31}), f_{14}(x_{32}))$     cnf(p2<sub>13</sub>, negated\_conjecture)  
 $p_8(x_{33}, x_{34}) \Rightarrow p_2(f_{15}(x_{33}), f_{15}(x_{34}))$     cnf(p2<sub>14</sub>, negated\_conjecture)  
 $p_8(x_{35}, x_{36}) \Rightarrow p_2(f_{16}(x_{35}), f_{16}(x_{36}))$     cnf(p2<sub>15</sub>, negated\_conjecture)  
 $p_2(x_{37}, x_{38}) \Rightarrow p_2(f_3(x_{37}), f_3(x_{38}))$     cnf(p2<sub>16</sub>, negated\_conjecture)  
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2)$     cnf(p10<sub>17</sub>, negated\_conjecture)  
 $(p_8(x_{51}, x_{52}) \text{ and } p_8(x_{51}, x_{53})) \Rightarrow p_8(x_{52}, x_{53})$     cnf(p8<sub>18</sub>, negated\_conjecture)  
 $(p_5(x_{46}, x_{47}) \text{ and } p_5(x_{46}, x_{48})) \Rightarrow p_5(x_{47}, x_{48})$     cnf(p5<sub>19</sub>, negated\_conjecture)  
 $(p_4(x_{39}, x_{40}) \text{ and } p_4(x_{39}, x_{41})) \Rightarrow p_4(x_{40}, x_{41})$     cnf(p4<sub>20</sub>, negated\_conjecture)  
 $(p_2(x_{18}, x_{19}) \text{ and } p_2(x_{18}, x_{20})) \Rightarrow p_2(x_{19}, x_{20})$     cnf(p2<sub>21</sub>, negated\_conjecture)  
 $p_2(f_{13}(x_{21}, x_{23}), f_{13}(x_{22}, x_{24})) \Rightarrow p_2(x_{23}, x_{24})$     cnf(p2<sub>22</sub>, negated\_conjecture)  
 $p_2(f_{13}(x_{21}, x_{23}), f_{13}(x_{22}, x_{24})) \Rightarrow p_2(x_{21}, x_{22})$     cnf(p2<sub>23</sub>, negated\_conjecture)  
 $p_{18}(x_{12}, f_6(c_{25})) \Rightarrow (p_{18}(x_{12}, f_6(c_{19})) \text{ or } p_2(f_{14}(x_{12}), c_{20}))$     cnf(p18<sub>24</sub>, negated\_conjecture)  
 $(p_2(x_7, x_5) \text{ and } p_2(x_8, x_6) \text{ and } p_{17}(x_7, x_8)) \Rightarrow p_{17}(x_5, x_6)$     cnf(p17<sub>25</sub>, negated\_conjecture)  
 $(p_5(x_{16}, x_{14}) \text{ and } p_8(x_{15}, x_{13}) \text{ and } p_{18}(x_{15}, x_{16})) \Rightarrow p_{18}(x_{13}, x_{14})$     cnf(p18<sub>26</sub>, negated\_conjecture)  
 $p_{18}(x_{12}, f_6(c_{25})) \Rightarrow (p_{18}(x_{12}, f_6(c_{19})) \text{ or } p_{17}(f_3(c_{21}), f_{15}(x_{12})))$     cnf(p18<sub>27</sub>, negated\_conjecture)

$(p_2(x_{55}, x_{57}) \text{ and } p_2(x_{54}, x_{56})) \Rightarrow p_8(f_9(x_{54}, x_{55}), f_9(x_{56}, x_{57}))$      $\text{cnf}(p8_{28}, \text{negated\_conjecture})$   
 $(p_2(x_{27}, x_{29}) \text{ and } p_2(x_{28}, x_{30})) \Rightarrow p_2(f_{13}(x_{27}, x_{28}), f_{13}(x_{29}, x_{30}))$      $\text{cnf}(p2_{29}, \text{negated\_conjecture})$   
 $(p_2(x_{21}, x_{22}) \text{ and } p_2(x_{23}, x_{24})) \Rightarrow p_2(f_{13}(x_{21}, x_{23}), f_{13}(x_{22}, x_{24}))$      $\text{cnf}(p2_{30}, \text{negated\_conjecture})$   
 $(p_2(x_{42}, x_{44}) \text{ and } p_4(x_{43}, x_{45})) \Rightarrow p_4(f_7(x_{42}, x_{43}), f_7(x_{44}, x_{45}))$      $\text{cnf}(p4_{31}, \text{negated\_conjecture})$   
 $(p_2(x_{59}, c_{20}) \text{ and } p_{17}(c_{21}, x_{58})) \Rightarrow \neg p_8(c_{24}, f_9(f_{13}(x_{59}, x_{58}), x_{60}))$      $\text{cnf}(\text{not\_}p2_{32}, \text{negated\_conjecture})$   
 $p_{18}(x_{12}, f_6(c_{25})) \Rightarrow (p_{18}(x_{12}, f_6(c_{19})) \text{ or } p_8(x_{12}, f_9(f_{13}(f_{14}(x_{12}), f_{15}(x_{12})), f_{16}(x_{12}))))$      $\text{cnf}(p18_{33}, \text{negated\_conjecture})$   
 $p_{18}(x_{17}, f_6(c_{19})) \Rightarrow (p_{18}(x_{17}, f_6(f_7(c_{22}, c_{23}))) \text{ or } p_8(x_{17}, f_9(f_{13}(c_{20}, c_{21}), f_{11}(f_{12}(f_7(c_{22}, c_{23}))))))$      $\text{cnf}(p18_{34}, \text{negated\_conjecture})$

### SYN620-1.p Harrison problem 3996

$p_{10}(x_0, x_0)$      $\text{cnf}(p10_1, \text{negated\_conjecture})$   
 $p_5(x_{56}, x_{56})$      $\text{cnf}(p5_2, \text{negated\_conjecture})$   
 $p_3(x_{45}, x_{45})$      $\text{cnf}(p3_3, \text{negated\_conjecture})$   
 $p_2(x_{33}, x_{33})$      $\text{cnf}(p2_4, \text{negated\_conjecture})$   
 $p_{11}(x_{20}, x_{20})$      $\text{cnf}(p11_5, \text{negated\_conjecture})$   
 $\neg p_{18}(f_6(c_{24}))$      $\text{cnf}(f6\_is\_not\_p18_6, \text{negated\_conjecture})$   
 $\neg p_{18}(f_6(c_{22}))$      $\text{cnf}(f6\_is\_not\_p18_7, \text{negated\_conjecture})$   
 $p_3(f_4(c_{22}), c_{23})$      $\text{cnf}(p3_8, \text{negated\_conjecture})$   
 $p_{19}(f_7(f_8(f_9(c_{25}))), c_{23})$      $\text{cnf}(p19_9, \text{negated\_conjecture})$   
 $(p_{18}(x_{28}) \text{ and } p_5(x_{28}, x_{27})) \Rightarrow p_{18}(x_{27})$      $\text{cnf}(p18_{10}, \text{negated\_conjecture})$   
 $p_{11}(x_{10}, x_{11}) \Rightarrow p_{10}(f_{14}(x_{10}), f_{14}(x_{11}))$      $\text{cnf}(p10_{11}, \text{negated\_conjecture})$   
 $p_2(x_{59}, x_{60}) \Rightarrow p_5(f_6(x_{59}), f_6(x_{60}))$      $\text{cnf}(p5_{12}, \text{negated\_conjecture})$   
 $p_3(x_{54}, x_{55}) \Rightarrow p_3(f_9(x_{54}), f_9(x_{55}))$      $\text{cnf}(p3_{13}, \text{negated\_conjecture})$   
 $p_3(x_{52}, x_{53}) \Rightarrow p_3(f_8(x_{52}), f_8(x_{53}))$      $\text{cnf}(p3_{14}, \text{negated\_conjecture})$   
 $p_3(x_{50}, x_{51}) \Rightarrow p_3(f_7(x_{50}), f_7(x_{51}))$      $\text{cnf}(p3_{15}, \text{negated\_conjecture})$   
 $p_2(x_{48}, x_{49}) \Rightarrow p_3(f_4(x_{48}), f_4(x_{49}))$      $\text{cnf}(p3_{16}, \text{negated\_conjecture})$   
 $p_3(x_{25}, x_{26}) \Rightarrow p_{11}(f_{15}(x_{25}), f_{15}(x_{26}))$      $\text{cnf}(p11_{17}, \text{negated\_conjecture})$   
 $p_{10}(x_{23}, x_{24}) \Rightarrow p_{11}(f_{12}(x_{23}), f_{12}(x_{24}))$      $\text{cnf}(p11_{18}, \text{negated\_conjecture})$   
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2)$      $\text{cnf}(p10_{19}, \text{negated\_conjecture})$   
 $(p_5(x_{56}, x_{57}) \text{ and } p_5(x_{56}, x_{58})) \Rightarrow p_5(x_{57}, x_{58})$      $\text{cnf}(p5_{20}, \text{negated\_conjecture})$   
 $(p_3(x_{45}, x_{46}) \text{ and } p_3(x_{45}, x_{47})) \Rightarrow p_3(x_{46}, x_{47})$      $\text{cnf}(p3_{21}, \text{negated\_conjecture})$   
 $(p_2(x_{33}, x_{34}) \text{ and } p_2(x_{33}, x_{35})) \Rightarrow p_2(x_{34}, x_{35})$      $\text{cnf}(p2_{22}, \text{negated\_conjecture})$   
 $(p_{11}(x_{20}, x_{21}) \text{ and } p_{11}(x_{20}, x_{22})) \Rightarrow p_{11}(x_{21}, x_{22})$      $\text{cnf}(p11_{23}, \text{negated\_conjecture})$   
 $p_{10}(f_{13}(f_6(c_{22}), x_9), f_{13}(f_6(c_{24}), f_{16}(c_{26}, x_9)))$      $\text{cnf}(p10_{24}, \text{negated\_conjecture})$   
 $\neg p_{10}(f_{13}(f_6(c_{22}), f_{14}(f_{15}(f_7(c_{25}))))), f_{14}(f_{15}(f_7(c_{25}))))$      $\text{cnf}(\text{not\_}p10_{25}, \text{negated\_conjecture})$   
 $(p_3(x_{43}, x_{41}) \text{ and } p_3(x_{44}, x_{42}) \text{ and } p_{21}(x_{43}, x_{44})) \Rightarrow p_{21}(x_{41}, x_{42})$      $\text{cnf}(p21_{26}, \text{negated\_conjecture})$   
 $(p_3(x_{31}, x_{29}) \text{ and } p_3(x_{32}, x_{30}) \text{ and } p_{19}(x_{31}, x_{32})) \Rightarrow p_{19}(x_{29}, x_{30})$      $\text{cnf}(p19_{27}, \text{negated\_conjecture})$   
 $(p_{11}(x_{39}, x_{37}) \text{ and } p_{20}(x_{38}, x_{39}) \text{ and } p_{11}(x_{38}, x_{36})) \Rightarrow p_{20}(x_{36}, x_{37})$      $\text{cnf}(p20_{28}, \text{negated\_conjecture})$   
 $(p_{10}(x_4, x_6) \text{ and } p_5(x_3, x_5)) \Rightarrow p_{10}(f_{13}(x_3, x_4), f_{13}(x_5, x_6))$      $\text{cnf}(p10_{29}, \text{negated\_conjecture})$   
 $(p_2(x_{17}, x_{19}) \text{ and } p_3(x_{16}, x_{18})) \Rightarrow p_{10}(f_{17}(x_{16}, x_{17}), f_{17}(x_{18}, x_{19}))$      $\text{cnf}(p10_{30}, \text{negated\_conjecture})$   
 $(p_{10}(x_{12}, x_{14}) \text{ and } p_{10}(x_{13}, x_{15})) \Rightarrow p_{10}(f_{16}(x_{12}, x_{13}), f_{16}(x_{14}, x_{15}))$      $\text{cnf}(p10_{31}, \text{negated\_conjecture})$   
 $p_{20}(f_{12}(f_{13}(f_6(c_{22}), f_{14}(f_{15}(f_7(c_{25}))))), f_{12}(f_{13}(f_6(c_{24}), x_{40})))$      $\text{cnf}(p20_{32}, \text{negated\_conjecture})$   
 $\neg p_{20}(f_{12}(f_{13}(f_6(c_{22}), f_{14}(f_{15}(f_7(c_{25}))))), f_{12}(f_{13}(f_6(c_{22}), c_{27})))$      $\text{cnf}(\text{not\_}p20_{33}, \text{negated\_conjecture})$   
 $(p_{21}(x_8, c_{23}) \text{ and } p_3(f_4(x_7), x_8)) \Rightarrow (p_{18}(f_6(x_7)) \text{ or } p_{10}(f_{13}(f_6(x_7), f_{17}(x_8, x_7)), f_{14}(f_{15}(f_7(c_{25}))))))$      $\text{cnf}(p18_{34}, \text{negated\_conjecture})$

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$p_{10}(x_0, x_0)$      $\text{cnf}(p10_1, \text{negated\_conjecture})$   
 $p_8(x_{78}, x_{78})$      $\text{cnf}(p8_2, \text{negated\_conjecture})$   
 $p_7(x_{71}, x_{71})$      $\text{cnf}(p7_3, \text{negated\_conjecture})$   
 $p_4(x_{38}, x_{38})$      $\text{cnf}(p4_4, \text{negated\_conjecture})$   
 $p_2(x_{12}, x_{12})$      $\text{cnf}(p2_5, \text{negated\_conjecture})$   
 $p_{13}(x_7, x_7)$      $\text{cnf}(p13_6, \text{negated\_conjecture})$   
 $\neg p_2(c_{23}, f_3(c_{24}))$      $\text{cnf}(\text{not\_}p2_7, \text{negated\_conjecture})$   
 $p_7(x_{10}, x_{11}) \Rightarrow p_{13}(f_{14}(x_{10}), f_{14}(x_{11}))$      $\text{cnf}(p13_8, \text{negated\_conjecture})$   
 $p_4(x_{59}, x_{60}) \Rightarrow p_4(f_5(x_{59}), f_5(x_{60}))$      $\text{cnf}(p4_9, \text{negated\_conjecture})$   
 $p_2(x_{45}, x_{46}) \Rightarrow p_4(f_{16}(x_{45}), f_{16}(x_{46}))$      $\text{cnf}(p4_{10}, \text{negated\_conjecture})$   
 $p_2(x_{24}, x_{25}) \Rightarrow p_2(f_3(x_{24}), f_3(x_{25}))$      $\text{cnf}(p2_{11}, \text{negated\_conjecture})$   
 $p_2(x_{22}, x_{23}) \Rightarrow p_2(f_{18}(x_{22}), f_{18}(x_{23}))$      $\text{cnf}(p2_{12}, \text{negated\_conjecture})$   
 $p_2(x_{20}, x_{21}) \Rightarrow p_2(f_{17}(x_{20}), f_{17}(x_{21}))$      $\text{cnf}(p2_{13}, \text{negated\_conjecture})$   
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2)$      $\text{cnf}(p10_{14}, \text{negated\_conjecture})$   
 $(p_8(x_{78}, x_{79}) \text{ and } p_8(x_{78}, x_{80})) \Rightarrow p_8(x_{79}, x_{80})$      $\text{cnf}(p8_{15}, \text{negated\_conjecture})$

$(p_7(x_{71}, x_{72}) \text{ and } p_7(x_{71}, x_{73})) \Rightarrow p_7(x_{72}, x_{73})$     cnf(p7<sub>16</sub>, negated\_conjecture)  
 $(p_4(x_{38}, x_{39}) \text{ and } p_4(x_{38}, x_{40})) \Rightarrow p_4(x_{39}, x_{40})$     cnf(p4<sub>17</sub>, negated\_conjecture)  
 $(p_{21}(x_{30}, x_{32}) \text{ and } p_{21}(x_{32}, x_{31})) \Rightarrow p_{21}(x_{30}, x_{31})$     cnf(p21<sub>18</sub>, negated\_conjecture)  
 $(p_2(x_{12}, x_{13}) \text{ and } p_2(x_{12}, x_{14})) \Rightarrow p_2(x_{13}, x_{14})$     cnf(p2<sub>19</sub>, negated\_conjecture)  
 $(p_{13}(x_7, x_8) \text{ and } p_{13}(x_7, x_9)) \Rightarrow p_{13}(x_8, x_9)$     cnf(p13<sub>20</sub>, negated\_conjecture)  
 $(p_4(x_{28}, x_{26}) \text{ and } p_4(x_{29}, x_{27}) \text{ and } p_{21}(x_{28}, x_{29})) \Rightarrow p_{21}(x_{26}, x_{27})$     cnf(p21<sub>21</sub>, negated\_conjecture)  
 $(p_{22}(x_{37}, x_{36}) \text{ and } p_4(x_{37}, x_{34}) \text{ and } p_{13}(x_{36}, x_{35})) \Rightarrow p_{22}(x_{34}, x_{35})$     cnf(p22<sub>22</sub>, negated\_conjecture)  
 $(p_{10}(x_{75}, x_{77}) \text{ and } p_2(x_{74}, x_{76})) \Rightarrow p_7(f_{11}(x_{74}, x_{75}), f_{11}(x_{76}, x_{77}))$     cnf(p7<sub>23</sub>, negated\_conjecture)  
 $(p_2(x_3, x_5) \text{ and } p_2(x_4, x_6)) \Rightarrow p_{10}(f_{12}(x_3, x_4), f_{12}(x_5, x_6))$     cnf(p10<sub>24</sub>, negated\_conjecture)  
 $(p_4(x_{41}, x_{43}) \text{ and } p_4(x_{42}, x_{44})) \Rightarrow p_4(f_{15}(x_{41}, x_{42}), f_{15}(x_{43}, x_{44}))$     cnf(p4<sub>25</sub>, negated\_conjecture)  
 $(p_4(x_{48}, x_{50}) \text{ and } p_7(x_{47}, x_{49})) \Rightarrow p_4(f_{19}(x_{47}, x_{48}), f_{19}(x_{49}, x_{50}))$     cnf(p4<sub>26</sub>, negated\_conjecture)  
 $(p_4(x_{61}, x_{63}) \text{ and } p_4(x_{62}, x_{64})) \Rightarrow p_4(f_6(x_{61}, x_{62}), f_6(x_{63}, x_{64}))$     cnf(p4<sub>27</sub>, negated\_conjecture)  
 $p_2(x_{15}, f_3(c_{24})) \text{ or } p_{22}(f_{20}(x_{17}, x_{15}, x_{18}, x_{16}), f_{14}(f_{11}(x_{17}, f_{12}(x_{15}, x_{18}))))$     cnf(p2<sub>28</sub>, negated\_conjecture)  
 $(p_7(x_{65}, x_{68}) \text{ and } p_8(x_{66}, x_{69}) \text{ and } p_4(x_{67}, x_{70})) \Rightarrow p_4(f_9(x_{65}, x_{66}, x_{67}), f_9(x_{68}, x_{69}, x_{70}))$     cnf(p4<sub>29</sub>, negated\_conjecture)  
 $(p_2(x_{53}, x_{57}) \text{ and } p_4(x_{54}, x_{58}) \text{ and } p_2(x_{51}, x_{55}) \text{ and } p_2(x_{52}, x_{56})) \Rightarrow p_4(f_{20}(x_{51}, x_{52}, x_{53}, x_{54}), f_{20}(x_{55}, x_{56}, x_{57}, x_{58}))$     cnf(p  
 $p_{22}(x_{33}, f_{14}(f_{11}(c_{25}, f_{12}(c_{23}, c_{26})))) \Rightarrow p_{21}(f_5(f_6(c_{27}, f_9(f_{11}(c_{25}, f_{12}(c_{23}, c_{26}))), c_{28}, c_{27}))), f_5(f_6(c_{27}, x_{33})))$     cnf(p21<sub>31</sub>, negat  
 $\neg p_{21}(f_5(f_6(c_{27}, f_9(f_{11}(c_{25}, f_{12}(c_{23}, c_{26}))), c_{28}, c_{27}))), f_{15}(f_{19}(f_{11}(c_{25}, f_{12}(c_{23}, c_{26}))), c_{27}), f_{16}(f_3(f_{17}(f_{18}(c_{24}))))))$     cnf(not\_p21  
 $p_{22}(x_{19}, f_{14}(f_{11}(x_{17}, f_{12}(x_{15}, x_{18})))) \Rightarrow (p_2(x_{15}, f_3(c_{24})) \text{ or } p_{21}(f_5(f_6(x_{16}, f_{20}(x_{17}, x_{15}, x_{18}, x_{16}))), f_5(f_6(x_{16}, x_{19}))))$     cnf(p  
 $p_2(x_{15}, f_3(c_{24})) \text{ or } p_{21}(f_5(f_6(x_{16}, f_{20}(x_{17}, x_{15}, x_{18}, x_{16}))), f_{15}(f_{19}(f_{11}(x_{17}, f_{12}(x_{15}, x_{18}))), x_{16}), f_{16}(f_3(f_{17}(f_{18}(c_{24}))))))$     cnf(1

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$p_{11}(x_0, x_0)$     cnf(p11<sub>1</sub>, negated\_conjecture)  
 $p_9(x_{60}, x_{60})$     cnf(p9<sub>2</sub>, negated\_conjecture)  
 $p_8(x_{36}, x_{36})$     cnf(p8<sub>3</sub>, negated\_conjecture)  
 $p_3(x_{25}, x_{25})$     cnf(p3<sub>4</sub>, negated\_conjecture)  
 $p_2(x_9, x_9)$     cnf(p2<sub>5</sub>, negated\_conjecture)  
 $p_3(f_4(c_{23}), c_{24})$     cnf(p3<sub>6</sub>, negated\_conjecture)  
 $p_{19}(f_5(f_6(f_7(c_{25}))), c_{24})$     cnf(p19<sub>7</sub>, negated\_conjecture)  
 $p_8(f_{16}(x_{50}, f_{17}(x_{51}, x_{50})), x_{51})$     cnf(p8<sub>8</sub>, negated\_conjecture)  
 $(p_{21}(x_{18}) \text{ and } p_{11}(x_{18}, x_{17})) \Rightarrow p_{21}(x_{17})$     cnf(p21<sub>9</sub>, negated\_conjecture)  
 $p_2(x_3, x_4) \Rightarrow p_{11}(f_{13}(x_3), f_{13}(x_4))$     cnf(p11<sub>10</sub>, negated\_conjecture)  
 $p_3(x_{65}, x_{66}) \Rightarrow p_9(f_{15}(x_{65}), f_{15}(x_{66}))$     cnf(p9<sub>11</sub>, negated\_conjecture)  
 $p_8(x_{63}, x_{64}) \Rightarrow p_9(f_{10}(x_{63}), f_{10}(x_{64}))$     cnf(p9<sub>12</sub>, negated\_conjecture)  
 $p_9(x_{44}, x_{45}) \Rightarrow p_8(f_{14}(x_{44}), f_{14}(x_{45}))$     cnf(p8<sub>13</sub>, negated\_conjecture)  
 $p_3(x_{34}, x_{35}) \Rightarrow p_3(f_7(x_{34}), f_7(x_{35}))$     cnf(p3<sub>14</sub>, negated\_conjecture)  
 $p_3(x_{32}, x_{33}) \Rightarrow p_3(f_6(x_{32}), f_6(x_{33}))$     cnf(p3<sub>15</sub>, negated\_conjecture)  
 $p_3(x_{30}, x_{31}) \Rightarrow p_3(f_5(x_{30}), f_5(x_{31}))$     cnf(p3<sub>16</sub>, negated\_conjecture)  
 $p_2(x_{28}, x_{29}) \Rightarrow p_3(f_4(x_{28}), f_4(x_{29}))$     cnf(p3<sub>17</sub>, negated\_conjecture)  
 $\neg p_8(f_{12}(f_{13}(c_{26}), c_{27}), f_{14}(f_{15}(f_5(c_{25}))))$     cnf(not\_p8<sub>18</sub>, negated\_conjecture)  
 $(p_{11}(x_0, x_1) \text{ and } p_{11}(x_0, x_2)) \Rightarrow p_{11}(x_1, x_2)$     cnf(p11<sub>19</sub>, negated\_conjecture)  
 $(p_9(x_{60}, x_{61}) \text{ and } p_9(x_{60}, x_{62})) \Rightarrow p_9(x_{61}, x_{62})$     cnf(p9<sub>20</sub>, negated\_conjecture)  
 $(p_8(x_{36}, x_{37}) \text{ and } p_8(x_{36}, x_{38})) \Rightarrow p_8(x_{37}, x_{38})$     cnf(p8<sub>21</sub>, negated\_conjecture)  
 $(p_3(x_{25}, x_{26}) \text{ and } p_3(x_{25}, x_{27})) \Rightarrow p_3(x_{26}, x_{27})$     cnf(p3<sub>22</sub>, negated\_conjecture)  
 $(p_2(x_9, x_{10}) \text{ and } p_2(x_9, x_{11})) \Rightarrow p_2(x_{10}, x_{11})$     cnf(p2<sub>23</sub>, negated\_conjecture)  
 $p_8(f_{12}(f_{13}(c_{23}), x_{43}), f_{12}(f_{13}(c_{26}), f_{16}(c_{27}, x_{43})))$     cnf(p8<sub>24</sub>, negated\_conjecture)  
 $p_{20}(f_{10}(f_{12}(f_{13}(c_{26}), c_{27})), f_{10}(f_{12}(f_{13}(c_{26}), x_{16})))$     cnf(p20<sub>25</sub>, negated\_conjecture)  
 $\neg p_8(f_{12}(f_{13}(c_{23}), f_{17}(c_{28}, c_{27})), f_{12}(f_{13}(c_{26}), c_{28}))$     cnf(not\_p8<sub>26</sub>, negated\_conjecture)  
 $(p_3(x_7, x_5) \text{ and } p_3(x_8, x_6) \text{ and } p_{19}(x_7, x_8)) \Rightarrow p_{19}(x_5, x_6)$     cnf(p19<sub>27</sub>, negated\_conjecture)  
 $(p_3(x_{23}, x_{21}) \text{ and } p_3(x_{24}, x_{22}) \text{ and } p_{22}(x_{23}, x_{24})) \Rightarrow p_{22}(x_{21}, x_{22})$     cnf(p22<sub>28</sub>, negated\_conjecture)  
 $(p_9(x_{14}, x_{12}) \text{ and } p_9(x_{15}, x_{13}) \text{ and } p_{20}(x_{14}, x_{15})) \Rightarrow p_{20}(x_{12}, x_{13})$     cnf(p20<sub>29</sub>, negated\_conjecture)  
 $(p_2(x_{57}, x_{59}) \text{ and } p_3(x_{56}, x_{58})) \Rightarrow p_8(f_{18}(x_{56}, x_{57}), f_{18}(x_{58}, x_{59}))$     cnf(p8<sub>30</sub>, negated\_conjecture)  
 $(p_{11}(x_{39}, x_{41}) \text{ and } p_8(x_{40}, x_{42})) \Rightarrow p_8(f_{12}(x_{39}, x_{40}), f_{12}(x_{41}, x_{42}))$     cnf(p8<sub>31</sub>, negated\_conjecture)  
 $(p_8(x_{46}, x_{48}) \text{ and } p_8(x_{47}, x_{49})) \Rightarrow p_8(f_{16}(x_{46}, x_{47}), f_{16}(x_{48}, x_{49}))$     cnf(p8<sub>32</sub>, negated\_conjecture)  
 $(p_8(x_{52}, x_{54}) \text{ and } p_8(x_{53}, x_{55})) \Rightarrow p_8(f_{17}(x_{52}, x_{53}), f_{17}(x_{54}, x_{55}))$     cnf(p8<sub>33</sub>, negated\_conjecture)  
 $(p_{22}(x_{20}, c_{24}) \text{ and } p_3(f_4(x_{19}), x_{20})) \Rightarrow (p_{21}(f_{13}(x_{19})) \text{ or } p_8(f_{12}(f_{13}(x_{19}), f_{18}(x_{20}, x_{19})), f_{14}(f_{15}(f_5(c_{25}))))))$     cnf(p21<sub>34</sub>, negat

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$p_{10}(x_0, x_0)$     cnf(p10<sub>1</sub>, negated\_conjecture)  
 $p_8(x_{58}, x_{58})$     cnf(p8<sub>2</sub>, negated\_conjecture)  
 $p_7(x_{51}, x_{51})$     cnf(p7<sub>3</sub>, negated\_conjecture)

$p_5(x_{48}, x_{48})$      $\text{cnf}(p_{5_4}, \text{negated\_conjecture})$   
 $p_3(x_{37}, x_{37})$      $\text{cnf}(p_{3_5}, \text{negated\_conjecture})$   
 $p_2(x_{30}, x_{30})$      $\text{cnf}(p_{2_6}, \text{negated\_conjecture})$   
 $p_{17}(x_{23}, x_{23})$      $\text{cnf}(p_{17_7}, \text{negated\_conjecture})$   
 $p_{14}(x_{10}, x_{10})$      $\text{cnf}(p_{14_8}, \text{negated\_conjecture})$   
 $p_{12}(x_3, x_3)$      $\text{cnf}(p_{12_9}, \text{negated\_conjecture})$   
 $p_{18}(c_{26}, c_{25})$      $\text{cnf}(p_{18_{10}}, \text{negated\_conjecture})$   
 $p_3(c_{22}, c_{23})$      $\text{cnf}(p_{3_{11}}, \text{negated\_conjecture})$   
 $p_2(c_{24}, c_{25})$      $\text{cnf}(p_{2_{12}}, \text{negated\_conjecture})$   
 $\neg p_{16}(c_{22}, c_{21})$      $\text{cnf}(\text{not\_}p_{16_{13}}, \text{negated\_conjecture})$   
 $p_3(c_{23}, f_4(c_{24}, c_{20}))$      $\text{cnf}(p_{3_{14}}, \text{negated\_conjecture})$   
 $p_{16}(f_4(c_{19}, c_{20}), c_{21})$      $\text{cnf}(p_{16_{15}}, \text{negated\_conjecture})$   
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2)$      $\text{cnf}(p_{10_{16}}, \text{negated\_conjecture})$   
 $(p_8(x_{58}, x_{59}) \text{ and } p_8(x_{58}, x_{60})) \Rightarrow p_8(x_{59}, x_{60})$      $\text{cnf}(p_{8_{17}}, \text{negated\_conjecture})$   
 $(p_7(x_{51}, x_{52}) \text{ and } p_7(x_{51}, x_{53})) \Rightarrow p_7(x_{52}, x_{53})$      $\text{cnf}(p_{7_{18}}, \text{negated\_conjecture})$   
 $(p_5(x_{48}, x_{49}) \text{ and } p_5(x_{48}, x_{50})) \Rightarrow p_5(x_{49}, x_{50})$      $\text{cnf}(p_{5_{19}}, \text{negated\_conjecture})$   
 $(p_3(x_{37}, x_{38}) \text{ and } p_3(x_{37}, x_{39})) \Rightarrow p_3(x_{38}, x_{39})$      $\text{cnf}(p_{3_{20}}, \text{negated\_conjecture})$   
 $(p_2(x_{30}, x_{31}) \text{ and } p_2(x_{30}, x_{32})) \Rightarrow p_2(x_{31}, x_{32})$      $\text{cnf}(p_{2_{21}}, \text{negated\_conjecture})$   
 $(p_{17}(x_{23}, x_{24}) \text{ and } p_{17}(x_{23}, x_{25})) \Rightarrow p_{17}(x_{24}, x_{25})$      $\text{cnf}(p_{17_{22}}, \text{negated\_conjecture})$   
 $(p_{14}(x_{10}, x_{11}) \text{ and } p_{14}(x_{10}, x_{12})) \Rightarrow p_{14}(x_{11}, x_{12})$      $\text{cnf}(p_{14_{23}}, \text{negated\_conjecture})$   
 $(p_{12}(x_3, x_4) \text{ and } p_{12}(x_3, x_5)) \Rightarrow p_{12}(x_4, x_5)$      $\text{cnf}(p_{12_{24}}, \text{negated\_conjecture})$   
 $p_{16}(f_4(f_6(c_{27}, c_{25}), x_{21}), x_{22}) \Rightarrow p_{16}(f_4(c_{25}, x_{21}), x_{22})$      $\text{cnf}(p_{16_{25}}, \text{negated\_conjecture})$   
 $(p_3(x_{15}, x_{13}) \text{ and } p_8(x_{16}, x_{14}) \text{ and } p_{16}(x_{15}, x_{16})) \Rightarrow p_{16}(x_{13}, x_{14})$      $\text{cnf}(p_{16_{26}}, \text{negated\_conjecture})$   
 $(p_{18}(x_{28}, x_{29}) \text{ and } p_2(x_{29}, x_{27}) \text{ and } p_{17}(x_{28}, x_{26})) \Rightarrow p_{18}(x_{26}, x_{27})$      $\text{cnf}(p_{18_{27}}, \text{negated\_conjecture})$   
 $(p_2(x_{62}, x_{64}) \text{ and } p_7(x_{61}, x_{63})) \Rightarrow p_8(f_9(x_{61}, x_{62}), f_9(x_{63}, x_{64}))$      $\text{cnf}(p_{8_{28}}, \text{negated\_conjecture})$   
 $(p_{14}(x_6, x_8) \text{ and } p_2(x_7, x_9)) \Rightarrow p_{12}(f_{15}(x_6, x_7), f_{15}(x_8, x_9))$      $\text{cnf}(p_{12_{29}}, \text{negated\_conjecture})$   
 $(p_2(x_{34}, x_{36}) \text{ and } p_5(x_{33}, x_{35})) \Rightarrow p_2(f_6(x_{33}, x_{34}), f_6(x_{35}, x_{36}))$      $\text{cnf}(p_{2_{30}}, \text{negated\_conjecture})$   
 $(p_{12}(x_{40}, x_{42}) \text{ and } p_2(x_{41}, x_{43})) \Rightarrow p_3(f_{13}(x_{40}, x_{41}), f_{13}(x_{42}, x_{43}))$      $\text{cnf}(p_{3_{31}}, \text{negated\_conjecture})$   
 $(p_2(x_{44}, x_{46}) \text{ and } p_3(x_{45}, x_{47})) \Rightarrow p_3(f_4(x_{44}, x_{45}), f_4(x_{46}, x_{47}))$      $\text{cnf}(p_{3_{32}}, \text{negated\_conjecture})$   
 $(p_{10}(x_{54}, x_{56}) \text{ and } p_2(x_{55}, x_{57})) \Rightarrow p_7(f_{11}(x_{54}, x_{55}), f_{11}(x_{56}, x_{57}))$      $\text{cnf}(p_{7_{33}}, \text{negated\_conjecture})$   
 $(p_2(x_{17}, x_{20}) \text{ and } p_{18}(c_{26}, x_{20}) \text{ and } p_{16}(f_4(c_{19}, x_{18}), x_{19}) \text{ and } p_{16}(f_4(x_{20}, f_{13}(f_{15}(c_{28}, x_{17}), x_{20})), f_9(f_{11}(c_{29}, x_{17}), x_{20}))) \Rightarrow$   
 $p_{16}(f_4(x_{17}, x_{18}), x_{19})$      $\text{cnf}(p_{16_{34}}, \text{negated\_conjecture})$   
 $(p_2(x_{17}, x_{20}) \text{ and } p_{18}(c_{26}, x_{20}) \text{ and } p_{16}(f_4(c_{19}, x_{18}), x_{19})) \Rightarrow (p_{16}(f_4(x_{17}, x_{18}), x_{19}) \text{ or } p_{16}(f_4(f_6(c_{27}, x_{20}), f_{13}(f_{15}(c_{28}, x_{17}), x_{20})), x_{20}))$

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$p_{10}(x_0, x_0)$      $\text{cnf}(p_{10_1}, \text{negated\_conjecture})$   
 $p_5(x_{57}, x_{57})$      $\text{cnf}(p_{5_2}, \text{negated\_conjecture})$   
 $p_3(x_{46}, x_{46})$      $\text{cnf}(p_{3_3}, \text{negated\_conjecture})$   
 $p_2(x_{34}, x_{34})$      $\text{cnf}(p_{2_4}, \text{negated\_conjecture})$   
 $p_{11}(x_{21}, x_{21})$      $\text{cnf}(p_{11_5}, \text{negated\_conjecture})$   
 $\neg p_{18}(f_6(c_{24}))$      $\text{cnf}(f6\_is\_not\_p_{18_6}, \text{negated\_conjecture})$   
 $\neg p_{18}(f_6(c_{22}))$      $\text{cnf}(f6\_is\_not\_p_{18_7}, \text{negated\_conjecture})$   
 $p_3(f_4(c_{22}), c_{23})$      $\text{cnf}(p_{3_8}, \text{negated\_conjecture})$   
 $p_{19}(f_7(f_8(f_9(c_{25}))), c_{23})$      $\text{cnf}(p_{19_9}, \text{negated\_conjecture})$   
 $(p_{18}(x_{29}) \text{ and } p_5(x_{29}, x_{28})) \Rightarrow p_{18}(x_{28})$      $\text{cnf}(p_{18_{10}}, \text{negated\_conjecture})$   
 $p_{10}(f_{16}(x_{16}, f_{14}(f_{15}(f_7(c_{25}))))), x_{16})$      $\text{cnf}(p_{10_{11}}, \text{negated\_conjecture})$   
 $p_{11}(x_{10}, x_{11}) \Rightarrow p_{10}(f_{14}(x_{10}), f_{14}(x_{11}))$      $\text{cnf}(p_{10_{12}}, \text{negated\_conjecture})$   
 $p_2(x_{60}, x_{61}) \Rightarrow p_5(f_6(x_{60}), f_6(x_{61}))$      $\text{cnf}(p_{5_{13}}, \text{negated\_conjecture})$   
 $p_3(x_{55}, x_{56}) \Rightarrow p_3(f_9(x_{55}), f_9(x_{56}))$      $\text{cnf}(p_{3_{14}}, \text{negated\_conjecture})$   
 $p_3(x_{53}, x_{54}) \Rightarrow p_3(f_8(x_{53}), f_8(x_{54}))$      $\text{cnf}(p_{3_{15}}, \text{negated\_conjecture})$   
 $p_3(x_{51}, x_{52}) \Rightarrow p_3(f_7(x_{51}), f_7(x_{52}))$      $\text{cnf}(p_{3_{16}}, \text{negated\_conjecture})$   
 $p_2(x_{49}, x_{50}) \Rightarrow p_3(f_4(x_{49}), f_4(x_{50}))$      $\text{cnf}(p_{3_{17}}, \text{negated\_conjecture})$   
 $p_3(x_{26}, x_{27}) \Rightarrow p_{11}(f_{15}(x_{26}), f_{15}(x_{27}))$      $\text{cnf}(p_{11_{18}}, \text{negated\_conjecture})$   
 $p_{10}(x_{24}, x_{25}) \Rightarrow p_{11}(f_{12}(x_{24}), f_{12}(x_{25}))$      $\text{cnf}(p_{11_{19}}, \text{negated\_conjecture})$   
 $\neg p_{10}(f_{13}(f_6(c_{24}), c_{26}), f_{14}(f_{15}(f_7(c_{25}))))$      $\text{cnf}(\text{not\_}p_{10_{20}}, \text{negated\_conjecture})$   
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2)$      $\text{cnf}(p_{10_{21}}, \text{negated\_conjecture})$   
 $(p_5(x_{57}, x_{58}) \text{ and } p_5(x_{57}, x_{59})) \Rightarrow p_5(x_{58}, x_{59})$      $\text{cnf}(p_{5_{22}}, \text{negated\_conjecture})$   
 $(p_3(x_{46}, x_{47}) \text{ and } p_3(x_{46}, x_{48})) \Rightarrow p_3(x_{47}, x_{48})$      $\text{cnf}(p_{3_{23}}, \text{negated\_conjecture})$   
 $(p_2(x_{34}, x_{35}) \text{ and } p_2(x_{34}, x_{36})) \Rightarrow p_2(x_{35}, x_{36})$      $\text{cnf}(p_{2_{24}}, \text{negated\_conjecture})$   
 $(p_{11}(x_{21}, x_{22}) \text{ and } p_{11}(x_{21}, x_{23})) \Rightarrow p_{11}(x_{22}, x_{23})$      $\text{cnf}(p_{11_{25}}, \text{negated\_conjecture})$

$p_{10}(f_{13}(f_6(c_{22}), x_9), f_{13}(f_6(c_{24}), f_{16}(c_{26}, x_9)))$      $\text{cnf}(p_{10_{26}}, \text{negated\_conjecture})$   
 $p_{20}(f_{12}(f_{13}(f_6(c_{24}), c_{26})), f_{12}(f_{13}(f_6(c_{24}), x_{41})))$      $\text{cnf}(p_{20_{27}}, \text{negated\_conjecture})$   
 $\neg p_{10}(f_{13}(f_6(c_{24}), c_{26}), f_{13}(f_6(c_{22}), f_{14}(f_{15}(f_7(c_{25}))))))$      $\text{cnf}(\text{not\_}p_{10_{28}}, \text{negated\_conjecture})$   
 $(p_3(x_{44}, x_{42}) \text{ and } p_3(x_{45}, x_{43}) \text{ and } p_{21}(x_{44}, x_{45})) \Rightarrow p_{21}(x_{42}, x_{43})$      $\text{cnf}(p_{21_{29}}, \text{negated\_conjecture})$   
 $(p_3(x_{32}, x_{30}) \text{ and } p_3(x_{33}, x_{31}) \text{ and } p_{19}(x_{32}, x_{33})) \Rightarrow p_{19}(x_{30}, x_{31})$      $\text{cnf}(p_{19_{30}}, \text{negated\_conjecture})$   
 $(p_{11}(x_{40}, x_{38}) \text{ and } p_{20}(x_{39}, x_{40}) \text{ and } p_{11}(x_{39}, x_{37})) \Rightarrow p_{20}(x_{37}, x_{38})$      $\text{cnf}(p_{20_{31}}, \text{negated\_conjecture})$   
 $(p_{10}(x_4, x_6) \text{ and } p_5(x_3, x_5)) \Rightarrow p_{10}(f_{13}(x_3, x_4), f_{13}(x_5, x_6))$      $\text{cnf}(p_{10_{32}}, \text{negated\_conjecture})$   
 $(p_2(x_{18}, x_{20}) \text{ and } p_3(x_{17}, x_{19})) \Rightarrow p_{10}(f_{17}(x_{17}, x_{18}), f_{17}(x_{19}, x_{20}))$      $\text{cnf}(p_{10_{33}}, \text{negated\_conjecture})$   
 $(p_{10}(x_{12}, x_{14}) \text{ and } p_{10}(x_{13}, x_{15})) \Rightarrow p_{10}(f_{16}(x_{12}, x_{13}), f_{16}(x_{14}, x_{15}))$      $\text{cnf}(p_{10_{34}}, \text{negated\_conjecture})$   
 $(p_{21}(x_8, c_{23}) \text{ and } p_3(f_4(x_7), x_8)) \Rightarrow (p_{18}(f_6(x_7)) \text{ or } p_{10}(f_{13}(f_6(x_7), f_{17}(x_8, x_7)), f_{14}(f_{15}(f_7(c_{25}))))))$      $\text{cnf}(p_{18_{35}}, \text{negated\_conjecture})$

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$p_{15}(c_{21})$      $\text{cnf}(c_{21\_is\_}p_{15_1}, \text{negated\_conjecture})$   
 $p_{10}(x_0, x_0)$      $\text{cnf}(p_{10_2}, \text{negated\_conjecture})$   
 $p_8(x_{71}, x_{71})$      $\text{cnf}(p_{8_3}, \text{negated\_conjecture})$   
 $p_6(x_{68}, x_{68})$      $\text{cnf}(p_{6_4}, \text{negated\_conjecture})$   
 $p_5(x_{47}, x_{47})$      $\text{cnf}(p_{5_5}, \text{negated\_conjecture})$   
 $p_3(x_{40}, x_{40})$      $\text{cnf}(p_{3_6}, \text{negated\_conjecture})$   
 $p_2(x_{33}, x_{33})$      $\text{cnf}(p_{2_7}, \text{negated\_conjecture})$   
 $\neg p_{15}(f_4(f_7(c_{19}, c_{20}), c_{21}))$      $\text{cnf}(f_{4\_is\_not\_}p_{15_8}, \text{negated\_conjecture})$   
 $p_5(x_{15}, x_{16}) \Rightarrow p_{16}(x_{14}, x_{15}, x_{16})$      $\text{cnf}(p_{16_9}, \text{negated\_conjecture})$   
 $p_{15}(x_7) \Rightarrow \neg p_{18}(f_9(x_7), x_{76}, x_{76})$      $\text{cnf}(\text{not\_}p_{15_{10}}, \text{negated\_conjecture})$   
 $(p_{15}(x_6) \text{ and } p_3(x_6, x_5)) \Rightarrow p_{15}(x_5)$      $\text{cnf}(p_{15_{11}}, \text{negated\_conjecture})$   
 $p_6(x_3, x_4) \Rightarrow p_{10}(f_{11}(x_3), f_{11}(x_4))$      $\text{cnf}(p_{10_{12}}, \text{negated\_conjecture})$   
 $p_3(x_{74}, x_{75}) \Rightarrow p_8(f_9(x_{74}), f_9(x_{75}))$      $\text{cnf}(p_{8_{13}}, \text{negated\_conjecture})$   
 $p_3(x_{66}, x_{67}) \Rightarrow p_5(f_{14}(x_{66}), f_{14}(x_{67}))$      $\text{cnf}(p_{5_{14}}, \text{negated\_conjecture})$   
 $p_{15}(x_7) \text{ or } p_{18}(f_9(x_7), f_{14}(x_7), f_{14}(x_7))$      $\text{cnf}(p_{15_{15}}, \text{negated\_conjecture})$   
 $p_{17}(x_{77}, f_{11}(c_{20})) \Rightarrow \neg p_{16}(f_9(c_{21}), x_{77}, c_{19})$      $\text{cnf}(\text{not\_}p_{17_{16}}, \text{negated\_conjecture})$   
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2)$      $\text{cnf}(p_{10_{17}}, \text{negated\_conjecture})$   
 $(p_8(x_{71}, x_{72}) \text{ and } p_8(x_{71}, x_{73})) \Rightarrow p_8(x_{72}, x_{73})$      $\text{cnf}(p_{8_{18}}, \text{negated\_conjecture})$   
 $(p_6(x_{68}, x_{69}) \text{ and } p_6(x_{68}, x_{70})) \Rightarrow p_6(x_{69}, x_{70})$      $\text{cnf}(p_{6_{19}}, \text{negated\_conjecture})$   
 $(p_5(x_{47}, x_{48}) \text{ and } p_5(x_{47}, x_{49})) \Rightarrow p_5(x_{48}, x_{49})$      $\text{cnf}(p_{5_{20}}, \text{negated\_conjecture})$   
 $(p_3(x_{40}, x_{41}) \text{ and } p_3(x_{40}, x_{42})) \Rightarrow p_3(x_{41}, x_{42})$      $\text{cnf}(p_{3_{21}}, \text{negated\_conjecture})$   
 $(p_2(x_{33}, x_{34}) \text{ and } p_2(x_{33}, x_{35})) \Rightarrow p_2(x_{34}, x_{35})$      $\text{cnf}(p_{2_{22}}, \text{negated\_conjecture})$   
 $(p_{16}(x_{14}, x_{15}, x_{17}) \text{ and } p_{16}(x_{14}, x_{17}, x_{16})) \Rightarrow p_{16}(x_{14}, x_{15}, x_{16})$      $\text{cnf}(p_{16_{23}}, \text{negated\_conjecture})$   
 $(p_{17}(x_{26}, x_{25}) \text{ and } p_5(x_{26}, x_{23}) \text{ and } p_{10}(x_{25}, x_{24})) \Rightarrow p_{17}(x_{23}, x_{24})$      $\text{cnf}(p_{17_{24}}, \text{negated\_conjecture})$   
 $(p_2(x_{43}, x_{45}) \text{ and } p_3(x_{44}, x_{46})) \Rightarrow p_3(f_4(x_{43}, x_{44}), f_4(x_{45}, x_{46}))$      $\text{cnf}(p_{3_{25}}, \text{negated\_conjecture})$   
 $(p_5(x_{36}, x_{38}) \text{ and } p_6(x_{37}, x_{39})) \Rightarrow p_2(f_7(x_{36}, x_{37}), f_7(x_{38}, x_{39}))$      $\text{cnf}(p_{2_{26}}, \text{negated\_conjecture})$   
 $p_{16}(x_{14}, x_{15}, x_{16}) \Rightarrow (p_5(x_{15}, x_{16}) \text{ or } p_{16}(x_{14}, x_{15}, f_{13}(x_{14}, x_{15}, x_{16})))$      $\text{cnf}(p_{5_{27}}, \text{negated\_conjecture})$   
 $p_{16}(x_{14}, x_{15}, x_{16}) \Rightarrow (p_5(x_{15}, x_{16}) \text{ or } p_{16}(x_{14}, f_{13}(x_{14}, x_{15}, x_{16}), x_{16}))$      $\text{cnf}(p_{5_{28}}, \text{negated\_conjecture})$   
 $(p_8(x_{11}, x_8) \text{ and } p_5(x_{13}, x_{10}) \text{ and } p_5(x_{12}, x_9) \text{ and } p_{16}(x_{11}, x_{12}, x_{13})) \Rightarrow p_{16}(x_8, x_9, x_{10})$      $\text{cnf}(p_{16_{29}}, \text{negated\_conjecture})$   
 $(p_8(x_{30}, x_{27}) \text{ and } p_5(x_{32}, x_{29}) \text{ and } p_5(x_{31}, x_{28}) \text{ and } p_{18}(x_{30}, x_{31}, x_{32})) \Rightarrow p_{18}(x_{27}, x_{28}, x_{29})$      $\text{cnf}(p_{18_{30}}, \text{negated\_conjecture})$   
 $(p_5(x_{62}, x_{65}) \text{ and } p_8(x_{60}, x_{63}) \text{ and } p_5(x_{61}, x_{64})) \Rightarrow p_5(f_{13}(x_{60}, x_{61}, x_{62}), f_{13}(x_{63}, x_{64}, x_{65}))$      $\text{cnf}(p_{5_{31}}, \text{negated\_conjecture})$   
 $p_{18}(f_9(f_4(f_7(x_{20}, x_{22}), x_{18})), x_{19}, x_{21}) \Rightarrow (p_{16}(f_9(x_{18}), x_{19}, x_{20}) \text{ or } p_{18}(f_9(x_{18}), x_{19}, x_{21}))$      $\text{cnf}(p_{16_{32}}, \text{negated\_conjecture})$   
 $p_{18}(f_9(f_4(f_7(x_{20}, x_{22}), x_{18})), x_{19}, x_{21}) \Rightarrow (p_{18}(f_9(x_{18}), x_{19}, x_{21}) \text{ or } p_{17}(f_{12}(x_{18}, x_{20}, x_{22}, x_{19}, x_{21}), f_{11}(x_{22})))$      $\text{cnf}(p_{18_{33}}, \text{negated\_conjecture})$   
 $p_{18}(f_9(f_4(f_7(x_{20}, x_{22}), x_{18})), x_{19}, x_{21}) \Rightarrow (p_{18}(f_9(x_{18}), x_{19}, x_{21}) \text{ or } p_{16}(f_9(x_{18}), f_{12}(x_{18}, x_{20}, x_{22}, x_{19}, x_{21}), x_{21}))$      $\text{cnf}(p_{18_{34}}, \text{negated\_conjecture})$   
 $(p_5(x_{54}, x_{59}) \text{ and } p_6(x_{52}, x_{57}) \text{ and } p_3(x_{50}, x_{55}) \text{ and } p_5(x_{51}, x_{56}) \text{ and } p_5(x_{53}, x_{58})) \Rightarrow p_5(f_{12}(x_{50}, x_{51}, x_{52}, x_{53}, x_{54}), f_{12}(x_{55}, x_{56}, x_{57}, x_{58}))$

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$p_{11}(x_0, x_0)$      $\text{cnf}(p_{11_1}, \text{negated\_conjecture})$   
 $p_7(x_{54}, x_{54})$      $\text{cnf}(p_{7_2}, \text{negated\_conjecture})$   
 $p_6(x_{47}, x_{47})$      $\text{cnf}(p_{6_3}, \text{negated\_conjecture})$   
 $p_3(x_{38}, x_{38})$      $\text{cnf}(p_{3_4}, \text{negated\_conjecture})$   
 $p_2(x_{33}, x_{33})$      $\text{cnf}(p_{2_5}, \text{negated\_conjecture})$   
 $p_{11}(f_{13}(f_{12}(x_5)), x_5)$      $\text{cnf}(p_{11_6}, \text{negated\_conjecture})$   
 $p_{14}(f_4(f_5(c_{20})), f_4(c_{21}))$      $\text{cnf}(p_{14_7}, \text{negated\_conjecture})$   
 $p_{15}(x_{14}, x_{15}) \Rightarrow p_{16}(x_{14}, x_{15})$      $\text{cnf}(p_{16_8}, \text{negated\_conjecture})$   
 $p_{15}(c_{22}, f_8(f_5(c_{20}), f_9(c_{23}, c_{24})))$      $\text{cnf}(p_{15_9}, \text{negated\_conjecture})$   
 $p_7(f_{12}(f_{13}(x_{20})), x_{20}) \Rightarrow p_{16}(c_{22}, x_{20})$      $\text{cnf}(p_{16_{10}}, \text{negated\_conjecture})$   
 $p_7(x_3, x_4) \Rightarrow p_{11}(f_{13}(x_3), f_{13}(x_4))$      $\text{cnf}(p_{11_{11}}, \text{negated\_conjecture})$



$p_{11}(x_{57}, x_{58}) \Rightarrow p_7(f_{12}(x_{57}), f_{12}(x_{58}))$     cnf(p7<sub>12</sub>, negated\_conjecture)  
 $p_2(x_{45}, x_{46}) \Rightarrow p_3(f_4(x_{45}), f_4(x_{46}))$     cnf(p3<sub>13</sub>, negated\_conjecture)  
 $p_2(x_{36}, x_{37}) \Rightarrow p_2(f_5(x_{36}), f_5(x_{37}))$     cnf(p2<sub>14</sub>, negated\_conjecture)  
 $p_{16}(c_{22}, x_{20}) \Rightarrow p_7(f_{12}(f_{13}(x_{20})), x_{20})$     cnf(p7<sub>15</sub>, negated\_conjecture)  
 $(p_{11}(x_0, x_1) \text{ and } p_{11}(x_0, x_2)) \Rightarrow p_{11}(x_1, x_2)$     cnf(p11<sub>16</sub>, negated\_conjecture)  
 $(p_7(x_{54}, x_{55}) \text{ and } p_7(x_{54}, x_{56})) \Rightarrow p_7(x_{55}, x_{56})$     cnf(p7<sub>17</sub>, negated\_conjecture)  
 $(p_6(x_{47}, x_{48}) \text{ and } p_6(x_{47}, x_{49})) \Rightarrow p_6(x_{48}, x_{49})$     cnf(p6<sub>18</sub>, negated\_conjecture)  
 $(p_3(x_{38}, x_{39}) \text{ and } p_3(x_{38}, x_{40})) \Rightarrow p_3(x_{39}, x_{40})$     cnf(p3<sub>19</sub>, negated\_conjecture)  
 $(p_2(x_{33}, x_{34}) \text{ and } p_2(x_{33}, x_{35})) \Rightarrow p_2(x_{34}, x_{35})$     cnf(p2<sub>20</sub>, negated\_conjecture)  
 $(p_{16}(x_{14}, x_{15}) \text{ and } p_{19}(x_{14}, x_{15})) \Rightarrow p_{15}(x_{14}, x_{15})$     cnf(p15<sub>21</sub>, negated\_conjecture)  
 $(p_{16}(x_{14}, x_{15}) \text{ and } p_{18}(x_{14}, x_{15})) \Rightarrow p_{15}(x_{14}, x_{15})$     cnf(p15<sub>22</sub>, negated\_conjecture)  
 $(p_{16}(x_{14}, x_{15}) \text{ and } p_{17}(x_{14}, x_{15})) \Rightarrow p_{15}(x_{14}, x_{15})$     cnf(p15<sub>23</sub>, negated\_conjecture)  
 $\neg p_{15}(c_{22}, f_{12}(f_{13}(f_8(f_5(c_{20})), f_9(c_{23}, c_{24}))))$     cnf(not\_p15<sub>24</sub>, negated\_conjecture)  
 $p_{15}(x_{14}, x_{15}) \Rightarrow (p_{17}(x_{14}, x_{15}) \text{ or } p_{18}(x_{14}, x_{15}) \text{ or } p_{19}(x_{14}, x_{15}))$     cnf(p17<sub>25</sub>, negated\_conjecture)  
 $(p_3(x_8, x_6) \text{ and } p_3(x_9, x_7) \text{ and } p_{14}(x_8, x_9)) \Rightarrow p_{14}(x_6, x_7)$     cnf(p14<sub>26</sub>, negated\_conjecture)  
 $(p_6(x_{31}, x_{29}) \text{ and } p_7(x_{32}, x_{30}) \text{ and } p_{19}(x_{31}, x_{32})) \Rightarrow p_{19}(x_{29}, x_{30})$     cnf(p19<sub>27</sub>, negated\_conjecture)  
 $(p_6(x_{27}, x_{25}) \text{ and } p_7(x_{28}, x_{26}) \text{ and } p_{18}(x_{27}, x_{28})) \Rightarrow p_{18}(x_{25}, x_{26})$     cnf(p18<sub>28</sub>, negated\_conjecture)  
 $(p_6(x_{23}, x_{21}) \text{ and } p_7(x_{24}, x_{22}) \text{ and } p_{17}(x_{23}, x_{24})) \Rightarrow p_{17}(x_{21}, x_{22})$     cnf(p17<sub>29</sub>, negated\_conjecture)  
 $(p_6(x_{18}, x_{16}) \text{ and } p_7(x_{19}, x_{17}) \text{ and } p_{16}(x_{18}, x_{19})) \Rightarrow p_{16}(x_{16}, x_{17})$     cnf(p16<sub>30</sub>, negated\_conjecture)  
 $(p_6(x_{12}, x_{10}) \text{ and } p_7(x_{13}, x_{11}) \text{ and } p_{15}(x_{12}, x_{13})) \Rightarrow p_{15}(x_{10}, x_{11})$     cnf(p15<sub>31</sub>, negated\_conjecture)  
 $p_3(f_{10}(c_{22}, f_{12}(f_{13}(f_8(f_5(c_{20})), f_9(c_{23}, c_{24}))))), f_4(c_{21}))$     cnf(p3<sub>32</sub>, negated\_conjecture)  
 $(p_2(x_{59}, x_{61}) \text{ and } p_6(x_{60}, x_{62})) \Rightarrow p_7(f_8(x_{59}, x_{60}), f_8(x_{61}, x_{62}))$     cnf(p7<sub>33</sub>, negated\_conjecture)  
 $(p_6(x_{41}, x_{43}) \text{ and } p_7(x_{42}, x_{44})) \Rightarrow p_3(f_{10}(x_{41}, x_{42}), f_{10}(x_{43}, x_{44}))$     cnf(p3<sub>34</sub>, negated\_conjecture)  
 $(p_2(x_{51}, x_{53}) \text{ and } p_2(x_{50}, x_{52})) \Rightarrow p_6(f_9(x_{50}, x_{51}), f_9(x_{52}, x_{53}))$     cnf(p6<sub>35</sub>, negated\_conjecture)

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$p_{10}(x_0, x_0)$     cnf(p10<sub>1</sub>, negated\_conjecture)  
 $p_8(x_{70}, x_{70})$     cnf(p8<sub>2</sub>, negated\_conjecture)  
 $p_6(x_{67}, x_{67})$     cnf(p6<sub>3</sub>, negated\_conjecture)  
 $p_5(x_{64}, x_{64})$     cnf(p5<sub>4</sub>, negated\_conjecture)  
 $p_3(x_{40}, x_{40})$     cnf(p3<sub>5</sub>, negated\_conjecture)  
 $p_2(x_{33}, x_{33})$     cnf(p2<sub>6</sub>, negated\_conjecture)  
 $p_{15}(c_{18}, c_{19})$     cnf(p15<sub>7</sub>, negated\_conjecture)  
 $\neg p_3(c_{23}, c_{24})$     cnf(not\_p3<sub>8</sub>, negated\_conjecture)  
 $p_3(c_{23}, f_4(f_7(c_{17}, c_{18}), c_{21}))$     cnf(p3<sub>9</sub>, negated\_conjecture)  
 $p_{16}(c_{17}, c_{20}, f_9(c_{19}, c_{18}), c_{21}, c_{22})$     cnf(p16<sub>10</sub>, negated\_conjecture)  
 $p_6(x_{55}, x_{56}) \Rightarrow p_3(f_{14}(x_{55}), f_{14}(x_{56}))$     cnf(p3<sub>11</sub>, negated\_conjecture)  
 $p_{10}(x_7, x_8) \Rightarrow p_{10}(f_{12}(x_7), f_{12}(x_8))$     cnf(p10<sub>12</sub>, negated\_conjecture)  
 $p_6(x_{53}, x_{54}) \Rightarrow p_3(f_{13}(x_{53}), f_{13}(x_{54}))$     cnf(p3<sub>13</sub>, negated\_conjecture)  
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2)$     cnf(p10<sub>14</sub>, negated\_conjecture)  
 $(p_8(x_{70}, x_{71}) \text{ and } p_8(x_{70}, x_{72})) \Rightarrow p_8(x_{71}, x_{72})$     cnf(p8<sub>15</sub>, negated\_conjecture)  
 $(p_6(x_{67}, x_{68}) \text{ and } p_6(x_{67}, x_{69})) \Rightarrow p_6(x_{68}, x_{69})$     cnf(p6<sub>16</sub>, negated\_conjecture)  
 $(p_5(x_{64}, x_{65}) \text{ and } p_5(x_{64}, x_{66})) \Rightarrow p_5(x_{65}, x_{66})$     cnf(p5<sub>17</sub>, negated\_conjecture)  
 $(p_3(x_{40}, x_{41}) \text{ and } p_3(x_{40}, x_{42})) \Rightarrow p_3(x_{41}, x_{42})$     cnf(p3<sub>18</sub>, negated\_conjecture)  
 $(p_2(x_{33}, x_{34}) \text{ and } p_2(x_{33}, x_{35})) \Rightarrow p_2(x_{34}, x_{35})$     cnf(p2<sub>19</sub>, negated\_conjecture)  
 $p_{15}(x_{32}, c_{19}) \Rightarrow p_3(c_{24}, f_4(f_7(c_{17}, x_{32}), f_{14}(x_{32})))$     cnf(p3<sub>20</sub>, negated\_conjecture)  
 $p_{15}(x_{31}, c_{19}) \Rightarrow p_3(c_{23}, f_4(f_7(c_{17}, x_{31}), f_{13}(x_{31})))$     cnf(p3<sub>21</sub>, negated\_conjecture)  
 $p_{15}(x_{31}, c_{19}) \Rightarrow p_{16}(c_{17}, c_{20}, f_9(c_{19}, x_{31}), f_{13}(x_{31}), c_{22})$     cnf(p16<sub>22</sub>, negated\_conjecture)  
 $p_{15}(x_{32}, c_{19}) \Rightarrow p_{16}(c_{17}, c_{20}, f_9(c_{19}, x_{32}), f_{14}(x_{32}), c_{25})$     cnf(p16<sub>23</sub>, negated\_conjecture)  
 $(p_6(x_{14}, x_{12}) \text{ and } p_8(x_{15}, x_{13}) \text{ and } p_{15}(x_{14}, x_{15})) \Rightarrow p_{15}(x_{12}, x_{13})$     cnf(p15<sub>24</sub>, negated\_conjecture)  
 $(p_6(x_{74}, x_{76}) \text{ and } p_8(x_{73}, x_{75})) \Rightarrow p_8(f_9(x_{73}, x_{74}), f_9(x_{75}, x_{76}))$     cnf(p8<sub>25</sub>, negated\_conjecture)  
 $(p_5(x_{36}, x_{38}) \text{ and } p_6(x_{37}, x_{39})) \Rightarrow p_2(f_7(x_{36}, x_{37}), f_7(x_{38}, x_{39}))$     cnf(p2<sub>26</sub>, negated\_conjecture)  
 $(p_2(x_{57}, x_{59}) \text{ and } p_3(x_{58}, x_{60})) \Rightarrow p_3(f_4(x_{57}, x_{58}), f_4(x_{59}, x_{60}))$     cnf(p3<sub>27</sub>, negated\_conjecture)  
 $(p_{16}(c_{17}, c_{20}, x_4, x_6, x_3) \text{ and } p_{16}(c_{17}, c_{20}, x_4, x_5, c_{22})) \Rightarrow p_3(x_5, x_6)$     cnf(p3<sub>28</sub>, negated\_conjecture)  
 $(p_{16}(c_{17}, c_{20}, x_4, x_6, x_3) \text{ and } p_{16}(c_{17}, c_{20}, x_4, x_5, c_{22})) \Rightarrow p_{10}(c_{22}, x_3)$     cnf(p10<sub>29</sub>, negated\_conjecture)  
 $(p_{16}(c_{17}, c_{20}, x_9, x_{11}, c_{25}) \text{ and } p_{16}(c_{17}, c_{20}, x_9, x_{10}, f_{12}(c_{22}))) \Rightarrow p_3(x_{10}, x_{11})$     cnf(p3<sub>30</sub>, negated\_conjecture)  
 $(p_{16}(c_{17}, c_{20}, x_9, x_{11}, c_{25}) \text{ and } p_{16}(c_{17}, c_{20}, x_9, x_{10}, f_{12}(c_{22}))) \Rightarrow p_{10}(f_{12}(c_{22}), c_{25})$     cnf(p10<sub>31</sub>, negated\_conjecture)  
 $p_6(x_{61}, x_{62}) \text{ or } p_3(f_4(f_7(c_{17}, x_{61}), f_4(f_7(c_{17}, x_{62}), x_{63})), f_4(f_7(c_{17}, x_{62}), f_4(f_7(c_{17}, x_{61}), x_{63})))$     cnf(p6<sub>32</sub>, negated\_conjecture)  
 $(p_{15}(x_{28}, x_{27}) \text{ and } p_{16}(c_{17}, x_{26}, x_{27}, x_{30}, f_{12}(x_{29}))) \Rightarrow p_3(x_{30}, f_4(f_7(c_{17}, x_{28}), f_{11}(x_{26}, x_{29}, x_{27}, x_{30}, x_{28})))$     cnf(p3<sub>33</sub>, negated\_conjecture)  
 $(p_{15}(x_{28}, x_{27}) \text{ and } p_{16}(c_{17}, x_{26}, x_{27}, x_{30}, f_{12}(x_{29}))) \Rightarrow p_{16}(c_{17}, x_{26}, f_9(x_{27}, x_{28}), f_{11}(x_{26}, x_{29}, x_{27}, x_{30}, x_{28}), x_{29})$     cnf(p16<sub>34</sub>, negated\_conjecture)

$(p_8(x_{24}, x_{18}) \text{ and } p_5(x_{22}, x_{16}) \text{ and } p_3(x_{25}, x_{19}) \text{ and } p_3(x_{23}, x_{17}) \text{ and } p_{10}(x_{21}, x_{20}) \text{ and } p_{16}(x_{22}, x_{23}, x_{24}, x_{25}, x_{21})) \Rightarrow$   
 $p_{16}(x_{16}, x_{17}, x_{18}, x_{19}, x_{20}) \quad \text{cnf}(p_{16}_{35}, \text{negated\_conjecture})$   
 $(p_6(x_{47}, x_{52}) \text{ and } p_8(x_{45}, x_{50}) \text{ and } p_{10}(x_{44}, x_{49}) \text{ and } p_3(x_{43}, x_{48}) \text{ and } p_3(x_{46}, x_{51})) \Rightarrow p_3(f_{11}(x_{43}, x_{44}, x_{45}, x_{46}, x_{47}), f_{11}(x_{48}, x_{49}, x_{50}, x_{51}, x_{52}))$

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$p_2(x_4, x_4) \quad \text{cnf}(p_{21}, \text{negated\_conjecture})$   
 $p_9(x_{40}, x_{40}) \quad \text{cnf}(p_{92}, \text{negated\_conjecture})$   
 $p_6(x_{33}, x_{33}) \quad \text{cnf}(p_{63}, \text{negated\_conjecture})$   
 $p_5(x_{24}, x_{24}) \quad \text{cnf}(p_{54}, \text{negated\_conjecture})$   
 $p_3(x_{19}, x_{19}) \quad \text{cnf}(p_{35}, \text{negated\_conjecture})$   
 $p_9(c_{28}, c_{22}) \quad \text{cnf}(p_{96}, \text{negated\_conjecture})$   
 $p_{20}(c_{22}, c_{28}) \quad \text{cnf}(p_{207}, \text{negated\_conjecture})$   
 $p_{20}(c_{28}, c_{26}) \quad \text{cnf}(p_{208}, \text{negated\_conjecture})$   
 $p_{21}(c_{27}, c_{22}) \quad \text{cnf}(p_{219}, \text{negated\_conjecture})$   
 $p_{19}(c_{22}, f_4(f_7(c_{23}, f_8(c_{24}, c_{25})))) \quad \text{cnf}(p_{19}_{10}, \text{negated\_conjecture})$   
 $p_{19}(c_{27}, f_4(f_7(c_{23}, f_8(c_{24}, c_{25})))) \quad \text{cnf}(p_{19}_{11}, \text{negated\_conjecture})$   
 $p_{19}(c_{26}, f_4(f_7(c_{23}, f_8(c_{24}, c_{25})))) \quad \text{cnf}(p_{19}_{12}, \text{negated\_conjecture})$   
 $p_9(x_{53}, x_{54}) \Rightarrow p_9(f_{16}(x_{53}), f_{16}(x_{54})) \quad \text{cnf}(p_{9}_{13}, \text{negated\_conjecture})$   
 $p_2(x_{22}, x_{23}) \Rightarrow p_3(f_4(x_{22}), f_4(x_{23})) \quad \text{cnf}(p_{3}_{14}, \text{negated\_conjecture})$   
 $p_5(x_{27}, x_{28}) \Rightarrow p_5(f_{12}(x_{27}), f_{12}(x_{28})) \quad \text{cnf}(p_{5}_{15}, \text{negated\_conjecture})$   
 $p_5(x_{29}, x_{30}) \Rightarrow p_5(f_{13}(x_{29}), f_{13}(x_{30})) \quad \text{cnf}(p_{5}_{16}, \text{negated\_conjecture})$   
 $p_5(x_{31}, x_{32}) \Rightarrow p_5(f_{14}(x_{31}), f_{14}(x_{32})) \quad \text{cnf}(p_{5}_{17}, \text{negated\_conjecture})$   
 $p_5(x_{47}, x_{48}) \Rightarrow p_9(f_{11}(x_{47}), f_{11}(x_{48})) \quad \text{cnf}(p_{9}_{18}, \text{negated\_conjecture})$   
 $(p_2(x_4, x_5) \text{ and } p_2(x_4, x_6)) \Rightarrow p_2(x_5, x_6) \quad \text{cnf}(p_{219}, \text{negated\_conjecture})$   
 $(p_9(x_{40}, x_{41}) \text{ and } p_9(x_{40}, x_{42})) \Rightarrow p_9(x_{41}, x_{42}) \quad \text{cnf}(p_{9}_{20}, \text{negated\_conjecture})$   
 $(p_6(x_{33}, x_{34}) \text{ and } p_6(x_{33}, x_{35})) \Rightarrow p_6(x_{34}, x_{35}) \quad \text{cnf}(p_{6}_{21}, \text{negated\_conjecture})$   
 $(p_5(x_{24}, x_{25}) \text{ and } p_5(x_{24}, x_{26})) \Rightarrow p_5(x_{25}, x_{26}) \quad \text{cnf}(p_{5}_{22}, \text{negated\_conjecture})$   
 $(p_3(x_{19}, x_{20}) \text{ and } p_3(x_{19}, x_{21})) \Rightarrow p_3(x_{20}, x_{21}) \quad \text{cnf}(p_{3}_{23}, \text{negated\_conjecture})$   
 $(p_3(x_3, x_1) \text{ and } p_9(x_2, x_0) \text{ and } p_{19}(x_2, x_3)) \Rightarrow p_{19}(x_0, x_1) \quad \text{cnf}(p_{19}_{24}, \text{negated\_conjecture})$   
 $(p_9(x_{17}, x_{15}) \text{ and } p_9(x_{18}, x_{16}) \text{ and } p_{21}(x_{17}, x_{18})) \Rightarrow p_{21}(x_{15}, x_{16}) \quad \text{cnf}(p_{21}_{25}, \text{negated\_conjecture})$   
 $(p_9(x_{13}, x_{11}) \text{ and } p_9(x_{14}, x_{12}) \text{ and } p_{20}(x_{13}, x_{14})) \Rightarrow p_{20}(x_{11}, x_{12}) \quad \text{cnf}(p_{20}_{26}, \text{negated\_conjecture})$   
 $(p_5(x_7, x_9) \text{ and } p_6(x_8, x_{10})) \Rightarrow p_2(f_7(x_7, x_8), f_7(x_9, x_{10})) \quad \text{cnf}(p_{27}, \text{negated\_conjecture})$   
 $(p_9(x_{59}, x_{61}) \text{ and } p_9(x_{60}, x_{62})) \Rightarrow p_9(f_{18}(x_{59}, x_{60}), f_{18}(x_{61}, x_{62})) \quad \text{cnf}(p_{9}_{28}, \text{negated\_conjecture})$   
 $(p_9(x_{55}, x_{57}) \text{ and } p_9(x_{56}, x_{58})) \Rightarrow p_9(f_{17}(x_{55}, x_{56}), f_{17}(x_{57}, x_{58})) \quad \text{cnf}(p_{9}_{29}, \text{negated\_conjecture})$   
 $(p_2(x_{49}, x_{51}) \text{ and } p_9(x_{50}, x_{52})) \Rightarrow p_9(f_{15}(x_{49}, x_{50}), f_{15}(x_{51}, x_{52})) \quad \text{cnf}(p_{9}_{30}, \text{negated\_conjecture})$   
 $(p_9(x_{43}, x_{45}) \text{ and } p_9(x_{44}, x_{46})) \Rightarrow p_9(f_{10}(x_{43}, x_{44}), f_{10}(x_{45}, x_{46})) \quad \text{cnf}(p_{9}_{31}, \text{negated\_conjecture})$   
 $(p_5(x_{36}, x_{38}) \text{ and } p_5(x_{37}, x_{39})) \Rightarrow p_6(f_8(x_{36}, x_{37}), f_8(x_{38}, x_{39})) \quad \text{cnf}(p_{6}_{32}, \text{negated\_conjecture})$   
 $(p_{21}(x_{63}, c_{26}) \text{ and } p_{21}(c_{22}, x_{63})) \Rightarrow \neg p_{19}(x_{63}, f_4(f_7(c_{23}, f_8(c_{24}, c_{25})))) \quad \text{cnf}(\text{not\_}p_{21}_{33}, \text{negated\_conjecture})$   
 $p_{20}(f_{16}(f_{17}(c_{28}, c_{27})), f_{10}(f_{15}(f_7(c_{23}, f_8(c_{24}, c_{25})), c_{28})), f_{11}(f_{12}(f_{13}(f_{14}(c_{29})))))) \quad \text{cnf}(p_{20}_{34}, \text{negated\_conjecture})$   
 $\neg p_{20}(f_{16}(f_{17}(c_{22}, c_{27})), f_{10}(f_{15}(f_7(c_{23}, f_8(c_{24}, c_{25})), c_{22})), f_{11}(f_{12}(f_{13}(f_{14}(c_{29})))))) \quad \text{cnf}(\text{not\_}p_{20}_{35}, \text{negated\_conjecture})$   
 $p_{20}(f_{15}(f_7(c_{23}, f_8(c_{24}, c_{25})), c_{28}), f_{18}(f_{11}(f_{12}(f_{13}(f_{14}(c_{29}))))), f_{15}(f_7(c_{23}, f_8(c_{24}, c_{25})), c_{22})) \quad \text{cnf}(p_{20}_{36}, \text{negated\_conjecture})$

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$p_2(x_4, x_4) \quad \text{cnf}(p_{21}, \text{negated\_conjecture})$   
 $p_9(x_{40}, x_{40}) \quad \text{cnf}(p_{92}, \text{negated\_conjecture})$   
 $p_6(x_{33}, x_{33}) \quad \text{cnf}(p_{63}, \text{negated\_conjecture})$   
 $p_5(x_{24}, x_{24}) \quad \text{cnf}(p_{54}, \text{negated\_conjecture})$   
 $p_3(x_{19}, x_{19}) \quad \text{cnf}(p_{35}, \text{negated\_conjecture})$   
 $p_9(c_{28}, c_{26}) \quad \text{cnf}(p_{96}, \text{negated\_conjecture})$   
 $p_{20}(c_{22}, c_{28}) \quad \text{cnf}(p_{207}, \text{negated\_conjecture})$   
 $p_{20}(c_{28}, c_{26}) \quad \text{cnf}(p_{208}, \text{negated\_conjecture})$   
 $p_{21}(c_{26}, c_{27}) \quad \text{cnf}(p_{219}, \text{negated\_conjecture})$   
 $p_{19}(c_{22}, f_4(f_7(c_{23}, f_8(c_{24}, c_{25})))) \quad \text{cnf}(p_{19}_{10}, \text{negated\_conjecture})$   
 $p_{19}(c_{27}, f_4(f_7(c_{23}, f_8(c_{24}, c_{25})))) \quad \text{cnf}(p_{19}_{11}, \text{negated\_conjecture})$   
 $p_{19}(c_{26}, f_4(f_7(c_{23}, f_8(c_{24}, c_{25})))) \quad \text{cnf}(p_{19}_{12}, \text{negated\_conjecture})$   
 $p_9(x_{53}, x_{54}) \Rightarrow p_9(f_{16}(x_{53}), f_{16}(x_{54})) \quad \text{cnf}(p_{9}_{13}, \text{negated\_conjecture})$   
 $p_2(x_{22}, x_{23}) \Rightarrow p_3(f_4(x_{22}), f_4(x_{23})) \quad \text{cnf}(p_{3}_{14}, \text{negated\_conjecture})$   
 $p_5(x_{27}, x_{28}) \Rightarrow p_5(f_{12}(x_{27}), f_{12}(x_{28})) \quad \text{cnf}(p_{5}_{15}, \text{negated\_conjecture})$   
 $p_5(x_{29}, x_{30}) \Rightarrow p_5(f_{13}(x_{29}), f_{13}(x_{30})) \quad \text{cnf}(p_{5}_{16}, \text{negated\_conjecture})$   
 $p_5(x_{31}, x_{32}) \Rightarrow p_5(f_{14}(x_{31}), f_{14}(x_{32})) \quad \text{cnf}(p_{5}_{17}, \text{negated\_conjecture})$

$p_5(x_{47}, x_{48}) \Rightarrow p_9(f_{11}(x_{47}), f_{11}(x_{48}))$     cnf(p9<sub>18</sub>, negated\_conjecture)  
 $(p_2(x_4, x_5) \text{ and } p_2(x_4, x_6)) \Rightarrow p_2(x_5, x_6)$     cnf(p2<sub>19</sub>, negated\_conjecture)  
 $(p_9(x_{40}, x_{41}) \text{ and } p_9(x_{40}, x_{42})) \Rightarrow p_9(x_{41}, x_{42})$     cnf(p9<sub>20</sub>, negated\_conjecture)  
 $(p_6(x_{33}, x_{34}) \text{ and } p_6(x_{33}, x_{35})) \Rightarrow p_6(x_{34}, x_{35})$     cnf(p6<sub>21</sub>, negated\_conjecture)  
 $(p_5(x_{24}, x_{25}) \text{ and } p_5(x_{24}, x_{26})) \Rightarrow p_5(x_{25}, x_{26})$     cnf(p5<sub>22</sub>, negated\_conjecture)  
 $(p_3(x_{19}, x_{20}) \text{ and } p_3(x_{19}, x_{21})) \Rightarrow p_3(x_{20}, x_{21})$     cnf(p3<sub>23</sub>, negated\_conjecture)  
 $(p_3(x_3, x_1) \text{ and } p_9(x_2, x_0) \text{ and } p_{19}(x_2, x_3)) \Rightarrow p_{19}(x_0, x_1)$     cnf(p19<sub>24</sub>, negated\_conjecture)  
 $(p_9(x_{17}, x_{15}) \text{ and } p_9(x_{18}, x_{16}) \text{ and } p_{21}(x_{17}, x_{18})) \Rightarrow p_{21}(x_{15}, x_{16})$     cnf(p21<sub>25</sub>, negated\_conjecture)  
 $(p_9(x_{13}, x_{11}) \text{ and } p_9(x_{14}, x_{12}) \text{ and } p_{20}(x_{13}, x_{14})) \Rightarrow p_{20}(x_{11}, x_{12})$     cnf(p20<sub>26</sub>, negated\_conjecture)  
 $(p_5(x_7, x_9) \text{ and } p_6(x_8, x_{10})) \Rightarrow p_2(f_7(x_7, x_8), f_7(x_9, x_{10}))$     cnf(p2<sub>27</sub>, negated\_conjecture)  
 $(p_9(x_{59}, x_{61}) \text{ and } p_9(x_{60}, x_{62})) \Rightarrow p_9(f_{18}(x_{59}, x_{60}), f_{18}(x_{61}, x_{62}))$     cnf(p9<sub>28</sub>, negated\_conjecture)  
 $(p_9(x_{55}, x_{57}) \text{ and } p_9(x_{56}, x_{58})) \Rightarrow p_9(f_{17}(x_{55}, x_{56}), f_{17}(x_{57}, x_{58}))$     cnf(p9<sub>29</sub>, negated\_conjecture)  
 $(p_2(x_{49}, x_{51}) \text{ and } p_9(x_{50}, x_{52})) \Rightarrow p_9(f_{15}(x_{49}, x_{50}), f_{15}(x_{51}, x_{52}))$     cnf(p9<sub>30</sub>, negated\_conjecture)  
 $(p_9(x_{43}, x_{45}) \text{ and } p_9(x_{44}, x_{46})) \Rightarrow p_9(f_{10}(x_{43}, x_{44}), f_{10}(x_{45}, x_{46}))$     cnf(p9<sub>31</sub>, negated\_conjecture)  
 $(p_5(x_{36}, x_{38}) \text{ and } p_5(x_{37}, x_{39})) \Rightarrow p_6(f_8(x_{36}, x_{37}), f_8(x_{38}, x_{39}))$     cnf(p6<sub>32</sub>, negated\_conjecture)  
 $(p_{21}(x_{63}, c_{26}) \text{ and } p_{21}(c_{22}, x_{63})) \Rightarrow \neg p_{19}(x_{63}, f_4(f_7(c_{23}, f_8(c_{24}, c_{25}))))$     cnf(not\_p21<sub>33</sub>, negated\_conjecture)  
 $p_{20}(f_{16}(f_{17}(c_{28}, c_{27})), f_{10}(f_{15}(f_7(c_{23}, f_8(c_{24}, c_{25}))), c_{28}), f_{11}(f_{12}(f_{13}(f_{14}(c_{29}))))))$     cnf(p20<sub>34</sub>, negated\_conjecture)  
 $\neg p_{20}(f_{16}(f_{17}(c_{26}, c_{27})), f_{10}(f_{15}(f_7(c_{23}, f_8(c_{24}, c_{25}))), c_{26}), f_{11}(f_{12}(f_{13}(f_{14}(c_{29}))))))$     cnf(not\_p20<sub>35</sub>, negated\_conjecture)  
 $p_{20}(f_{15}(f_7(c_{23}, f_8(c_{24}, c_{25}))), c_{28}), f_{18}(f_{11}(f_{12}(f_{13}(f_{14}(c_{29}))))), f_{15}(f_7(c_{23}, f_8(c_{24}, c_{25}))), c_{26}))$     cnf(p20<sub>36</sub>, negated\_conjecture)

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$p_{10}(x_0, x_0)$     cnf(p10<sub>1</sub>, negated\_conjecture)  
 $p_9(x_{74}, x_{74})$     cnf(p9<sub>2</sub>, negated\_conjecture)  
 $p_7(x_{65}, x_{65})$     cnf(p7<sub>3</sub>, negated\_conjecture)  
 $p_6(x_{62}, x_{62})$     cnf(p6<sub>4</sub>, negated\_conjecture)  
 $p_5(x_{37}, x_{37})$     cnf(p5<sub>5</sub>, negated\_conjecture)  
 $p_3(x_{32}, x_{32})$     cnf(p3<sub>6</sub>, negated\_conjecture)  
 $p_2(x_{12}, x_{12})$     cnf(p2<sub>7</sub>, negated\_conjecture)  
 $p_{12}(x_5, x_5)$     cnf(p12<sub>8</sub>, negated\_conjecture)  
 $p_{22}(c_{25}, c_{28})$     cnf(p22<sub>9</sub>, negated\_conjecture)  
 $p_5(f_{17}(f_{18}(x_{48}, x_{49})), x_{48})$     cnf(p5<sub>10</sub>, negated\_conjecture)  
 $p_5(f_{16}(f_{18}(x_{44}, x_{45})), x_{45})$     cnf(p5<sub>11</sub>, negated\_conjecture)  
 $p_{23}f_{13}(c_{27}, f_{14}(c_{28}), f_{11}(f_{15}(c_{24})))$     cnf(p23<sub>12</sub>, negated\_conjecture)  
 $\neg p_{23}(f_{13}(f_{16}(c_{27}), f_{14}(c_{28})), f_{11}(c_{24}))$     cnf(not\_p23<sub>13</sub>, negated\_conjecture)  
 $p_9(x_{77}, x_{78}) \Rightarrow p_9(f_{15}(x_{77}), f_{15}(x_{78}))$     cnf(p9<sub>14</sub>, negated\_conjecture)  
 $p_9(x_3, x_4) \Rightarrow p_{10}(f_{11}(x_3), f_{11}(x_4))$     cnf(p10<sub>15</sub>, negated\_conjecture)  
 $p_2(x_{35}, x_{36}) \Rightarrow p_3(f_4(x_{35}), f_4(x_{36}))$     cnf(p3<sub>16</sub>, negated\_conjecture)  
 $p_6(x_{40}, x_{41}) \Rightarrow p_5(f_{14}(x_{40}), f_{14}(x_{41}))$     cnf(p5<sub>17</sub>, negated\_conjecture)  
 $p_5(x_{42}, x_{43}) \Rightarrow p_5(f_{16}(x_{42}), f_{16}(x_{43}))$     cnf(p5<sub>18</sub>, negated\_conjecture)  
 $p_5(x_{46}, x_{47}) \Rightarrow p_5(f_{17}(x_{46}), f_{17}(x_{47}))$     cnf(p5<sub>19</sub>, negated\_conjecture)  
 $p_5(x_{60}, x_{61}) \Rightarrow p_5(f_{20}(x_{60}), f_{20}(x_{61}))$     cnf(p5<sub>20</sub>, negated\_conjecture)  
 $(p_{10}(x_0, x_1) \text{ and } p_{10}(x_0, x_2)) \Rightarrow p_{10}(x_1, x_2)$     cnf(p10<sub>21</sub>, negated\_conjecture)  
 $(p_9(x_{74}, x_{75}) \text{ and } p_9(x_{74}, x_{76})) \Rightarrow p_9(x_{75}, x_{76})$     cnf(p9<sub>22</sub>, negated\_conjecture)  
 $(p_7(x_{65}, x_{66}) \text{ and } p_7(x_{65}, x_{67})) \Rightarrow p_7(x_{66}, x_{67})$     cnf(p7<sub>23</sub>, negated\_conjecture)  
 $(p_6(x_{62}, x_{63}) \text{ and } p_6(x_{62}, x_{64})) \Rightarrow p_6(x_{63}, x_{64})$     cnf(p6<sub>24</sub>, negated\_conjecture)  
 $(p_5(x_{37}, x_{38}) \text{ and } p_5(x_{37}, x_{39})) \Rightarrow p_5(x_{38}, x_{39})$     cnf(p5<sub>25</sub>, negated\_conjecture)  
 $(p_3(x_{32}, x_{33}) \text{ and } p_3(x_{32}, x_{34})) \Rightarrow p_3(x_{33}, x_{34})$     cnf(p3<sub>26</sub>, negated\_conjecture)  
 $(p_2(x_{12}, x_{13}) \text{ and } p_2(x_{12}, x_{14})) \Rightarrow p_2(x_{13}, x_{14})$     cnf(p2<sub>27</sub>, negated\_conjecture)  
 $(p_{12}(x_5, x_6) \text{ and } p_{12}(x_5, x_7)) \Rightarrow p_{12}(x_6, x_7)$     cnf(p12<sub>28</sub>, negated\_conjecture)  
 $(p_{12}(x_{28}, x_{25}) \text{ and } p_{23}(x_{28}, x_{27}) \text{ and } p_{10}(x_{27}, x_{26})) \Rightarrow p_{23}(x_{25}, x_{26})$     cnf(p23<sub>29</sub>, negated\_conjecture)  
 $(p_3(x_{18}, x_{16}) \text{ and } p_7(x_{17}, x_{15}) \text{ and } p_{21}(x_{17}, x_{18})) \Rightarrow p_{21}(x_{15}, x_{16})$     cnf(p21<sub>30</sub>, negated\_conjecture)  
 $(p_3(x_{23}, x_{21}) \text{ and } p_6(x_{24}, x_{22}) \text{ and } p_{22}(x_{23}, x_{24})) \Rightarrow p_{22}(x_{21}, x_{22})$     cnf(p22<sub>31</sub>, negated\_conjecture)  
 $(p_5(x_8, x_{10}) \text{ and } p_5(x_9, x_{11})) \Rightarrow p_{12}(f_{13}(x_8, x_9), f_{13}(x_{10}, x_{11}))$     cnf(p12<sub>32</sub>, negated\_conjecture)  
 $(p_5(x_{50}, x_{52}) \text{ and } p_5(x_{51}, x_{53})) \Rightarrow p_5(f_{18}(x_{50}, x_{51}), f_{18}(x_{52}, x_{53}))$     cnf(p5<sub>33</sub>, negated\_conjecture)  
 $p_{23}(f_{13}(x_{30}, x_{31}), f_{11}(f_{15}(x_{29}))) \Rightarrow p_5(x_{30}, f_{18}(f_{20}(c_{29}), f_{19}(x_{29}, x_{30}, x_{31})))$     cnf(p5<sub>34</sub>, negated\_conjecture)  
 $p_{23}(f_{13}(x_{30}, x_{31}), f_{11}(f_{15}(x_{29}))) \Rightarrow p_{23}(f_{13}(f_{19}(x_{29}, x_{30}, x_{31}), x_{31}), f_{11}(x_{29}))$     cnf(p23<sub>35</sub>, negated\_conjecture)  
 $(p_{22}(c_{25}, x_{20}) \text{ and } p_{23}(f_{13}(x_{19}, f_{14}(x_{20})), f_{11}(c_{24}))) \Rightarrow p_{21}(f_8(c_{26}, x_{19}, x_{20}), f_4(c_{26}))$     cnf(p21<sub>36</sub>, negated\_conjecture)  
 $(p_5(x_{69}, x_{72}) \text{ and } p_6(x_{70}, x_{73}) \text{ and } p_2(x_{68}, x_{71})) \Rightarrow p_7(f_8(x_{68}, x_{69}, x_{70}), f_8(x_{71}, x_{72}, x_{73}))$     cnf(p7<sub>37</sub>, negated\_conjecture)  
 $(p_5(x_{56}, x_{59}) \text{ and } p_9(x_{54}, x_{57}) \text{ and } p_5(x_{55}, x_{58})) \Rightarrow p_5(f_{19}(x_{54}, x_{55}, x_{56}), f_{19}(x_{57}, x_{58}, x_{59}))$     cnf(p5<sub>38</sub>, negated\_conjecture)

**SYN632-1.p** Harrison problem 4144

$p_{11}(x_0, x_0)$       cnf(p11<sub>1</sub>, negated\_conjecture)  
 $p_9(x_{70}, x_{70})$       cnf(p9<sub>2</sub>, negated\_conjecture)  
 $p_8(x_{67}, x_{67})$       cnf(p8<sub>3</sub>, negated\_conjecture)  
 $p_6(x_{60}, x_{60})$       cnf(p6<sub>4</sub>, negated\_conjecture)  
 $p_4(x_{53}, x_{53})$       cnf(p4<sub>5</sub>, negated\_conjecture)  
 $p_3(x_{46}, x_{46})$       cnf(p3<sub>6</sub>, negated\_conjecture)  
 $p_2(x_{27}, x_{27})$       cnf(p2<sub>7</sub>, negated\_conjecture)  
 $p_{19}(x_{24}, x_{24})$       cnf(p19<sub>8</sub>, negated\_conjecture)  
 $p_{17}(x_{17}, x_{17})$       cnf(p17<sub>9</sub>, negated\_conjecture)  
 $p_{15}(x_{10}, x_{10})$       cnf(p15<sub>10</sub>, negated\_conjecture)  
 $p_{13}(x_3, x_3)$       cnf(p13<sub>11</sub>, negated\_conjecture)  
 $(p_{11}(x_0, x_1) \text{ and } p_{11}(x_0, x_2)) \Rightarrow p_{11}(x_1, x_2)$       cnf(p11<sub>12</sub>, negated\_conjecture)  
 $(p_9(x_{70}, x_{71}) \text{ and } p_9(x_{70}, x_{72})) \Rightarrow p_9(x_{71}, x_{72})$       cnf(p9<sub>13</sub>, negated\_conjecture)  
 $(p_8(x_{67}, x_{68}) \text{ and } p_8(x_{67}, x_{69})) \Rightarrow p_8(x_{68}, x_{69})$       cnf(p8<sub>14</sub>, negated\_conjecture)  
 $(p_6(x_{60}, x_{61}) \text{ and } p_6(x_{60}, x_{62})) \Rightarrow p_6(x_{61}, x_{62})$       cnf(p6<sub>15</sub>, negated\_conjecture)  
 $(p_4(x_{53}, x_{54}) \text{ and } p_4(x_{53}, x_{55})) \Rightarrow p_4(x_{54}, x_{55})$       cnf(p4<sub>16</sub>, negated\_conjecture)  
 $(p_3(x_{46}, x_{47}) \text{ and } p_3(x_{46}, x_{48})) \Rightarrow p_3(x_{47}, x_{48})$       cnf(p3<sub>17</sub>, negated\_conjecture)  
 $(p_2(x_{27}, x_{28}) \text{ and } p_2(x_{27}, x_{29})) \Rightarrow p_2(x_{28}, x_{29})$       cnf(p2<sub>18</sub>, negated\_conjecture)  
 $(p_{19}(x_{24}, x_{25}) \text{ and } p_{19}(x_{24}, x_{26})) \Rightarrow p_{19}(x_{25}, x_{26})$       cnf(p19<sub>19</sub>, negated\_conjecture)  
 $(p_{17}(x_{17}, x_{18}) \text{ and } p_{17}(x_{17}, x_{19})) \Rightarrow p_{17}(x_{18}, x_{19})$       cnf(p17<sub>20</sub>, negated\_conjecture)  
 $(p_{15}(x_{10}, x_{11}) \text{ and } p_{15}(x_{10}, x_{12})) \Rightarrow p_{15}(x_{11}, x_{12})$       cnf(p15<sub>21</sub>, negated\_conjecture)  
 $(p_{13}(x_3, x_4) \text{ and } p_{13}(x_3, x_5)) \Rightarrow p_{13}(x_4, x_5)$       cnf(p13<sub>22</sub>, negated\_conjecture)  
 $(p_3(x_{37}, x_{35}) \text{ and } p_4(x_{36}, x_{34}) \text{ and } p_{21}(x_{36}, x_{37})) \Rightarrow p_{21}(x_{34}, x_{35})$       cnf(p21<sub>23</sub>, negated\_conjecture)  
 $p_{21}(f_5(f_7(f_{10}(c_{24}, f_{12}(c_{28}, f_{12}(c_{25}, c_{26}))), c_{22}), c_{23}), c_{27})$       cnf(p21<sub>24</sub>, negated\_conjecture)  
 $(p_{11}(x_{73}, x_{75}) \text{ and } p_9(x_{74}, x_{76})) \Rightarrow p_9(f_{12}(x_{73}, x_{74}), f_{12}(x_{75}, x_{76}))$       cnf(p9<sub>25</sub>, negated\_conjecture)  
 $(p_{15}(x_6, x_8) \text{ and } p_2(x_7, x_9)) \Rightarrow p_{13}(f_{16}(x_6, x_7), f_{16}(x_8, x_9))$       cnf(p13<sub>26</sub>, negated\_conjecture)  
 $(p_{17}(x_{13}, x_{15}) \text{ and } p_3(x_{14}, x_{16})) \Rightarrow p_{15}(f_{18}(x_{13}, x_{14}), f_{18}(x_{15}, x_{16}))$       cnf(p15<sub>27</sub>, negated\_conjecture)  
 $(p_{19}(x_{20}, x_{22}) \text{ and } p_9(x_{21}, x_{23})) \Rightarrow p_{17}(f_{20}(x_{20}, x_{21}), f_{20}(x_{22}, x_{23}))$       cnf(p17<sub>28</sub>, negated\_conjecture)  
 $(p_2(x_{31}, x_{33}) \text{ and } p_6(x_{30}, x_{32})) \Rightarrow p_2(f_7(x_{30}, x_{31}), f_7(x_{32}, x_{33}))$       cnf(p2<sub>29</sub>, negated\_conjecture)  
 $(p_{13}(x_{49}, x_{51}) \text{ and } p_3(x_{50}, x_{52})) \Rightarrow p_3(f_{14}(x_{49}, x_{50}), f_{14}(x_{51}, x_{52}))$       cnf(p3<sub>30</sub>, negated\_conjecture)  
 $(p_2(x_{56}, x_{58}) \text{ and } p_3(x_{57}, x_{59})) \Rightarrow p_4(f_5(x_{56}, x_{57}), f_5(x_{58}, x_{59}))$       cnf(p4<sub>31</sub>, negated\_conjecture)  
 $(p_8(x_{63}, x_{65}) \text{ and } p_9(x_{64}, x_{66})) \Rightarrow p_6(f_{10}(x_{63}, x_{64}), f_{10}(x_{65}, x_{66}))$       cnf(p6<sub>32</sub>, negated\_conjecture)  
 $p_{21}(f_5(f_7(f_{10}(c_{24}, f_{12}(c_{25}, c_{26}))), x_{42}), x_{43}), x_{44}) \Rightarrow p_3(x_{43}, x_{44})$       cnf(p3<sub>33</sub>, negated\_conjecture)  
 $p_3(x_{43}, x_{44}) \Rightarrow p_{21}(f_5(f_7(f_{10}(c_{24}, f_{12}(c_{25}, c_{26}))), x_{42}), x_{43}), x_{44})$       cnf(p21<sub>34</sub>, negated\_conjecture)  
 $p_{21}(f_5(c_{22}, c_{23}), x_{77}) \Rightarrow \neg p_{21}(f_5(f_7(f_{10}(c_{24}, f_{12}(c_{25}, c_{26}))), c_{22}), x_{77}), c_{27})$       cnf(not\_p21<sub>35</sub>, negated\_conjecture)  
 $p_{21}(f_5(f_7(f_{10}(c_{24}, f_{12}(c_{28}, x_{39}))), x_{38}), x_{40}), x_{41}) \Rightarrow p_{21}(f_5(x_{38}, f_{14}(f_{16}(f_{18}(f_{20}(c_{29}, x_{39}), x_{40}), x_{38}), x_{41}))), x_{41})$       cnf(p21<sub>36</sub>, negated\_conjecture)  
 $(p_{21}(f_5(x_{38}, x_{45}), x_{41}) \text{ and } p_{21}(f_5(f_7(f_{10}(c_{24}, x_{39}), x_{38}), x_{40}), x_{45})) \Rightarrow p_{21}(f_5(f_7(f_{10}(c_{24}, f_{12}(c_{28}, x_{39}))), x_{38}), x_{40}), x_{41})$       cnf(p21<sub>37</sub>, negated\_conjecture)  
 $p_{21}(f_5(f_7(f_{10}(c_{24}, f_{12}(c_{28}, x_{39}))), x_{38}), x_{40}), x_{41}) \Rightarrow p_{21}(f_5(f_7(f_{10}(c_{24}, x_{39}), x_{38}), x_{40}), f_{14}(f_{16}(f_{18}(f_{20}(c_{29}, x_{39}), x_{40}), x_{38}), x_{41})))$       cnf(p21<sub>38</sub>, negated\_conjecture)

**SYN641-1.p** Harrison problem 4296

$p_{15}(f_3(c_{19}))$       cnf(f3\_is\_p15<sub>1</sub>, negated\_conjecture)  
 $p_{15}(f_3(c_{18}))$       cnf(f3\_is\_p15<sub>2</sub>, negated\_conjecture)  
 $p_{11}(x_0, x_0)$       cnf(p11<sub>3</sub>, negated\_conjecture)  
 $p_6(x_{45}, x_{45})$       cnf(p6<sub>4</sub>, negated\_conjecture)  
 $p_4(x_{36}, x_{36})$       cnf(p4<sub>5</sub>, negated\_conjecture)  
 $p_2(x_{27}, x_{27})$       cnf(p2<sub>6</sub>, negated\_conjecture)  
 $p_{16}(x_{18}, x_{18})$       cnf(p16<sub>7</sub>, negated\_conjecture)  
 $p_{12}(x_3, x_3)$       cnf(p12<sub>8</sub>, negated\_conjecture)  
 $p_6(f_8(f_3(c_{19})), f_8(c_{19}))$       cnf(p6<sub>9</sub>, negated\_conjecture)  
 $p_4(f_5(f_3(c_{18})), f_5(c_{18}))$       cnf(p4<sub>10</sub>, negated\_conjecture)  
 $p_4(f_5(f_3(c_{19})), f_5(c_{19}))$       cnf(p4<sub>11</sub>, negated\_conjecture)  
 $p_6(f_7(f_3(c_{18})), f_7(c_{18}))$       cnf(p6<sub>12</sub>, negated\_conjecture)  
 $p_6(f_7(f_3(c_{19})), f_7(c_{19}))$       cnf(p6<sub>13</sub>, negated\_conjecture)  
 $p_6(f_8(f_3(c_{18})), f_8(c_{18}))$       cnf(p6<sub>14</sub>, negated\_conjecture)  
 $(p_{15}(x_{17}) \text{ and } p_2(x_{17}, x_{16})) \Rightarrow p_{15}(x_{16})$       cnf(p15<sub>15</sub>, negated\_conjecture)  
 $p_{11}(x_6, x_7) \Rightarrow p_{12}(f_{13}(x_6), f_{13}(x_7))$       cnf(p12<sub>16</sub>, negated\_conjecture)  
 $p_2(x_{50}, x_{51}) \Rightarrow p_6(f_8(x_{50}), f_8(x_{51}))$       cnf(p6<sub>17</sub>, negated\_conjecture)  
 $p_2(x_{48}, x_{49}) \Rightarrow p_6(f_7(x_{48}), f_7(x_{49}))$       cnf(p6<sub>18</sub>, negated\_conjecture)  
 $p_2(x_{43}, x_{44}) \Rightarrow p_4(f_5(x_{43}), f_5(x_{44}))$       cnf(p4<sub>19</sub>, negated\_conjecture)

$p_2(x_{34}, x_{35}) \Rightarrow p_2(f_3(x_{34}), f_3(x_{35}))$      $\text{cnf}(p_{2_{20}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15})) \Rightarrow p_{15}(f_{10}(x_{14}, x_{15}))$      $\text{cnf}(p_{15_{21}}, \text{negated\_conjecture})$   
 $(p_{11}(x_0, x_1) \text{ and } p_{11}(x_0, x_2)) \Rightarrow p_{11}(x_1, x_2)$      $\text{cnf}(p_{11_{22}}, \text{negated\_conjecture})$   
 $(p_6(x_{45}, x_{46}) \text{ and } p_6(x_{45}, x_{47})) \Rightarrow p_6(x_{46}, x_{47})$      $\text{cnf}(p_{6_{23}}, \text{negated\_conjecture})$   
 $(p_4(x_{36}, x_{37}) \text{ and } p_4(x_{36}, x_{38})) \Rightarrow p_4(x_{37}, x_{38})$      $\text{cnf}(p_{4_{24}}, \text{negated\_conjecture})$   
 $(p_2(x_{27}, x_{28}) \text{ and } p_2(x_{27}, x_{29})) \Rightarrow p_2(x_{28}, x_{29})$      $\text{cnf}(p_{2_{25}}, \text{negated\_conjecture})$   
 $(p_{16}(x_{18}, x_{19}) \text{ and } p_{16}(x_{18}, x_{20})) \Rightarrow p_{16}(x_{19}, x_{20})$      $\text{cnf}(p_{16_{26}}, \text{negated\_conjecture})$   
 $(p_{12}(x_3, x_4) \text{ and } p_{12}(x_3, x_5)) \Rightarrow p_{12}(x_4, x_5)$      $\text{cnf}(p_{12_{27}}, \text{negated\_conjecture})$   
 $\neg p_6(f_7(f_{10}(f_3(c_{19})), f_3(c_{18}))), f_9(f_7(c_{19}), f_7(c_{18})))$      $\text{cnf}(\text{not\_}p_{6_{28}}, \text{negated\_conjecture})$   
 $p_{17}(x_8, x_9, f_3(c_{19})) \Rightarrow (p_{12}(f_{13}(x_8), c_{20}) \text{ or } p_{17}(x_8, x_9, c_{19}))$      $\text{cnf}(p_{12_{29}}, \text{negated\_conjecture})$   
 $p_{17}(x_{10}, x_{11}, f_3(c_{18})) \Rightarrow (p_{12}(f_{13}(x_{10}), c_{20}) \text{ or } p_{17}(x_{10}, x_{11}, c_{18}))$      $\text{cnf}(p_{12_{30}}, \text{negated\_conjecture})$   
 $p_{17}(x_8, x_9, c_{19}) \Rightarrow (p_{12}(f_{13}(x_8), c_{20}) \text{ or } p_{17}(x_8, x_9, f_3(c_{19})))$      $\text{cnf}(p_{12_{31}}, \text{negated\_conjecture})$   
 $p_{17}(x_{10}, x_{11}, c_{18}) \Rightarrow (p_{12}(f_{13}(x_{10}), c_{20}) \text{ or } p_{17}(x_{10}, x_{11}, f_3(c_{18})))$      $\text{cnf}(p_{12_{32}}, \text{negated\_conjecture})$   
 $(p_6(x_{53}, x_{55}) \text{ and } p_6(x_{52}, x_{54})) \Rightarrow p_6(f_9(x_{52}, x_{53}), f_9(x_{54}, x_{55}))$      $\text{cnf}(p_{6_{33}}, \text{negated\_conjecture})$   
 $(p_2(x_{30}, x_{32}) \text{ and } p_2(x_{31}, x_{33})) \Rightarrow p_2(f_{10}(x_{30}, x_{31}), f_{10}(x_{32}, x_{33}))$      $\text{cnf}(p_{2_{34}}, \text{negated\_conjecture})$   
 $(p_4(x_{39}, x_{41}) \text{ and } p_4(x_{40}, x_{42})) \Rightarrow p_4(f_{14}(x_{39}, x_{40}), f_{14}(x_{41}, x_{42}))$      $\text{cnf}(p_{4_{35}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15})) \Rightarrow p_6(f_8(f_{10}(x_{14}, x_{15})), f_9(f_8(x_{14}), f_8(x_{15})))$      $\text{cnf}(p_{6_{36}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15})) \Rightarrow p_4(f_5(f_{10}(x_{14}, x_{15})), f_{14}(f_5(x_{14}), f_5(x_{15})))$      $\text{cnf}(p_{4_{37}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15})) \Rightarrow p_6(f_7(f_{10}(x_{14}, x_{15})), f_9(f_7(x_{14}), f_7(x_{15})))$      $\text{cnf}(p_{6_{38}}, \text{negated\_conjecture})$   
 $(p_2(x_{26}, x_{23}) \text{ and } p_{16}(x_{25}, x_{22}) \text{ and } p_{11}(x_{24}, x_{21}) \text{ and } p_{17}(x_{24}, x_{25}, x_{26})) \Rightarrow p_{17}(x_{21}, x_{22}, x_{23})$      $\text{cnf}(p_{17_{39}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15})) \Rightarrow (p_{12}(f_{13}(x_{12}), c_{20}) \text{ or } p_{17}(x_{12}, x_{13}, x_{14}) \text{ or } p_{17}(x_{12}, x_{13}, f_{10}(x_{14}, x_{15})))$      $\text{cnf}(p_{12_{40}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15}) \text{ and } p_{17}(x_{12}, x_{13}, x_{15})) \Rightarrow (p_{12}(f_{13}(x_{12}), c_{20}) \text{ or } p_{17}(x_{12}, x_{13}, f_{10}(x_{14}, x_{15})))$      $\text{cnf}(p_{12_{41}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15}) \text{ and } p_{17}(x_{12}, x_{13}, x_{14}) \text{ and } p_{17}(x_{12}, x_{13}, f_{10}(x_{14}, x_{15}))) \Rightarrow (p_{12}(f_{13}(x_{12}), c_{20}) \text{ or } p_{17}(x_{12}, x_{13}, x_{15}))$

#### SYN642-1.p Harrison problem 4297

$p_{15}(f_3(c_{19}))$      $\text{cnf}(f3\_is\_p15_1, \text{negated\_conjecture})$   
 $p_{15}(f_3(c_{18}))$      $\text{cnf}(f3\_is\_p15_2, \text{negated\_conjecture})$   
 $p_{11}(x_0, x_0)$      $\text{cnf}(p_{11_3}, \text{negated\_conjecture})$   
 $p_6(x_{45}, x_{45})$      $\text{cnf}(p_{6_4}, \text{negated\_conjecture})$   
 $p_4(x_{36}, x_{36})$      $\text{cnf}(p_{4_5}, \text{negated\_conjecture})$   
 $p_2(x_{27}, x_{27})$      $\text{cnf}(p_{2_6}, \text{negated\_conjecture})$   
 $p_{16}(x_{18}, x_{18})$      $\text{cnf}(p_{16_7}, \text{negated\_conjecture})$   
 $p_{12}(x_3, x_3)$      $\text{cnf}(p_{12_8}, \text{negated\_conjecture})$   
 $p_6(f_8(f_3(c_{19})), f_8(c_{19}))$      $\text{cnf}(p_{6_9}, \text{negated\_conjecture})$   
 $p_4(f_5(f_3(c_{18})), f_5(c_{18}))$      $\text{cnf}(p_{4_{10}}, \text{negated\_conjecture})$   
 $p_4(f_5(f_3(c_{19})), f_5(c_{19}))$      $\text{cnf}(p_{4_{11}}, \text{negated\_conjecture})$   
 $p_6(f_7(f_3(c_{18})), f_7(c_{18}))$      $\text{cnf}(p_{6_{12}}, \text{negated\_conjecture})$   
 $p_6(f_7(f_3(c_{19})), f_7(c_{19}))$      $\text{cnf}(p_{6_{13}}, \text{negated\_conjecture})$   
 $p_6(f_8(f_3(c_{18})), f_8(c_{18}))$      $\text{cnf}(p_{6_{14}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{17}) \text{ and } p_2(x_{17}, x_{16})) \Rightarrow p_{15}(x_{16})$      $\text{cnf}(p_{15_{15}}, \text{negated\_conjecture})$   
 $p_{11}(x_6, x_7) \Rightarrow p_{12}(f_{13}(x_6), f_{13}(x_7))$      $\text{cnf}(p_{12_{16}}, \text{negated\_conjecture})$   
 $p_2(x_{50}, x_{51}) \Rightarrow p_6(f_8(x_{50}), f_8(x_{51}))$      $\text{cnf}(p_{6_{17}}, \text{negated\_conjecture})$   
 $p_2(x_{48}, x_{49}) \Rightarrow p_6(f_7(x_{48}), f_7(x_{49}))$      $\text{cnf}(p_{6_{18}}, \text{negated\_conjecture})$   
 $p_2(x_{43}, x_{44}) \Rightarrow p_4(f_5(x_{43}), f_5(x_{44}))$      $\text{cnf}(p_{4_{19}}, \text{negated\_conjecture})$   
 $p_2(x_{34}, x_{35}) \Rightarrow p_2(f_3(x_{34}), f_3(x_{35}))$      $\text{cnf}(p_{2_{20}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15})) \Rightarrow p_{15}(f_{10}(x_{14}, x_{15}))$      $\text{cnf}(p_{15_{21}}, \text{negated\_conjecture})$   
 $(p_{11}(x_0, x_1) \text{ and } p_{11}(x_0, x_2)) \Rightarrow p_{11}(x_1, x_2)$      $\text{cnf}(p_{11_{22}}, \text{negated\_conjecture})$   
 $(p_6(x_{45}, x_{46}) \text{ and } p_6(x_{45}, x_{47})) \Rightarrow p_6(x_{46}, x_{47})$      $\text{cnf}(p_{6_{23}}, \text{negated\_conjecture})$   
 $(p_4(x_{36}, x_{37}) \text{ and } p_4(x_{36}, x_{38})) \Rightarrow p_4(x_{37}, x_{38})$      $\text{cnf}(p_{4_{24}}, \text{negated\_conjecture})$   
 $(p_2(x_{27}, x_{28}) \text{ and } p_2(x_{27}, x_{29})) \Rightarrow p_2(x_{28}, x_{29})$      $\text{cnf}(p_{2_{25}}, \text{negated\_conjecture})$   
 $(p_{16}(x_{18}, x_{19}) \text{ and } p_{16}(x_{18}, x_{20})) \Rightarrow p_{16}(x_{19}, x_{20})$      $\text{cnf}(p_{16_{26}}, \text{negated\_conjecture})$   
 $(p_{12}(x_3, x_4) \text{ and } p_{12}(x_3, x_5)) \Rightarrow p_{12}(x_4, x_5)$      $\text{cnf}(p_{12_{27}}, \text{negated\_conjecture})$   
 $\neg p_6(f_8(f_{10}(f_3(c_{19})), f_3(c_{18}))), f_9(f_8(c_{19}), f_8(c_{18})))$      $\text{cnf}(\text{not\_}p_{6_{28}}, \text{negated\_conjecture})$   
 $p_{17}(x_8, x_9, f_3(c_{19})) \Rightarrow (p_{12}(f_{13}(x_8), c_{20}) \text{ or } p_{17}(x_8, x_9, c_{19}))$      $\text{cnf}(p_{12_{29}}, \text{negated\_conjecture})$   
 $p_{17}(x_{10}, x_{11}, f_3(c_{18})) \Rightarrow (p_{12}(f_{13}(x_{10}), c_{20}) \text{ or } p_{17}(x_{10}, x_{11}, c_{18}))$      $\text{cnf}(p_{12_{30}}, \text{negated\_conjecture})$   
 $p_{17}(x_8, x_9, c_{19}) \Rightarrow (p_{12}(f_{13}(x_8), c_{20}) \text{ or } p_{17}(x_8, x_9, f_3(c_{19})))$      $\text{cnf}(p_{12_{31}}, \text{negated\_conjecture})$   
 $p_{17}(x_{10}, x_{11}, c_{18}) \Rightarrow (p_{12}(f_{13}(x_{10}), c_{20}) \text{ or } p_{17}(x_{10}, x_{11}, f_3(c_{18})))$      $\text{cnf}(p_{12_{32}}, \text{negated\_conjecture})$   
 $(p_6(x_{53}, x_{55}) \text{ and } p_6(x_{52}, x_{54})) \Rightarrow p_6(f_9(x_{52}, x_{53}), f_9(x_{54}, x_{55}))$      $\text{cnf}(p_{6_{33}}, \text{negated\_conjecture})$   
 $(p_2(x_{30}, x_{32}) \text{ and } p_2(x_{31}, x_{33})) \Rightarrow p_2(f_{10}(x_{30}, x_{31}), f_{10}(x_{32}, x_{33}))$      $\text{cnf}(p_{2_{34}}, \text{negated\_conjecture})$   
 $(p_4(x_{39}, x_{41}) \text{ and } p_4(x_{40}, x_{42})) \Rightarrow p_4(f_{14}(x_{39}, x_{40}), f_{14}(x_{41}, x_{42}))$      $\text{cnf}(p_{4_{35}}, \text{negated\_conjecture})$

$(p_{15}(x_{14}) \text{ and } p_{15}(x_{15})) \Rightarrow p_6(f_8(f_{10}(x_{14}, x_{15})), f_9(f_8(x_{14}), f_8(x_{15})))$      $\text{cnf}(p_{6_{36}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15})) \Rightarrow p_4(f_5(f_{10}(x_{14}, x_{15})), f_{14}(f_5(x_{14}), f_5(x_{15})))$      $\text{cnf}(p_{4_{37}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15})) \Rightarrow p_6(f_7(f_{10}(x_{14}, x_{15})), f_9(f_7(x_{14}), f_7(x_{15})))$      $\text{cnf}(p_{6_{38}}, \text{negated\_conjecture})$   
 $(p_2(x_{26}, x_{23}) \text{ and } p_{16}(x_{25}, x_{22}) \text{ and } p_{11}(x_{24}, x_{21}) \text{ and } p_{17}(x_{24}, x_{25}, x_{26})) \Rightarrow p_{17}(x_{21}, x_{22}, x_{23})$      $\text{cnf}(p_{17_{39}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15})) \Rightarrow (p_{12}(f_{13}(x_{12}), c_{20}) \text{ or } p_{17}(x_{12}, x_{13}, x_{14}) \text{ or } p_{17}(x_{12}, x_{13}, f_{10}(x_{14}, x_{15})))$      $\text{cnf}(p_{12_{40}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15}) \text{ and } p_{17}(x_{12}, x_{13}, x_{15})) \Rightarrow (p_{12}(f_{13}(x_{12}), c_{20}) \text{ or } p_{17}(x_{12}, x_{13}, f_{10}(x_{14}, x_{15})))$      $\text{cnf}(p_{12_{41}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15}) \text{ and } p_{17}(x_{12}, x_{13}, x_{14}) \text{ and } p_{17}(x_{12}, x_{13}, f_{10}(x_{14}, x_{15}))) \Rightarrow (p_{12}(f_{13}(x_{12}), c_{20}) \text{ or } p_{17}(x_{12}, x_{13}, x_{15}))$

### SYN643-1.p Harrison problem 4298

$p_{15}(f_3(c_{19}))$      $\text{cnf}(f3\_is\_p15_1, \text{negated\_conjecture})$   
 $p_{15}(f_3(c_{18}))$      $\text{cnf}(f3\_is\_p15_2, \text{negated\_conjecture})$   
 $p_{11}(x_0, x_0)$      $\text{cnf}(p11_3, \text{negated\_conjecture})$   
 $p_6(x_{45}, x_{45})$      $\text{cnf}(p6_4, \text{negated\_conjecture})$   
 $p_4(x_{36}, x_{36})$      $\text{cnf}(p4_5, \text{negated\_conjecture})$   
 $p_2(x_{27}, x_{27})$      $\text{cnf}(p2_6, \text{negated\_conjecture})$   
 $p_{16}(x_{18}, x_{18})$      $\text{cnf}(p16_7, \text{negated\_conjecture})$   
 $p_{12}(x_3, x_3)$      $\text{cnf}(p12_8, \text{negated\_conjecture})$   
 $p_6(f_8(f_3(c_{19})), f_8(c_{19}))$      $\text{cnf}(p6_9, \text{negated\_conjecture})$   
 $p_4(f_5(f_3(c_{18})), f_5(c_{18}))$      $\text{cnf}(p4_{10}, \text{negated\_conjecture})$   
 $p_4(f_5(f_3(c_{19})), f_5(c_{19}))$      $\text{cnf}(p4_{11}, \text{negated\_conjecture})$   
 $p_6(f_7(f_3(c_{18})), f_7(c_{18}))$      $\text{cnf}(p6_{12}, \text{negated\_conjecture})$   
 $p_6(f_7(f_3(c_{19})), f_7(c_{19}))$      $\text{cnf}(p6_{13}, \text{negated\_conjecture})$   
 $p_6(f_8(f_3(c_{18})), f_8(c_{18}))$      $\text{cnf}(p6_{14}, \text{negated\_conjecture})$   
 $(p_{15}(x_{17}) \text{ and } p_2(x_{17}, x_{16})) \Rightarrow p_{15}(x_{16})$      $\text{cnf}(p15_{15}, \text{negated\_conjecture})$   
 $p_{11}(x_6, x_7) \Rightarrow p_{12}(f_{13}(x_6), f_{13}(x_7))$      $\text{cnf}(p12_{16}, \text{negated\_conjecture})$   
 $p_2(x_{54}, x_{55}) \Rightarrow p_6(f_8(x_{54}), f_8(x_{55}))$      $\text{cnf}(p6_{17}, \text{negated\_conjecture})$   
 $p_2(x_{52}, x_{53}) \Rightarrow p_6(f_7(x_{52}), f_7(x_{53}))$      $\text{cnf}(p6_{18}, \text{negated\_conjecture})$   
 $p_2(x_{39}, x_{40}) \Rightarrow p_4(f_5(x_{39}), f_5(x_{40}))$      $\text{cnf}(p4_{19}, \text{negated\_conjecture})$   
 $p_2(x_{34}, x_{35}) \Rightarrow p_2(f_3(x_{34}), f_3(x_{35}))$      $\text{cnf}(p2_{20}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15})) \Rightarrow p_{15}(f_{10}(x_{14}, x_{15}))$      $\text{cnf}(p15_{21}, \text{negated\_conjecture})$   
 $(p_{11}(x_0, x_1) \text{ and } p_{11}(x_0, x_2)) \Rightarrow p_{11}(x_1, x_2)$      $\text{cnf}(p11_{22}, \text{negated\_conjecture})$   
 $(p_6(x_{45}, x_{46}) \text{ and } p_6(x_{45}, x_{47})) \Rightarrow p_6(x_{46}, x_{47})$      $\text{cnf}(p6_{23}, \text{negated\_conjecture})$   
 $(p_4(x_{36}, x_{37}) \text{ and } p_4(x_{36}, x_{38})) \Rightarrow p_4(x_{37}, x_{38})$      $\text{cnf}(p4_{24}, \text{negated\_conjecture})$   
 $(p_2(x_{27}, x_{28}) \text{ and } p_2(x_{27}, x_{29})) \Rightarrow p_2(x_{28}, x_{29})$      $\text{cnf}(p2_{25}, \text{negated\_conjecture})$   
 $(p_{16}(x_{18}, x_{19}) \text{ and } p_{16}(x_{18}, x_{20})) \Rightarrow p_{16}(x_{19}, x_{20})$      $\text{cnf}(p16_{26}, \text{negated\_conjecture})$   
 $(p_{12}(x_3, x_4) \text{ and } p_{12}(x_3, x_5)) \Rightarrow p_{12}(x_4, x_5)$      $\text{cnf}(p12_{27}, \text{negated\_conjecture})$   
 $\neg p_4(f_5(f_{10}(f_3(c_{19}), f_3(c_{18}))), f_9(f_5(c_{19}), f_5(c_{18})))$      $\text{cnf}(\text{not\_}p4_{28}, \text{negated\_conjecture})$   
 $p_{17}(x_8, x_9, f_3(c_{19})) \Rightarrow (p_{12}(f_{13}(x_8), c_{20}) \text{ or } p_{17}(x_8, x_9, c_{19}))$      $\text{cnf}(p12_{29}, \text{negated\_conjecture})$   
 $p_{17}(x_{10}, x_{11}, f_3(c_{18})) \Rightarrow (p_{12}(f_{13}(x_{10}), c_{20}) \text{ or } p_{17}(x_{10}, x_{11}, c_{18}))$      $\text{cnf}(p12_{30}, \text{negated\_conjecture})$   
 $p_{17}(x_8, x_9, c_{19}) \Rightarrow (p_{12}(f_{13}(x_8), c_{20}) \text{ or } p_{17}(x_8, x_9, f_3(c_{19})))$      $\text{cnf}(p12_{31}, \text{negated\_conjecture})$   
 $p_{17}(x_{10}, x_{11}, c_{18}) \Rightarrow (p_{12}(f_{13}(x_{10}), c_{20}) \text{ or } p_{17}(x_{10}, x_{11}, f_3(c_{18})))$      $\text{cnf}(p12_{32}, \text{negated\_conjecture})$   
 $(p_6(x_{48}, x_{50}) \text{ and } p_6(x_{49}, x_{51})) \Rightarrow p_6(f_{14}(x_{48}, x_{49}), f_{14}(x_{50}, x_{51}))$      $\text{cnf}(p6_{33}, \text{negated\_conjecture})$   
 $(p_2(x_{30}, x_{32}) \text{ and } p_2(x_{31}, x_{33})) \Rightarrow p_2(f_{10}(x_{30}, x_{31}), f_{10}(x_{32}, x_{33}))$      $\text{cnf}(p2_{34}, \text{negated\_conjecture})$   
 $(p_4(x_{42}, x_{44}) \text{ and } p_4(x_{41}, x_{43})) \Rightarrow p_4(f_9(x_{41}, x_{42}), f_9(x_{43}, x_{44}))$      $\text{cnf}(p4_{35}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15})) \Rightarrow p_6(f_8(f_{10}(x_{14}, x_{15})), f_{14}(f_8(x_{14}), f_8(x_{15})))$      $\text{cnf}(p6_{36}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15})) \Rightarrow p_4(f_5(f_{10}(x_{14}, x_{15})), f_9(f_5(x_{14}), f_5(x_{15})))$      $\text{cnf}(p4_{37}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15})) \Rightarrow p_6(f_7(f_{10}(x_{14}, x_{15})), f_{14}(f_7(x_{14}), f_7(x_{15})))$      $\text{cnf}(p6_{38}, \text{negated\_conjecture})$   
 $(p_2(x_{26}, x_{23}) \text{ and } p_{16}(x_{25}, x_{22}) \text{ and } p_{11}(x_{24}, x_{21}) \text{ and } p_{17}(x_{24}, x_{25}, x_{26})) \Rightarrow p_{17}(x_{21}, x_{22}, x_{23})$      $\text{cnf}(p_{17_{39}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15})) \Rightarrow (p_{12}(f_{13}(x_{12}), c_{20}) \text{ or } p_{17}(x_{12}, x_{13}, x_{14}) \text{ or } p_{17}(x_{12}, x_{13}, f_{10}(x_{14}, x_{15})))$      $\text{cnf}(p_{12_{40}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15}) \text{ and } p_{17}(x_{12}, x_{13}, x_{15})) \Rightarrow (p_{12}(f_{13}(x_{12}), c_{20}) \text{ or } p_{17}(x_{12}, x_{13}, f_{10}(x_{14}, x_{15})))$      $\text{cnf}(p_{12_{41}}, \text{negated\_conjecture})$   
 $(p_{15}(x_{14}) \text{ and } p_{15}(x_{15}) \text{ and } p_{17}(x_{12}, x_{13}, x_{14}) \text{ and } p_{17}(x_{12}, x_{13}, f_{10}(x_{14}, x_{15}))) \Rightarrow (p_{12}(f_{13}(x_{12}), c_{20}) \text{ or } p_{17}(x_{12}, x_{13}, x_{15}))$

### SYN720-1.p Synthetic domain theory for EBL

include('Axioms/SYN001-0.ax')

### SYN721+1.p Peter Andrews Problem LX1

$(r(a, b) \text{ and } \forall x: (\exists y: r(x, y) \Rightarrow q(x, x)) \text{ and } \forall u, v: (q(u, v) \Rightarrow \forall z: r(z, v))) \Rightarrow \exists w: (r(b, w) \text{ and } q(w, a))$      $\text{fof}(lx_1, \text{conjecture})$

### SYN721-1.p Peter Andrews Problem LX1

$r(a, b)$      $\text{cnf}(lx_{11}, \text{negated\_conjecture})$   
 $r(a, b) \Rightarrow q(a, a)$      $\text{cnf}(lx_{12}, \text{negated\_conjecture})$

$q(a, b) \Rightarrow r(c, b)$     cnf(lx13, negated\_conjecture)  
 $q(a, a) \Rightarrow \neg r(b, a)$     cnf(lx14, negated\_conjecture)

**SYN722+1.p** Peter Andrews Problem THM119

$\neg \forall z: ((p(z) \text{ or } r(z)) \text{ and } q(z)) \text{ and } \forall x: \exists y: (p(x) \text{ or } \neg q(x) \text{ or } \neg q(y) \text{ or } \neg q(c) \text{ or } \neg q(d)) \text{ and } (\neg p(a) \text{ or } \neg p(b))$     fof(thm119)

**SYN723+1.p** Peter Andrews Problem THM138

$\exists x: \forall y: (p(x) \iff p(y)) \iff ((\exists x: q(x) \iff \forall y: r(y)) \iff ((\exists x: \forall y: (q(x) \iff q(y)) \iff (\exists x: r(x) \iff \forall y: s(y))) \iff (\exists x: \forall y: (r(x) \iff r(y)) \iff ((\exists x: s(x) \iff \forall y: p(y)) \iff (\exists x: \forall y: (s(x) \iff s(y)) \iff (\exists x: p(x) \iff \forall y: q(y))))))$     fof(thm138, conjecture)

**SYN724+1.p** Peter Andrews Problem THM31

$\forall x: (r(x) \Rightarrow s(x)) \iff \forall x: ((r(x) \text{ and } s(x)) \iff r(x))$     fof(thm31, conjecture)

**SYN724-1.p** Peter Andrews Problem THM31

$r(a) \Rightarrow s(a)$     cnf(thm313, negated\_conjecture)  
 $r(\text{sk}_1) \text{ or } r(\text{sk}_2)$     cnf(thm314, negated\_conjecture)  
 $(r(\text{sk}_2) \text{ and } s(\text{sk}_2)) \Rightarrow r(\text{sk}_1)$     cnf(thm319, negated\_conjecture)  
 $s(\text{sk}_1) \Rightarrow r(\text{sk}_2)$     cnf(thm3110, negated\_conjecture)  
 $(r(\text{sk}_2) \text{ and } s(\text{sk}_1)) \Rightarrow \neg s(\text{sk}_2)$     cnf(thm3115, negated\_conjecture)

**SYN725+1.p** Peter Andrews Problem THM39

$\forall x: (r(x) \text{ or } (s(x) \iff (r(x) \text{ and } s(x)))) \Rightarrow \forall x: (r(x) \Rightarrow s(x))$     fof(thm39, conjecture)

**SYN726+1.p** Peter Andrews Problem THM400

$((\forall x, y, z: ((p(x, y) \text{ and } p(y, z)) \Rightarrow p(x, z)) \text{ and } \forall x, y, z: ((q(x, y) \text{ and } q(y, z)) \Rightarrow q(x, z)) \text{ and } \forall x, y: (q(x, y) \Rightarrow q(y, x)) \text{ and } \forall x, y: (p(x, y) \text{ or } q(x, y)) \Rightarrow \forall x, y: p(x, y) \text{ or } \forall x, y: q(x, y))$     fof(thm400, conjecture)

**SYN726-1.p** Peter Andrews Problem THM400

$(p(a, b) \text{ and } p(b, c)) \Rightarrow p(a, c)$     cnf(thm4001, negated\_conjecture)  
 $(q(a, b) \text{ and } q(b, c)) \Rightarrow q(a, c)$     cnf(thm4002, negated\_conjecture)  
 $q(a, b) \Rightarrow q(b, a)$     cnf(thm4003, negated\_conjecture)  
 $p(a, b) \text{ or } q(a, b)$     cnf(thm4004, negated\_conjecture)  
 $\neg p(\text{sk}_1, \text{sk}_2)$     cnf(thm4005, negated\_conjecture)  
 $\neg q(\text{sk}_3, \text{sk}_4)$     cnf(thm4006, negated\_conjecture)

**SYN727+1.p** Peter Andrews Problem THM68

$(\forall x: \text{likes}(x, \text{bruce}) \text{ and } \forall y: (\exists z: \text{likes}(y, z) \Rightarrow \text{likes}(\text{lyle}, y))) \Rightarrow \exists u: \forall v: \text{likes}(u, v)$     fof(thm68, conjecture)

**SYN727-1.p** Peter Andrews Problem THM68

$\text{likes}(a, \text{bruce})$     cnf(thm681, negated\_conjecture)  
 $\text{likes}(a, b) \Rightarrow \text{likes}(\text{lyle}, a)$     cnf(thm682, negated\_conjecture)  
 $\neg \text{likes}(a, \text{sk}_1(a))$     cnf(thm683, negated\_conjecture)

**SYN728+1.p** Peter Andrews Problem THM69

$(\forall x: (\exists y: p(x, y) \Rightarrow \forall z: p(z, z)) \text{ and } \forall r: \exists s: (p(r, s) \text{ or } (m(r) \text{ and } q(f(r, s)))) \text{ and } \forall w: (q(w) \Rightarrow \neg m(g(w)))) \Rightarrow \forall u: \exists v: (p(g(u), v) \text{ and } p(u, u))$     fof(thm69, conjecture)

**SYN728-1.p** Peter Andrews Problem THM69

$p(a, b) \Rightarrow p(c, c)$     cnf(thm691, negated\_conjecture)  
 $m(a) \text{ or } p(a, \text{sk}_1(a))$     cnf(thm692, negated\_conjecture)  
 $q(f(a, \text{sk}_1(a))) \text{ or } p(a, \text{sk}_1(a))$     cnf(thm693, negated\_conjecture)  
 $m(g(a)) \Rightarrow \neg q(a)$     cnf(thm694, negated\_conjecture)  
 $p(\text{sk}_2, \text{sk}_2) \Rightarrow \neg p(g(\text{sk}_2), a)$     cnf(thm695, negated\_conjecture)

**SYN729+1.p** Peter Andrews Problem THM72

$(\forall x: \exists y: (p(x) \Rightarrow (l(x, g(h(y))) \text{ and } p(y))) \text{ and } \forall w: (p(w) \Rightarrow (p(g(w)) \text{ and } p(h(w)))) \Rightarrow \forall x: (p(x) \Rightarrow \exists y: (l(x, y) \text{ and } p(y)))$     fof(thm72, conjecture)

**SYN729-1.p** Peter Andrews Problem THM72

$p(a) \Rightarrow l(a, g(h(\text{sk}_1(a))))$     cnf(thm721, negated\_conjecture)  
 $p(a) \Rightarrow p(\text{sk}_1(a))$     cnf(thm722, negated\_conjecture)  
 $p(a) \Rightarrow p(g(a))$     cnf(thm723, negated\_conjecture)  
 $p(a) \Rightarrow p(h(a))$     cnf(thm724, negated\_conjecture)  
 $p(\text{sk}_2)$     cnf(thm725, negated\_conjecture)  
 $p(a) \Rightarrow \neg l(\text{sk}_2, a)$     cnf(thm726, negated\_conjecture)

**SYN730+1.p** Peter Andrews Problem THM75

$\exists v: \forall j: \exists q: ((p(a, j, h(j)) \text{ or } p(v, j, k(j))) \Rightarrow p(v, j, q))$     fof(thm<sub>75</sub>, conjecture)

**SYN731+1.p** Peter Andrews Problem X2150

$\exists w: (\forall x: \exists y: p(w, x, y) \Rightarrow \exists z: p(z, z, w))$     fof(x<sub>2150</sub>, conjecture)

**SYN731-1.p** Peter Andrews Problem X2150

$p(a, b, \text{sk}_1(b, a))$     cnf(x<sub>2150</sub><sub>1</sub>, negated\_conjecture)

$\neg p(a, a, b)$     cnf(x<sub>2150</sub><sub>2</sub>, negated\_conjecture)

**SYN731^5.p** TPS problem X2150

cP:  $\$i \rightarrow \$i \rightarrow \$i \rightarrow \$o$     thf(cP, type)

$\exists w: \$i: (\forall x: \$i: \exists y: \$i: (cP@w@x@y) \Rightarrow \exists z: \$i: (cP@z@z@w))$     thf(cX<sub>2150</sub>, conjecture)

**SYN732+1.p** Peter Andrews Problem X3411

$\forall y: (\forall x: p(x, y) \Rightarrow \forall u: q(u, y)) \Rightarrow \exists z: (\exists v: p(v, z) \Rightarrow \exists w: (p(z, w) \text{ or } q(w, z)))$     fof(x<sub>3411</sub>, conjecture)

**SYN732^5.p** TPS problem X3411

cQ:  $\$i \rightarrow \$i \rightarrow \$o$     thf(cQ, type)

cP:  $\$i \rightarrow \$i \rightarrow \$o$     thf(cP, type)

$\forall xy: \$i: (\forall xx: \$i: (cP@xx@xy) \Rightarrow \forall xu: \$i: (cQ@xu@xy)) \Rightarrow \exists xz: \$i: (\exists xv: \$i: (cP@xv@xz) \Rightarrow \exists xw: \$i: (cP@xz@xw \text{ or } cQ@xw@xz))$

**SYN733+1.p** Peter Andrews Problem Y2141

$\forall x: \exists y: (p(x) \text{ and } (q(y) \text{ or } q(x))) \Rightarrow \exists z: (p(z) \text{ and } q(z))$     fof(y<sub>2141</sub>, conjecture)

**SYN734-1.p** PSAT - K=4 C=20 V=4 D=1.2

ssRr( $u$ , skf<sub>1</sub>( $u$ ))    cnf(clause<sub>1</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>4</sub>( $v$ ))  $\Rightarrow$  (ssPv<sub>1</sub>( $u$ ) or ssPv<sub>2</sub>( $u$ ) or ssPv<sub>4</sub>( $u$ ))    cnf(clause<sub>2</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>3</sub>( $v$ ))  $\Rightarrow$  (ssPv<sub>1</sub>( $u$ ) or ssPv<sub>2</sub>( $u$ ) or ssPv<sub>3</sub>( $u$ ))    cnf(clause<sub>3</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>1</sub>( $u$ ) and ssPv<sub>2</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>1</sub>( $v$ ) or ssPv<sub>3</sub>( $u$ ))    cnf(clause<sub>4</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>1</sub>( $u$ ) and ssPv<sub>3</sub>( $u$ ) and ssPv<sub>4</sub>( $u$ ))  $\Rightarrow$  ssPv<sub>4</sub>( $v$ )    cnf(clause<sub>5</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>1</sub>( $v$ ) and ssPv<sub>3</sub>( $u$ ) and ssPv<sub>4</sub>( $u$ ))  $\Rightarrow$  ssPv<sub>2</sub>( $u$ )    cnf(clause<sub>6</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>4</sub>( $v$ ) and ssPv<sub>1</sub>( $u$ ) and ssPv<sub>2</sub>( $u$ ))  $\Rightarrow$   $\neg$ ssPv<sub>3</sub>( $u$ )    cnf(clause<sub>7</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssRr( $u$ ,  $w$ ))  $\Rightarrow$  (ssPv<sub>4</sub>( $v$ ) or ssPv<sub>2</sub>( $w$ ) or ssPv<sub>1</sub>( $u$ ) or ssPv<sub>4</sub>( $u$ ))    cnf(clause<sub>8</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>2</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>2</sub>( $v$ ) or ssPv<sub>1</sub>( $w$ ) or ssPv<sub>4</sub>( $u$ ))    cnf(clause<sub>9</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>4</sub>( $v$ ) and ssRr( $u$ ,  $w$ ))  $\Rightarrow$  (ssPv<sub>3</sub>( $w$ ) or ssPv<sub>1</sub>( $u$ ) or ssPv<sub>3</sub>( $u$ ))    cnf(clause<sub>10</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>3</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>1</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>3</sub>( $w$ ) or ssPv<sub>3</sub>( $u$ ))    cnf(clause<sub>11</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>4</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>1</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>1</sub>( $w$ ) or ssPv<sub>2</sub>( $u$ ))    cnf(clause<sub>12</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>1</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>4</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>4</sub>( $w$ ) or ssPv<sub>1</sub>( $u$ ))    cnf(clause<sub>13</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>4</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>4</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>3</sub>( $w$ ) or ssPv<sub>1</sub>( $u$ ))    cnf(clause<sub>14</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>4</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>3</sub>( $w$ ))  $\Rightarrow$  (ssPv<sub>1</sub>( $u$ ) or ssPv<sub>2</sub>( $u$ ))    cnf(clause<sub>15</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>1</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>2</sub>( $u$ ) and ssPv<sub>4</sub>( $u$ ))  $\Rightarrow$  ssPv<sub>2</sub>( $w$ )    cnf(clause<sub>16</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>3</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>1</sub>( $w$ ) and ssPv<sub>2</sub>( $u$ ))  $\Rightarrow$   $\neg$ ssPv<sub>4</sub>( $u$ )    cnf(clause<sub>17</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssRr( $u$ ,  $w$ ) and ssRr( $u$ ,  $x$ ) and ssPv<sub>4</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>4</sub>( $v$ ) or ssPv<sub>3</sub>( $w$ ) or ssPv<sub>1</sub>( $x$ ))    cnf(clause<sub>18</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>4</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssRr( $u$ ,  $x$ ) and ssPv<sub>4</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>4</sub>( $w$ ) or ssPv<sub>3</sub>( $x$ ))    cnf(clause<sub>19</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>3</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>1</sub>( $w$ ) and ssRr( $u$ ,  $x$ ))  $\Rightarrow$  (ssPv<sub>3</sub>( $x$ ) or ssPv<sub>1</sub>( $u$ ))    cnf(clause<sub>20</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>2</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>1</sub>( $w$ ) and ssRr( $u$ ,  $x$ ) and ssPv<sub>4</sub>( $u$ ))  $\Rightarrow$  ssPv<sub>3</sub>( $x$ )    cnf(clause<sub>21</sub>, negated\_conjecture)

**SYN735-1.p** PSAT - K=4 C=20 V=4 D=1.8

ssRr( $u$ , skf<sub>1</sub>( $u$ ))    cnf(clause<sub>1</sub>, negated\_conjecture)

ssRr( $u$ ,  $v$ )  $\Rightarrow$  (ssPv<sub>1</sub>( $v$ ) or ssPv<sub>1</sub>( $u$ ) or ssPv<sub>3</sub>( $u$ ) or ssPv<sub>4</sub>( $u$ ))    cnf(clause<sub>2</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>2</sub>( $v$ ) and ssPv<sub>2</sub>( $u$ ) and ssPv<sub>4</sub>( $u$ ))  $\Rightarrow$  ssPv<sub>3</sub>( $u$ )    cnf(clause<sub>3</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssRr( $u$ ,  $w$ ))  $\Rightarrow$  (ssPv<sub>3</sub>( $v$ ) or ssPv<sub>2</sub>( $w$ ) or ssPv<sub>1</sub>( $u$ ) or ssPv<sub>3</sub>( $u$ ))    cnf(clause<sub>4</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>1</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>4</sub>( $v$ ) or ssPv<sub>2</sub>( $w$ ) or ssPv<sub>2</sub>( $u$ ))    cnf(clause<sub>5</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>4</sub>( $v$ ) and ssRr( $u$ ,  $w$ ))  $\Rightarrow$  (ssPv<sub>2</sub>( $w$ ) or ssPv<sub>2</sub>( $u$ ) or ssPv<sub>3</sub>( $u$ ))    cnf(clause<sub>6</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>2</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>4</sub>( $v$ ) or ssPv<sub>3</sub>( $w$ ) or ssPv<sub>1</sub>( $u$ ))    cnf(clause<sub>7</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>1</sub>( $u$ ) and ssPv<sub>4</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>4</sub>( $v$ ) or ssPv<sub>3</sub>( $w$ ))    cnf(clause<sub>8</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>1</sub>( $u$ ) and ssPv<sub>4</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>4</sub>( $v$ ) or ssPv<sub>2</sub>( $w$ ))    cnf(clause<sub>9</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>3</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>4</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>1</sub>( $w$ ) or ssPv<sub>2</sub>( $u$ ))    cnf(clause<sub>10</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>1</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>3</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>3</sub>( $w$ ) or ssPv<sub>2</sub>( $u$ ))    cnf(clause<sub>11</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>4</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>1</sub>( $w$ ))  $\Rightarrow$  (ssPv<sub>2</sub>( $u$ ) or ssPv<sub>3</sub>( $u$ ))    cnf(clause<sub>12</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>3</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssPv<sub>1</sub>( $u$ ) and ssPv<sub>4</sub>( $u$ ))  $\Rightarrow$  ssPv<sub>3</sub>( $w$ )    cnf(clause<sub>13</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>2</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssRr( $u$ ,  $x$ ))  $\Rightarrow$  (ssPv<sub>4</sub>( $w$ ) or ssPv<sub>3</sub>( $x$ ) or ssPv<sub>2</sub>( $u$ ))    cnf(clause<sub>14</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>4</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssRr( $u$ ,  $x$ ) and ssPv<sub>3</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>3</sub>( $w$ ) or ssPv<sub>1</sub>( $x$ ))    cnf(clause<sub>15</sub>, negated\_conjecture)

(ssRr( $u$ ,  $v$ ) and ssPv<sub>1</sub>( $v$ ) and ssRr( $u$ ,  $w$ ) and ssRr( $u$ ,  $x$ ) and ssPv<sub>2</sub>( $u$ ))  $\Rightarrow$  (ssPv<sub>3</sub>( $w$ ) or ssPv<sub>2</sub>( $x$ ))    cnf(clause<sub>16</sub>, negated\_conjecture)







$b_6 \neq b_8$     cnf(at\_least\_11\_68, negated\_conjecture)  
 $b_6 \neq b_9$     cnf(at\_least\_11\_69, negated\_conjecture)  
 $b_6 \neq b_{10}$     cnf(at\_least\_11\_610, negated\_conjecture)  
 $b_6 \neq b_{11}$     cnf(at\_least\_11\_611, negated\_conjecture)  
 $b_7 \neq b_8$     cnf(at\_least\_11\_78, negated\_conjecture)  
 $b_7 \neq b_9$     cnf(at\_least\_11\_79, negated\_conjecture)  
 $b_7 \neq b_{10}$     cnf(at\_least\_11\_710, negated\_conjecture)  
 $b_7 \neq b_{11}$     cnf(at\_least\_11\_711, negated\_conjecture)  
 $b_8 \neq b_9$     cnf(at\_least\_11\_89, negated\_conjecture)  
 $b_8 \neq b_{10}$     cnf(at\_least\_11\_810, negated\_conjecture)  
 $b_8 \neq b_{11}$     cnf(at\_least\_11\_811, negated\_conjecture)  
 $b_9 \neq b_{10}$     cnf(at\_least\_11\_910, negated\_conjecture)  
 $b_9 \neq b_{11}$     cnf(at\_least\_11\_911, negated\_conjecture)  
 $b_{10} \neq b_{11}$     cnf(at\_least\_11\_1011, negated\_conjecture)

**SYN915+1.p** TRUE

\$true    fof(truth, conjecture)

**SYN915-1.p** FALSE

\$false    cnf(false\_clause, negated\_conjecture)

**SYN915^4.p** TRUE

include('Axioms/LCL010^0.ax')

ivalid@(iatom@itrue)    thf(truth, conjecture)

**SYN916+1.p** FALSE

\$false    fof(falsity, conjecture)

**SYN916-1.p** FALSE

\$true    cnf(true\_clause, negated\_conjecture)

**SYN916^4.p** FALSE

include('Axioms/LCL010^0.ax')

ivalid@(iatom@ifalse)    thf(falsity, conjecture)

**SYN917+1.p** Combined problems from Smullyan

$((\forall x: ((f(x) \text{ and } g(x)) \Rightarrow h(x)) \Rightarrow \exists y: (f(y) \text{ and } \neg g(y))) \text{ and } (\forall w: (f(w) \Rightarrow g(w)) \text{ or } \forall z: (f(z) \Rightarrow h(z)))) \Rightarrow (\forall r: ((f(r) \text{ and } h(r)) \Rightarrow g(r)) \Rightarrow \exists v: (f(v) \text{ and } g(v) \text{ and } \neg h(v)))) \text{ and } ((\forall x, y: (r(x, y) \Rightarrow r(y, x)) \text{ and } \forall x, y, z: ((r(x, y) \text{ and } r(y, z)) \Rightarrow r(x, z))) \Rightarrow \forall x, y: (r(x, y) \Rightarrow r(x, x))) \text{ and } ((\forall x: ((f(x) \text{ and } g(x)) \Rightarrow h(x)) \Rightarrow \exists x: (f(x) \text{ and } \neg g(x))) \text{ and } (\forall w: (f(w) \Rightarrow g(w)) \text{ or } \forall z: (f(z) \Rightarrow h(z)))) \Rightarrow (\forall r: ((f(r) \text{ and } h(r)) \Rightarrow g(r)) \Rightarrow \exists v: (f(v) \text{ and } g(v) \text{ and } \neg h(v)))) \text{ and } \exists x: \forall y: ((p(y) \Rightarrow q(x)) \Rightarrow (p(x) \Rightarrow q(x))) \text{ and } (\forall x: (p(x) \text{ and } q(x)) \Leftrightarrow (\forall x: p(x) \text{ and } \forall x: q(x))) \text{ and } ((\forall x: p(x) \text{ or } \forall x: q(x)) \Rightarrow \forall x: (p(x) \text{ or } q(x))) \text{ and } (\exists x: (p(x) \text{ or } q(x)) \Leftrightarrow (\exists x: p(x) \text{ or } \exists x: q(x))) \text{ and } (\exists x: p(x) \text{ and } (\exists x: (p(x) \text{ and } q(x)) \Rightarrow (\exists x: p(x) \text{ and } \exists x: q(x))) \text{ and } \forall y: (\forall x: p(x) \Rightarrow p(y)) \text{ and } (\forall x: p(x) \Rightarrow \exists x: p(x)) \text{ and } (\neg \exists y: p(y) \Rightarrow \forall y: (\exists x: p(x) \Rightarrow p(y))) \text{ and } (\forall x: (p(x) \text{ or } c) \Leftrightarrow (\forall x: p(x) \text{ or } c)) \text{ and } (\exists x: (p(x) \text{ and } c) \Leftrightarrow (\exists x: p(x) \text{ and } c)) \text{ and } (\exists x: c \Leftrightarrow c) \text{ and } (\forall x: c \Leftrightarrow c) \text{ and } (\exists x: (c \Rightarrow p(x)) \Leftrightarrow (c \Rightarrow \exists x: p(x))) \text{ and } (\exists x: (p(x) \Rightarrow c) \Leftrightarrow (\forall x: p(x) \Rightarrow c)) \text{ and } (\forall x: (c \Rightarrow p(x)) \Leftrightarrow (c \Rightarrow \forall x: p(x))) \text{ and } (\forall x: (p(x) \Rightarrow c) \Leftrightarrow (\exists x: p(x) \Rightarrow c)))$

**SYN918+1.p** From Smullyan

$(\forall x: ((f(x) \text{ and } g(x)) \Rightarrow h(x)) \Rightarrow \exists y: (f(y) \text{ and } \neg g(y))) \text{ and } (\forall w: (f(w) \Rightarrow g(w)) \text{ or } \forall z: (f(z) \Rightarrow h(z))) \Rightarrow (\forall r: ((f(r) \text{ and } h(r)) \Rightarrow g(r)) \Rightarrow \exists v: (f(v) \text{ and } g(v) \text{ and } \neg h(v)))$     fof(prove\_this, conjecture)

**SYN919+1.p** From Smullyan

$(\forall x, y: (r(x, y) \Rightarrow r(y, x)) \text{ and } \forall x, y, z: ((r(x, y) \text{ and } r(y, z)) \Rightarrow r(x, z))) \Rightarrow \forall x, y: (r(x, y) \Rightarrow r(x, x))$     fof(prove\_this, conjecture)

**SYN920+1.p** From Smullyan

$((\forall x: ((f(x) \text{ and } g(x)) \Rightarrow h(x)) \Rightarrow \exists x: (f(x) \text{ and } \neg g(x))) \text{ and } (\forall w: (f(w) \Rightarrow g(w)) \text{ or } \forall z: (f(z) \Rightarrow h(z)))) \Rightarrow (\forall r: ((f(r) \text{ and } h(r)) \Rightarrow g(r)) \Rightarrow \exists v: (f(v) \text{ and } g(v) \text{ and } \neg h(v)))$     fof(prove\_this, conjecture)

**SYN921+1.p** From Smullyan

$\exists x: \forall y: ((p(y) \Rightarrow q(x)) \Rightarrow (p(x) \Rightarrow q(x)))$     fof(prove\_this, conjecture)

**SYN922+1.p** From Smullyan

$\forall x: (p(x) \text{ and } q(x)) \Leftrightarrow (\forall x: p(x) \text{ and } \forall x: q(x))$     fof(prove\_this, conjecture)

**SYN923+1.p** From Smullyan

$(\forall x: p(x) \text{ or } \forall x: q(x)) \Rightarrow \forall x: (p(x) \text{ or } q(x))$     fof(prove\_this, conjecture)

**SYN924+1.p** From Smullyan

$$\exists x: (p(x) \text{ or } q(x)) \iff (\exists x: p(x) \text{ or } \exists x: q(x)) \quad \text{fof(prove\_this, conjecture)}$$

**SYN925+1.p** From Smullyan

$$\exists y: (p(y) \Rightarrow \forall x: p(x)) \quad \text{fof(prove\_this, conjecture)}$$

**SYN926+1.p** From Smullyan

$$\exists x: (p(x) \text{ and } q(x)) \Rightarrow (\exists x: p(x) \text{ and } \exists x: q(x)) \quad \text{fof(prove\_this, conjecture)}$$

**SYN927+1.p** From Smullyan

$$\forall y: (\forall x: p(x) \Rightarrow p(y)) \quad \text{fof(prove\_this, conjecture)}$$

**SYN928+1.p** From Smullyan

$$\forall x: p(x) \Rightarrow \exists x: p(x) \quad \text{fof(prove\_this, conjecture)}$$

**SYN929+1.p** From Smullyan

$$\neg \exists y: p(y) \Rightarrow \forall y: (\exists x: p(x) \Rightarrow p(y)) \quad \text{fof(prove\_this, conjecture)}$$

**SYN930+1.p** From Smullyan

$$\forall x: (p(x) \text{ or } c) \iff (\forall x: p(x) \text{ or } c) \quad \text{fof(prove\_this, conjecture)}$$

**SYN931+1.p** From Smullyan

$$\exists x: (p(x) \text{ and } c) \iff (\exists x: p(x) \text{ and } c) \quad \text{fof(prove\_this, conjecture)}$$

**SYN932+1.p** From Smullyan

$$\exists x: c \iff c \quad \text{fof(prove\_this, conjecture)}$$

**SYN933+1.p** From Smullyan

$$\forall x: c \iff c \quad \text{fof(prove\_this, conjecture)}$$

**SYN934+1.p** From Smullyan

$$\exists x: (c \Rightarrow p(x)) \iff (c \Rightarrow \exists x: p(x)) \quad \text{fof(prove\_this, conjecture)}$$

**SYN935+1.p** From Smullyan

$$\exists x: (p(x) \Rightarrow c) \iff (\forall x: p(x) \Rightarrow c) \quad \text{fof(prove\_this, conjecture)}$$

**SYN936+1.p** From Smullyan

$$\forall x: (c \Rightarrow p(x)) \iff (c \Rightarrow \forall x: p(x)) \quad \text{fof(prove\_this, conjecture)}$$

**SYN937+1.p** From Smullyan

$$\forall x: (p(x) \Rightarrow c) \iff (\exists x: p(x) \Rightarrow c) \quad \text{fof(prove\_this, conjecture)}$$

**SYN939+1.p** Syntactic from Shults

$$\forall c, b: (\forall z: q(f(z)) \Rightarrow \exists x, y: ((p(f(y)) \Rightarrow p(x)) \text{ and } (r(y) \Rightarrow (r(b) \text{ and } r(c))) \text{ and } q(x))) \quad \text{fof(prove\_this, conjecture)}$$

**SYN940+1.p** Syntactic from Shults

$$\forall b, c: (\forall z: q(f(z)) \Rightarrow \exists x, y: ((p(f(y)) \Rightarrow (p(x) \text{ and } (r(y) \Rightarrow (r(b) \text{ and } r(c)))) \text{ and } q(x))) \quad \text{fof(prove\_this, conjecture)}$$

**SYN941+1.p** Syntactic from Shults

$$\forall b, c: (q(f(b)) \Rightarrow \exists x, y: ((p(f(y)) \Rightarrow (p(x) \text{ and } (r(y) \Rightarrow (r(b) \text{ and } r(c)))) \text{ and } q(x))) \quad \text{fof(prove\_this, conjecture)}$$

**SYN942+1.p** Syntactic from Shults

$$(\forall x: (a(x) \Rightarrow (b(x) \text{ or } c(x))) \text{ and } \neg \forall x: (a(x) \Rightarrow b(x))) \Rightarrow \exists x: (a(x) \text{ and } c(x)) \quad \text{fof(prove\_this, conjecture)}$$

**SYN943+1.p** Syntactic from Shults

$$\forall a: \exists x, x_2, x_3, x_4, y: ((p(a) \text{ and } e(a) \text{ and } (e(x) \Rightarrow (g(x) \text{ or } s(x, f(x)))) \text{ and } (e(x_2) \Rightarrow (g(x_2) \text{ or } c(f(x_2)))) \text{ and } (s(a, y) \Rightarrow p(y))) \Rightarrow ((p(x_3) \text{ and } g(x_3)) \text{ or } (p(x_4) \text{ and } c(x_4)))) \quad \text{fof(prove\_this, conjecture)}$$

**SYN944+1.p** Syntactic from Shults

$$\forall a, b, c: ((s(a) \text{ and } s(b) \text{ and } r(b, c) \text{ and } \forall x: (s(x) \Rightarrow p(x)) \text{ and } \forall x, y: (r(x, y) \Rightarrow q(x, y))) \Rightarrow \exists x, y: (p(x) \text{ and } q(x, y))) \quad \text{fof(prove\_this, conjecture)}$$

**SYN945+1.p** Syntactic from Shults

$$\forall x: p(x) \Rightarrow \forall a, b: (p(a) \text{ and } p(b)) \quad \text{fof(prove\_this, conjecture)}$$

**SYN946+1.p** Syntactic from Shults

$$(\forall x: p(x) \text{ and } \exists y: q(y)) \Rightarrow \exists z: \forall y: (p(y) \text{ or } r(z)) \quad \text{fof(prove\_this, conjecture)}$$

**SYN947+1.p** Syntactic from Shults

$$\forall x: \exists y: (p(x) \text{ and } q(y)) \Rightarrow \exists z: \forall y: (p(y) \text{ or } r(z)) \quad \text{fof(prove\_this, conjecture)}$$

**SYN948+1.p** Syntactic from Shults

$$\forall x: \exists y: (a(x, y) \text{ and } a(y, y)) \Rightarrow \exists z: a(z, z) \quad \text{fof(prove\_this, conjecture)}$$

**SYN949+1.p** Syntactic from Shults

$\forall a, b, c: ((s(a) \text{ and } s(b) \text{ and } r(b, c) \text{ and } \forall x: (s(x) \Rightarrow p(x)) \text{ and } \forall x, y: (r(x, y) \Rightarrow q(x, y))) \Rightarrow \exists x, y: (p(x) \text{ and } q(x, y)))$  fo

**SYN950+1.p** Syntactic from Shults

$\forall a, b: (\forall y: (q(y) \Rightarrow p(y)) \Rightarrow \exists x: ((p(x) \Rightarrow p(a)) \text{ and } (q(x) \Rightarrow p(b))))$  fof(prove\_this, conjecture)

**SYN951+1.p** Syntactic from Shults

$\exists x: p(x) \Rightarrow (\exists x: p(x) \text{ and } (a \Rightarrow ((b \text{ or } \neg b) \text{ and } (q \Rightarrow q))))$  fof(prove\_this, conjecture)

**SYN952+1.p** Syntactic from Shults

$\forall x: p(x) \Rightarrow \exists y: p(y)$  fof(prove\_this, conjecture)

**SYN953+1.p** Syntactic from Shults

$\forall x: (p(x) \Rightarrow q(x)) \Rightarrow (\forall x: p(x) \Rightarrow \forall x: q(x))$  fof(prove\_this, conjecture)

**SYN954+1.p** Syntactic from Shults

$\forall a, b: (\forall z: (q(z) \Rightarrow p(z)) \Rightarrow \exists x: ((p(x) \Rightarrow p(a)) \text{ and } (q(x) \Rightarrow p(b))))$  fof(prove\_this, conjecture)

**SYN955+1.p** Syntactic from Shults

$\forall x: (a(x) \Rightarrow b(x)) \Rightarrow (\exists x: a(x) \Rightarrow \exists x: b(x))$  fof(prove\_this, conjecture)

**SYN956+1.p** Syntactic from Shults

$\exists x: (a(x) \Rightarrow b(x)) \Rightarrow (\forall x: a(x) \Rightarrow \exists x: b(x))$  fof(prove\_this, conjecture)

**SYN957+1.p** Syntactic from Shults

$\neg \exists y: \forall x: (a(x, y) \iff \neg a(x, x))$  fof(prove\_this, conjecture)

**SYN958+1.p** Syntactic from Shults

$(\exists x: a(x) \text{ and } \forall x: b(x)) \Rightarrow \exists x: (a(x) \text{ and } b(x))$  fof(prove\_this, conjecture)

**SYN959+1.p** Syntactic from Shults

$\exists x: b(x) \Rightarrow \exists x: (a(x) \text{ or } b(x))$  fof(prove\_this, conjecture)

**SYN960+1.p** Syntactic from Shults

$\exists x, y: a(x, y) \iff \exists y, x: a(x, y)$  fof(prove\_this, conjecture)

**SYN961+1.p** Syntactic from Shults

$\forall a, b: (\forall x: p(x) \Rightarrow (p(a) \text{ and } p(b)))$  fof(prove\_this, conjecture)

**SYN962+1.p** Syntactic from Shults

$\forall x: p(x) \Rightarrow (\forall x: p(x) \text{ and } \forall y: p(y))$  fof(prove\_this, conjecture)

**SYN963+1.p** Syntactic from Shults

$\exists x: p(x) \iff \exists y: p(y)$  fof(prove\_this, conjecture)

**SYN964+1.p** Syntactic from Shults

$\exists x: p(x) \Rightarrow \exists z: p(z)$  fof(prove\_this, conjecture)

**SYN965+1.p** Syntactic from Shults

$\exists z: \forall x: \exists y: ((p(y, x) \Rightarrow \exists w: p(w, y)) \text{ and } ((p(z, y) \text{ and } p(y, z)) \Rightarrow p(y, x)))$  fof(prove\_this, conjecture)

**SYN966+1.p** Syntactic from Shults

$\forall x, y: (eq(x, y) \iff \forall z: (a\_member\_of(z, x) \iff a\_member\_of(z, y))) \Rightarrow \forall a, b: (eq(a, b) \Rightarrow eq(b, a))$  fof(prove\_this, conjecture)

**SYN967+1.p** Syntactic from Shults

$\forall a, b: (\forall y: (q(y) \Rightarrow p(y)) \Rightarrow \exists x: ((p(x) \Rightarrow p(a)) \text{ and } (q(x) \Rightarrow p(b))))$  fof(prove\_this, conjecture)

**SYN968+1.p** Syntactic from Shults

$\exists x: \forall y: (p(x) \Rightarrow p(y))$  fof(prove\_this, conjecture)

**SYN969+1.p** Syntactic from Shults

$\forall b: ((\forall x: (p(x) \Rightarrow q(x)) \text{ and } r(b)) \Rightarrow (\forall y: (r(y) \Rightarrow p(y)) \Rightarrow q(b)))$  fof(prove\_this, conjecture)

**SYN970+1.p** Syntactic from Shults

$\forall a, b: \exists x, y: ((p(x) \Rightarrow r(y)) \Rightarrow (p(a) \Rightarrow r(b)))$  fof(prove\_this, conjecture)

**SYN971+1.p** Syntactic from Shults

$\exists y: (\exists x: p(x) \Rightarrow p(y))$  fof(prove\_this, conjecture)

**SYN972+1.p** Syntactic from Shults

$\exists x: \forall y: p(x, y) \Rightarrow \forall y: \exists x: p(x, y)$  fof(prove\_this, conjecture)

**SYN973+1.p** Syntactic from Shults

$p(z) \Rightarrow p(z)$  fof(prove\_this, conjecture)

**SYN974+1.p** Syntactic from Shults

$\exists x: p(x) \Rightarrow \exists y: p(y)$     fof(prove\_this, conjecture)

**SYN975+1.p** Syntactic from Shults

$\forall x, y: p(x, y) \Rightarrow \forall x: p(x, x)$     fof(prove\_this, conjecture)

**SYN976+1.p** Syntactic from Shults

$\forall a: (((f \text{ or } g) \text{ and } \forall x: (p(x) \text{ and } q(x))) \Rightarrow q(a))$     fof(prove\_this, conjecture)

**SYN977+1.p** Syntactic from Shults

$(a \iff b) \text{ or } a \text{ or } b$     fof(prove\_this, conjecture)

**SYN977^4.p** Syntactic from Shults

include('Axioms/LCL010^0.ax')

$a: \$i \rightarrow \$o$     thf(a\_type, type)

$b: \$i \rightarrow \$o$     thf(b\_type, type)

ivalid@(ior@(iequiv@(iatom@a)@(iatom@b))@(ior@(iatom@a)@(iatom@b)))    thf(prove\_this, conjecture)

**SYN978+1.p** Syntactic from Shults

$(a \text{ and } b) \Rightarrow (a \iff b)$     fof(prove\_this, conjecture)

**SYN978^4.p** Syntactic from Shults

include('Axioms/LCL010^0.ax')

$a: \$i \rightarrow \$o$     thf(a\_type, type)

$b: \$i \rightarrow \$o$     thf(b\_type, type)

ivalid@(iimplies@(iand@(iatom@a)@(iatom@b))@(iequiv@(iatom@a)@(iatom@b)))    thf(prove\_this, conjecture)

**SYN979+1.p** Syntactic from Shults

$\forall a, b: \exists x, y: (((q(x) \Rightarrow p(x, a)) \text{ and } q(a) \text{ and } q(b) \text{ and } (r(y) \Rightarrow p(b, y)) \text{ and } r(a) \text{ and } r(b) \text{ and } (s(a) \Rightarrow p(x, y)) \text{ and } s(a)) \Rightarrow p(a, b))$     fof(prove\_this, conjecture)

**SYN980+1.p** Syntactic from Shults

$\forall b: (\forall y: ((r(b) \Rightarrow r(y)) \Rightarrow p(f(y), y)) \Rightarrow \exists x, y: (p(x, y) \text{ and } (q(f(b), b) \Rightarrow q(x, y))))$     fof(prove\_this, conjecture)

**SYN981+1.p** Syntactic from Shults

$(\forall x: (p(x) \Rightarrow q(x)) \text{ and } \exists y: (q(y) \Rightarrow r(y))) \Rightarrow \exists z: (p(z) \Rightarrow r(z))$     fof(prove\_this, conjecture)

**SYN982-1.p** Problem that's Horn but resists hyper-resolution

ssNonce(na)    cnf(clause<sub>1</sub>, axiom)

ssP(t)    cnf(clause<sub>2</sub>, axiom)

ssBf(na)    cnf(clause<sub>3</sub>, axiom)

ssP(b)    cnf(clause<sub>4</sub>, axiom)

ssP(a)    cnf(clause<sub>5</sub>, axiom)

ssNonce(nb(u))    cnf(clause<sub>6</sub>, axiom)

ssNonce(tb(u))    cnf(clause<sub>7</sub>, axiom)

$\neg$ ssNonce(kt(u))    cnf(clause<sub>8</sub>, axiom)

ssTk(key(bt, b))    cnf(clause<sub>9</sub>, axiom)

ssTk(key(at, a))    cnf(clause<sub>10</sub>, axiom)

ssBk(key(bt, t))    cnf(clause<sub>11</sub>, axiom)

ssSa(pair(b, na))    cnf(clause<sub>12</sub>, axiom)

ssAk(key(at, t))    cnf(clause<sub>13</sub>, axiom)

ssIm(pair(u, v))  $\Rightarrow$  ssIm(v)    cnf(clause<sub>14</sub>, axiom)

ssIm(pair(u, v))  $\Rightarrow$  ssIm(u)    cnf(clause<sub>15</sub>, axiom)

ssM(sent(a, b, pair(a, na)))    cnf(clause<sub>16</sub>, axiom)

ssIm(triple(u, v, w))  $\Rightarrow$  ssIm(w)    cnf(clause<sub>17</sub>, axiom)

ssIm(triple(u, v, w))  $\Rightarrow$  ssIm(v)    cnf(clause<sub>18</sub>, axiom)

ssIm(triple(u, v, w))  $\Rightarrow$  ssIm(u)    cnf(clause<sub>19</sub>, axiom)

ssM(sent(u, v, w))  $\Rightarrow$  ssIm(w)    cnf(clause<sub>20</sub>, axiom)

ssIm(quadr(u, v, w, x))  $\Rightarrow$  ssIm(x)    cnf(clause<sub>21</sub>, axiom)

ssIm(quadr(u, v, w, x))  $\Rightarrow$  ssIm(w)    cnf(clause<sub>22</sub>, axiom)

ssIm(quadr(u, v, w, x))  $\Rightarrow$  ssIm(v)    cnf(clause<sub>23</sub>, axiom)

ssIm(quadr(u, v, w, x))  $\Rightarrow$  ssIm(u)    cnf(clause<sub>24</sub>, axiom)

(ssIm(u) and ssP(v))  $\Rightarrow$  ssIk(key(u, v))    cnf(clause<sub>25</sub>, axiom)

(ssIm(u) and ssIm(v))  $\Rightarrow$  ssIm(pair(u, v))    cnf(clause<sub>26</sub>, axiom)

(ssIm(u) and ssP(v) and ssP(w))  $\Rightarrow$  ssM(sent(v, w, u))    cnf(clause<sub>27</sub>, axiom)

(ssIm(u) and ssIm(v) and ssIm(w))  $\Rightarrow$  ssIm(triple(u, v, w))    cnf(clause<sub>28</sub>, axiom)

$(\text{ssIm}(u) \text{ and } \text{ssIk}(\text{key}(v, w)) \text{ and } \text{ssP}(w)) \Rightarrow \text{ssIm}(\text{encr}(u, v)) \quad \text{cnf}(\text{clause}_{29}, \text{axiom})$   
 $(\text{ssM}(\text{sent}(u, b, \text{pair}(u, v))) \text{ and } \text{ssBf}(v)) \Rightarrow \text{ssSb}(\text{pair}(u, v)) \quad \text{cnf}(\text{clause}_{30}, \text{axiom})$   
 $(\text{ssIm}(u) \text{ and } \text{ssIm}(v) \text{ and } \text{ssIm}(w) \text{ and } \text{ssIm}(x)) \Rightarrow \text{ssIm}(\text{quadr}(u, v, w, x)) \quad \text{cnf}(\text{clause}_{31}, \text{axiom})$   
 $(\text{ssM}(\text{sent}(t, a, \text{triple}(\text{encr}(\text{quadr}(u, v, w, x), \text{at}), y, z))) \text{ and } \text{ssSa}(\text{pair}(u, v))) \Rightarrow \text{ssAk}(\text{key}(w, u)) \quad \text{cnf}(\text{clause}_{32}, \text{axiom})$   
 $(\text{ssM}(\text{sent}(u, b, \text{pair}(u, v))) \text{ and } \text{ssBf}(v)) \Rightarrow \text{ssM}(\text{sent}(b, t, \text{triple}(b, \text{nb}(v), \text{encr}(\text{triple}(u, v, \text{tb}(v)), \text{bt})))) \quad \text{cnf}(\text{clause}_{33}, \text{axiom})$   
 $(\text{ssM}(\text{sent}(u, b, \text{pair}(\text{encr}(\text{triple}(u, v, \text{tb}(w)), \text{bt}), \text{encr}(\text{nb}(w), v)))) \text{ and } \text{ssSb}(\text{pair}(u, w))) \Rightarrow \text{ssBk}(\text{key}(v, u)) \quad \text{cnf}(\text{clause}_{34}, \text{axiom})$   
 $(\text{ssM}(\text{sent}(t, a, \text{triple}(\text{encr}(\text{quadr}(u, v, w, x), \text{at}), y, z))) \text{ and } \text{ssSa}(\text{pair}(u, v))) \Rightarrow \text{ssM}(\text{sent}(a, u, \text{pair}(y, \text{encr}(z, w)))) \quad \text{cnf}(\text{clause}_{35}, \text{axiom})$   
 $(\text{ssM}(\text{sent}(u, t, \text{triple}(u, v, \text{encr}(\text{triple}(w, x, y), z)))) \text{ and } \text{ssTk}(\text{key}(z, u)) \text{ and } \text{ssTk}(\text{key}(x_1, w)) \text{ and } \text{ssNonce}(x)) \Rightarrow \text{ssM}(\text{sent}(t, u, \text{pair}(u, v))) \quad \text{cnf}(\text{clause}_{36}, \text{axiom})$   
 $\text{ssIk}(\text{key}(u, b)) \Rightarrow \neg \text{ssBk}(\text{key}(u, a)) \quad \text{cnf}(\text{clause}_{37}, \text{negated\_conjecture})$

**SYN983^1.p** Factoring application over conjunction

$a: \$o \quad \text{thf}(a\_const, \text{type})$   
 $b: \$o \quad \text{thf}(b\_const, \text{type})$   
 $p: \$o \rightarrow \$o \quad \text{thf}(p\_const, \text{type})$   
 $(p@a \text{ and } p@b) \Rightarrow (p@(a \text{ and } b)) \quad \text{thf}(\text{thm}, \text{conjecture})$

**SYN984^1.p** Factoring application over conjunction with lambda

Variation of BB-1 with functional extensionality

$a: \$o \quad \text{thf}(a\_const, \text{type})$   
 $b: \$o \quad \text{thf}(b\_const, \text{type})$   
 $p: (\$i \rightarrow \$o) \rightarrow \$o \quad \text{thf}(p\_const, \text{type})$   
 $(p@\lambda x: \$i: a \text{ and } p@\lambda x: \$i: b) \Rightarrow (p@\lambda x: \$i: (a \text{ and } b)) \quad \text{thf}(\text{thm}, \text{conjecture})$

**SYN985^1.p** Factoring application over conjunction with abstraction

Variation of BB-1 with functional extensionality

$\neg \forall p: (\$i \rightarrow \$o) \rightarrow \$o, a: \$i \rightarrow \$o, b: \$i \rightarrow \$o: ((p@\lambda x: \$i: (a@x) \text{ and } p@\lambda x: \$i: (b@x)) \Rightarrow (p@\lambda x: \$i: (a@x \text{ and } b@x))) \quad \text{thf}(\text{thm}, \text{conjecture})$

**SYN986+1.000.p** Orevkov formula - size 0

hyp(2,k,1) is defined. Each Ck has a non-normal natural deduction of size linear in k, and each normal deduction of Ck has at least hyp(2,k,1)=2.k nodes.

$\text{include}('Axioms/SYN002+0.ax')$   
 $\exists z_0: r(0, 0, z_0) \quad \text{fof}(\text{ck}, \text{conjecture})$

**SYN986+1.001.p** Orevkov formula - size 1

hyp(2,k,1) is defined. Each Ck has a non-normal natural deduction of size linear in k, and each normal deduction of Ck has at least hyp(2,k,1)=2.k nodes.

$\text{include}('Axioms/SYN002+0.ax')$   
 $\exists z_1, z_0: (r(0, 0, z_1) \text{ and } r(0, z_1, z_0)) \quad \text{fof}(\text{ck}, \text{conjecture})$

**SYN986+1.002.p** Orevkov formula - size 2

hyp(2,k,1) is defined. Each Ck has a non-normal natural deduction of size linear in k, and each normal deduction of Ck has at least hyp(2,k,1)=2.k nodes.

$\text{include}('Axioms/SYN002+0.ax')$   
 $\exists z_2, z_1, z_0: (r(0, 0, z_2) \text{ and } r(0, z_2, z_1) \text{ and } r(0, z_1, z_0)) \quad \text{fof}(\text{ck}, \text{conjecture})$

**SYN986+1.003.p** Orevkov formula - size 3

hyp(2,k,1) is defined. Each Ck has a non-normal natural deduction of size linear in k, and each normal deduction of Ck has at least hyp(2,k,1)=2.k nodes.

$\text{include}('Axioms/SYN002+0.ax')$   
 $\exists z_3, z_2, z_1, z_0: (r(0, 0, z_3) \text{ and } r(0, z_3, z_2) \text{ and } r(0, z_2, z_1) \text{ and } r(0, z_1, z_0)) \quad \text{fof}(\text{ck}, \text{conjecture})$

**SYN986+1.004.p** Orevkov formula - size 4

hyp(2,k,1) is defined. Each Ck has a non-normal natural deduction of size linear in k, and each normal deduction of Ck has at least hyp(2,k,1)=2.k nodes.

$\text{include}('Axioms/SYN002+0.ax')$   
 $\exists z_4, z_3, z_2, z_1, z_0: (r(0, 0, z_4) \text{ and } r(0, z_4, z_3) \text{ and } r(0, z_3, z_2) \text{ and } r(0, z_2, z_1) \text{ and } r(0, z_1, z_0)) \quad \text{fof}(\text{ck}, \text{conjecture})$

**SYN986+1.005.p** Orevkov formula - size 5

hyp(2,k,1) is defined. Each Ck has a non-normal natural deduction of size linear in k, and each normal deduction of Ck has at least hyp(2,k,1)=2.k nodes.

$\text{include}('Axioms/SYN002+0.ax')$   
 $\exists z_5, z_4, z_3, z_2, z_1, z_0: (r(0, 0, z_5) \text{ and } r(0, z_5, z_4) \text{ and } r(0, z_4, z_3) \text{ and } r(0, z_3, z_2) \text{ and } r(0, z_2, z_1) \text{ and } r(0, z_1, z_0)) \quad \text{fof}(\text{ck}, \text{conjecture})$

**SYN986+1.006.p** Orevkov formula - size 6

hyp(2,k,1) is defined. Each Ck has a non-normal natural deduction of size linear in k, and each normal deduction of Ck has at least hyp(2,k,1)=2.k nodes.

include('Axioms/SYN002+0.ax')

$\exists z_6, z_5, z_4, z_3, z_2, z_1, z_0: (r(0, 0, z_6) \text{ and } r(0, z_6, z_5) \text{ and } r(0, z_5, z_4) \text{ and } r(0, z_4, z_3) \text{ and } r(0, z_3, z_2) \text{ and } r(0, z_2, z_1) \text{ and } r(0, z_1, z_0))$

**SYN987^1.p** All things are true

$\forall x: \$o: x \quad \text{thf}(\text{thm}, \text{conjecture})$

**SYN987^2.p** All things are true

$\forall x: \$o: x \quad \text{thf}(\text{thm}, \text{axiom})$

**SYN988^1.p** All things are false

$\forall x: \$o: \neg x \quad \text{thf}(\text{thm}, \text{conjecture})$

**SYN988^2.p** All things are false

$\forall x: \$o: \neg x \quad \text{thf}(\text{thm}, \text{axiom})$

**SYN989^1.p** All things are true or false

$\forall x: \$o: (x \text{ or } \neg x) \quad \text{thf}(\text{thm}, \text{conjecture})$

**SYN989^2.p** All things are true or false

$\forall x: \$o: (x \text{ or } \neg x) \quad \text{thf}(\text{thm}, \text{axiom})$

**SYN989^3.p** All things are true or false

$p: \$o \quad \text{thf}(p, \text{type})$

$p \text{ or } \neg p \quad \text{thf}(\text{cTRIV}_0, \text{conjecture})$

**SYN990^1.p** Simple test for satisfiability

There are two individuals, a and b. Everything is either a or b. There are three functions from individuals to individuals: f,g,h. They are all different.

$a: \$i \quad \text{thf}(a, \text{type})$

$b: \$i \quad \text{thf}(b, \text{type})$

$f: \$i \rightarrow \$i \quad \text{thf}(f, \text{type})$

$g: \$i \rightarrow \$i \quad \text{thf}(g, \text{type})$

$h: \$i \rightarrow \$i \quad \text{thf}(h, \text{type})$

$\forall x: \$i: (x = a \text{ or } x = b) \quad \text{thf}(\text{ab}, \text{axiom})$

$f \neq g \quad \text{thf}(\text{fg}, \text{axiom})$

$g \neq h \quad \text{thf}(\text{gh}, \text{axiom})$

$f \neq h \quad \text{thf}(\text{fh}, \text{axiom})$

**SYN991^1.p** Inconsistency of axioms that says all relations are reflexive

$\text{refl}: (\$i \rightarrow \$i \rightarrow \$o) \rightarrow \$o \quad \text{thf}(\text{refl\_type}, \text{type})$

$\text{refl} = (\lambda r: \$i \rightarrow \$i \rightarrow \$o: \forall x: \$i: (r@x@x)) \quad \text{thf}(\text{refl}, \text{definition})$

$\forall r: \$i \rightarrow \$i \rightarrow \$o: (\text{refl}@r) \quad \text{thf}(\text{ax}, \text{axiom})$

**SYN992^1.p** There exists a reflexive relation

$\text{refl}: (\$i \rightarrow \$i \rightarrow \$o) \rightarrow \$o \quad \text{thf}(\text{refl\_type}, \text{type})$

$\text{refl} = (\lambda r: \$i \rightarrow \$i \rightarrow \$o: \forall x: \$i: (r@x@x)) \quad \text{thf}(\text{refl}, \text{definition})$

$\exists r: \$i \rightarrow \$i \rightarrow \$o: (\text{refl}@r) \quad \text{thf}(\text{ax}, \text{conjecture})$

**SYN993^1.p** Skolemization test 1

$q: \$i \rightarrow \$i \rightarrow \$o \quad \text{thf}(q\_decl, \text{type})$

$\exists x: \$i: \forall y: \$i: (q@x@y) \text{ or } \exists u: \$i: \forall v: \$i: \neg q@v@u \quad \text{thf}(\text{conj}, \text{conjecture})$

**SYN994^1.p** Skolemization test 2

$q: \$i \rightarrow \$i \rightarrow \$o \quad \text{thf}(q\_decl, \text{type})$

$\exists y: \$i: \forall x: \$i: (\forall z: \$i: (q@x@z) \text{ or } \neg q@x@y) \quad \text{thf}(\text{conj}, \text{conjecture})$

**SYN995^1.p** Every function has a fixed point

$\text{leibeq}: \$i \rightarrow \$i \rightarrow \$o \quad \text{thf}(\text{leibeq\_decl}, \text{type})$

$\text{leibeq} = (\lambda x: \$i, y: \$i: \forall p: \$i \rightarrow \$o: ((p@x) \iff (p@y))) \quad \text{thf}(\text{leibeq}, \text{definition})$

$\forall f: \$i \rightarrow \$i: \exists x: \$i: (\text{leibeq}@ (f@x)@x) \quad \text{thf}(\text{conj}, \text{conjecture})$

**SYN996^1.p** Test for naive Skolemization

$r: \$i \rightarrow \$i \rightarrow \$o \quad \text{thf}(r\_decl, \text{type})$

$\forall x: \$i: \exists y: \$i: (r@x@y) \Rightarrow \exists f: \$i \rightarrow \$i: \forall x: \$i: (r@x@(f@x)) \quad \text{thf}(\text{conj}, \text{conjecture})$

**SYN997^1.p** Test for validity of axiom of choice

$\exists e: (\$i \rightarrow \$o) \rightarrow \$i: \forall p: \$i \rightarrow \$o: (\exists y: \$i: (p@y) \Rightarrow (p@(e@p))) \quad \text{thf}(\text{conj}, \text{conjecture})$



**SYN998**<sup>1.p</sup> Leibniz equality is reflexive

leibeq:  $\$i \rightarrow \$i \rightarrow \$o$     thf(leibeq\_decl, type)

leibeq =  $(\lambda x: \$i, y: \$i: \forall p: \$i \rightarrow \$o: ((p@x) \Rightarrow (p@y)))$     thf(leibeq, definition)

$\forall x: \$i: (\text{leibeq}@x@x)$     thf(conj, conjecture)

**SYN999**<sup>1.p</sup> Leibniz equality is symmetric

leibeq:  $\$i \rightarrow \$i \rightarrow \$o$     thf(leibeq\_decl, type)

leibeq =  $(\lambda x: \$i, y: \$i: \forall p: \$i \rightarrow \$o: ((p@x) \Rightarrow (p@y)))$     thf(leibeq, definition)

$\forall x: \$i, y: \$i: ((\text{leibeq}@x@y) \Rightarrow (\text{leibeq}@y@x))$     thf(conj, conjecture)